

11.5.7:

(a). Since this truth table has three entries of F,

$$\psi_1 \stackrel{\text{def}}{=} \neg p \vee \neg q$$

$$\psi_2 \stackrel{\text{def}}{=} p \vee \neg q$$

$$\psi_3 \stackrel{\text{def}}{=} \neg p \vee p$$

The resulting  $\phi$  in CNF is therefore

$$(\neg p \vee \neg q) \wedge (p \vee \neg q) \wedge (\neg p \vee p)$$

(b)

$$\psi_1 \stackrel{\text{def}}{=} \neg p \vee \neg q \vee r$$

$$\psi_2 \stackrel{\text{def}}{=} \neg p \vee q \vee \neg r$$

$$\psi_3 \stackrel{\text{def}}{=} \neg p \vee q \vee r$$

$$\psi_4 \stackrel{\text{def}}{=} p \vee \neg q \vee r$$

$$\psi_5 \stackrel{\text{def}}{=} p \vee q \vee r$$

The resulting  $\phi$  in CNF is therefore

$$(\neg p \vee \neg q \vee r) \wedge (\neg p \vee q \vee \neg r) \wedge (\neg p \vee q \vee r) \wedge (p \vee \neg q \vee r) \wedge (p \vee q \vee r)$$

(c).

$$\psi_1 \stackrel{\text{def}}{=} \neg p \vee \neg q \vee \neg r$$

$$\psi_2 \stackrel{\text{def}}{=} \neg p \vee q \vee \neg r$$

$$\psi_3 \stackrel{\text{def}}{=} p \vee \neg q \vee \neg r$$

$$\psi_4 \stackrel{\text{def}}{=} p \vee q \vee r$$

$$\psi_5 \stackrel{\text{def}}{=} p \vee q \vee \neg r$$

The resulting  $\phi$  in CNF is therefore

$$(\neg p \vee \neg q \vee \neg r) \wedge (\neg p \vee q \vee \neg r) \wedge (p \vee \neg q \vee \neg r) \wedge (p \vee q \vee r) \wedge (p \vee q \vee \neg r)$$

1.5.9

$$\text{IMPL-FREE} = \neg(\neg p \vee (\neg(q \vee (p \vee q))))$$

↓

NNF

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$$\text{CNF} = p \wedge (q \wedge (p \vee q))$$