Lecture 5 AES Standard

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UTAS Sultanate of Oman September 2022

CSSY2201: Introduction to Cryptography



Plan

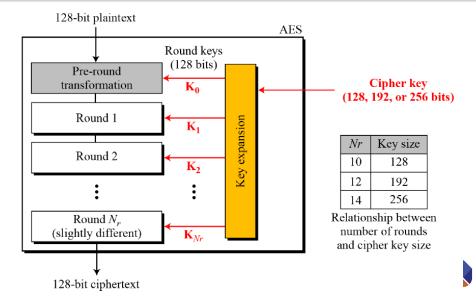
- General Overview
- AES Transformations
 - Substitution
 - Permutation
 - Mixing
 - Key Adding
- KEY EXPANSION
- Summary



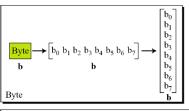
- In February 2001, NIST announced that a draft of the Federal Information Processing Standard (FIPS) was available for public review and comment. Finally, AES was published as FIPS 197 in the Federal Register in December 2001.
- AES is a non-Feistel cipher that encrypts and decrypts a data block of 128 bits. It uses 10, 12, or 14 rounds. The key size, which can be 128, 192, or 256 bits, depends on the number of rounds.
- AES has defined three versions, with 10, 12, and 14 rounds. Each version uses a different cipher key size (128, 192, or 256).
- Round keys are always 128 bits.

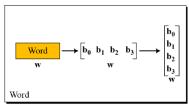


General design of AES encryption cipher



Data units used in AES

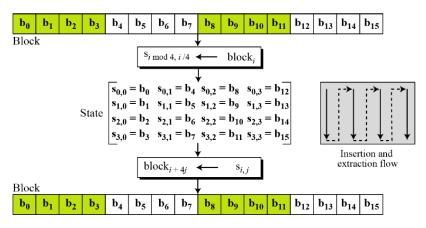




$$S \longrightarrow \begin{bmatrix} s_{0,0} & s_{0,1} & s_{0,2} & s_{0,3} \\ s_{1,0} & s_{1,1} & s_{1,2} & s_{1,3} \\ s_{2,0} & s_{2,1} & s_{2,2} & s_{2,3} \\ \underline{s_{3,0}} & s_{3,1} & s_{3,2} & s_{3,3} \end{bmatrix} \longrightarrow \begin{bmatrix} w_0 & w_1 & w_2 & w_3 \end{bmatrix}$$
State



Block-to-state and state-to-block transformation



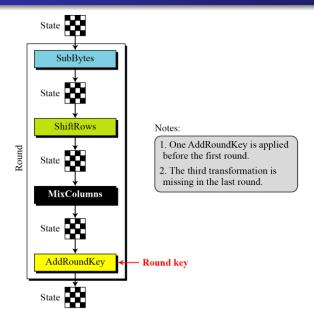


Example: Changing plaintext to state

Text	A	Е	S	U	S	Е	S	A	M	A	T	R	Ι	X	Z	Z
Hexadecimal	00	04	12	14	12	04	12	00	0C	00	13	11	08	23	19	19
							Гоо	12	0C	08]						
							04	04	00	23	Ctat					
							12	12	00 13	19	Stat	e				
							14	00	11	19						



Structure of Each Round



TRANSFORMATIONS

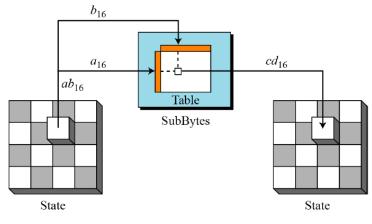
To provide security, AES uses four types of transformations : substitution, permutation, mixing, and key-adding.

- Substitution: SubBytes and InvSubBytes
- Permutation :
- Mixing
- Key Adding



Substitution: SubBytes

- SubBytes, is used at the encryption site. To substitute a byte, we interpret the byte as two hexadecimal digits.
- The SubBytes operation involves 16 independent byte-to-byte transformations.



SubByte Transformation Table : S-Box

	0	1	2	3	4	5	6	7	8	9	Α	В	С	D	E	F
0	63	7C	77	7B	F2	6B	6F	C5	30	01	67	2B	FE	D7	AB	76
1	CA	82	C9	7D	FA	59	47	F0	AD	D4	A2	AF	9C	A4	72	CO
2	В7	FD	93	26	36	3F	F7	СС	34	A5	E5	F1	71	D8	31	15
3	04	C7	23	СЗ	18	96	05	9A	07	12	80	E2	EB	27	B2	75
4	09	83	2C	1A	1B	6E	5A	A0	52	3B	D6	В3	29	E3	2F	84
5	53	D1	00	ED	20	FC	B1	5B	6A	СВ	BE	39	4A	4C	58	CF
6	D0	EF	AA	FB	43	4D	33	85	45	F9	02	7F	50	3C	9F	A8
7	51	А3	40	8F	92	9D	38	F5	вс	В6	DA	21	10	FF	F3	D2
8	CD	0C	13	EC	5F	97	44	17	C4	Α7	7E	3D	64	5D	19	73
9	60	81	4F	DC	22	2A	90	88	46	EE	В8	14	DE	5E	0B	DB
Α	E0	32	3A	0A	49	06	24	5C	C2	D3	AC	62	91	95	E4	79
В	E7	C8	37	6D	8D	D5	4E	A9	6C	56	F4	EA	65	7A	AE	08
С	ВА	78	25	2E	1C	A6	В4	C6	E8	DD	74	1F	4B	BD	8B	8A
D	70	3E	B5	66	48	03	F6	0E	61	35	57	В9	86	C1	1D	9E
Е	E1	F8	98	11	69	D9	8E	94	9B	1E	87	E9	CE	55	28	DF
F	8C	Δ1	89	0D	BF	F6	42	68	41	99	2D	0F	B0	54	BB	16





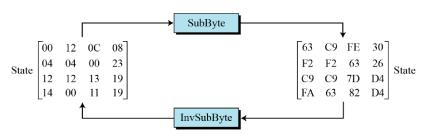
InvSubBytes Transformation Table: Inverse S-Box

									,	1							
		0	1	2	3	4	5	6	7	8	9	а	b	С	d	e	f
	0	52	09	6A	D5	30	36	A5	38	BF	40	АЗ	9E	81	F3	D7	FB
	1	7C	E3	39	82	9B	2F	FF	87	34	83	43	44	C4	DE	E9	CB
	2	54	7B	94	32	A6	C2	23	3D	EE	4C	95	OB	42	FA	C3	4E
	3	08	2E	A1	66	28	D9	24	B2	76	5B	A2	49	6D	8B	D1	25
	4	72	F8	F6	64	86	68	98	16	D4	A4	5C	CC	5D	65	B6	92
	5	6C	70	48	50	FD	ED	В9	DA	5E	15	46	57	A7	8D	9D	84
	6	90	D8	AB	00	8C	BC	D3	OA	F7	E4	58	05	В8	B 3	45	06
х	7	D0	2C	1E	8F	CA	3F	OF	02	C1	AF	BD	03	01	13	8A	6B
^	8	ЗА	91	11	41	4F	67	DC	EA	97	F2	CF	CE	FO	B4	E6	73
	9	96	AC	74	22	E7	AD	35	85	E2	F9	37	E8	1C	75	DF	6E
	а	47	F1	1A	71	1D	29	C5	89	6F	B7	62	0E	AA	18	BE	1B
	b	FC	56	3E	4B	C6	D2	79	20	9A	DB	CO	FE	78	CD	5A	F4
	С	1F	DD	A8	33	88	07	C7	31	B1	12	10	59	27	80	EC	5F
	d	60	51	7F	Α9	19	B5	4A	OD	2D	E5	7A	9F	93	C9	9C	EF
	е	A0	EO	3B	4D	AE	2A	F5	BO	C8	EB	BB	3C	83	53	99	61
	f	17	2B	04	7E	BA	77	D6	26	E1	69	14	63	55	21	OC	7D



Example using SubByte and InvSubByte

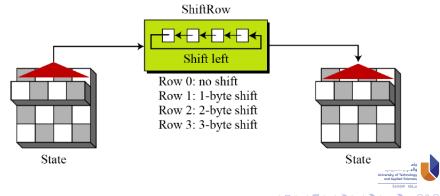
the figure shows how a state is transformed using the SubBytes transformation. The figure also shows that the InvSubBytes transformation creates the original one.



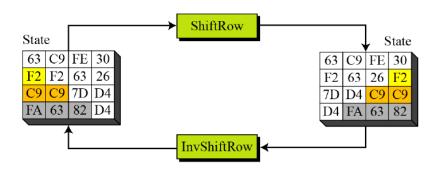


Permutation: ShiftRows and InvShiftRows

- ShiftRows permutes the bytes.
- In the encryption, the transformation is called ShiftRows (Shift to the left)
- in the decryption, it is called InvShiftRows (Shift to the right)



the Figure shows how a state is transformed using ShiftRows transformation. The figure also shows that InvShiftRows transformation creates the original state.





Mixing

We need an interbyte transformation that changes the bits inside a byte, based on the bits inside the neighboring bytes. We need to mix bytes to provide diffusion at the bit level.

$$a\mathbf{x} + b\mathbf{y} + c\mathbf{z} + d\mathbf{t} \longrightarrow$$

$$e\mathbf{x} + f\mathbf{y} + g\mathbf{z} + h\mathbf{t} \longrightarrow$$

$$i\mathbf{x} + j\mathbf{y} + k\mathbf{z} + l\mathbf{t} \longrightarrow$$

$$m\mathbf{x} + n\mathbf{y} + o\mathbf{z} + p\mathbf{t} \longrightarrow$$

$$= \begin{bmatrix} a & b & c & d \\ e & f & g & h \\ i & j & k & l \\ m & n & o & p \end{bmatrix} \times \begin{bmatrix} \mathbf{x} & \mathbf{y} \\ \mathbf{z} \\ \mathbf{t} \end{bmatrix}$$

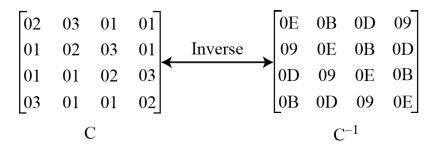
New matrix

Constant matrix

Old matrix



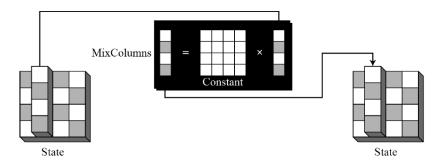
Constant matrices used by MixColumns and InvMixColumns





MixColumns

The MixColumns transformation operates at the column level; it transforms each column of the state to a new column.





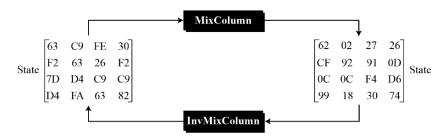
The InvMixColumns transformation is basically the same as the MixColumns transformation.

Note

The MixColumns and InvMixColumns transformations are inverses of each other.



the Figure shows how a state is transformed using the MixColumns transformation. The figure also shows that the InvMixColumns transformation creates the original one.



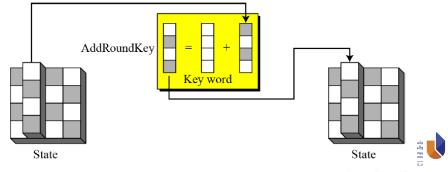


Key Adding

AddRoundKey proceeds one column at a time. AddRoundKey adds a round key word with each state column matrix; the operation in AddRoundKey is matrix addition.

Note

The AddRoundKey transformation is the inverse of itself.



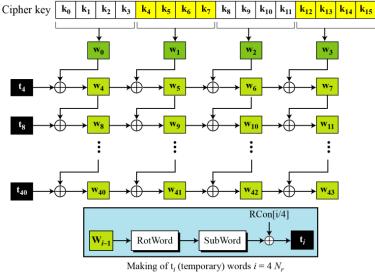
KEY EXPANSION

To create round keys for each round, AES uses a keyexpansion process. If the number of rounds is Nr , the key-expansion routine creates Nr + 1 128-bit round keys from one single 128-bit cipher key.

Figure – words for each round

Round		,	Words	
Pre-round	\mathbf{w}_0	\mathbf{w}_1	\mathbf{w}_2	\mathbf{w}_3
1	\mathbf{w}_4	\mathbf{w}_5	\mathbf{w}_6	\mathbf{w}_7
2	\mathbf{w}_8	\mathbf{w}_9	\mathbf{w}_{10}	\mathbf{w}_{11}
N_r	\mathbf{w}_{4N_r}	\mathbf{w}_{4N_r+1}	\mathbf{w}_{4N_r+2}	\mathbf{w}_{4N_r+3}

Key Expansion in AES-128



the Rcon constants

Round	Constant (RCon)	Round	Constant (RCon)
1	(<u>01</u> 00 00 00) ₁₆	6	(<u>20</u> 00 00 00) ₁₆
2	(<u>02</u> 00 00 00) ₁₆	7	(<u>40</u> 00 00 00) ₁₆
3	(<u>04</u> 00 00 00) ₁₆	8	(<u>80</u> 00 00 00) ₁₆
4	(<u>08</u> 00 00 00) ₁₆	9	(<u>1B</u> 00 00 00) ₁₆
5	(<u>10</u> 00 00 00) ₁₆	10	(<u>36</u> 00 00 00) ₁₆



The Table shows how the keys for each round are calculated assuming that the 128-bit cipher key agreed upon by Alice and Bob is $(2475A2B33475568831E2120013AA5487)_{16}$.

Round	Values of t's	First word in the round	Second word in the round	Third word in the round	Fourth word in the round
_		$w_{00} = 2475 \text{A}2 \text{B}3$	w_{01} = 34755688	$w_{02} = 31E21200$	$w_{03} = 13AA5487$
1	AD20177D	$w_{04} = 8955B5CE$	$w_{05} = BD20E346$	$w_{06} = 8CC2F146$	$w_{07} = 9$ F68A5C1
2	470678DB	$w_{08} = CE53CD15$	$w_{09} = 73732E53$	$w_{10} = FFB1DF15$	$w_{11} = 60D97AD4$
3	31DA48D0	$w_{12} = FF8985C5$	$w_{13} = 8$ CFAAB96	$w_{14} = 734B7483$	$w_{15} = 2475$ A2B3
4	47AB5B7D	$w_{16} = B822 deb8$	$w_{17} = 34D8752E$	$w_{18} = 479301 AD$	$w_{19} = 54010$ FFA
5	6C762D20	$w_{20} = D454F398$	$w_{21} = E08C86B6$	$w_{22} = A71F871B$	$w_{23} = F31E88E1$
6	52C4F80D	$w_{24} = 86900B95$	$w_{25} = 661 \text{C8D23}$	$w_{26} = C1030A38$	$w_{27} = 321D82D9$
7	E4133523	w ₂₈ = 62833EB6	$w_{29} = 049$ FB395	$w_{30} = C59CB9AD$	$w_{31} = F7813B74$
8	8CE29268	$w_{32} = \text{EE61ACDE}$	$w_{33} = EAFE1F4B$	$w_{34} = 2F62A6E6$	$w_{35} = D8E39D92$
9	0A5E4F61	$w_{36} = E43FE3BF$	$w_{37} = 0$ EC1FCF4	$w_{38} = 21A35A12$	$w_{39} = F940C780$
10	3FC6CD99	$w_{40} = DBF92E26$	$w_{41} = D538D2D2$	$w_{42} = F49B88C0$	$w_{43} = 0$ DDB4F40



Each round key in AES depends on the previous round key. The dependency, however, is nonlinear because of SubWord transformation. The addition of the round constants also guarantees that each round key will be different from the previous one. Example: The two sets of round keys can be created from two cipher keys that are different only in one bit.

Cipher Key 1: 12 45 A2 A1 23 31 A4 A3 B2 CC A**A** 34 C2 BB 77 23 Cipher Key 2: 12 45 A2 A1 23 31 A4 A3 B2 CC A**B** 34 C2 BB 77 23



Comparing two sets of round keys

R.		Round key	vs for set 1		Round keys for set 2					
_	1245A2A1	2331A4A3	B2CCA <u>A</u> 34	C2BB7723	1245A2A1	2331A4A3	B2CCA <u>B</u> 34	C2BB7723	01	
1	F9B08484	DA812027	684D8 <u>A</u> 13	AAF6F <u>D</u> 30	F9B08484	DA812027	684D8 <u>B</u> 13	AAF6F <u>C</u> 30	02	
2	B9E48028	6365A00F	0B282A1C	A1DED72C	B9008028	6381A00F	0BCC2B1C	A13AD72C	17	
3	A0EAF11A	C38F5115	C8A77B09	6979AC25	3D0EF11A	5E8F5115	55437A09	F479AD25	30	
4	1E7BCEE3	DDF49FF6	1553E4FF	7C2A48DA	839BCEA5	DD149FB0	8857E5B9	7C2E489C	31	
5	EB2999F3	36DD0605	238EE2FA	5FA4AA20	A2C910B5	7FDD8F05	F78A6ABC	8BA42220	34	
6	82852E3C	B4582839	97D6CAC3	C87260E3	CB5AA788	B487288D	430D4231	C8A96011	56	
7	82553FD4	360D17ED	A1DBDD2E	69A9BDCD	588A2560	EC0D0DED	AF004FDC	67A92FCD	50	
8	D12F822D	E72295C0	46F948EE	2F50F523	0B9F98E5	E7929508	4892DAD4	2F3BF519	44	
9	99C9A438	7EEB31F8	38127916	17428C35	F2794CF0	15EBD9F8	5D79032C	7242F635	51	
10	83AD32C8	FD460330	C5547A26	D216F613	E83BDAB0	FDD00348	A0A90064	D2EBF651	52	



The concept of weak keys, does not apply to AES. Assume that all bits in the cipher key are 0s. The following shows the words for some rounds:

Pre-round:	0000000	00000000	0000000	00000000
Round 01:	62636363	62636363	62636363	62636363
Round 02:	9B9898C9	F9FBFBAA	9B9898C9	F9FBFBAA
Round 03:	90973450	696CCFFA	F2F45733	0B0FAC99
Round 10:	B4EF5BCB	3E92E211	23E951CF	6F8F188E

The words in the pre-round and the first round are all the same. In the second round, the first word matches with the third; the second word matches with the fourth. However, after the second round the pattern disappears; every word is different.

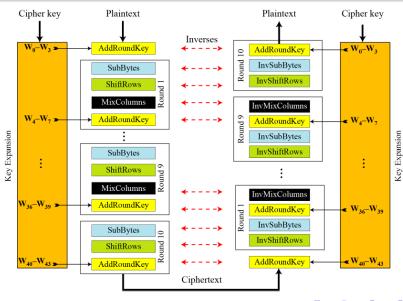


The AES Cipher: Summary

AES uses four types of transformations for encryption and decryption. In the standard, the encryption algorithm is referred to as the cipher and the decryption algorithm as the inverse cipher.



AES cipher and inverse cipher



AES pseudocode

```
Cipher (InBlock [16], OutBlock [16], w[0 ... 43])
    BlockToState (InBlock, S)
   S \leftarrow AddRoundKey (S, w[0...3])
    for (round = 1 to 10)
        S \leftarrow SubBytes(S)
        S \leftarrow ShiftRows(S)
         if (round \neq 10) \mathbf{S} \leftarrow \text{MixColumns}(\mathbf{S})
         S \leftarrow AddRoundKey (S, w[4 \times round, 4 \times round + 3])
```

StateToBlock (S, OutBlock);

Security of AES

- AES was designed after DES. Most of the known attacks on DES were already tested on AES.
- Brute-Force Attack : AES is definitely more secure than DES due to the larger-size key.
- Statistical Attacks: Numerous tests have failed to do statistical analysis of the ciphertext.
- Differential and Linear Attacks: There are no differential and linear attacks on AES as yet.

