

Upwork.com Template for a L^AT_EX Document

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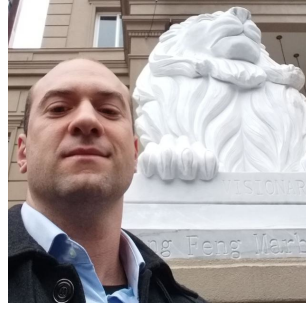
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Abstract

Hello, and welcome to the sample LaTeX document demo page. I used Latex2HTML for conversion and made some adjustments to the html code then. In the following sections you will be able to check how I can easily edit your documents and turn them into a dynamic page, a pdf whether it is a book, a report, an article or a presentation.

1 Using Excel2LaTeX for Gujarati Appendix C

In this section I will replicate Appendix C of Damodar N. Gujarati's book Basic Econometrics, Fourth Edition (see references at end) [1], demonstrating the applicability of matrix calculation for OLS estimation using Excel spreadsheet.

(You can see the e-book [in this link](#))

1.1 C.10 SUMMARY OF THE MATRIX APPROACH: AN ILLUSTRATIVE EXAMPLE

Consider the data given in Table C.4. These data pertain to per capita personal consumption expenditure (PPCE) and per capital personal disposable income (PPDI) and time or the trend variable. By including the trend variable in the model, we are trying to find out the relationship of PPCE to PPDI net of the trend variable (which may represent a host of other factors, such as technology, change in tastes, etc.)

For empirical purposes, therefore, the regression model is

$$Y_i = \hat{\beta}_1 + \hat{\beta}_2 X_{2i} + \hat{\beta}_3 X_{3i} + \hat{\mu}_i$$

where Y = per capita consumption expenditure, X_2 = per capita disposable income, and X_3 = time. The data required to run the regression are given in Table as follows:

Table 1: PER CAPITA PERSONAL CONSUMPTION EXPENDITURE (PPCE) AND PER CAPITA PERSONAL DISPOSABLE INCOME (PPDI) IN THE UNITED STATES, 1956–1970, IN 1958 DOLLARS

PPCE, Y	PPDI, X_2	Time, X
1673	1839	1 (= 1956)
1688	1844	2
1666	1831	3
1735	1881	4
1749	1883	5
1756	1910	6
1815	1969	7
1867	2016	8
1948	2126	9
2048	2239	10
2128	2336	11
2165	2404	12
2257	2487	13
2316	2535	14
2324	2595	15 (= 1970)

Source: Economic Report of the President, January 1972, Table B-16.

In matrix notation, our problem may be shown as follows:

$$\begin{array}{ccccccc}
 \begin{bmatrix} 1673 \\ 1688 \\ 1666 \\ 1735 \\ 1749 \\ 1756 \\ 1815 \\ 1867 \\ 1948 \\ 2048 \\ 2128 \\ 2165 \\ 2257 \\ 2316 \\ 2324 \end{bmatrix} & = & \begin{bmatrix} 1 & 1839 & 1 \\ 1 & 1844 & 2 \\ 1 & 1831 & 3 \\ 1 & 1881 & 4 \\ 1 & 1883 & 5 \\ 1 & 1910 & 6 \\ 1 & 1969 & 7 \\ 1 & 2016 & 8 \\ 1 & 2126 & 9 \\ 1 & 2239 & 10 \\ 1 & 2336 & 11 \\ 1 & 2404 & 12 \\ 1 & 2487 & 13 \\ 1 & 2535 & 14 \\ 1 & 2595 & 15 \end{bmatrix} & \begin{bmatrix} \hat{\beta}_1 \\ \hat{\beta}_2 \\ \hat{\beta}_3 \end{bmatrix} & + & \begin{bmatrix} \hat{u}_1 \\ \hat{u}_2 \\ \hat{u}_3 \\ \hat{u}_4 \\ \hat{u}_5 \\ \hat{u}_6 \\ \hat{u}_7 \\ \hat{u}_8 \\ \hat{u}_9 \\ \hat{u}_{10} \\ \hat{u}_{11} \\ \hat{u}_{12} \\ \hat{u}_{13} \\ \hat{u}_{14} \\ \hat{u}_{15} \end{bmatrix} \\
\mathbf{y} & = & \mathbf{X} & \hat{\boldsymbol{\beta}} & + & \hat{\mathbf{u}} \\
15 \times 1 & & 15 \times 3 & 3 \times 1 & & 15 \times 1
\end{array}$$

From the preceding data we obtain the following quantities:

$$\begin{aligned}
 \bar{Y} &= 1942.333 & \bar{X}_2 &= 2126.333 & \bar{X}_3 &= 8.0 \\
 \sum(Y_i - \bar{Y})^2 &= 830,121.333 \\
 \sum(X_{2i} - \bar{X}_2)^2 &= 1,103,111.333 & \sum(X_{3i} - \bar{X}_3)^2 &= 280.0 \\
 \mathbf{X}'\mathbf{X} &= \begin{bmatrix} 1 & 1 & 1 & \dots & 1 \\ X_2 & 1 & X_2 & 2 & X_2 & 3 & \dots & X_{2n} \\ X_3 & 1 & X_3 & 2 & X_3 & 3 & \dots & X_{3n} \end{bmatrix} \begin{bmatrix} 1 & X_{21} & X_{31} \\ 1 & X_{22} & X_{32} \\ 1 & X_{23} & X_{33} \\ \vdots & \vdots & \vdots \\ 1 & X_{2n} & X_{3n} \end{bmatrix} \\
 &= \begin{bmatrix} n & \sum X_{2i} & \sum X_{3i} \\ \sum X_{2i} & \sum X_{2i}^2 & \sum X_{2i}X_{3i} \\ \sum X_{3i} & \sum X_{2i}X_{3i} & \sum X_{3i}^2 \end{bmatrix} \\
 &= \begin{bmatrix} 15 & 31,895 & 120 \\ 31,895 & 68,922.513 & 272,144 \\ 120 & 272,144 & 1240 \end{bmatrix} \\
 \mathbf{X}'\mathbf{y} &= \begin{bmatrix} 29,135 \\ 62,905,821 \\ 247,934 \end{bmatrix}
 \end{aligned}$$

Using the rules of matrix inversion given in Appendix B, one can see that

$$(\mathbf{X}'\mathbf{X})^{-1} = \begin{bmatrix} 37.232491 & -0.0225082 & 1.336707 \\ -0.0225082 & 0.0000137 & -0.0008319 \\ 1.336707 & -0.0008319 & 0.054034 \end{bmatrix}$$

Therefore,

$$\hat{\boldsymbol{\beta}} = (\mathbf{X}'\mathbf{X})^{-1}\mathbf{X}'\mathbf{y} = \begin{bmatrix} 300.28625 \\ 0.74198 \\ 8.04356 \end{bmatrix}$$

The residual sum of squares can now be computed as

$$\begin{aligned}
\sum \hat{u}_i^2 &= \hat{u}'\hat{u} \\
&= y'y - \beta'X'y \\
&= 57,420,003 - [300.28625 \quad 0.74198 \quad 8.04356] \begin{bmatrix} 29,135 \\ 62,905,821 \\ 247,934 \end{bmatrix} \\
&= 1976.85574
\end{aligned}$$

whence we obtain

$$\hat{\sigma}^2 = \frac{\hat{u}'\hat{u}}{12} = 164.73797$$

The variance-covariance matrix for $\hat{\beta}$ can therefore be shown as

$$\text{var-cov}(\hat{\beta}) = \hat{\sigma}^2(X'X)^{-1} = \begin{bmatrix} 6133.650 & 3.70794 & 220.20634 \\ 3.70794 & 0.00226 & 0.13705 \\ 220.20634 & 0.13705 & 8.90155 \end{bmatrix}$$

The diagonal elements of this matrix give the variances of $\hat{\beta}_1$, $\hat{\beta}_2$ and $\hat{\beta}_3$ respectively, and their positive square roots give the corresponding standard errors.

From the previous data, it can be readily verified that

$$\text{ESS: } \hat{\beta}'X'y - n\bar{Y}^2 = 828,144.47786$$

$$\text{TSS: } y'y - n\bar{Y}^2 = 830,121.333$$

Therefore,

$$\begin{aligned}
R^2 &= \frac{\hat{\beta}'X'y - n\bar{Y}^2}{y'y - n\bar{Y}^2} \\
&= \frac{828,144.47786}{830,121.333} \\
&= 0.99761
\end{aligned}$$

Applying the **adjusted coefficient of determination** can be seen to be

$$\bar{R}^2 = 0.99722$$

Collecting our results thus far, we have

$$\begin{aligned}
\hat{Y}_i &= 300.28625 + 0.74198X_{2i} + 8.04356X_{3i} \\
&\quad (78.31763) \quad (0.04753) \quad (2.98354) \\
t &= (3.83421) \quad (15.60956) \quad (2.69598) \\
R^2 &= 0.99761 \quad \bar{R}^2 = 0.99722 \quad df = 12
\end{aligned}$$

The interpretation of (C.10.14) is this: If both X_2 and X_3 are fixed at zero value, the average value of per capita personal consumption expenditure is estimated at about \$300. As usual, this mechanical interpretation of the intercept should be taken with a grain of salt. The partial regression coefficient of

0.74198 means that, holding all other variables constant, an increase in per capita income of, say, a dollar is accompanied by an increase in the mean per capita personal consumption expenditure of about 74 cents. In short, the marginal propensity to consume is estimated to be about 0.74, or 74 percent. Similarly, holding all other variables constant, the mean per capita personal consumption expenditure increased at the rate of about \$8 per year during the period of the study, 1956–1970. The R^2 value of 0.9976 shows that the two explanatory variables accounted for over 99 percent of the variation in per capita consumption expenditure in the United States over the period 1956–1970. Although \bar{R}^2 dips slightly, it is still very high.

Turning to the statistical significance of the estimated coefficients, we see from (C.10.14) that each of the estimated coefficients is individually statistically significant at, say, the 5 percent level of significance: The ratios of the estimated coefficients to their standard errors (that is, t ratios) are 3.83421, 15.61077, and 2.69598, respectively. Using a two-tail t test at the 5 percent level of significance, we see that the critical t value for 12 df is 2.179. Each of the computed t values exceeds this critical value. Hence, individually we may reject the null hypothesis that the true population value of the relevant coefficient is zero.

As noted previously, we cannot apply the usual t test to test the hypothesis that $\beta_2 = \beta_3 = 0$ simultaneously because the t -test procedure assumes that an independent sample is drawn every time the t test is applied. If the same sample is used to test hypotheses about β_2 and β_3 simultaneously, it is likely that the estimators $\hat{\beta}_2$ and $\hat{\beta}_3$ are correlated, thus violating the assumption underlying the t -test procedure¹. As a matter of fact, a look at the variance–covariance matrix of $\hat{\beta}$ given in (C.10.9) shows that the estimators $\hat{\beta}_2$ and $\hat{\beta}_3$ are negatively correlated (the covariance between the two is 0.13705). Hence we cannot use the t test to test the null hypothesis that $\beta_2 = \beta_3 = 0$.

But recall that a null hypothesis like $\beta_2 = \beta_3 = 0$, simultaneously, can be tested by the analysis of variance technique and the attendant F test, which were introduced in Chapter 8. For our problem, the analysis of variance table is Table C.5. Under the usual assumptions, we obtain

$$F = \frac{414,072.3893}{164.73797} = 2513.52$$

which is distributed as the F distribution with 2 and 12 df . The computed F value is obviously highly significant; we can reject the null hypothesis that $\beta_2 = \beta_3 = 0$, that is, that per capita personal consumption expenditure is not linearly related to per capita disposable income and trend. In Section C.9 we discussed the mechanics of forecasting, mean as well as individual. Assume that for 1971 the PPDI figure is \$2610 and we wish to forecast the PPCE corresponding to this figure. Then, the mean as well as individual forecast of PPCE for 1971 is the same and is given as

$$\begin{aligned} (PPCE_{1971}|PPDI_{1971}, X_3 = 16) &= x'_{1971}\hat{\beta} \\ &= [1261016] \begin{bmatrix} 300.28625 \\ 0.74198 \\ 8.04356 \end{bmatrix} \\ &= 2365.55 \end{aligned}$$

where use is made of (C.9.3). The variances of \hat{Y}_{1971} and \hat{Y}_{1971} , as we know from Section C.9, are different and are as follows:

$$\begin{aligned} var(\hat{Y}_{1971}|x'_{1971}) &= \hat{\sigma}^2[x'_{1971}(X'X)^{-1}x_{1971}] \\ &= 164.73797 \begin{bmatrix} 1 & 2610 & 16 \end{bmatrix} (X'X)^{-1} \begin{bmatrix} 1 \\ 2610 \\ 16 \end{bmatrix} \end{aligned}$$

where $(X'X)^{-1}$ is as shown in (C.10.5). Substituting this into (C.10.17), the reader should verify that

$$var(\hat{Y}_{1971}|x'_{1971}) = 48.6426$$

¹See Sec. 8.5 for details.

Table 2: THE ANOVA TABLE FOR THE DATA OF TABLE C.4

Source of variation	SS	df	MSS
Due to X2,X3	828,144.47786	2	414,072.3893
Due to residuals	1,976.85574	<u>12</u>	164.73797
Total	830,121.33360	14	

and therefore

$$se(\hat{Y}_{1971}|x'_{1971}) = 6.9744$$

We leave it to the reader to verify, using (C.9.6), that

$$var(Y_{1971}|x'_{1971}) = 14.6076$$

Note: $var(Y_{1971}|x'_{1971}) = E[Y_{1971} - \hat{Y}_{1971}|x'_{1971}]^2$. In Section C.5 we introduced the correlation matrix R . For our data, the correlation matrix is as follows:

	Y	X ₂	X ₃
Y	1	0.9980	0.9743
X ₂	0.9980	1	0.9664
X ₃	0.9743	0.9664	1

Note that in (C.10.20) we have bordered the correlation matrix by the variables of the model so that we can readily identify which variables are involved in the computation of the correlation coefficient. Thus, the coefficient 0.9980 in the first row of matrix (C.10.20) tells us that it is the correlation coefficient between Y and X_2 (that is, r_{12}). From the zero-order correlations given in the correlation matrix (C.10.20) one can easily derive the first-order correlation coefficients. (See exercise C.7.)

2 Using Excel for matricial approach, Gujarati Appendix C

References

- [1] Gujarati, D.,N. **Basic Econometrics**, fourth edition, McGraw-Hill/Irwin.