MM209 Programming Assignment (Report)

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Group members:

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P7) Write a program which will generate phase diagram for Al2O3-Cr2O3 isomorphous system. Assume ideal solution for both solid and liquid phases.

Assumptions:

- 1. Solid and liquid phases form ideal solutions (Given) i.e., ideal solution model and complete miscibility in solid and liquid phases can be assumed.
- 2. Total Pressure = 1atm
- 3. Phase diagram is the 2D representation with composition of solutions (mol fraction (X)) along x axis and Temperature (in Kelvin) along y axis.
- 4. The $delC_p$ for pure solid = liquid eqm is 0 J/K/mol.

• Methodology/Principle used for solving the above problem:

- Since the system is isomorphous (Given), delH_{mix}=0 Joules/mol for the solution. The solid and liquid phases follow ideal model solution. This is why, this system gives the most ideal and simplest phase diagram as shown in the graph below.
- The delGO for pure liquid ≒ solid eqm is zero only at the melting temperature of pure solid. In a two-component system, equilibrium can be achieved at any temperature between the melting temperatures of two pure solids.
- The equations below explain that at any Temp (T) between T_{melting} of pure solids, equilibrium between solid and liquid can be achieved which results in different compositions of solid phase and liquid phase at T.

$$Cr_2O_{3 (s)} \stackrel{\longleftarrow}{\hookrightarrow} Cr_2O_{3(l)}$$
 -(i)
 $Al_2O_{3 (s)} \stackrel{\longleftarrow}{\hookrightarrow} Al_2O_{3 (l)}$ - (ii)

 $delC_p = 0 J/K/mol$ (for above equilibrium equations)

del G0 Melting,
$$Cr2O3$$
 = del H0 Melting, $Cr2O3$ - T(del H0 Melting, $Cr2O3$ / Tmelting, $Cr2O3$) del G0 Melting, $Al2O3$ = del H0 Melting, $Al2O3$ - T(del H0 Melting, $Al2O3$ / Tmelting, $Al2O3$)

del
$$G_1$$
 = del G_0 Melting, C_{r2O3} + RT $In(a_{C_{r2O3(1)}}/a_{C_{r2O3(s)}})$ for eqn(i)

since, the liquid solution and solid solution both are ideal and P_T is 1 atm we can write $a_{Cr2O3(s)}=X_{Cr2O3(s)}$

$$a_{Cr2O3(I)} = X_{Cr2O3(I)}$$

At equilibrium del G = 0; this gives us the following equation;

$$del G_1 = del GO_{Melting, Cr2O3} + RT ln (X_{Cr2O3(I)} / X_{Cr2O3(s)}) = 0$$
 -(iii)

Similarly, using

$$X_{A12O3(s)} + X_{Cr2O3(s)} = 1$$

$$X_{A12O3(I)} + X_{Cr2O3(I)} = 1$$

we obtain;

$$del G_2 = del GO_{Melting, Al2O3} + RT \ln((1-X_{Cr2O3(I)})/(1-X_{Cr2O3(S)})) = 0 -(iv)$$

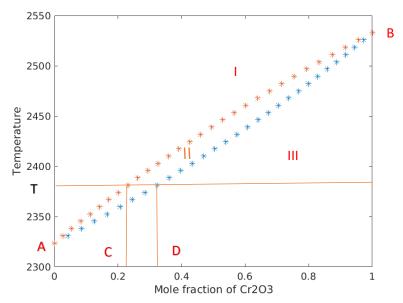
- At any temp (T), we can obtain different equilibrium compositions $(X_{Cr2O3(I)})$ of the solid $(X_{2O3(s)})$ and liquid solutions respectively from equation (iii) and (iv).
- This makes us possible to get the phase diagram for such system as shown below.

• Phase diagram plot:

(We have used MATLAB to obtain the phase diagram plot.)

- Numerical Data used includes
 - 1. $delH_{melting (Al2O3)} = 107500 J/mol$
 - 2. delH_{melting (Cr2O3)} = 117400 J/mol
 - 3. $delS_{melting (Al2O3)} = 46.26 J/ K/mol$
 - 4. $delS_{melting (Cr2O3)} = 46.35 J/K/mol$
- Source for numerical data:

INTRODUCTION TO THE THERMODYNAMICS OF MATERIALS (FOURTH EDITION)-David R. Gaskell



• Explanations of the plots and results:

- Region I is a single-phase region (Liquid) with degrees of freedom, F=1.
- Region II is two phases region (Liquid [←] Solid) with F=2.
- Region III is single phase region with F=1.
- Line separating regions I and II is called liquidus and line separating regions II and III is called solidus.
- Point A on y axis is $T_{Melting}$ of Al_2O_3 and point B is $T_{Melting}$ of Cr_2O_3
- The plot shows mol fraction of Cr2O3 along x axis and temperature (in Kelvin) along y axis.
- At temp T as shown by red horizontal line, we obtain different equilibrium compositions for solid and liquid phase respectively.
- Eqm value of $X_{Cr2O3(I)}$ i.e., (liquid eqm composition) is given by point C on x axis and $X_{Cr2O3(s)}$ i.e., (solid eqm composition) is given by point D on x axis.
- Therefore, at Temp T if we fix the eqm composition of solid solution we obtain a fixed eqm composition for liquid solution and vice-versa.

• Contributions made by each member:

- Each member contributed equally in developing the code and worked on getting the methodology right for the problem.
- Sahensu Soni (190110078) researched and obtained the numerical data needed.
- Rhythm Shah (190110074) created the final code and obtained the plots.
- Neha Parasharam Jadhav (190110053) worked on the explanations of the results, plots and made the final report.

• Github link to the project:

https://github.com/rhythm-shah/MM209CodingAssignment