

# Programmable Logic Devices

A programmable logic device is an integrated circuit capable of implementing logic functions.

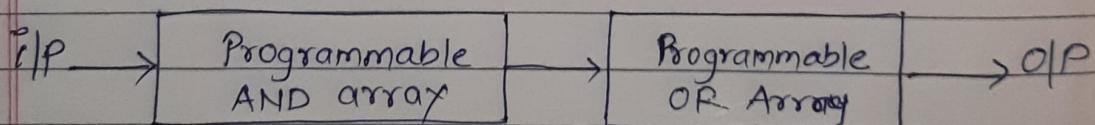
The main advantage of PLD is that they can replace a number of circuits in many applications.

## Classification of PLD's

- ① Programmable Logic Array (PLA)
- ② Programmable Array Logic (PAL)
- ③ Programmable Read Only Memory (PROM)

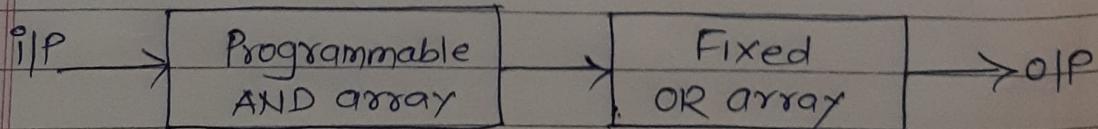
## Programmable Logic Array (PLA)

PLA is a logic device with both AND and OR arrays programmable.



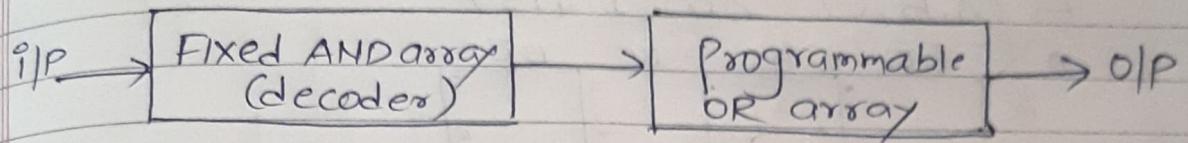
## Programmable Array Logic (PAL)

PAL is a logic device with programmable AND array & a fixed OR array.

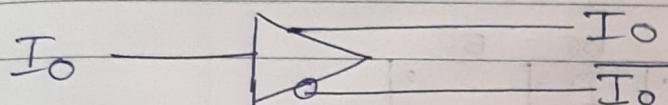


## Programmable Read only Memory (PROM)

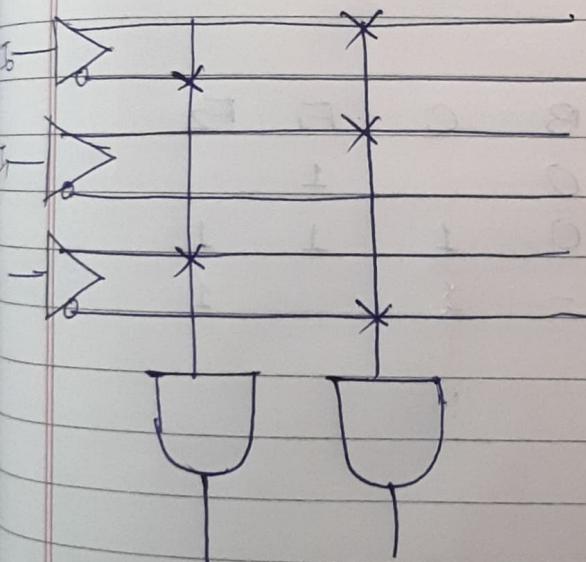
It has a fixed AND array that is constructed as a decoder and a programmable OR array.



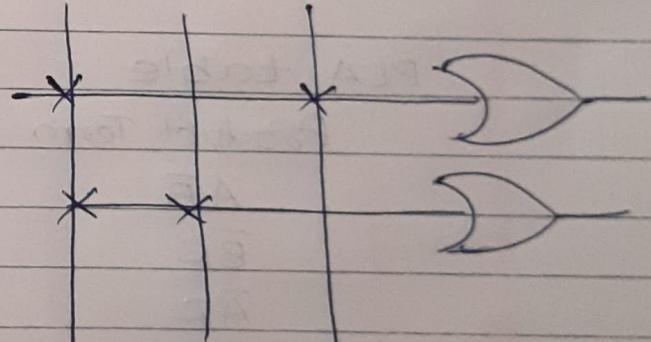
Input buffer



AND matrix



OR matrix



# Programmable Logic Array (PLA)

A combinational circuit is defined by function

$$F_1(A, B, C) = \sum m(1, 4, 5)$$

$$F_2(A, B, C) = \sum m(1, 3, 5)$$

Implement circuit with PLA.

$$F_1(A, B, C) = \sum m(1, 4, 5)$$

	$\bar{B}\bar{C}$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	•	(1)	•	•
A	(1)	4	(1)	5
	7	6		

$$F_1 = A\bar{B} + \bar{B}C$$

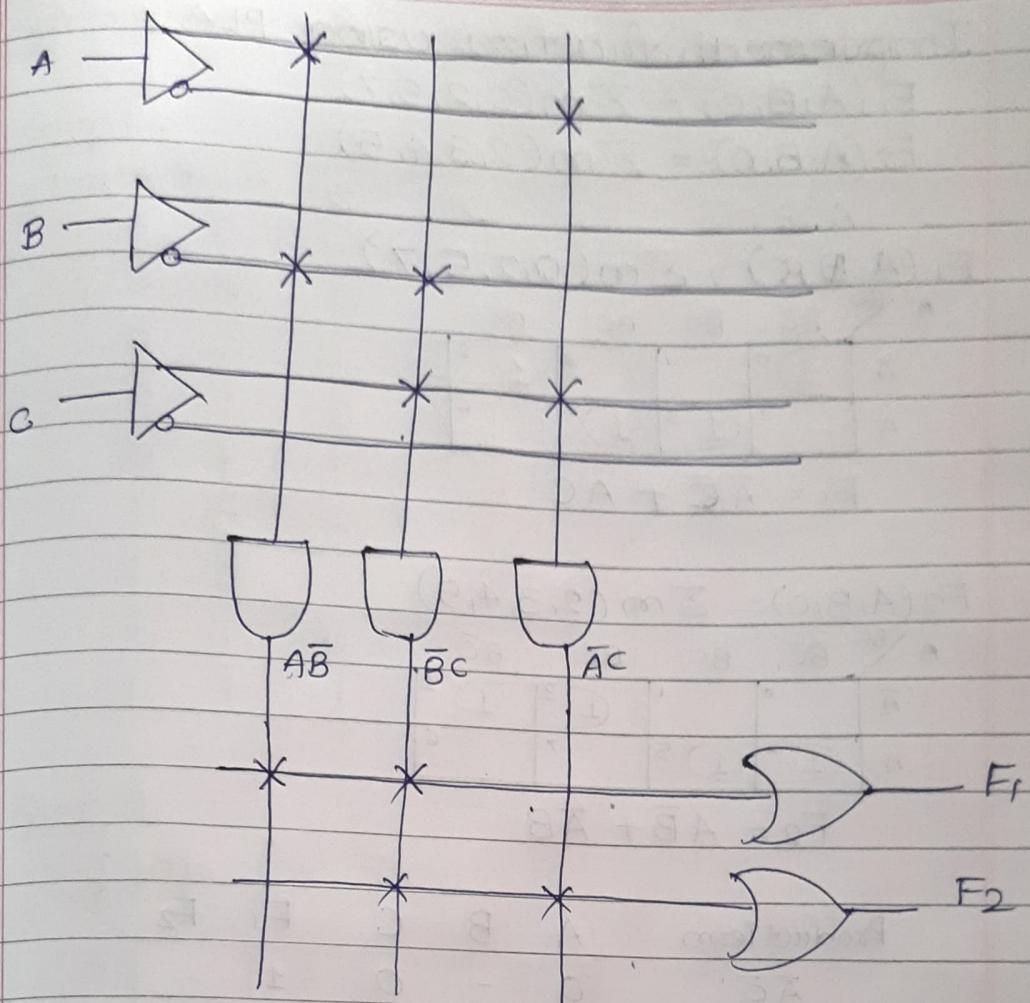
$$F_2(A, B, C) = \sum m(1, 3, 5)$$

	$\bar{B}C$	$\bar{B}C$	$BC$	$B\bar{C}$
$\bar{A}$	•	(1)	(1)	3
A	4	1	5	6
	7			2

$$F_2 = \bar{B}C + \bar{A}C$$

PLA table

Product Term	A	B	C	$F_1$	$F_2$
$A\bar{B}$	1	0	-	1	-
$\bar{B}C$	-	0	1	1	1
$\bar{A}C$	0	-	1	-	1



Implement function using PLA

$$F_1(A, B, C) = \sum m(0, 2, 5, 7)$$

$$F_2(A, B, C) = \sum m(2, 3, 4, 5)$$

$$F_1(A, B, C) = \sum m(0, 2, 5, 7)$$

	$\bar{B}C$	$\bar{B}C$	$BC$	$BC$
$A$	1	0	1	2
$A$	4	5	1	6

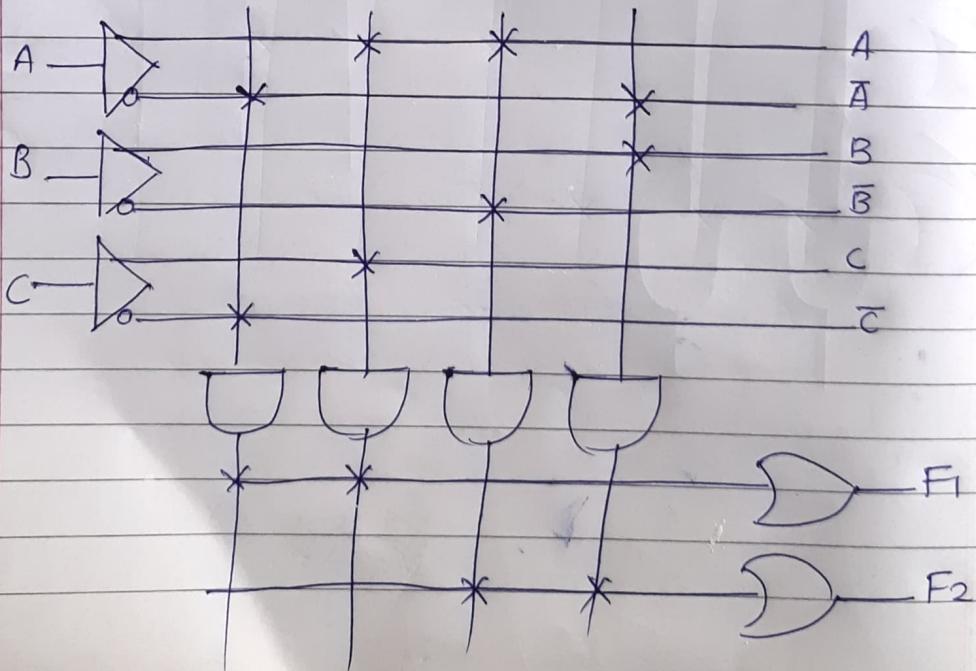
$$F_1 = \bar{A}\bar{B} + AC$$

$$F_2(A, B, C) = \sum m(2, 3, 4, 5)$$

	$\bar{B}C$	$\bar{B}C$	$BC$	$BC$
$\bar{A}$	0	1	3	2
$A$	1	4	5	6

$$F_2 = A\bar{B} + \bar{A}B$$

Product Term	A	B	C	$F_1$	$F_2$
$\bar{A}C$	0	-	0	1	
$AC$	1	-	1	1	
$A\bar{B}$	1	0	-		1
$\bar{A}B$	0	1	-		1



# Implement full Adder using PLA

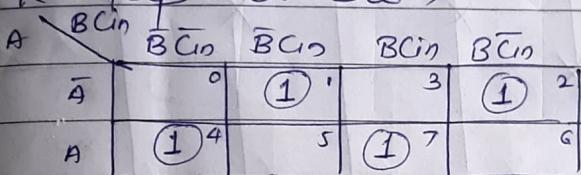
## Step 1

Truth Table

A	B	Cin	Sum	Cout
0	0	0	0	0
0	0	1	1	0
0	1	0	1	0
0	1	1	0	1
1	0	0	1	0
1	0	1	0	1
1	1	0	0	1
1	1	1	1	1

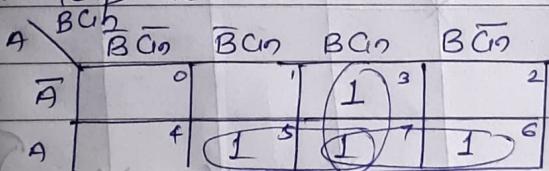
## Step 2

K-Map for Sum



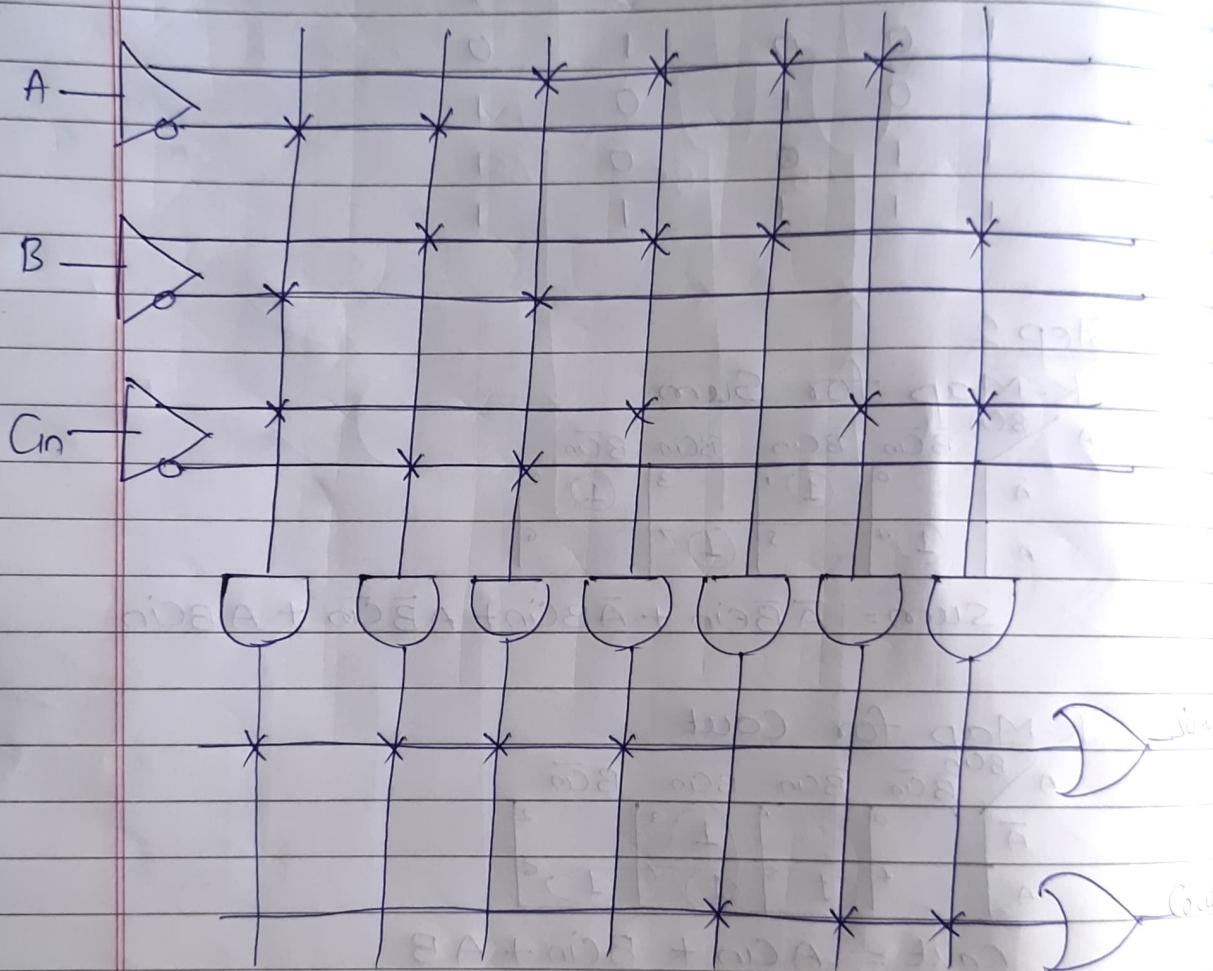
$$\text{Sum} = \bar{A}\bar{B}C_{in} + \bar{A}BC_{in} + A\bar{B}\bar{C}_{in} + ABC_{in}$$

K-Map for Cout



$$\text{Cout} = AC_{in} + BC_{in} + AB$$

Product Term	A	B	Cin	Sum	Cout
$\bar{A} \bar{B} \text{Cin}$	0	0	1	1	-
$\bar{A} B \bar{\text{Cin}}$	0	1	0	1	-
$A \bar{B} \bar{\text{Cin}}$	1	0	0	1	-
$A B \text{Cin}$	1	1	1	1	-
$AB$	1	1	-	-	1
$A \text{Cin}$	1	-	1	-	1
$B \text{Cin}$	-	1	1	1	-



Implement following function using PLA

$$F_1(A, B, C, D) = \sum m(3, 7, 8, 9, 11, 15)$$

$$F_2(A, B, C, D) = \sum m(3, 4, 5, 7, 10, 14, 15)$$

### Step 1

K-Map for  $F_1$

AB \ CD	$\bar{C}\bar{D}$	$\bar{C}D$	$C\bar{D}$	$CD$	
$\bar{A}\bar{B}$	0	1	1	3	2
$\bar{A}B$	4	5	1	7	6
$A\bar{B}$	12	13	1	15	14
$AB$	1	8	1	11	10

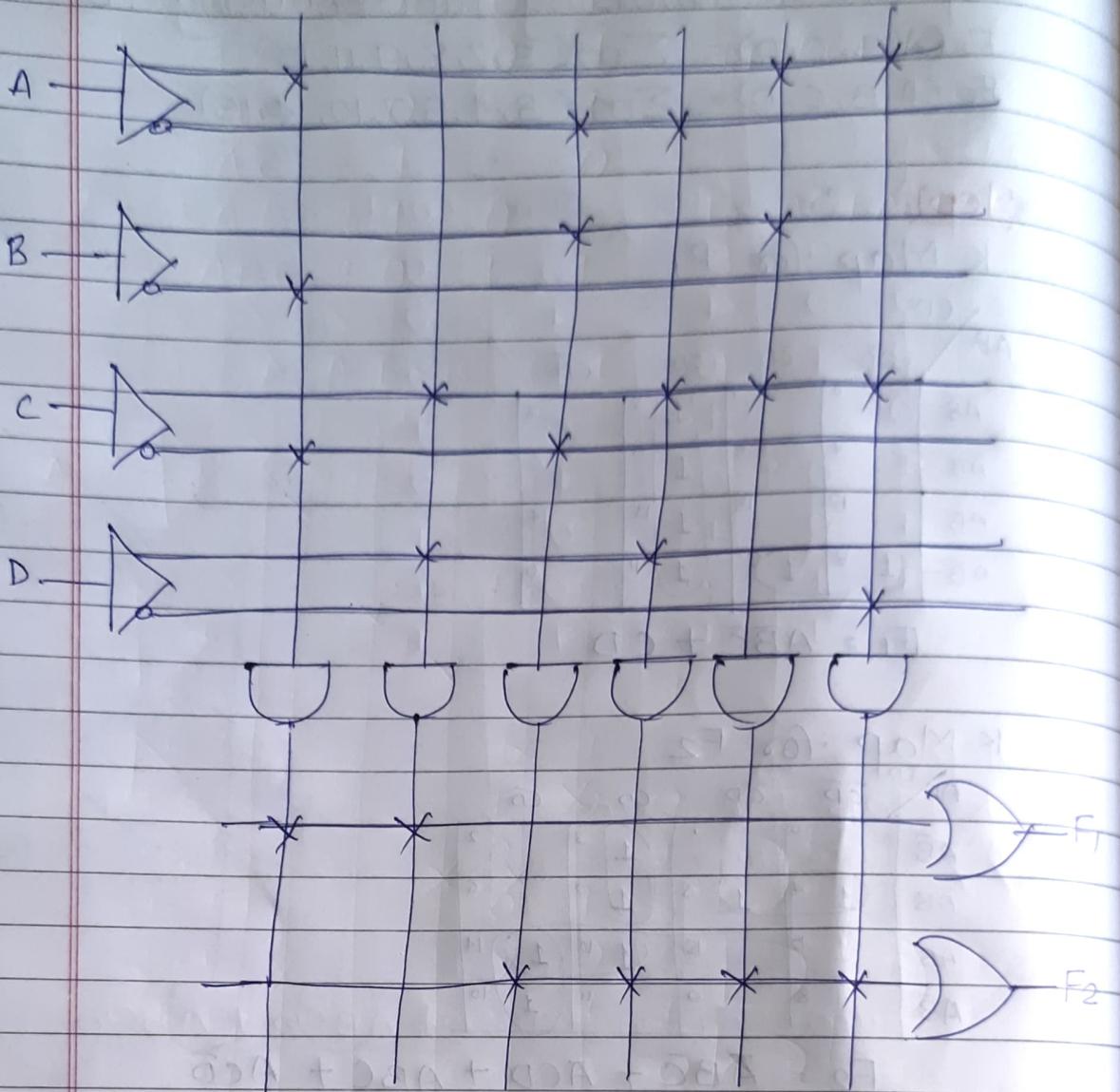
$$F_1 = A\bar{B}\bar{C} + CD$$

K-Map for  $F_2$

AB \ CD	$\bar{C}\bar{D}$	$\bar{C}D$	$C\bar{D}$	$CD$	
$\bar{A}\bar{B}$	0	1	1	3	2
$\bar{A}B$	1	4	1	5	1
$A\bar{B}$	12	13	1	15	1
$AB$	8	9	11	1	10

$$F_2 = \bar{A}B\bar{C} + ACD + ABC + AC\bar{D}$$

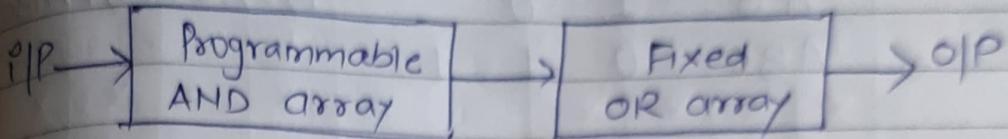
Product Term	A	B	C	D	$F_1$	$F_2$
$A\bar{B}\bar{C}$	1	0	0	-	1	
$CD$	-	-	1	1		1
$\bar{A}B\bar{C}$	0	1	0	-	-	1
$\bar{A}CD$	0	-	1	1	-	1
$ABC$	1	1	1	-	-	1
$AC\bar{D}$	1	-	1	1	-	1



S E D O B A M T H I S  
I - O D P C B A  
I - I I - B C D  
I - O I P C B A  
I - I I - B C B  
I - I I - B C B  
I - I I - B C B

## Programmable Array Logic (PAL)

It is a programmable logic device that has programmable AND array & fixed OR array



Implement the following function using PAL

$$F_1(A, B, C) = \sum m(0, 1, 3, 4)$$

$$F_2(A, B, C) = \sum m(3, 4, 5, 6)$$

Step 1

K-Map for  $F_1$

		BC	$\bar{B}\bar{C}$	$\bar{B}C$	BC	$B\bar{C}$	
		A	0	1	1	3	2
		A	1	4	5	7	6

$$F_1 = \bar{B}\bar{C} + \bar{A}C$$

K-Map for  $F_2$

		BC	$\bar{B}\bar{C}$	$\bar{B}C$	BC	$B\bar{C}$	
		A	0	1	(1) <sup>3</sup>	2	
		A	1	4	5	7	(1) <sup>6</sup>

$$F_2 = A\bar{C} + A\bar{B} + \bar{A}BC$$

Product Term A B C O/P

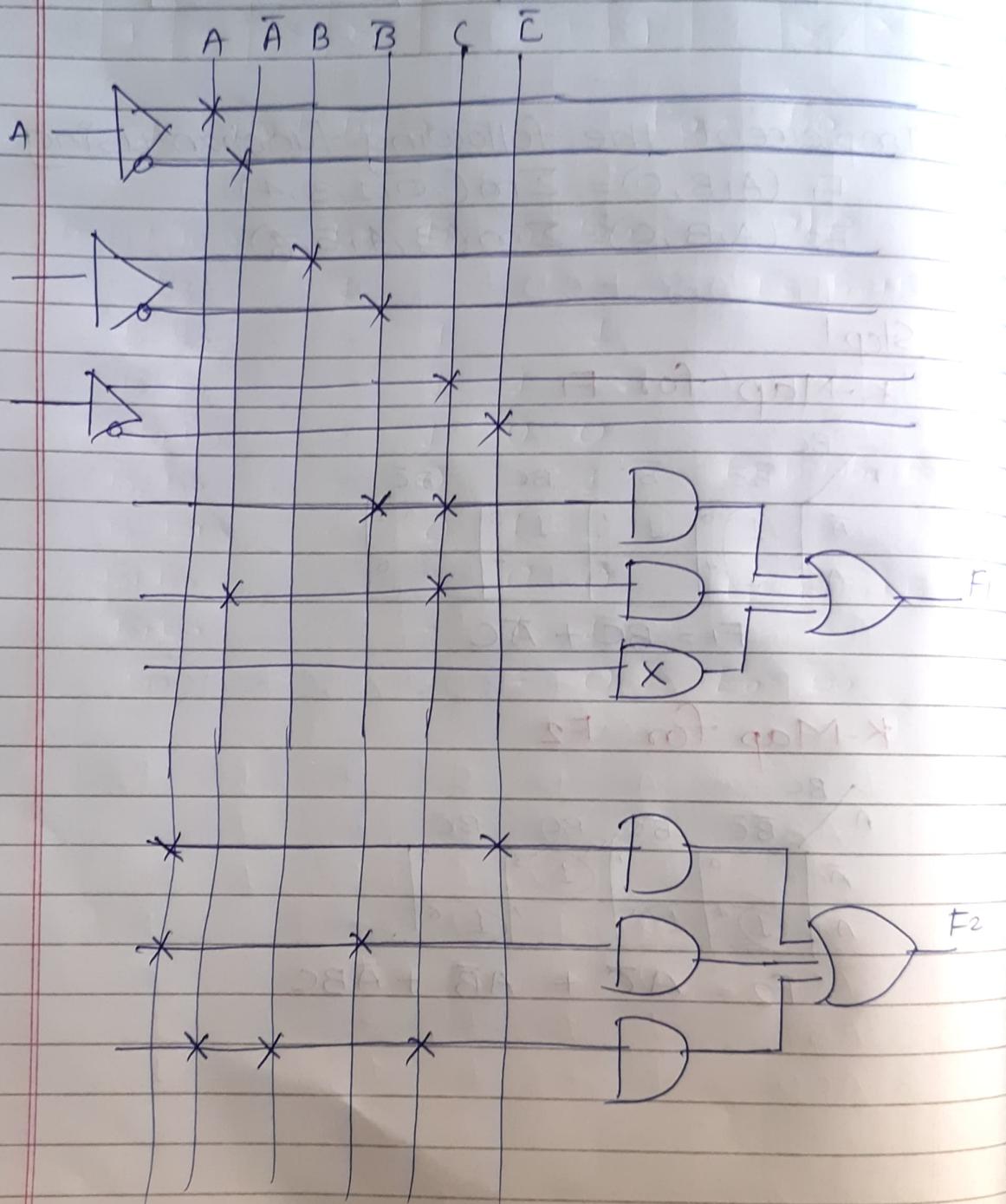
$$\bar{B}C \quad - \quad 0 \quad 1 \quad F_1 = \bar{B}C + \bar{A}C$$

$$\bar{A}C \quad 0 \quad - \quad 1 \quad F_1 = \bar{B}C + \bar{A}C$$

$$A\bar{C} \quad 1 \quad - \quad 0 \quad F_2 = A\bar{C} + AB + \bar{A}BC$$

$$AB \quad 1 \quad 0 \quad F_2 = A\bar{C} + AB + \bar{A}BC$$

$$\bar{A}BC \quad 0 \quad 1 \quad 1 \quad F_2 = A\bar{C} + AB + \bar{A}BC$$



Design BCD to Excess-3 code converter using PAL

### Step 1 Truth Table

Decimal	BCD				Excess-3			
	B <sub>3</sub>	B <sub>2</sub>	B <sub>1</sub>	B <sub>0</sub>	E <sub>3</sub>	E <sub>2</sub>	E <sub>1</sub>	E <sub>0</sub>
0	0	0	0	0	0	0	1	1
1	0	0	0	1	0	1	0	0
2	0	0	1	0	0	1	0	1
3	0	0	1	1	0	1	1	0
4	0	1	0	0	0	1	1	1
5	0	1	0	1	1	0	0	0
6	0	1	1	0	1	0	0	1
7	0	1	1	1	1	0	1	0
8	1	0	0	0	1	1	0	1
9	1	0	0	1	1	1	0	0

### Step 2

K-Map for E<sub>3</sub>

B <sub>1</sub> , B <sub>0</sub>		B <sub>3</sub> , B <sub>2</sub>			
		̄B <sub>1</sub> ̄B <sub>0</sub>	B <sub>1</sub> ̄B <sub>0</sub>	B <sub>1</sub> B <sub>0</sub>	̄B <sub>1</sub> B <sub>0</sub>
̄B <sub>3</sub> ̄B <sub>2</sub>	0	0	1	1	2
̄B <sub>3</sub> B <sub>2</sub>	4	1	5	1	6
B <sub>3</sub> ̄B <sub>2</sub>	X <sup>12</sup>	X <sup>13</sup>	X <sup>15</sup>	X <sup>14</sup>	
B <sub>3</sub> B <sub>2</sub>	1 <sup>8</sup>	1 <sup>9</sup>	X <sup>11</sup>	X <sup>10</sup>	

K-Map for E<sub>2</sub>

B <sub>1</sub> , B <sub>0</sub>		B <sub>3</sub> , B <sub>2</sub>			
		̄B <sub>1</sub> ̄B <sub>0</sub>	B <sub>1</sub> ̄B <sub>0</sub>	B <sub>1</sub> B <sub>0</sub>	̄B <sub>1</sub> B <sub>0</sub>
̄B <sub>3</sub> ̄B <sub>2</sub>	0	1	1	3	1
̄B <sub>3</sub> B <sub>2</sub>	(1) <sup>4</sup>		5	7	6
B <sub>3</sub> ̄B <sub>2</sub>	(X) <sup>12</sup>	X <sup>13</sup>	X <sup>15</sup>	X <sup>14</sup>	
B <sub>3</sub> B <sub>2</sub>	X <sup>8</sup>	1 <sup>9</sup>	X <sup>11</sup>	X <sup>10</sup>	

$$E_3 = B_3 + B_2 B_0 + B_2 B_1$$

$$E_2 = B_2 \bar{B}_1 \bar{B}_0 + \bar{B}_2 B_0 +$$

$$\bar{B}_2 B_1$$

K-Map for E<sub>1</sub>

		B <sub>1</sub> B <sub>0</sub>	B <sub>1</sub> $\bar{B}_0$	$\bar{B}_1$ B <sub>0</sub>	$\bar{B}_1\bar{B}_0$
		B <sub>3</sub> B <sub>2</sub>	$\bar{B}_3$ B <sub>2</sub>	B <sub>3</sub> $\bar{B}_2$	$\bar{B}_3\bar{B}_2$
B <sub>3</sub>	B <sub>2</sub>	1	0	1	3
$\bar{B}_3$	B <sub>2</sub>	1	4	5	7
B <sub>3</sub>	$\bar{B}_2$	X	X	X	X
$\bar{B}_3$	$\bar{B}_2$	1	8	9	10

$$E_1 = \bar{B}_1\bar{B}_0 + B_1B_0$$

K-Map for E<sub>0</sub>

		B <sub>1</sub> B <sub>0</sub>	B <sub>1</sub> $\bar{B}_0$	$\bar{B}_1$ B <sub>0</sub>	$\bar{B}_1\bar{B}_0$
		B <sub>3</sub> B <sub>2</sub>	$\bar{B}_3$ B <sub>2</sub>	B <sub>3</sub> $\bar{B}_2$	$\bar{B}_3\bar{B}_2$
B <sub>3</sub>	B <sub>2</sub>	1	0	1	3
$\bar{B}_3$	B <sub>2</sub>	1	4	5	7
B <sub>3</sub>	$\bar{B}_2$	X	X	X	X
$\bar{B}_3$	$\bar{B}_2$	1	8	9	10

$$E_0 = \bar{B}_0$$

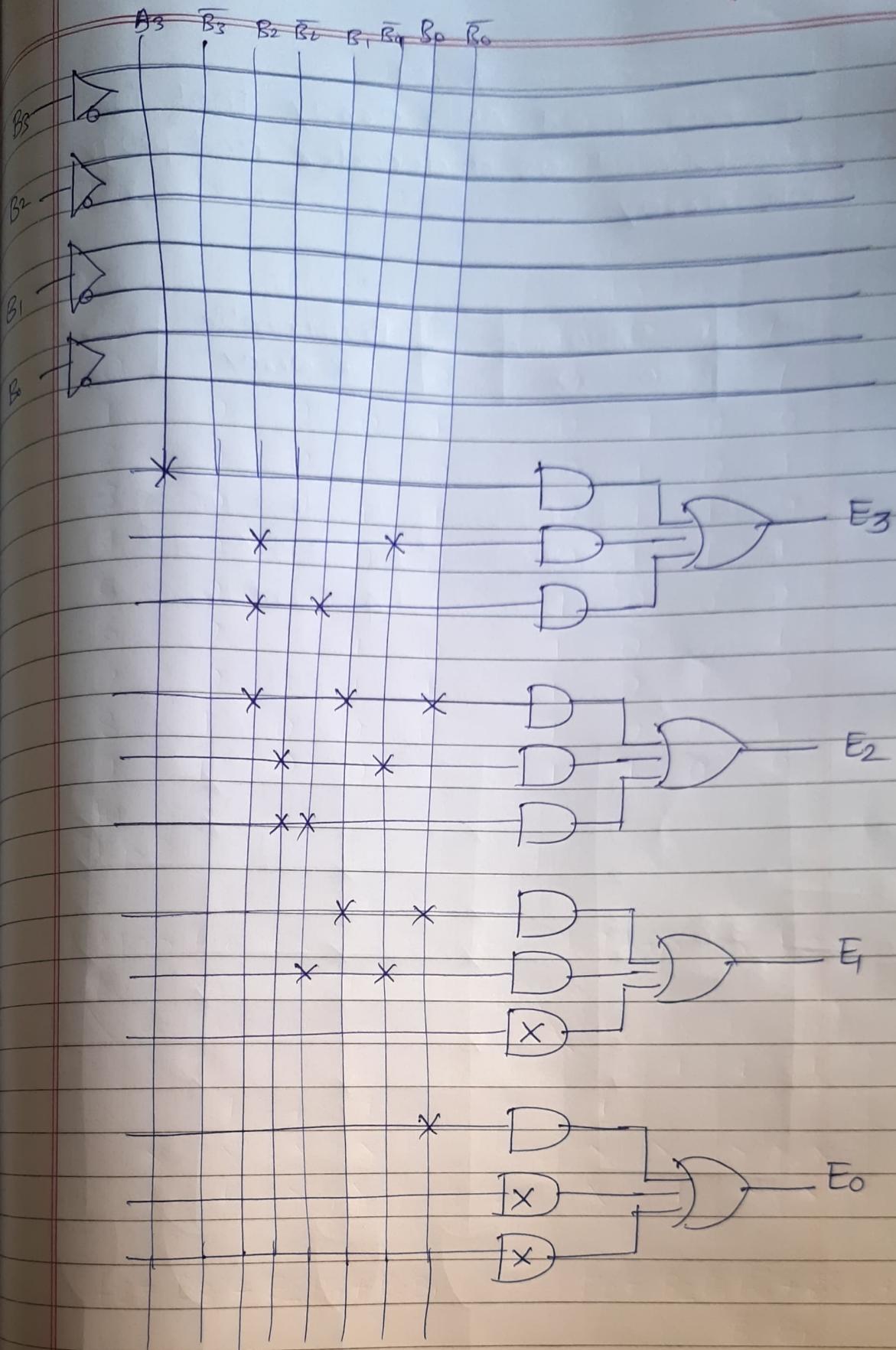
Product Term

B<sub>3</sub> B<sub>2</sub> B<sub>1</sub> B<sub>0</sub>

0 | P

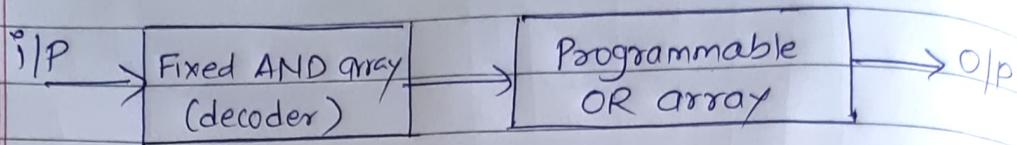
B <sub>3</sub>	1	-	1	-	0	E <sub>3</sub> = B <sub>3</sub> + B <sub>2</sub> B <sub>0</sub> + B <sub>2</sub> $\bar{B}_0$
B <sub>2</sub> B <sub>0</sub>	-	1	-	1	1	
B <sub>2</sub> B <sub>1</sub>	-	1	1	-	1	
B <sub>2</sub> $\bar{B}_1$ B <sub>0</sub>	-	1	0	0	1	
$\bar{B}_2$ B <sub>0</sub>	-	0	-	1	0	E <sub>2</sub> = B <sub>2</sub> $\bar{B}_1$ B <sub>0</sub> + B <sub>2</sub> B <sub>0</sub> + B <sub>2</sub> $\bar{B}_0$
$\bar{B}_2$ B <sub>1</sub>	-	0	1	-	0	
B <sub>1</sub> $\bar{B}_0$	-	-	0	0	0	E <sub>1</sub> = B <sub>1</sub> $\bar{B}_0 + B1B0$
B <sub>1</sub> B <sub>0</sub>	-	-	1	1	0	
$\bar{B}_0$	-	-	-	0	0	E <sub>0</sub> = $\bar{B}_0$

$$(B_3 + B_2B_0 + B_2\bar{B}_0) + (B_1\bar{B}_0 + B_1B_0) + \bar{B}_0 = E$$



## Programmable ROM

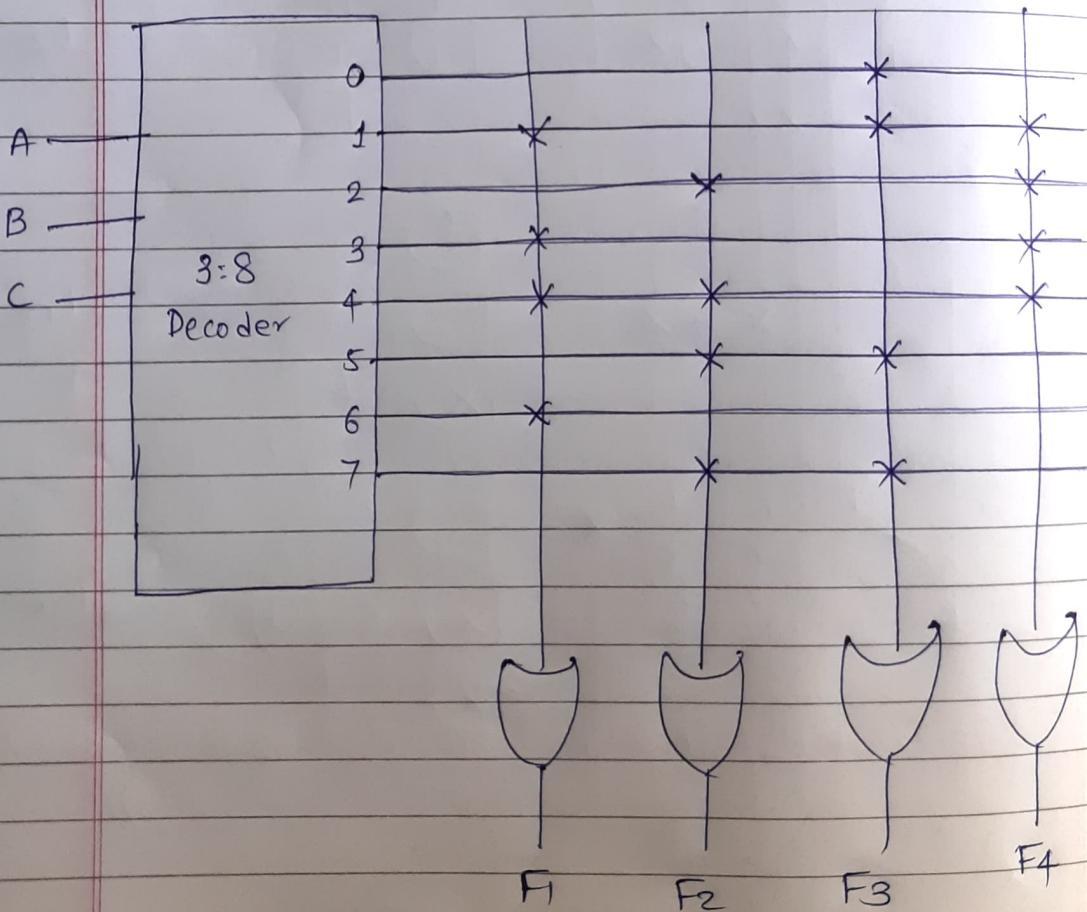
It has fixed AND array that is constructed as a decoder and programmable OR array.



Implement following function using PROM.

$$F_1 = \sum m(1, 3, 4, 6) \quad F_2 = \sum m(2, 4, 5, 7)$$

$$F_3 = \sum m(0, 1, 5, 7) \quad F_4 = \sum m(1, 2, 3, 4)$$



Design 3 bit Binary to Gray code converter using PROM.

### Step 1 Truth Table

	Binary Code			Gray Code		
	B <sub>2</sub>	B <sub>1</sub>	B <sub>0</sub>	G <sub>2</sub>	G <sub>1</sub>	G <sub>0</sub>
0	0	0	0	0	0	0
1	0	0	1	0	0	1
2	0	1	0	0	1	1
3	0	1	1	0	1	0
4	1	0	0	1	1	0
5	1	0	1	1	1	1
6	1	1	0	1	0	1
7	1	1	1	1	0	0

$$G_2 = \sum m(4, 5, 6, 7)$$

$$G_1 = \sum m(2, 3, 4, 5)$$

$$G_0 = \sum m(1, 2, 5, 6)$$

