

In this project, We worked on Denoising Diffusion Probabilistic Models (DDPMs) implementation, as well as performing several application such as sample generation and image inpainting. The model proposed extends score-based modeling by incorporating a time-dependent noise schedule and a reverse denoising process to generate high-quality samples.

## Modeling

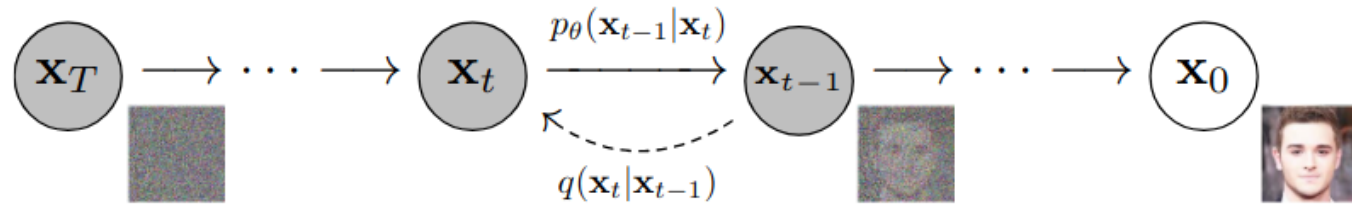


Figure : Directed graphical diffusion model introduced in [1]

- **Forward process** : Add Gaussian noise to the input data step-by-step until it becomes pure noise

$$q(x_t | x_{t-1}) := \mathcal{N}(x_t; (1-\beta_t)x_{t-1}, \beta_t I)$$

- **Reverse process** : Reverse the noising process to recover the original data

$$p_\theta(x_{t-1} | x_t) := \mathcal{N}(x_{t-1}; \mu_\theta(x_t, t), \Sigma_\theta(x_t, t))$$

where  $\beta_t$  represents the noise scheduler

- **Variational Objective / ELBO** :

$$\mathcal{L}_{\text{simple}} = \mathbb{E}_{t \sim [1, T]} \mathbb{E}_{x_0 \sim q(x_0)} \mathbb{E}_{\epsilon_t \sim \mathcal{N}(0, I)} [\|\epsilon_t - \epsilon_\theta(x_t, t)\|^2]$$

where  $\epsilon_t$  represents the true noise

## Experiments

- **Selecting schedulers**

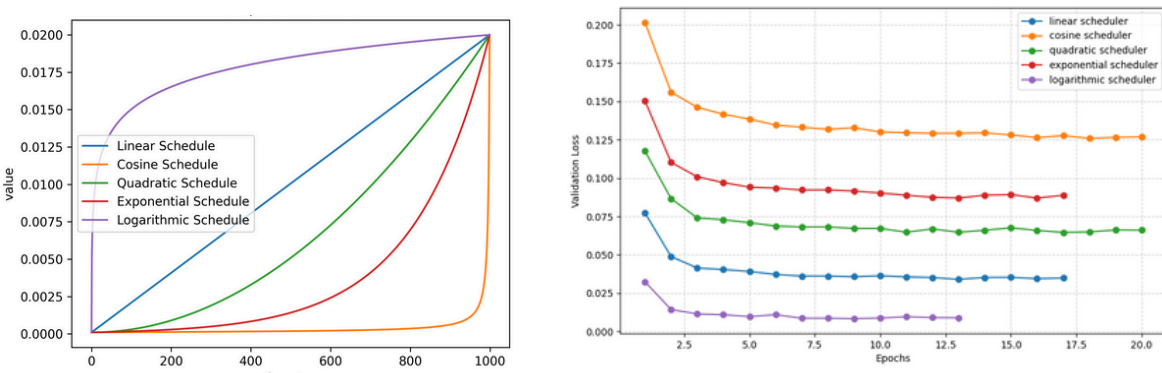


Figure : Shape of the five test schedulers on left, MSE validation on the right.

- **Hyperparameter Tuning using Bayesian Optimization**

Dataset	T	beta_min	beta_max	Best Loss
Fashion	1757	0.0007645481	0.0328679383	0.01454419
CIFAR	1132	0.0004998979	0.0387503176	0.02055065
MNIST	1722	0.0000252098	0.0479183811	0.01064030

Table : Results of hyperparameter tuning (diffusion using Linear Scheduler).

Dataset	T	beta_min	beta_max	Best Loss
Fashion	1927	1.1146056 - 05	0.041009289	0.00310464
CIFAR	1931	6.4127417 - 05	0.042472445	0.00290811
MNIST	1931	0.0003399997	0.039108512	0.00201147

Table : Results of hyperparameter tuning (diffusion using Log Scheduler).

- **Neural Network Architecture:**

- UNET architecture containing Convolutional layers, residual blocks, DownSampling and UpSampling blocks.
- Same UNET with additional attention blocks after the DownSampling and UpSampling blocks

## Sampling

The reverse process is used :

- sample random noise  $x_T \sim \mathcal{N}(0, I)$

- remove the noise using the reverse process

$$x_{t-1} = \frac{1}{\sqrt{1-\beta_t}} \left( x_t - \frac{\beta_t}{\sqrt{1-\beta_t}} \epsilon_\theta(x_t, t) \right) + \sigma_t z$$

- After T iterations, the final output is the denoised data sample

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## RePainting (Linear vs Log scheduler)

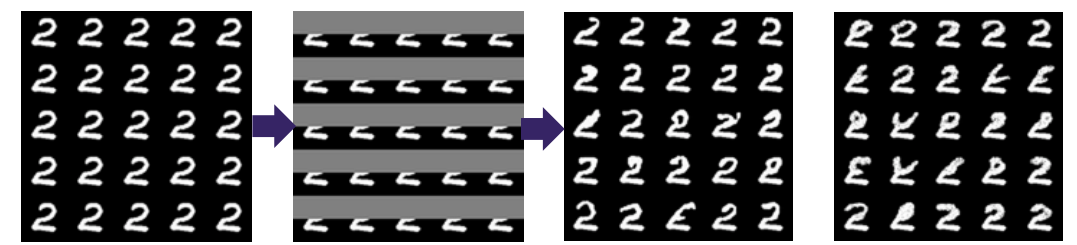


Figure : MNIST samples: original, masked, repainted (Linear scheduler), repainted (Log scheduler) in order.

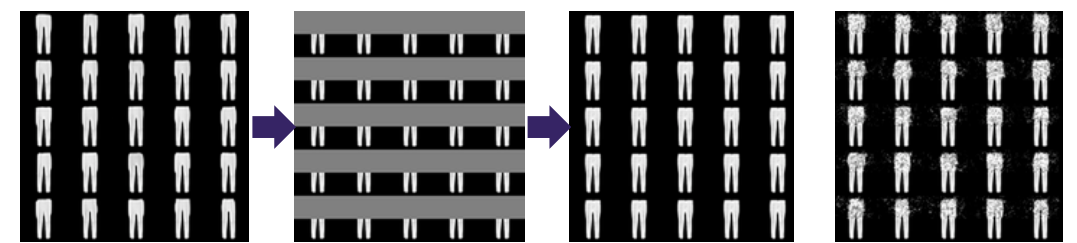


Figure : Fashion-MNIST samples: original, masked, repainted (Linear scheduler), repainted (Log scheduler) in order.



Figure : CIFAR samples: original, masked, repainted (Linear scheduler), repainted (Log scheduler) in order.

## RePainting (U-Net w/wo Attention)

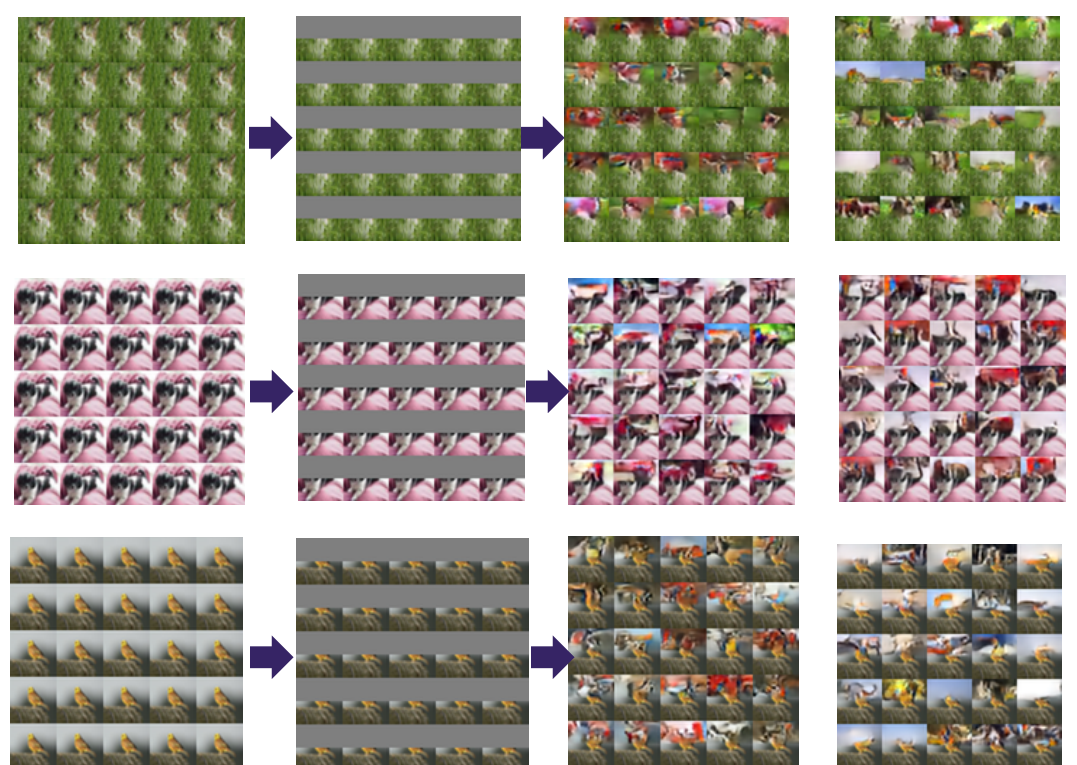


Figure : CIFAR samples: original, masked, simple UNET, UNET with Attention

## Discussion

- The linear and Logarithmic schedulers perform better than the other schedulers based on validation data.
- The logarithmic scheduler introduces more noise in the generated samples as well as the repainted samples, compared to the linear scheduler.
- The attention-based UNet generates inpainted regions that are more consistent with the global distribution of the image, compared to the basic UNet model.
- Including the FID score during training will provide a better evaluation of the generated images' quality with respect to the global distribution of the data.
- Including class labels will improve model performance.

## References

- [1] **Ho Jonathan, Ajay Jain, and Pieter Abbeel.** "Denoising diffusion probabilistic models.", *NeurIPS 2020*
- [2] **A. Lugmayr, M. Danelljan, A. Romero, F. Yu, R. Timofte, and L. Van Gool.** "RePaint: Inpainting using Denoising Diffusion Probabilistic Models.", *IEEE/CVF 2022*