CHAPTER 1
Preliminaries

What Is This Book About?

This book is concerned with the nuts and bolts of manipulating, processing, cleaning, and crunching data in Python. It is also a practical, modern introduction to scientific computing in Python, tailored for data-intensive applications. This is a book about the parts of the Python language and libraries you'll need to effectively solve a broad set of data analysis problems. This book is *not* an exposition on analytical methods using Python as the implementation language.

When I say "data", what am I referring to exactly? The primary focus is on *structured data*, a deliberately vague term that encompasses many different common forms of data, such as

- Multidimensional arrays (matrices)
- Tabular or spreadsheet-like data in which each column may be a different type (string, numeric, date, or otherwise). This includes most kinds of data commonly stored in relational databases or tab- or comma-delimited text files
- Multiple tables of data interrelated by key columns (what would be primary or foreign keys for a SQL user)
- Evenly or unevenly spaced time series

This is by no means a complete list. Even though it may not always be obvious, a large percentage of data sets can be transformed into a structured form that is more suitable for analysis and modeling. If not, it may be possible to extract features from a data set into a structured form. As an example, a collection of news articles could be processed into a word frequency table which could then be used to perform sentiment analysis.

Most users of spreadsheet programs like Microsoft Excel, perhaps the most widely used data analysis tool in the world, will not be strangers to these kinds of data.

Why Python for Data Analysis?

For many people (myself among them), the Python language is easy to fall in love with. Since its first appearance in 1991, Python has become one of the most popular dynamic, programming languages, along with Perl, Ruby, and others. Python and Ruby have become especially popular in recent years for building websites using their numerous web frameworks, like Rails (Ruby) and Django (Python). Such languages are often called *scripting* languages as they can be used to write quick-and-dirty small programs, or *scripts*. I don't like the term "scripting language" as it carries a connotation that they cannot be used for building mission-critical software. Among interpreted languages Python is distinguished by its large and active *scientific computing* community. Adoption of Python for scientific computing in both industry applications and academic research has increased significantly since the early 2000s.

For data analysis and interactive, exploratory computing and data visualization, Python will inevitably draw comparisons with the many other domain-specific open source and commercial programming languages and tools in wide use, such as R, MATLAB, SAS, Stata, and others. In recent years, Python's improved library support (primarily pandas) has made it a strong alternative for data manipulation tasks. Combined with Python's strength in general purpose programming, it is an excellent choice as a single language for building data-centric applications.

Python as Glue

Part of Python's success as a scientific computing platform is the ease of integrating C, C++, and FORTRAN code. Most modern computing environments share a similar set of legacy FORTRAN and C libraries for doing linear algebra, optimization, integration, fast fourier transforms, and other such algorithms. The same story has held true for many companies and national labs that have used Python to glue together 30 years' worth of legacy software.

Most programs consist of small portions of code where most of the time is spent, with large amounts of "glue code" that doesn't run often. In many cases, the execution time of the glue code is insignificant; effort is most fruitfully invested in optimizing the computational bottlenecks, sometimes by moving the code to a lower-level language like C.

In the last few years, the Cython project (*http://cython.org*) has become one of the preferred ways of both creating fast compiled extensions for Python and also interfacing with C and C++ code.

Solving the "Two-Language" Problem

In many organizations, it is common to research, prototype, and test new ideas using a more domain-specific computing language like MATLAB or R then later port those

ideas to be part of a larger production system written in, say, Java, C#, or C++. What people are increasingly finding is that Python is a suitable language not only for doing research and prototyping but also building the production systems, too. I believe that more and more companies will go down this path as there are often significant organizational benefits to having both scientists and technologists using the same set of programmatic tools.

Why Not Python?

While Python is an excellent environment for building computationally-intensive scientific applications and building most kinds of general purpose systems, there are a number of uses for which Python may be less suitable.

As Python is an interpreted programming language, in general most Python code will run substantially slower than code written in a compiled language like Java or C++. As *programmer time* is typically more valuable than *CPU time*, many are happy to make this tradeoff. However, in an application with very low latency requirements (for example, a high frequency trading system), the time spent programming in a lower-level, lower-productivity language like C++ to achieve the maximum possible performance might be time well spent.

Python is not an ideal language for highly concurrent, multithreaded applications, particularly applications with many CPU-bound threads. The reason for this is that it has what is known as the *global interpreter lock* (GIL), a mechanism which prevents the interpreter from executing more than one Python bytecode instruction at a time. The technical reasons for why the GIL exists are beyond the scope of this book, but as of this writing it does not seem likely that the GIL will disappear anytime soon. While it is true that in many big data processing applications, a cluster of computers may be required to process a data set in a reasonable amount of time, there are still situations where a single-process, multithreaded system is desirable.

This is not to say that Python cannot execute truly multithreaded, parallel code; that code just cannot be executed in a single Python process. As an example, the Cython project features easy integration with OpenMP, a C framework for parallel computing, in order to to parallelize loops and thus significantly speed up numerical algorithms.

Essential Python Libraries

For those who are less familiar with the scientific Python ecosystem and the libraries used throughout the book, I present the following overview of each library.

NumPy

NumPy, short for Numerical Python, is the foundational package for scientific computing in Python. The majority of this book will be based on NumPy and libraries built on top of NumPy. It provides, among other things:

- A fast and efficient multidimensional array object *ndarray*
- Functions for performing element-wise computations with arrays or mathematical operations between arrays
- Tools for reading and writing array-based data sets to disk
- Linear algebra operations, Fourier transform, and random number generation
- Tools for integrating connecting C, C++, and Fortran code to Python

Beyond the fast array-processing capabilities that NumPy adds to Python, one of its primary purposes with regards to data analysis is as the primary container for data to be passed between algorithms. For numerical data, NumPy arrays are a much more efficient way of storing and manipulating data than the other built-in Python data structures. Also, libraries written in a lower-level language, such as C or Fortran, can operate on the data stored in a NumPy array without copying any data.

pandas

pandas provides rich data structures and functions designed to make working with structured data fast, easy, and expressive. It is, as you will see, one of the critical ingredients enabling Python to be a powerful and productive data analysis environment. The primary object in pandas that will be used in this book is the `DataFrame`, a two-dimensional tabular, column-oriented data structure with both row and column labels:

```
>>> frame
    total_bill  tip   sex     smoker  day  time    size
1   16.99       1.01  Female  No      Sun  Dinner  2
2   10.34       1.66  Male    No      Sun  Dinner  3
3   21.01       3.5   Male    No      Sun  Dinner  3
4   23.68       3.31  Male    No      Sun  Dinner  2
5   24.59       3.61  Female  No      Sun  Dinner  4
6   25.29       4.71  Male    No      Sun  Dinner  4
7   8.77        2     Male    No      Sun  Dinner  2
8   26.88       3.12  Male    No      Sun  Dinner  4
9   15.04       1.96  Male    No      Sun  Dinner  2
10  14.78       3.23  Male    No      Sun  Dinner  2
```

pandas combines the high performance array-computing features of NumPy with the flexible data manipulation capabilities of spreadsheets and relational databases (such as SQL). It provides sophisticated indexing functionality to make it easy to reshape, slice and dice, perform aggregations, and select subsets of data. pandas is the primary tool that we will use in this book.

For financial users, pandas features rich, high-performance time series functionality and tools well-suited for working with financial data. In fact, I initially designed pandas as an ideal tool for financial data analysis applications.

For users of the R language for statistical computing, the DataFrame name will be familiar, as the object was named after the similar R `data.frame` object. They are not the same, however; the functionality provided by `data.frame` in R is essentially a strict subset of that provided by the pandas `DataFrame`. While this is a book about Python, I will occasionally draw comparisons with R as it is one of the most widely-used open source data analysis environments and will be familiar to many readers.

The pandas name itself is derived from *panel data*, an econometrics term for multidimensional structured data sets, and *Python data analysis* itself.

matplotlib

matplotlib is the most popular Python library for producing plots and other 2D data visualizations. It was originally created by John D. Hunter (JDH) and is now maintained by a large team of developers. It is well-suited for creating plots suitable for publication. It integrates well with IPython (see below), thus providing a comfortable interactive environment for plotting and exploring data. The plots are also *interactive*; you can zoom in on a section of the plot and pan around the plot using the toolbar in the plot window.

IPython

IPython is the component in the standard scientific Python toolset that ties everything together. It provides a robust and productive environment for interactive and exploratory computing. It is an enhanced Python shell designed to accelerate the writing, testing, and debugging of Python code. It is particularly useful for interactively working with data and visualizing data with matplotlib. IPython is usually involved with the majority of my Python work, including running, debugging, and testing code.

Aside from the standard terminal-based IPython shell, the project also provides

- A Mathematica-like HTML notebook for connecting to IPython through a web browser (more on this later).
- A Qt framework-based GUI console with inline plotting, multiline editing, and syntax highlighting
- An infrastructure for interactive parallel and distributed computing

I will devote a chapter to IPython and how to get the most out of its features. I strongly recommend using it while working through this book.

SciPy

SciPy is a collection of packages addressing a number of different standard problem domains in scientific computing. Here is a sampling of the packages included:

- `scipy.integrate`: numerical integration routines and differential equation solvers
- `scipy.linalg`: linear algebra routines and matrix decompositions extending beyond those provided in `numpy.linalg`.
- `scipy.optimize`: function optimizers (minimizers) and root finding algorithms
- `scipy.signal`: signal processing tools
- `scipy.sparse`: sparse matrices and sparse linear system solvers
- `scipy.special`: wrapper around SPECFUN, a Fortran library implementing many common mathematical functions, such as the gamma function
- `scipy.stats`: standard continuous and discrete probability distributions (density functions, samplers, continuous distribution functions), various statistical tests, and more descriptive statistics
- `scipy.weave`: tool for using inline C++ code to accelerate array computations

Together NumPy and SciPy form a reasonably complete computational replacement for much of MATLAB along with some of its add-on toolboxes.

Installation and Setup

Since everyone uses Python for different applications, there is no single solution for setting up Python and required add-on packages. Many readers will not have a complete scientific Python environment suitable for following along with this book, so here I will give detailed instructions to get set up on each operating system. I recommend using one of the following base Python distributions:

- Enthought Python Distribution: a scientific-oriented Python distribution from Enthought (*http://www.enthought.com*). This includes EPDFree, a free base scientific distribution (with NumPy, SciPy, matplotlib, Chaco, and IPython) and EPD Full, a comprehensive suite of more than 100 scientific packages across many domains. EPD Full is free for academic use but has an annual subscription for non-academic users.
- Python(x,y) (*http://pythonxy.googlecode.com*): A free scientific-oriented Python distribution for Windows.

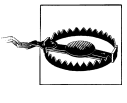
I will be using EPDFree for the installation guides, though you are welcome to take another approach depending on your needs. At the time of this writing, EPD includes Python 2.7, though this might change at some point in the future. After installing, you will have the following packages installed and importable:

- Scientific Python base: NumPy, SciPy, matplotlib, and IPython. These are all included in EPDFree.
- IPython Notebook dependencies: tornado and pyzmq. These are included in EPDFree.
- pandas (version 0.8.2 or higher).

At some point while reading you may wish to install one or more of the following packages: statsmodels, PyTables, PyQt (or equivalently, PySide), xlrd, lxml, basemap, pymongo, and requests. These are used in various examples. Installing these optional libraries is not necessary, and I would would suggest waiting until you need them. For example, installing PyQt or PyTables from source on OS X or Linux can be rather arduous. For now, it's most important to get up and running with the bare minimum: EPDFree and pandas.

For information on each Python package and links to binary installers or other help, see the Python Package Index (PyPI, *http://pypi.python.org*). This is also an excellent resource for finding new Python packages.

To avoid confusion and to keep things simple, I am avoiding discussion of more complex environment management tools like pip and virtualenv. There are many excellent guides available for these tools on the Internet.



Some users may be interested in alternate Python implementations, such as IronPython, Jython, or PyPy. To make use of the tools presented in this book, it is (currently) necessary to use the standard C-based Python interpreter, known as CPython.

Windows

To get started on Windows, download the EPDFree installer from *http://www.enthought.com*, which should be an MSI installer named like `epd_free-7.3-1-win-x86.msi`. Run the installer and accept the default installation location `C:\Python27`. If you had previously installed Python in this location, you may want to delete it manually first (or using Add/Remove Programs).

Next, you need to verify that Python has been successfully added to the system path and that there are no conflicts with any prior-installed Python versions. First, open a command prompt by going to the Start Menu and starting the Command Prompt application, also known as `cmd.exe`. Try starting the Python interpreter by typing `python`. You should see a message that matches the version of EPDFree you installed:

```
C:\Users\Wes>python
Python 2.7.3 |EPD_free 7.3-1 (32-bit)| (default, Apr 12 2012, 14:30:37) on win32
Type "credits", "demo" or "enthought" for more information.
>>>
```

If you see a message for a different version of EPD or it doesn't work at all, you will need to clean up your Windows environment variables. On Windows 7 you can start typing "environment variables" in the programs search field and select `Edit environment variables for your account`. On Windows XP, you will have to go to `Control Panel > System > Advanced > Environment Variables`. On the window that pops up, you are looking for the `Path` variable. It needs to contain the following two directory paths, separated by semicolons:

```
C:\Python27;C:\Python27\Scripts
```

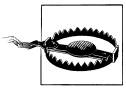
If you installed other versions of Python, be sure to delete any other Python-related directories from both the system and user `Path` variables. After making a path alternation, you have to restart the command prompt for the changes to take effect.

Once you can launch Python successfully from the command prompt, you need to install pandas. The easiest way is to download the appropriate binary installer from *http://pypi.python.org/pypi/pandas*. For EPDFree, this should be `pandas-0.9.0.win32-py2.7.exe`. After you run this, let's launch IPython and check that things are installed correctly by importing pandas and making a simple matplotlib plot:

```
C:\Users\Wes>ipython --pylab
Python 2.7.3 |EPD_free 7.3-1 (32-bit)|
Type "copyright", "credits" or "license" for more information.

IPython 0.12.1 -- An enhanced Interactive Python.
?         -> Introduction and overview of IPython's features.
%quickref -> Quick reference.
help      -> Python's own help system.
object?   -> Details about 'object', use 'object??' for extra details.

Welcome to pylab, a matplotlib-based Python environment [backend: WXAgg].
For more information, type 'help(pylab)'.

In [1]: import pandas

In [2]: plot(arange(10))
```

If successful, there should be no error messages and a plot window will appear. You can also check that the IPython HTML notebook can be successfully run by typing:

```
$ ipython notebook --pylab=inline
```



If you use the IPython notebook application on Windows and normally use Internet Explorer, you will likely need to install and run Mozilla Firefox or Google Chrome instead.

EPDFree on Windows contains only 32-bit executables. If you want or need a 64-bit setup on Windows, using EPD Full is the most painless way to accomplish that. If you would rather install from scratch and not pay for an EPD subscription, Christoph Gohlke at the University of California, Irvine, publishes unofficial binary installers for

all of the book's necessary packages (*http://www.lfd.uci.edu/~gohlke/pythonlibs/*) for 32- and 64-bit Windows.

Apple OS X

To get started on OS X, you must first install Xcode, which includes Apple's suite of software development tools. The necessary component for our purposes is the gcc C and C++ compiler suite. The Xcode installer can be found on the OS X install DVD that came with your computer or downloaded from Apple directly.

Once you've installed Xcode, launch the terminal (Terminal.app) by navigating to `Applications > Utilities`. Type `gcc` and press enter. You should hopefully see something like:

```
$ gcc
i686-apple-darwin10-gcc-4.2.1: no input files
```

Now you need to install EPDFree. Download the installer which should be a disk image named something like `epd_free-7.3-1-macosx-i386.dmg`. Double-click the `.dmg` file to mount it, then double-click the `.mpkg` file inside to run the installer.

When the installer runs, it automatically appends the EPDFree executable path to your `.bash_profile` file. This is located at `/Users/your_uname/.bash_profile`:

```
# Setting PATH for EPD_free-7.3-1
PATH="/Library/Frameworks/Python.framework/Versions/Current/bin:${PATH}"
export PATH
```

Should you encounter any problems in the following steps, you'll want to inspect your `.bash_profile` and potentially add the above directory to your path.

Now, it's time to install pandas. Execute this command in the terminal:

```
$ sudo easy_install pandas
Searching for pandas
Reading http://pypi.python.org/simple/pandas/
Reading http://pandas.pydata.org
Reading http://pandas.sourceforge.net
Best match: pandas 0.9.0
Downloading http://pypi.python.org/packages/source/p/pandas/pandas-0.9.0.zip
Processing pandas-0.9.0.zip
Writing /tmp/easy_install-H5mIX6/pandas-0.9.0/setup.cfg
Running pandas-0.9.0/setup.py -q bdist_egg --dist-dir /tmp/easy_install-H5mIX6/
pandas-0.9.0/egg-dist-tmp-RhLGOz
Adding pandas 0.9.0 to easy-install.pth file

Installed /Library/Frameworks/Python.framework/Versions/7.3/lib/python2.7/
site-packages/pandas-0.9.0-py2.7-macosx-10.5-i386.egg
Processing dependencies for pandas
Finished processing dependencies for pandas
```

To verify everything is working, launch IPython in Pylab mode and test importing pandas then making a plot interactively:

```
$ ipython --pylab
22:29 ~/VirtualBox VMs/WindowsXP $ ipython
Python 2.7.3 |EPD_free 7.3-1 (32-bit)| (default, Apr 12 2012, 11:28:34)
Type "copyright", "credits" or "license" for more information.

IPython 0.12.1 -- An enhanced Interactive Python.
?         -> Introduction and overview of IPython's features.
%quickref -> Quick reference.
help      -> Python's own help system.
object?   -> Details about 'object', use 'object??' for extra details.

Welcome to pylab, a matplotlib-based Python environment [backend: WXAgg].
For more information, type 'help(pylab)'.

In [1]: import pandas

In [2]: plot(arange(10))
```

If this succeeds, a plot window with a straight line should pop up.

GNU/Linux

Some, but not all, Linux distributions include sufficiently up-to-date versions of all the required Python packages and can be installed using the built-in package management tool like `apt`. I detail setup using EPD-Free as it's easily reproducible across distributions.

Linux details will vary a bit depending on your Linux flavor, but here I give details for Debian-based GNU/Linux systems like Ubuntu and Mint. Setup is similar to OS X with the exception of how EPDFree is installed. The installer is a shell script that must be executed in the terminal. Depending on whether you have a 32-bit or 64-bit system, you will either need to install the `x86` (32-bit) or `x86_64` (64-bit) installer. You will then have a file named something similar to `epd_free-7.3-1-rh5-x86_64.sh`. To install it, execute this script with bash:

```
$ bash epd_free-7.3-1-rh5-x86_64.sh
```

After accepting the license, you will be presented with a choice of where to put the EPDFree files. I recommend installing the files in your home directory, say `/home/wesm/epd` (substituting your own username for `wesm`).

Once the installer has finished, you need to add EPDFree's `bin` directory to your `$PATH` variable. If you are using the bash shell (the default in Ubuntu, for example), this means adding the following path addition in your `.bashrc`:

```
export PATH=/home/wesm/epd/bin:$PATH
```

Obviously, substitute the installation directory you used for `/home/wesm/epd/`. After doing this you can either start a new terminal process or execute your `.bashrc` again with `source ~/.bashrc`.

You need a C compiler such as gcc to move forward; many Linux distributions include gcc, but others may not. On Debian systems, you can install gcc by executing:

```
sudo apt-get install gcc
```

If you type `gcc` on the command line it should say something like:

```
$ gcc
gcc: no input files
```

Now, time to install pandas:

```
$ easy_install pandas
```

If you installed EPDFree as root, you may need to add `sudo` to the command and enter the sudo or root password. To verify things are working, perform the same checks as in the OS X section.

Python 2 and Python 3

The Python community is currently undergoing a drawn-out transition from the Python 2 series of interpreters to the Python 3 series. Until the appearance of Python 3.0, all Python code was backwards compatible. The community decided that in order to move the language forward, certain backwards incompatible changes were necessary.

I am writing this book with Python 2.7 as its basis, as the majority of the scientific Python community has not yet transitioned to Python 3. The good news is that, with a few exceptions, you should have no trouble following along with the book if you happen to be using Python 3.2.

Integrated Development Environments (IDEs)

When asked about my standard development environment, I almost always say "IPython plus a text editor". I typically write a program and iteratively test and debug each piece of it in IPython. It is also useful to be able to play around with data interactively and visually verify that a particular set of data manipulations are doing the right thing. Libraries like pandas and NumPy are designed to be easy-to-use in the shell.

However, some will still prefer to work in an IDE instead of a text editor. They do provide many nice "code intelligence" features like completion or quickly pulling up the documentation associated with functions and classes. Here are some that you can explore:

- Eclipse with PyDev Plugin
- Python Tools for Visual Studio (for Windows users)
- PyCharm
- Spyder
- Komodo IDE

Community and Conferences

Outside of an Internet search, the scientific Python mailing lists are generally helpful and responsive to questions. Some ones to take a look at are:

- pydata: a Google Group list for questions related to Python for data analysis and pandas
- pystatsmodels: for statsmodels or pandas-related questions
- numpy-discussion: for NumPy-related questions
- scipy-user: for general SciPy or scientific Python questions

I deliberately did not post URLs for these in case they change. They can be easily located via Internet search.

Each year many conferences are held all over the world for Python programmers. PyCon and EuroPython are the two main general Python conferences in the United States and Europe, respectively. SciPy and EuroSciPy are scientific-oriented Python conferences where you will likely find many "birds of a feather" if you become more involved with using Python for data analysis after reading this book.

Navigating This Book

If you have never programmed in Python before, you may actually want to start at the *end* of the book, where I have placed a condensed tutorial on Python syntax, language features, and built-in data structures like tuples, lists, and dicts. These things are considered prerequisite knowledge for the remainder of the book.

The book starts by introducing you to the IPython environment. Next, I give a short introduction to the key features of NumPy, leaving more advanced NumPy use for another chapter at the end of the book. Then, I introduce pandas and devote the rest of the book to data analysis topics applying pandas, NumPy, and matplotlib (for visualization). I have structured the material in the most incremental way possible, though there is occasionally some minor cross-over between chapters.

Data files and related material for each chapter are hosted as a git repository on GitHub:

```
http://github.com/pydata/pydata-book
```

I encourage you to download the data and use it to replicate the book's code examples and experiment with the tools presented in each chapter. I will happily accept contributions, scripts, IPython notebooks, or any other materials you wish to contribute to the book's repository for all to enjoy.

Code Examples

Most of the code examples in the book are shown with input and output as it would appear executed in the IPython shell.

```
In [5]: code
Out[5]: output
```

At times, for clarity, multiple code examples will be shown side by side. These should be read left to right and executed separately.

```
In [5]: code          In [6]: code2
Out[5]: output        Out[6]: output2
```

Data for Examples

Data sets for the examples in each chapter are hosted in a repository on GitHub: *http://github.com/pydata/pydata-book*. You can download this data either by using the git revision control command-line program or by downloading a zip file of the repository from the website.

I have made every effort to ensure that it contains everything necessary to reproduce the examples, but I may have made some mistakes or omissions. If so, please send me an e-mail: `wesmckinn@gmail.com`.

Import Conventions

The Python community has adopted a number of naming conventions for commonly-used modules:

```
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
```

This means that when you see `np.arange`, this is a reference to the `arange` function in NumPy. This is done as it's considered bad practice in Python software development to import everything (`from numpy import *`) from a large package like NumPy.

Jargon

I'll use some terms common both to programming and data science that you may not be familiar with. Thus, here are some brief definitions:

Munge/Munging/Wrangling
: Describes the overall process of manipulating unstructured and/or messy data into a structured or clean form. The word has snuck its way into the jargon of many modern day data hackers. Munge rhymes with "lunge".

Pseudocode
: A description of an algorithm or process that takes a code-like form while likely not being actual valid source code.

Syntactic sugar
: Programming syntax which does not add new features, but makes something more convenient or easier to type.

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It would have been difficult for me to write this book without the support of a large number of people.

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I got many great ideas for examples and data sets from friends and colleagues in the data community, among them: Mike Dewar, Jeff Hammerbacher, James Johndrow, Kristian Lum, Adam Klein, Hilary Mason, Chang She, and Ashley Williams.

I am of course indebted to the many leaders in the open source scientific Python community who've built the foundation for my development work and gave encouragement while I was writing this book: the IPython core team (Fernando Pérez, Brian Granger, Min Ragan-Kelly, Thomas Kluyver, and others), John Hunter, Skipper Seabold, Travis Oliphant, Peter Wang, Eric Jones, Robert Kern, Josef Perktold, Francesc Alted, Chris Fonnesbeck, and too many others to mention. Several other people provided a great deal of support, ideas, and encouragement along the way: Drew Conway, Sean Taylor, Giuseppe Paleologo, Jared Lander, David Epstein, John Krowas, Joshua Bloom, Den Pilsworth, John Myles-White, and many others I've forgotten.

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On the personal side, Casey Dinkin provided invaluable day-to-day support during the writing process, tolerating my highs and lows as I hacked together the final draft on

top of an already overcommitted schedule. Lastly, my parents, Bill and Kim, taught me to always follow my dreams and to never settle for less.

CHAPTER 2

Introductory Examples

This book teaches you the Python tools to work productively with data. While readers may have many different end goals for their work, the tasks required generally fall into a number of different broad groups:

Interacting with the outside world
: Reading and writing with a variety of file formats and databases.

Preparation
: Cleaning, munging, combining, normalizing, reshaping, slicing and dicing, and transforming data for analysis.

Transformation
: Applying mathematical and statistical operations to groups of data sets to derive new data sets. For example, aggregating a large table by group variables.

Modeling and computation
: Connecting your data to statistical models, machine learning algorithms, or other computational tools

Presentation
: Creating interactive or static graphical visualizations or textual summaries

In this chapter I will show you a few data sets and some things we can do with them. These examples are just intended to pique your interest and thus will only be explained at a high level. Don't worry if you have no experience with any of these tools; they will be discussed in great detail throughout the rest of the book. In the code examples you'll see input and output prompts like `In [15]:`; these are from the IPython shell.

1.usa.gov data from bit.ly

In 2011, URL shortening service bit.ly partnered with the United States government website `usa.gov` to provide a feed of anonymous data gathered from users who shorten links ending with `.gov` or `.mil`. As of this writing, in addition to providing a live feed, hourly snapshots are available as downloadable text files.[1]

In the case of the hourly snapshots, each line in each file contains a common form of web data known as JSON, which stands for JavaScript Object Notation. For example, if we read just the first line of a file you may see something like

```
In [15]: path = 'ch02/usagov_bitly_data2012-03-16-1331923249.txt'

In [16]: open(path).readline()
Out[16]: '{ "a": "Mozilla\\/5.0 (Windows NT 6.1; WOW64) AppleWebKit\\/535.11
(KHTML, like Gecko) Chrome\\/17.0.963.78 Safari\\/535.11", "c": "US", "nk": 1,
"tz": "America\\/New_York", "gr": "MA", "g": "A6qOVH", "h": "wfLQtf", "l":
"orofrog", "al": "en-US,en;q=0.8", "hh": "1.usa.gov", "r":
"http:\\/\\/www.facebook.com\\/l\\/7AQEFzjSi\\/1.usa.gov\\/wfLQtf", "u":
"http:\\/\\/www.ncbi.nlm.nih.gov\\/pubmed\\/22415991", "t": 1331923247, "hc":
1331822918, "cy": "Danvers", "ll": [ 42.576698, -70.954903 ] }\n'
```

Python has numerous built-in and 3rd party modules for converting a JSON string into a Python dictionary object. Here I'll use the `json` module and its `loads` function invoked on each line in the sample file I downloaded:

```
import json
path = 'ch02/usagov_bitly_data2012-03-16-1331923249.txt'
records = [json.loads(line) for line in open(path)]
```

If you've never programmed in Python before, the last expression here is called a *list comprehension*, which is a concise way of applying an operation (like `json.loads`) to a collection of strings or other objects. Conveniently, iterating over an open file handle gives you a sequence of its lines. The resulting object `records` is now a list of Python dicts:

```
In [18]: records[0]
Out[18]:
{u'a': u'Mozilla/5.0 (Windows NT 6.1; WOW64) AppleWebKit/535.11 (KHTML, like
Gecko) Chrome/17.0.963.78 Safari/535.11',
 u'al': u'en-US,en;q=0.8',
 u'c': u'US',
 u'cy': u'Danvers',
 u'g': u'A6qOVH',
 u'gr': u'MA',
 u'h': u'wfLQtf',
 u'hc': 1331822918,
 u'hh': u'1.usa.gov',
 u'l': u'orofrog',
 u'll': [42.576698, -70.954903],
 u'nk': 1,
 u'r': u'http://www.facebook.com/l/7AQEFzjSi/1.usa.gov/wfLQtf',
 u't': 1331923247,
 u'tz': u'America/New_York',
 u'u': u'http://www.ncbi.nlm.nih.gov/pubmed/22415991'}
```

1. *http://www.usa.gov/About/developer-resources/1usagov.shtml*

Note that Python indices start at 0 and not 1 like some other languages (like R). It's now easy to access individual values within records by passing a string for the key you wish to access:

```
In [19]: records[0]['tz']
Out[19]: u'America/New_York'
```

The `u` here in front of the quotation stands for *unicode*, a standard form of string encoding. Note that IPython shows the time zone string object *representation* here rather than its print equivalent:

```
In [20]: print records[0]['tz']
America/New_York
```

Counting Time Zones in Pure Python

Suppose we were interested in the most often-occurring time zones in the data set (the `tz` field). There are many ways we could do this. First, let's extract a list of time zones again using a list comprehension:

```
In [25]: time_zones = [rec['tz'] for rec in records]
---------------------------------------------------------------------------
KeyError                                  Traceback (most recent call last)
/home/wesm/book_scripts/whetting/<ipython> in <module>()
----> 1 time_zones = [rec['tz'] for rec in records]

KeyError: 'tz'
```

Oops! Turns out that not all of the records have a time zone field. This is easy to handle as we can add the check `if 'tz' in rec` at the end of the list comprehension:

```
In [26]: time_zones = [rec['tz'] for rec in records if 'tz' in rec]

In [27]: time_zones[:10]
Out[27]:
[u'America/New_York',
 u'America/Denver',
 u'America/New_York',
 u'America/Sao_Paulo',
 u'America/New_York',
 u'America/New_York',
 u'Europe/Warsaw',
 u'',
 u'',
 u'']
```

Just looking at the first 10 time zones we see that some of them are unknown (empty). You can filter these out also but I'll leave them in for now. Now, to produce counts by time zone I'll show two approaches: the harder way (using just the Python standard library) and the easier way (using pandas). One way to do the counting is to use a dict to store counts while we iterate through the time zones:

```
def get_counts(sequence):
    counts = {}
```

```
    for x in sequence:
        if x in counts:
            counts[x] += 1
        else:
            counts[x] = 1
    return counts
```

If you know a bit more about the Python standard library, you might prefer to write the same thing more briefly:

```
from collections import defaultdict

def get_counts2(sequence):
    counts = defaultdict(int) # values will initialize to 0
    for x in sequence:
        counts[x] += 1
    return counts
```

I put this logic in a function just to make it more reusable. To use it on the time zones, just pass the `time_zones` list:

```
In [31]: counts = get_counts(time_zones)

In [32]: counts['America/New_York']
Out[32]: 1251

In [33]: len(time_zones)
Out[33]: 3440
```

If we wanted the top 10 time zones and their counts, we have to do a little bit of dictionary acrobatics:

```
def top_counts(count_dict, n=10):
    value_key_pairs = [(count, tz) for tz, count in count_dict.items()]
    value_key_pairs.sort()
    return value_key_pairs[-n:]
```

We have then:

```
In [35]: top_counts(counts)
Out[35]:
[(33, u'America/Sao_Paulo'),
 (35, u'Europe/Madrid'),
 (36, u'Pacific/Honolulu'),
 (37, u'Asia/Tokyo'),
 (74, u'Europe/London'),
 (191, u'America/Denver'),
 (382, u'America/Los_Angeles'),
 (400, u'America/Chicago'),
 (521, u''),
 (1251, u'America/New_York')]
```

If you search the Python standard library, you may find the `collections.Counter` class, which makes this task a lot easier:

```
In [49]: from collections import Counter

In [50]: counts = Counter(time_zones)

In [51]: counts.most_common(10)
Out[51]:
[(u'America/New_York', 1251),
 (u'', 521),
 (u'America/Chicago', 400),
 (u'America/Los_Angeles', 382),
 (u'America/Denver', 191),
 (u'Europe/London', 74),
 (u'Asia/Tokyo', 37),
 (u'Pacific/Honolulu', 36),
 (u'Europe/Madrid', 35),
 (u'America/Sao_Paulo', 33)]
```

Counting Time Zones with pandas

The main pandas data structure is the *DataFrame*, which you can think of as representing a table or spreadsheet of data. Creating a DataFrame from the original set of records is simple:

```
In [289]: from pandas import DataFrame, Series

In [290]: import pandas as pd

In [291]: frame = DataFrame(records)

In [292]: frame
Out[292]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 3560 entries, 0 to 3559
Data columns:
_heartbeat_    120  non-null values
a              3440  non-null values
al             3094  non-null values
c              2919  non-null values
cy             2919  non-null values
g              3440  non-null values
gr             2919  non-null values
h              3440  non-null values
hc             3440  non-null values
hh             3440  non-null values
kw             93  non-null values
l              3440  non-null values
ll             2919  non-null values
nk             3440  non-null values
r              3440  non-null values
t              3440  non-null values
tz             3440  non-null values
```

```
u              3440  non-null values
dtypes: float64(4), object(14)

In [293]: frame['tz'][:10]
Out[293]:
0     America/New_York
1       America/Denver
2     America/New_York
3    America/Sao_Paulo
4     America/New_York
5     America/New_York
6        Europe/Warsaw
7
8
9
Name: tz
```

The output shown for the `frame` is the *summary view*, shown for large DataFrame objects. The Series object returned by `frame['tz']` has a method `value_counts` that gives us what we're looking for:

```
In [294]: tz_counts = frame['tz'].value_counts()

In [295]: tz_counts[:10]
Out[295]:
America/New_York       1251
                        521
America/Chicago         400
America/Los_Angeles     382
America/Denver          191
Europe/London            74
Asia/Tokyo               37
Pacific/Honolulu         36
Europe/Madrid            35
America/Sao_Paulo        33
```

Then, we might want to make a plot of this data using plotting library, matplotlib. You can do a bit of munging to fill in a substitute value for unknown and missing time zone data in the records. The `fillna` function can replace missing (NA) values and unknown (empty strings) values can be replaced by boolean array indexing:

```
In [296]: clean_tz = frame['tz'].fillna('Missing')

In [297]: clean_tz[clean_tz == ''] = 'Unknown'

In [298]: tz_counts = clean_tz.value_counts()

In [299]: tz_counts[:10]
Out[299]:
America/New_York       1251
Unknown                 521
America/Chicago         400
America/Los_Angeles     382
America/Denver          191
Missing                 120
```

```
Europe/London           74
Asia/Tokyo              37
Pacific/Honolulu        36
Europe/Madrid           35
```

Making a horizontal bar plot can be accomplished using the `plot` method on the `counts` objects:

```
In [301]: tz_counts[:10].plot(kind='barh', rot=0)
```

See Figure 2-1 for the resulting figure. We'll explore more tools for working with this kind of data. For example, the `a` field contains information about the browser, device, or application used to perform the URL shortening:

```
In [302]: frame['a'][1]
Out[302]: u'GoogleMaps/RochesterNY'

In [303]: frame['a'][50]
Out[303]: u'Mozilla/5.0 (Windows NT 5.1; rv:10.0.2) Gecko/20100101 Firefox/10.0.2'

In [304]: frame['a'][51]
Out[304]: u'Mozilla/5.0 (Linux; U; Android 2.2.2; en-us; LG-P925/V10e Build/FRG83G) AppleWebKit/533.1 (
```

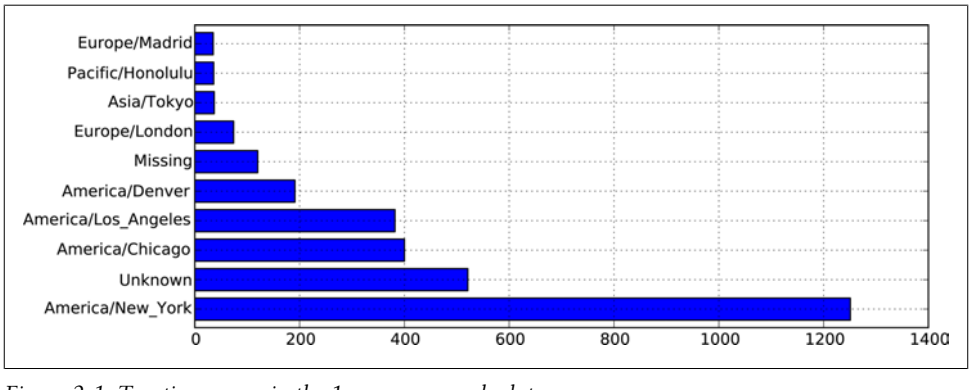


Figure 2-1. Top time zones in the 1.usa.gov sample data

Parsing all of the interesting information in these "agent" strings may seem like a daunting task. Luckily, once you have mastered Python's built-in string functions and regular expression capabilities, it is really not so bad. For example, we could split off the first token in the string (corresponding roughly to the browser capability) and make another summary of the user behavior:

```
In [305]: results = Series([x.split()[0] for x in frame.a.dropna()])

In [306]: results[:5]
Out[306]:
0               Mozilla/5.0
1    GoogleMaps/RochesterNY
2               Mozilla/4.0
3               Mozilla/5.0
4               Mozilla/5.0
```

```
In [307]: results.value_counts()[:8]
Out[307]:
Mozilla/5.0                 2594
Mozilla/4.0                  601
GoogleMaps/RochesterNY       121
Opera/9.80                    34
TEST_INTERNET_AGENT           24
GoogleProducer                21
Mozilla/6.0                    5
BlackBerry8520/5.0.0.681       4
```

Now, suppose you wanted to decompose the top time zones into Windows and non-Windows users. As a simplification, let's say that a user is on Windows if the string `'Windows'` is in the agent string. Since some of the agents are missing, I'll exclude these from the data:

```
In [308]: cframe = frame[frame.a.notnull()]
```

We want to then compute a value whether each row is Windows or not:

```
In [309]: operating_system = np.where(cframe['a'].str.contains('Windows'),
   .....:                             'Windows', 'Not Windows')

In [310]: operating_system[:5]
Out[310]:
0        Windows
1    Not Windows
2        Windows
3    Not Windows
4        Windows
Name: a
```

Then, you can group the data by its time zone column and this new list of operating systems:

```
In [311]: by_tz_os = cframe.groupby(['tz', operating_system])
```

The group counts, analogous to the `value_counts` function above, can be computed using `size`. This result is then reshaped into a table with `unstack`:

```
In [312]: agg_counts = by_tz_os.size().unstack().fillna(0)

In [313]: agg_counts[:10]
Out[313]:
a                             Not Windows  Windows
tz
                                      245      276
Africa/Cairo                            0        3
Africa/Casablanca                       0        1
Africa/Ceuta                            0        2
Africa/Johannesburg                     0        1
Africa/Lusaka                           0        1
America/Anchorage                       4        1
America/Argentina/Buenos_Aires          1        0
```

```
America/Argentina/Cordoba                0        1
America/Argentina/Mendoza                0        1
```

Finally, let's select the top overall time zones. To do so, I construct an indirect index array from the row counts in `agg_counts`:

```
# Use to sort in ascending order
In [314]: indexer = agg_counts.sum(1).argsort()

In [315]: indexer[:10]
Out[315]:
tz
                                  24
Africa/Cairo                      20
Africa/Casablanca                 21
Africa/Ceuta                      92
Africa/Johannesburg               87
Africa/Lusaka                     53
America/Anchorage                 54
America/Argentina/Buenos_Aires    57
America/Argentina/Cordoba         26
America/Argentina/Mendoza         55
```

I then use `take` to select the rows in that order, then slice off the last 10 rows:

```
In [316]: count_subset = agg_counts.take(indexer)[-10:]

In [317]: count_subset
Out[317]:
a                   Not Windows  Windows
tz
America/Sao_Paulo              13       20
Europe/Madrid                  16       19
Pacific/Honolulu               0        36
Asia/Tokyo                     2        35
Europe/London                  43       31
America/Denver                 132      59
America/Los_Angeles            130      252
America/Chicago                115      285
                               245      276
America/New_York               339      912
```

Then, as shown in the preceding code block, this can be plotted in a bar plot; I'll make it a stacked bar plot by passing `stacked=True` (see Figure 2-2) :

```
In [319]: count_subset.plot(kind='barh', stacked=True)
```

The plot doesn't make it easy to see the relative percentage of Windows users in the smaller groups, but the rows can easily be normalized to sum to 1 then plotted again (see Figure 2-3):

```
In [321]: normed_subset = count_subset.div(count_subset.sum(1), axis=0)

In [322]: normed_subset.plot(kind='barh', stacked=True)
```

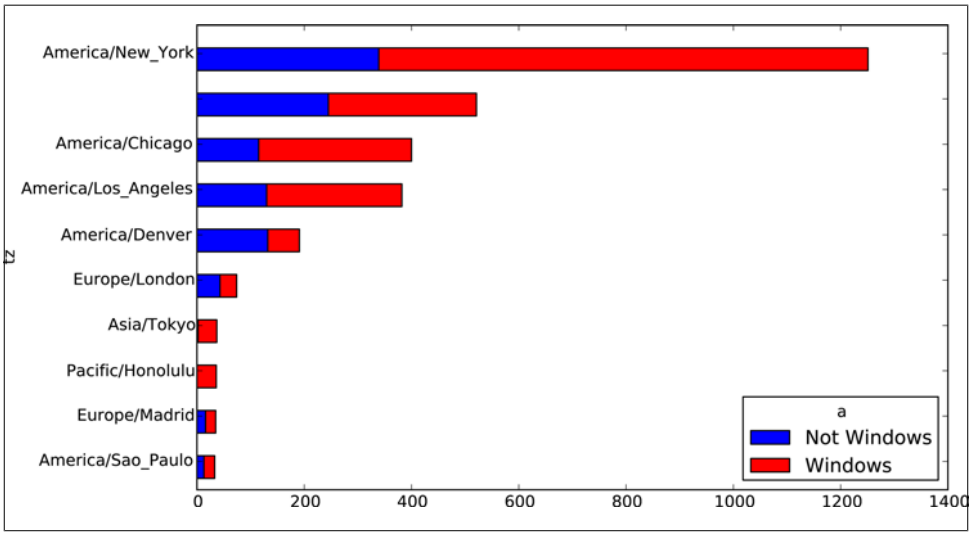


Figure 2-2. Top time zones by Windows and non-Windows users

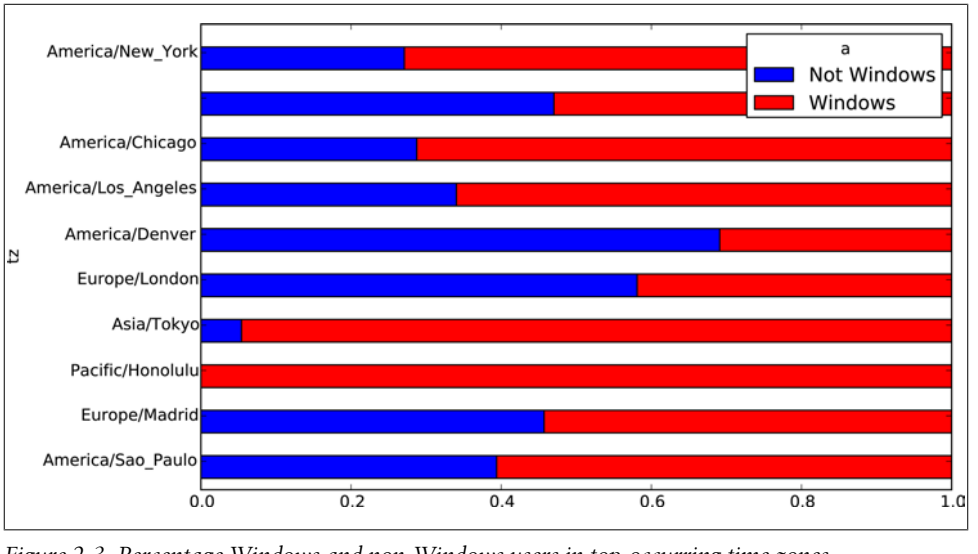


Figure 2-3. Percentage Windows and non-Windows users in top-occurring time zones

All of the methods employed here will be examined in great detail throughout the rest of the book.

MovieLens 1M Data Set

GroupLens Research (*http://www.grouplens.org/node/73*) provides a number of collections of movie ratings data collected from users of MovieLens in the late 1990s and

early 2000s. The data provide movie ratings, movie metadata (genres and year), and demographic data about the users (age, zip code, gender, and occupation). Such data is often of interest in the development of recommendation systems based on machine learning algorithms. While I will not be exploring machine learning techniques in great detail in this book, I will show you how to slice and dice data sets like these into the exact form you need.

The MovieLens 1M data set contains 1 million ratings collected from 6000 users on 4000 movies. It's spread across 3 tables: ratings, user information, and movie information. After extracting the data from the zip file, each table can be loaded into a pandas DataFrame object using `pandas.read_table`:

```
import pandas as pd

unames = ['user_id', 'gender', 'age', 'occupation', 'zip']
users = pd.read_table('ml-1m/users.dat', sep='::', header=None,
                      names=unames)

rnames = ['user_id', 'movie_id', 'rating', 'timestamp']
ratings = pd.read_table('ml-1m/ratings.dat', sep='::', header=None,
                        names=rnames)

mnames = ['movie_id', 'title', 'genres']
movies = pd.read_table('ml-1m/movies.dat', sep='::', header=None,
                        names=mnames)
```

You can verify that everything succeeded by looking at the first few rows of each DataFrame with Python's slice syntax:

```
In [334]: users[:5]
Out[334]:
   user_id gender  age  occupation    zip
0        1      F    1          10  48067
1        2      M   56          16  70072
2        3      M   25          15  55117
3        4      M   45           7  02460
4        5      M   25          20  55455

In [335]: ratings[:5]
Out[335]:
   user_id  movie_id  rating  timestamp
0        1      1193       5  978300760
1        1       661       3  978302109
2        1       914       3  978301968
3        1      3408       4  978300275
4        1      2355       5  978824291

In [336]: movies[:5]
Out[336]:
   movie_id                               title                        genres
0         1                   Toy Story (1995)   Animation|Children's|Comedy
1         2                     Jumanji (1995)  Adventure|Children's|Fantasy
2         3            Grumpier Old Men (1995)                Comedy|Romance
3         4           Waiting to Exhale (1995)                  Comedy|Drama
```

```
4         5  Father of the Bride Part II (1995)                    Comedy

In [337]: ratings
Out[337]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 1000209 entries, 0 to 1000208
Data columns:
user_id      1000209  non-null values
movie_id     1000209  non-null values
rating       1000209  non-null values
timestamp    1000209  non-null values
dtypes: int64(4)
```

Note that ages and occupations are coded as integers indicating groups described in the data set's `README` file. Analyzing the data spread across three tables is not a simple task; for example, suppose you wanted to compute mean ratings for a particular movie by sex and age. As you will see, this is much easier to do with all of the data merged together into a single table. Using pandas's `merge` function, we first merge `ratings` with `users` then merging that result with the `movies` data. pandas infers which columns to use as the merge (or *join*) keys based on overlapping names:

```
In [338]: data = pd.merge(pd.merge(ratings, users), movies)

In [339]: data
Out[339]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 1000209 entries, 0 to 1000208
Data columns:
user_id       1000209  non-null values
movie_id      1000209  non-null values
rating        1000209  non-null values
timestamp     1000209  non-null values
gender        1000209  non-null values
age           1000209  non-null values
occupation    1000209  non-null values
zip           1000209  non-null values
title         1000209  non-null values
genres        1000209  non-null values
dtypes: int64(6), object(4)

In [340]: data.ix[0]
Out[340]:
user_id                                   1
movie_id                                  1
rating                                    5
timestamp                         978824268
gender                                    F
age                                       1
occupation                               10
zip                                   48067
title                     Toy Story (1995)
genres        Animation|Children's|Comedy
Name: 0
```

In this form, aggregating the ratings grouped by one or more user or movie attributes is straightforward once you build some familiarity with pandas. To get mean movie ratings for each film grouped by gender, we can use the `pivot_table` method:

```
In [341]: mean_ratings = data.pivot_table('rating', rows='title',
   .....:                                  cols='gender', aggfunc='mean')

In [342]: mean_ratings[:5]
Out[342]:
gender                                F         M
title
$1,000,000 Duck (1971)         3.375000  2.761905
'Night Mother (1986)           3.388889  3.352941
'Til There Was You (1997)      2.675676  2.733333
'burbs, The (1989)             2.793478  2.962085
...And Justice for All (1979)  3.828571  3.689024
```

This produced another DataFrame containing mean ratings with movie totals as row labels and gender as column labels. First, I'm going to filter down to movies that received at least 250 ratings (a completely arbitrary number); to do this, I group the data by title and use `size()` to get a Series of group sizes for each title:

```
In [343]: ratings_by_title = data.groupby('title').size()

In [344]: ratings_by_title[:10]
Out[344]:
title
$1,000,000 Duck (1971)               37
'Night Mother (1986)                 70
'Til There Was You (1997)            52
'burbs, The (1989)                  303
...And Justice for All (1979)       199
1-900 (1994)                          2
10 Things I Hate About You (1999)   700
101 Dalmatians (1961)               565
101 Dalmatians (1996)               364
12 Angry Men (1957)                 616

In [345]: active_titles = ratings_by_title.index[ratings_by_title >= 250]

In [346]: active_titles
Out[346]:
Index(['burbs, The (1989), 10 Things I Hate About You (1999),
       101 Dalmatians (1961), ..., Young Sherlock Holmes (1985),
       Zero Effect (1998), eXistenZ (1999)], dtype=object)
```

The index of titles receiving at least 250 ratings can then be used to select rows from `mean_ratings` above:

```
In [347]: mean_ratings = mean_ratings.ix[active_titles]

In [348]: mean_ratings
Out[348]:
<class 'pandas.core.frame.DataFrame'>
Index: 1216 entries, 'burbs, The (1989) to eXistenZ (1999)
```

```
Data columns:
F    1216  non-null values
M    1216  non-null values
dtypes: float64(2)
```

To see the top films among female viewers, we can sort by the `F` column in descending order:

```
In [350]: top_female_ratings = mean_ratings.sort_index(by='F', ascending=False)

In [351]: top_female_ratings[:10]
Out[351]:
gender                                                 F         M
Close Shave, A (1995)                                  4.644444  4.473795
Wrong Trousers, The (1993)                             4.588235  4.478261
Sunset Blvd. (a.k.a. Sunset Boulevard) (1950)          4.572650  4.464589
Wallace & Gromit: The Best of Aardman Animation (1996) 4.563107  4.385075
Schindler's List (1993)                                4.562602  4.491415
Shawshank Redemption, The (1994)                       4.539075  4.560625
Grand Day Out, A (1992)                                4.537879  4.293255
To Kill a Mockingbird (1962)                           4.536667  4.372611
Creature Comforts (1990)                               4.513889  4.272277
Usual Suspects, The (1995)                             4.513317  4.518248
```

Measuring rating disagreement

Suppose you wanted to find the movies that are most divisive between male and female viewers. One way is to add a column to `mean_ratings` containing the difference in means, then sort by that:

```
In [352]: mean_ratings['diff'] = mean_ratings['M'] - mean_ratings['F']
```

Sorting by `'diff'` gives us the movies with the greatest rating difference and which were preferred by women:

```
In [353]: sorted_by_diff = mean_ratings.sort_index(by='diff')

In [354]: sorted_by_diff[:15]
Out[354]:
gender                                     F         M      diff
Dirty Dancing (1987)                3.790378  2.959596 -0.830782
Jumpin' Jack Flash (1986)           3.254717  2.578358 -0.676359
Grease (1978)                       3.975265  3.367041 -0.608224
Little Women (1994)                 3.870588  3.321739 -0.548849
Steel Magnolias (1989)              3.901734  3.365957 -0.535777
Anastasia (1997)                    3.800000  3.281609 -0.518391
Rocky Horror Picture Show, The (1975)  3.673016  3.160131 -0.512885
Color Purple, The (1985)            4.158192  3.659341 -0.498851
Age of Innocence, The (1993)        3.827068  3.339506 -0.487561
Free Willy (1993)                   2.921348  2.438776 -0.482573
French Kiss (1995)                  3.535714  3.056962 -0.478752
Little Shop of Horrors, The (1960)  3.650000  3.179688 -0.470312
Guys and Dolls (1955)               4.051724  3.583333 -0.468391
Mary Poppins (1964)                 4.197740  3.730594 -0.467147
Patch Adams (1998)                  3.473282  3.008746 -0.464536
```

CHAPTER 10
Time Series

Time series data is an important form of structured data in many different fields, such as finance, economics, ecology, neuroscience, or physics. Anything that is observed or measured at many points in time forms a time series. Many time series are *fixed frequency*, which is to say that data points occur at regular intervals according to some rule, such as every 15 seconds, every 5 minutes, or once per month. Time series can also be *irregular* without a fixed unit or time or offset between units. How you mark and refer to time series data depends on the application and you may have one of the following:

- *Timestamps*, specific instants in time
- Fixed *periods*, such as the month January 2007 or the full year 2010
- *Intervals* of time, indicated by a start and end timestamp. Periods can be thought of as special cases of intervals
- Experiment or elapsed time; each timestamp is a measure of time relative to a particular start time. For example, the diameter of a cookie baking each second since being placed in the oven

In this chapter, I am mainly concerned with time series in the first 3 categories, though many of the techniques can be applied to experimental time series where the index may be an integer or floating point number indicating elapsed time from the start of the experiment. The simplest and most widely used kind of time series are those indexed by timestamp.

pandas provides a standard set of time series tools and data algorithms. With this, you can efficiently work with very large time series and easily slice and dice, aggregate, and resample irregular and fixed frequency time series. As you might guess, many of these tools are especially useful for financial and economics applications, but you could certainly use them to analyze server log data, too.

Some of the features and code, in particular period logic, presented in this chapter were derived from the now defunct `scikits.timeseries` library.

Date and Time Data Types and Tools

The Python standard library includes data types for date and time data, as well as calendar-related functionality. The `datetime`, `time`, and `calendar` modules are the main places to start. The `datetime.datetime` type, or simply `datetime`, is widely used:

```
In [317]: from datetime import datetime

In [318]: now = datetime.now()

In [319]: now
Out[319]: datetime.datetime(2012, 8, 4, 17, 9, 21, 832092)

In [320]: now.year, now.month, now.day
Out[320]: (2012, 8, 4)
```

`datetime` stores both the date and time down to the microsecond. `datetime.timedelta` represents the temporal difference between two `datetime` objects:

```
In [321]: delta = datetime(2011, 1, 7) - datetime(2008, 6, 24, 8, 15)

In [322]: delta
Out[322]: datetime.timedelta(926, 56700)

In [323]: delta.days        In [324]: delta.seconds
Out[323]: 926               Out[324]: 56700
```

You can add (or subtract) a `timedelta` or multiple thereof to a `datetime` object to yield a new shifted object:

```
In [325]: from datetime import timedelta

In [326]: start = datetime(2011, 1, 7)

In [327]: start + timedelta(12)
Out[327]: datetime.datetime(2011, 1, 19, 0, 0)

In [328]: start - 2 * timedelta(12)
Out[328]: datetime.datetime(2010, 12, 14, 0, 0)
```

The data types in the `datetime` module are summarized in Table 10-1. While this chapter is mainly concerned with the data types in pandas and higher level time series manipulation, you will undoubtedly encounter the `datetime`-based types in many other places in Python the wild.

Table 10-1. Types in datetime module

Type	Description
`date`	Store calendar date (year, month, day) using the Gregorian calendar.
`time`	Store time of day as hours, minutes, seconds, and microseconds
`datetime`	Stores both date and time
`timedelta`	Represents the difference between two datetime values (as days, seconds, and microseconds)

Converting between string and datetime

`datetime` objects and pandas `Timestamp` objects, which I'll introduce later, can be formatted as strings using `str` or the `strftime` method, passing a format specification:

```
In [329]: stamp = datetime(2011, 1, 3)

In [330]: str(stamp)                    In [331]: stamp.strftime('%Y-%m-%d')
Out[330]: '2011-01-03 00:00:00'         Out[331]: '2011-01-03'
```

See Table 10-2 for a complete list of the format codes. These same format codes can be used to convert strings to dates using `datetime.strptime`:

```
In [332]: value = '2011-01-03'

In [333]: datetime.strptime(value, '%Y-%m-%d')
Out[333]: datetime.datetime(2011, 1, 3, 0, 0)

In [334]: datestrs = ['7/6/2011', '8/6/2011']

In [335]: [datetime.strptime(x, '%m/%d/%Y') for x in datestrs]
Out[335]: [datetime.datetime(2011, 7, 6, 0, 0), datetime.datetime(2011, 8, 6, 0, 0)]
```

`datetime.strptime` is the best way to parse a date with a known format. However, it can be a bit annoying to have to write a format spec each time, especially for common date formats. In this case, you can use the `parser.parse` method in the third party `dateutil` package:

```
In [336]: from dateutil.parser import parse

In [337]: parse('2011-01-03')
Out[337]: datetime.datetime(2011, 1, 3, 0, 0)
```

`dateutil` is capable of parsing almost any human-intelligible date representation:

```
In [338]: parse('Jan 31, 1997 10:45 PM')
Out[338]: datetime.datetime(1997, 1, 31, 22, 45)
```

In international locales, day appearing before month is very common, so you can pass `dayfirst=True` to indicate this:

```
In [339]: parse('6/12/2011', dayfirst=True)
Out[339]: datetime.datetime(2011, 12, 6, 0, 0)
```

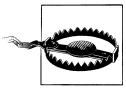
pandas is generally oriented toward working with arrays of dates, whether used as an axis index or a column in a DataFrame. The `to_datetime` method parses many different kinds of date representations. Standard date formats like ISO8601 can be parsed very quickly.

```
In [340]: datestrs
Out[340]: ['7/6/2011', '8/6/2011']

In [341]: pd.to_datetime(datestrs)
Out[341]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2011-07-06 00:00:00, 2011-08-06 00:00:00]
Length: 2, Freq: None, Timezone: None
```

It also handles values that should be considered missing (`None`, empty string, etc.):

```
In [342]: idx = pd.to_datetime(datestrs + [None])

In [343]: idx
Out[343]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2011-07-06 00:00:00, ..., NaT]
Length: 3, Freq: None, Timezone: None

In [344]: idx[2]
Out[344]: NaT

In [345]: pd.isnull(idx)
Out[345]: array([False, False, True], dtype=bool)
```

`NaT` (Not a Time) is pandas's NA value for timestamp data.



`dateutil.parser` is a useful, but not perfect tool. Notably, it will recognize some strings as dates that you might prefer that it didn't, like `'42'` will be parsed as the year `2042` with today's calendar date.

Table 10-2. Datetime format specification (ISO C89 compatible)

Type	Description
%Y	4-digit year
%y	2-digit year
%m	2-digit month [01, 12]
%d	2-digit day [01, 31]
%H	Hour (24-hour clock) [00, 23]
%I	Hour (12-hour clock) [01, 12]
%M	2-digit minute [00, 59]
%S	Second [00, 61] (seconds 60, 61 account for leap seconds)
%w	Weekday as integer [0 (Sunday), 6]

Type	Description
%U	Week number of the year [00, 53]. Sunday is considered the first day of the week, and days before the first Sunday of the year are "week 0".
%W	Week number of the year [00, 53]. Monday is considered the first day of the week, and days before the first Monday of the year are "week 0".
%z	UTC time zone offset as +HHMM or -HHMM, empty if time zone naive
%F	Shortcut for %Y-%m-%d, for example 2012-4-18
%D	Shortcut for %m/%d/%y, for example 04/18/12

`datetime` objects also have a number of locale-specific formatting options for systems in other countries or languages. For example, the abbreviated month names will be different on German or French systems compared with English systems.

Table 10-3. Locale-specific date formatting

Type	Description
%a	Abbreviated weekday name
%A	Full weekday name
%b	Abbreviated month name
%B	Full month name
%c	Full date and time, for example 'Tue 01 May 2012 04:20:57 PM'
%p	Locale equivalent of AM or PM
%x	Locale-appropriate formatted date; e.g. in US May 1, 2012 yields '05/01/2012'
%X	Locale-appropriate time, e.g. '04:24:12 PM'

Time Series Basics

The most basic kind of time series object in pandas is a Series indexed by timestamps, which is often represented external to pandas as Python strings or `datetime` objects:

```
In [346]: from datetime import datetime

In [347]: dates = [datetime(2011, 1, 2), datetime(2011, 1, 5), datetime(2011, 1, 7),
   .....:          datetime(2011, 1, 8), datetime(2011, 1, 10), datetime(2011, 1, 12)]

In [348]: ts = Series(np.random.randn(6), index=dates)

In [349]: ts
Out[349]:
2011-01-02    0.690002
2011-01-05    1.001543
2011-01-07   -0.503087
2011-01-08   -0.622274
```

```
2011-01-10   -0.921169
2011-01-12   -0.726213
```

Under the hood, these `datetime` objects have been put in a `DatetimeIndex`, and the variable `ts` is now of type `TimeSeries`:

```
In [350]: type(ts)
Out[350]: pandas.core.series.TimeSeries

In [351]: ts.index
Out[351]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2011-01-02 00:00:00, ..., 2011-01-12 00:00:00]
Length: 6, Freq: None, Timezone: None
```

It's not necessary to use the `TimeSeries` constructor explicitly; when creating a Series with a `DatetimeIndex`, pandas knows that the object is a time series.

Like other Series, arithmetic operations between differently-indexed time series automatically align on the dates:

```
In [352]: ts + ts[::2]
Out[352]:
2011-01-02    1.380004
2011-01-05         NaN
2011-01-07   -1.006175
2011-01-08         NaN
2011-01-10   -1.842337
2011-01-12         NaN
```

pandas stores timestamps using NumPy's `datetime64` data type at the nanosecond resolution:

```
In [353]: ts.index.dtype
Out[353]: dtype('datetime64[ns]')
```

Scalar values from a `DatetimeIndex` are pandas `Timestamp` objects

```
In [354]: stamp = ts.index[0]

In [355]: stamp
Out[355]: <Timestamp: 2011-01-02 00:00:00>
```

A `Timestamp` can be substituted anywhere you would use a `datetime` object. Additionally, it can store frequency information (if any) and understands how to do time zone conversions and other kinds of manipulations. More on both of these things later.

Indexing, Selection, Subsetting

TimeSeries is a subclass of Series and thus behaves in the same way with regard to indexing and selecting data based on label:

```
In [356]: stamp = ts.index[2]

In [357]: ts[stamp]
Out[357]: -0.50308739136034464
```

As a convenience, you can also pass a string that is interpretable as a date:

```
In [358]: ts['1/10/2011']             In [359]: ts['20110110']
Out[358]: -0.92116860801301081        Out[359]: -0.92116860801301081
```

For longer time series, a year or only a year and month can be passed to easily select slices of data:

```
In [360]: longer_ts = Series(np.random.randn(1000),
   .....:                    index=pd.date_range('1/1/2000', periods=1000))

In [361]: longer_ts
Out[361]:
2000-01-01    0.222896
2000-01-02    0.051316
2000-01-03   -1.157719
2000-01-04    0.816707
...
2002-09-23   -0.395813
2002-09-24   -0.180737
2002-09-25    1.337508
2002-09-26   -0.416584
Freq: D, Length: 1000

In [362]: longer_ts['2001']           In [363]: longer_ts['2001-05']
Out[362]:                             Out[363]:
2001-01-01   -1.499503                2001-05-01    1.662014
2001-01-02    0.545154                2001-05-02   -1.189203
2001-01-03    0.400823                2001-05-03    0.093597
2001-01-04   -1.946230                2001-05-04   -0.539164
...                                   ...
2001-12-28   -1.568139                2001-05-28   -0.683066
2001-12-29   -0.900887                2001-05-29   -0.950313
2001-12-30    0.652346                2001-05-30    0.400710
2001-12-31    0.871600                2001-05-31   -0.126072
Freq: D, Length: 365                  Freq: D, Length: 31
```

Slicing with dates works just like with a regular Series:

```
In [364]: ts[datetime(2011, 1, 7):]
Out[364]:
2011-01-07   -0.503087
2011-01-08   -0.622274
2011-01-10   -0.921169
2011-01-12   -0.726213
```

Because most time series data is ordered chronologically, you can slice with timestamps not contained in a time series to perform a range query:

```
In [365]: ts                  In [366]: ts['1/6/2011':'1/11/2011']
Out[365]:                     Out[366]:
2011-01-02    0.690002        2011-01-07   -0.503087
```

```
2011-01-05    1.001543        2011-01-08   -0.622274
2011-01-07   -0.503087        2011-01-10   -0.921169
2011-01-08   -0.622274
2011-01-10   -0.921169
2011-01-12   -0.726213
```

As before you can pass either a string date, datetime, or Timestamp. Remember that slicing in this manner produces views on the source time series just like slicing NumPy arrays. There is an equivalent instance method `truncate` which slices a TimeSeries between two dates:

```
In [367]: ts.truncate(after='1/9/2011')
Out[367]:
2011-01-02    0.690002
2011-01-05    1.001543
2011-01-07   -0.503087
2011-01-08   -0.622274
```

All of the above holds true for DataFrame as well, indexing on its rows:

```
In [368]: dates = pd.date_range('1/1/2000', periods=100, freq='W-WED')

In [369]: long_df = DataFrame(np.random.randn(100, 4),
   .....:                     index=dates,
   .....:                     columns=['Colorado', 'Texas', 'New York', 'Ohio'])

In [370]: long_df.ix['5-2001']
Out[370]:
            Colorado     Texas  New York      Ohio
2001-05-02  0.943479 -0.349366  0.530412 -0.508724
2001-05-09  0.230643 -0.065569 -0.248717 -0.587136
2001-05-16 -1.022324  1.060661  0.954768 -0.511824
2001-05-23 -1.387680  0.767902 -1.164490  1.527070
2001-05-30  0.287542  0.715359 -0.345805  0.470886
```

Time Series with Duplicate Indices

In some applications, there may be multiple data observations falling on a particular timestamp. Here is an example:

```
In [371]: dates = pd.DatetimeIndex(['1/1/2000', '1/2/2000', '1/2/2000', '1/2/2000',
   .....:                           '1/3/2000'])

In [372]: dup_ts = Series(np.arange(5), index=dates)

In [373]: dup_ts
Out[373]:
2000-01-01    0
2000-01-02    1
2000-01-02    2
2000-01-02    3
2000-01-03    4
```

We can tell that the index is not unique by checking its `is_unique` property:

```
In [374]: dup_ts.index.is_unique
Out[374]: False
```

Indexing into this time series will now either produce scalar values or slices depending on whether a timestamp is duplicated:

```
In [375]: dup_ts['1/3/2000']  # not duplicated
Out[375]: 4

In [376]: dup_ts['1/2/2000']  # duplicated
Out[376]:
2000-01-02    1
2000-01-02    2
2000-01-02    3
```

Suppose you wanted to aggregate the data having non-unique timestamps. One way to do this is to use `groupby` and pass `level=0` (the only level of indexing!):

```
In [377]: grouped = dup_ts.groupby(level=0)

In [378]: grouped.mean()
Out[378]:
2000-01-01    0
2000-01-02    2
2000-01-03    4

In [379]: grouped.count()
Out[379]:
2000-01-01    1
2000-01-02    3
2000-01-03    1
```

Date Ranges, Frequencies, and Shifting

Generic time series in pandas are assumed to be irregular; that is, they have no fixed frequency. For many applications this is sufficient. However, it's often desirable to work relative to a fixed frequency, such as daily, monthly, or every 15 minutes, even if that means introducing missing values into a time series. Fortunately pandas has a full suite of standard time series frequencies and tools for resampling, inferring frequencies, and generating fixed frequency date ranges. For example, in the example time series, converting it to be fixed daily frequency can be accomplished by calling `resample`:

```
In [380]: ts
Out[380]:
2011-01-02    0.690002
2011-01-05    1.001543
2011-01-07   -0.503087
2011-01-08   -0.622274
2011-01-10   -0.921169
2011-01-12   -0.726213

In [381]: ts.resample('D')
Out[381]:
2011-01-02    0.690002
2011-01-03         NaN
2011-01-04         NaN
2011-01-05    1.001543
2011-01-06         NaN
2011-01-07   -0.503087
2011-01-08   -0.622274
2011-01-09         NaN
2011-01-10   -0.921169
2011-01-11         NaN
2011-01-12   -0.726213
Freq: D
```

Conversion between frequencies or *resampling* is a big enough topic to have its own section later. Here I'll show you how to use the base frequencies and multiples thereof.

Generating Date Ranges

While I used it previously without explanation, you may have guessed that `pandas.date_range` is responsible for generating a `DatetimeIndex` with an indicated length according to a particular frequency:

```
In [382]: index = pd.date_range('4/1/2012', '6/1/2012')

In [383]: index
Out[383]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-04-01 00:00:00, ..., 2012-06-01 00:00:00]
Length: 62, Freq: D, Timezone: None
```

By default, `date_range` generates daily timestamps. If you pass only a start or end date, you must pass a number of periods to generate:

```
In [384]: pd.date_range(start='4/1/2012', periods=20)
Out[384]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-04-01 00:00:00, ..., 2012-04-20 00:00:00]
Length: 20, Freq: D, Timezone: None

In [385]: pd.date_range(end='6/1/2012', periods=20)
Out[385]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-05-13 00:00:00, ..., 2012-06-01 00:00:00]
Length: 20, Freq: D, Timezone: None
```

The start and end dates define strict boundaries for the generated date index. For example, if you wanted a date index containing the last business day of each month, you would pass the `'BM'` frequency (business end of month) and only dates falling on or inside the date interval will be included:

```
In [386]: pd.date_range('1/1/2000', '12/1/2000', freq='BM')
Out[386]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2000-01-31 00:00:00, ..., 2000-11-30 00:00:00]
Length: 11, Freq: BM, Timezone: None
```

`date_range` by default preserves the time (if any) of the start or end timestamp:

```
In [387]: pd.date_range('5/2/2012 12:56:31', periods=5)
Out[387]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-05-02 12:56:31, ..., 2012-05-06 12:56:31]
Length: 5, Freq: D, Timezone: None
```

Sometimes you will have start or end dates with time information but want to generate a set of timestamps *normalized* to midnight as a convention. To do this, there is a `normalize` option:

```
In [388]: pd.date_range('5/2/2012 12:56:31', periods=5, normalize=True)
Out[388]:
<class 'pandas.tseries.index.DatetimeIndex'>
```

```
[2012-05-02 00:00:00, ..., 2012-05-06 00:00:00]
Length: 5, Freq: D, Timezone: None
```

Frequencies and Date Offsets

Frequencies in pandas are composed of a *base frequency* and a multiplier. Base frequencies are typically referred to by a string alias, like `'M'` for monthly or `'H'` for hourly. For each base frequency, there is an object defined generally referred to as a *date offset*. For example, hourly frequency can be represented with the `Hour` class:

```
In [389]: from pandas.tseries.offsets import Hour, Minute

In [390]: hour = Hour()

In [391]: hour
Out[391]: <1 Hour>
```

You can define a multiple of an offset by passing an integer:

```
In [392]: four_hours = Hour(4)

In [393]: four_hours
Out[393]: <4 Hours>
```

In most applications, you would never need to explicitly create one of these objects, instead using a string alias like `'H'` or `'4H'`. Putting an integer before the base frequency creates a multiple:

```
In [394]: pd.date_range('1/1/2000', '1/3/2000 23:59', freq='4h')
Out[394]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2000-01-01 00:00:00, ..., 2000-01-03 20:00:00]
Length: 18, Freq: 4H, Timezone: None
```

Many offsets can be combined together by addition:

```
In [395]: Hour(2) + Minute(30)
Out[395]: <150 Minutes>
```

Similarly, you can pass frequency strings like `'2h30min'` which will effectively be parsed to the same expression:

```
In [396]: pd.date_range('1/1/2000', periods=10, freq='1h30min')
Out[396]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2000-01-01 00:00:00, ..., 2000-01-01 13:30:00]
Length: 10, Freq: 90T, Timezone: None
```

Some frequencies describe points in time that are not evenly spaced. For example, `'M'` (calendar month end) and `'BM'` (last business/weekday of month) depend on the number of days in a month and, in the latter case, whether the month ends on a weekend or not. For lack of a better term, I call these *anchored* offsets.

See Table 10-4 for a listing of frequency codes and date offset classes available in pandas.

Users can define their own custom frequency classes to provide date logic not available in pandas, though the full details of that are outside the scope of this book.

Table 10-4. Base Time Series Frequencies

Alias	Offset Type	Description
D	Day	Calendar daily
B	BusinessDay	Business daily
H	Hour	Hourly
T or min	Minute	Minutely
S	Second	Secondly
L or ms	Milli	Millisecond (1/1000th of 1 second)
U	Micro	Microsecond (1/1000000th of 1 second)
M	MonthEnd	Last calendar day of month
BM	BusinessMonthEnd	Last business day (weekday) of month
MS	MonthBegin	First calendar day of month
BMS	BusinessMonthBegin	First weekday of month
`W-MON, W-TUE, ...`	Week	Weekly on given day of week: MON, TUE, WED, THU, FRI, SAT, or SUN.
`WOM-1MON, WOM-2MON, ...`	WeekOfMonth	Generate weekly dates in the first, second, third, or fourth week of the month. For example, `WOM-3FRI` for the 3rd Friday of each month.
`Q-JAN, Q-FEB, ...`	QuarterEnd	Quarterly dates anchored on last calendar day of each month, for year ending in indicated month: JAN, FEB, MAR, APR, MAY, JUN, JUL, AUG, SEP, OCT, NOV, or DEC.
`BQ-JAN, BQ-FEB, ...`	BusinessQuarterEnd	Quarterly dates anchored on last weekday day of each month, for year ending in indicated month
`QS-JAN, QS-FEB, ...`	QuarterBegin	Quarterly dates anchored on first calendar day of each month, for year ending in indicated month
`BQS-JAN, BQS-FEB, ...`	BusinessQuarterBegin	Quarterly dates anchored on first weekday day of each month, for year ending in indicated month
`A-JAN, A-FEB, ...`	YearEnd	Annual dates anchored on last calendar day of given month: JAN, FEB, MAR, APR, MAY, JUN, JUL, AUG, SEP, OCT, NOV, or DEC.
`BA-JAN, BA-FEB, ...`	BusinessYearEnd	Annual dates anchored on last weekday of given month
`AS-JAN, AS-FEB, ...`	YearBegin	Annual dates anchored on first day of given month
`BAS-JAN, BAS-FEB, ...`	BusinessYearBegin	Annual dates anchored on first weekday of given month

Week of month dates

One useful frequency class is "week of month", starting with `WOM`. This enables you to get dates like the third Friday of each month:

```
In [397]: rng = pd.date_range('1/1/2012', '9/1/2012', freq='WOM-3FRI')

In [398]: list(rng)
Out[398]:
[<Timestamp: 2012-01-20 00:00:00>,
 <Timestamp: 2012-02-17 00:00:00>,
 <Timestamp: 2012-03-16 00:00:00>,
 <Timestamp: 2012-04-20 00:00:00>,
 <Timestamp: 2012-05-18 00:00:00>,
 <Timestamp: 2012-06-15 00:00:00>,
 <Timestamp: 2012-07-20 00:00:00>,
 <Timestamp: 2012-08-17 00:00:00>]
```

Traders of US equity options will recognize these dates as the standard dates of monthly expiry.

Shifting (Leading and Lagging) Data

"Shifting" refers to moving data backward and forward through time. Both Series and DataFrame have a `shift` method for doing naive shifts forward or backward, leaving the index unmodified:

```
In [399]: ts = Series(np.random.randn(4),
   .....:             index=pd.date_range('1/1/2000', periods=4, freq='M'))

In [400]: ts                In [401]: ts.shift(2)       In [402]: ts.shift(-2)
Out[400]:                   Out[401]:                   Out[402]:
2000-01-31    0.575283      2000-01-31         NaN      2000-01-31    1.814582
2000-02-29    0.304205      2000-02-29         NaN      2000-02-29    1.634858
2000-03-31    1.814582      2000-03-31    0.575283      2000-03-31         NaN
2000-04-30    1.634858      2000-04-30    0.304205      2000-04-30         NaN
Freq: M                     Freq: M                     Freq: M
```

A common use of `shift` is computing percent changes in a time series or multiple time series as DataFrame columns. This is expressed as

```
ts / ts.shift(1) - 1
```

Because naive shifts leave the index unmodified, some data is discarded. Thus if the frequency is known, it can be passed to `shift` to advance the timestamps instead of simply the data:

```
In [403]: ts.shift(2, freq='M')
Out[403]:
2000-03-31    0.575283
2000-04-30    0.304205
2000-05-31    1.814582
2000-06-30    1.634858
Freq: M
```

Other frequencies can be passed, too, giving you a lot of flexibility in how to lead and lag the data:

```
In [404]: ts.shift(3, freq='D')
Out[404]:
2000-02-03    0.575283
2000-03-03    0.304205
2000-04-03    1.814582
2000-05-03    1.634858

In [405]: ts.shift(1, freq='3D')
Out[405]:
2000-02-03    0.575283
2000-03-03    0.304205
2000-04-03    1.814582
2000-05-03    1.634858

In [406]: ts.shift(1, freq='90T')
Out[406]:
2000-01-31 01:30:00    0.575283
2000-02-29 01:30:00    0.304205
2000-03-31 01:30:00    1.814582
2000-04-30 01:30:00    1.634858
```

Shifting dates with offsets

The pandas date offsets can also be used with `datetime` or `Timestamp` objects:

```
In [407]: from pandas.tseries.offsets import Day, MonthEnd

In [408]: now = datetime(2011, 11, 17)

In [409]: now + 3 * Day()
Out[409]: datetime.datetime(2011, 11, 20, 0, 0)
```

If you add an anchored offset like `MonthEnd`, the first increment will `roll forward` a date to the next date according to the frequency rule:

```
In [410]: now + MonthEnd()
Out[410]: datetime.datetime(2011, 11, 30, 0, 0)

In [411]: now + MonthEnd(2)
Out[411]: datetime.datetime(2011, 12, 31, 0, 0)
```

Anchored offsets can explicitly "roll" dates forward or backward using their `rollforward` and `rollback` methods, respectively:

```
In [412]: offset = MonthEnd()

In [413]: offset.rollforward(now)
Out[413]: datetime.datetime(2011, 11, 30, 0, 0)

In [414]: offset.rollback(now)
Out[414]: datetime.datetime(2011, 10, 31, 0, 0)
```

A clever use of date offsets is to use these methods with `groupby`:

```
In [415]: ts = Series(np.random.randn(20),
   .....:             index=pd.date_range('1/15/2000', periods=20, freq='4d'))

In [416]: ts.groupby(offset.rollforward).mean()
Out[416]:
2000-01-31   -0.448874
```

```
2000-02-29   -0.683663
2000-03-31    0.251920
```

Of course, an easier and faster way to do this is using `resample` (much more on this later):

```
In [417]: ts.resample('M', how='mean')
Out[417]:
2000-01-31   -0.448874
2000-02-29   -0.683663
2000-03-31    0.251920
Freq: M
```

Time Zone Handling

Working with time zones is generally considered one of the most unpleasant parts of time series manipulation. In particular, daylight savings time (DST) transitions are a common source of complication. As such, many time series users choose to work with time series in *coordinated universal time* or *UTC*, which is the successor to Greenwich Mean Time and is the current international standard. Time zones are expressed as offsets from UTC; for example, New York is four hours behind UTC during daylight savings time and 5 hours the rest of the year.

In Python, time zone information comes from the 3rd party `pytz` library, which exposes the *Olson database*, a compilation of world time zone information. This is especially important for historical data because the DST transition dates (and even UTC offsets) have been changed numerous times depending on the whims of local governments. In the United States,the DST transition times have been changed many times since 1900!

For detailed information about `pytz` library, you'll need to look at that library's documentation. As far as this book is concerned, pandas wraps `pytz`'s functionality so you can ignore its API outside of the time zone names. Time zone names can be found interactively and in the docs:

```
In [418]: import pytz

In [419]: pytz.common_timezones[-5:]
Out[419]: ['US/Eastern', 'US/Hawaii', 'US/Mountain', 'US/Pacific', 'UTC']
```

To get a time zone object from `pytz`, use `pytz.timezone`:

```
In [420]: tz = pytz.timezone('US/Eastern')

In [421]: tz
Out[421]: <DstTzInfo 'US/Eastern' EST-1 day, 19:00:00 STD>
```

Methods in pandas will accept either time zone names or these objects. I recommend just using the names.

Localization and Conversion

By default, time series in pandas are *time zone naive*. Consider the following time series:

```
rng = pd.date_range('3/9/2012 9:30', periods=6, freq='D')
ts = Series(np.random.randn(len(rng)), index=rng)
```

The index's `tz` field is `None`:

```
In [423]: print(ts.index.tz)
None
```

Date ranges can be generated with a time zone set:

```
In [424]: pd.date_range('3/9/2012 9:30', periods=10, freq='D', tz='UTC')
Out[424]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-03-09 09:30:00, ..., 2012-03-18 09:30:00]
Length: 10, Freq: D, Timezone: UTC
```

Conversion from naive to *localized* is handled by the `tz_localize` method:

```
In [425]: ts_utc = ts.tz_localize('UTC')

In [426]: ts_utc
Out[426]:
2012-03-09 09:30:00+00:00    0.414615
2012-03-10 09:30:00+00:00    0.427185
2012-03-11 09:30:00+00:00    1.172557
2012-03-12 09:30:00+00:00   -0.351572
2012-03-13 09:30:00+00:00    1.454593
2012-03-14 09:30:00+00:00    2.043319
Freq: D

In [427]: ts_utc.index
Out[427]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-03-09 09:30:00, ..., 2012-03-14 09:30:00]
Length: 6, Freq: D, Timezone: UTC
```

Once a time series has been localized to a particular time zone, it can be converted to another time zone using `tz_convert`:

```
In [428]: ts_utc.tz_convert('US/Eastern')
Out[428]:
2012-03-09 04:30:00-05:00    0.414615
2012-03-10 04:30:00-05:00    0.427185
2012-03-11 05:30:00-04:00    1.172557
2012-03-12 05:30:00-04:00   -0.351572
2012-03-13 05:30:00-04:00    1.454593
2012-03-14 05:30:00-04:00    2.043319
Freq: D
```

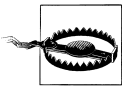
In the case of the above time series, which straddles a DST transition in the US/Eastern time zone, we could localize to EST and convert to, say, UTC or Berlin time:

```
In [429]: ts_eastern = ts.tz_localize('US/Eastern')
```

```
In [430]: ts_eastern.tz_convert('UTC')
Out[430]:
2012-03-09 14:30:00+00:00    0.414615
2012-03-10 14:30:00+00:00    0.427185
2012-03-11 13:30:00+00:00    1.172557
2012-03-12 13:30:00+00:00   -0.351572
2012-03-13 13:30:00+00:00    1.454593
2012-03-14 13:30:00+00:00    2.043319
Freq: D

In [431]: ts_eastern.tz_convert('Europe/Berlin')
Out[431]:
2012-03-09 15:30:00+01:00    0.414615
2012-03-10 15:30:00+01:00    0.427185
2012-03-11 14:30:00+01:00    1.172557
2012-03-12 14:30:00+01:00   -0.351572
2012-03-13 14:30:00+01:00    1.454593
2012-03-14 14:30:00+01:00    2.043319
Freq: D
```

`tz_localize` and `tz_convert` are also instance methods on `DatetimeIndex`:

```
In [432]: ts.index.tz_localize('Asia/Shanghai')
Out[432]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-03-09 09:30:00, ..., 2012-03-14 09:30:00]
Length: 6, Freq: D, Timezone: Asia/Shanghai
```



Localizing naive timestamps also checks for ambiguous or non-existent times around daylight savings time transitions.

Operations with Time Zone–aware Timestamp Objects

Similar to time series and date ranges, individual Timestamp objects similarly can be localized from naive to time zone-aware and converted from one time zone to another:

```
In [433]: stamp = pd.Timestamp('2011-03-12 04:00')

In [434]: stamp_utc = stamp.tz_localize('utc')

In [435]: stamp_utc.tz_convert('US/Eastern')
Out[435]: <Timestamp: 2011-03-11 23:00:00-0500 EST, tz=US/Eastern>
```

You can also pass a time zone when creating the Timestamp:

```
In [436]: stamp_moscow = pd.Timestamp('2011-03-12 04:00', tz='Europe/Moscow')

In [437]: stamp_moscow
Out[437]: <Timestamp: 2011-03-12 04:00:00+0300 MSK, tz=Europe/Moscow>
```

Time zone-aware Timestamp objects internally store a UTC timestamp value as nanoseconds since the UNIX epoch (January 1, 1970); this UTC value is invariant between time zone conversions:

```
In [438]: stamp_utc.value
Out[438]: 1299902400000000000

In [439]: stamp_utc.tz_convert('US/Eastern').value
Out[439]: 1299902400000000000
```

When performing time arithmetic using pandas's `DateOffset` objects, daylight savings time transitions are respected where possible:

```
# 30 minutes before DST transition
In [440]: from pandas.tseries.offsets import Hour

In [441]: stamp = pd.Timestamp('2012-03-12 01:30', tz='US/Eastern')

In [442]: stamp
Out[442]: <Timestamp: 2012-03-12 01:30:00-0400 EDT, tz=US/Eastern>

In [443]: stamp + Hour()
Out[443]: <Timestamp: 2012-03-12 02:30:00-0400 EDT, tz=US/Eastern>

# 90 minutes before DST transition
In [444]: stamp = pd.Timestamp('2012-11-04 00:30', tz='US/Eastern')

In [445]: stamp
Out[445]: <Timestamp: 2012-11-04 00:30:00-0400 EDT, tz=US/Eastern>

In [446]: stamp + 2 * Hour()
Out[446]: <Timestamp: 2012-11-04 01:30:00-0500 EST, tz=US/Eastern>
```

Operations between Different Time Zones

If two time series with different time zones are combined, the result will be UTC. Since the timestamps are stored under the hood in UTC, this is a straightforward operation and requires no conversion to happen:

```
In [447]: rng = pd.date_range('3/7/2012 9:30', periods=10, freq='B')

In [448]: ts = Series(np.random.randn(len(rng)), index=rng)

In [449]: ts
Out[449]:
2012-03-07 09:30:00   -1.749309
2012-03-08 09:30:00   -0.387235
2012-03-09 09:30:00   -0.208074
2012-03-12 09:30:00   -1.221957
2012-03-13 09:30:00   -0.067460
2012-03-14 09:30:00    0.229005
2012-03-15 09:30:00   -0.576234
2012-03-16 09:30:00    0.816895
2012-03-19 09:30:00   -0.772192
2012-03-20 09:30:00   -1.333576
Freq: B

In [450]: ts1 = ts[:7].tz_localize('Europe/London')
```

```
In [451]: ts2 = ts1[2:].tz_convert('Europe/Moscow')

In [452]: result = ts1 + ts2

In [453]: result.index
Out[453]:
<class 'pandas.tseries.index.DatetimeIndex'>
[2012-03-07 09:30:00, ..., 2012-03-15 09:30:00]
Length: 7, Freq: B, Timezone: UTC
```

Periods and Period Arithmetic

Periods represent time spans, like days, months, quarters, or years. The `Period` class represents this data type, requiring a string or integer and a frequency from the above table:

```
In [454]: p = pd.Period(2007, freq='A-DEC')

In [455]: p
Out[455]: Period('2007', 'A-DEC')
```

In this case, the `Period` object represents the full timespan from January 1, 2007 to December 31, 2007, inclusive. Conveniently, adding and subtracting integers from periods has the effect of shifting by their frequency:

```
In [456]: p + 5                          In [457]: p - 2
Out[456]: Period('2012', 'A-DEC')        Out[457]: Period('2005', 'A-DEC')
```

If two periods have the same frequency, their difference is the number of units between them:

```
In [458]: pd.Period('2014', freq='A-DEC') - p
Out[458]: 7
```

Regular ranges of periods can be constructed using the `period_range` function:

```
In [459]: rng = pd.period_range('1/1/2000', '6/30/2000', freq='M')

In [460]: rng
Out[460]:
<class 'pandas.tseries.period.PeriodIndex'>
freq: M
[2000-01, ..., 2000-06]
length: 6
```

The `PeriodIndex` class stores a sequence of periods and can serve as an axis index in any pandas data structure:

```
In [461]: Series(np.random.randn(6), index=rng)
Out[461]:
2000-01   -0.309119
2000-02    0.028558
2000-03    1.129605
2000-04   -0.374173
2000-05   -0.011401
```

```
2000-06    0.272924
Freq: M
```

If you have an array of strings, you can also appeal to the `PeriodIndex` class itself:

```
In [462]: values = ['2001Q3', '2002Q2', '2003Q1']

In [463]: index = pd.PeriodIndex(values, freq='Q-DEC')

In [464]: index
Out[464]:
<class 'pandas.tseries.period.PeriodIndex'>
freq: Q-DEC
[2001Q3, ..., 2003Q1]
length: 3
```

Period Frequency Conversion

Periods and `PeriodIndex` objects can be converted to another frequency using their `asfreq` method. As an example, suppose we had an annual period and wanted to convert it into a monthly period either at the start or end of the year. This is fairly straightforward:

```
In [465]: p = pd.Period('2007', freq='A-DEC')

In [466]: p.asfreq('M', how='start')      In [467]: p.asfreq('M', how='end')
Out[466]: Period('2007-01', 'M')         Out[467]: Period('2007-12', 'M')
```

You can think of `Period('2007', 'A-DEC')` as being a cursor pointing to a span of time, subdivided by monthly periods. See Figure 10-1 for an illustration of this. For a *fiscal year* ending on a month other than December, the monthly subperiods belonging are different:

```
In [468]: p = pd.Period('2007', freq='A-JUN')

In [469]: p.asfreq('M', 'start')       In [470]: p.asfreq('M', 'end')
Out[469]: Period('2006-07', 'M')      Out[470]: Period('2007-07', 'M')
```

When converting from high to low frequency, the superperiod will be determined depending on where the subperiod "belongs". For example, in `A-JUN` frequency, the month `Aug-2007` is actually part of the `2008` period:

```
In [471]: p = pd.Period('2007-08', 'M')

In [472]: p.asfreq('A-JUN')
Out[472]: Period('2008', 'A-JUN')
```

Whole `PeriodIndex` objects or TimeSeries can be similarly converted with the same semantics:

```
In [473]: rng = pd.period_range('2006', '2009', freq='A-DEC')

In [474]: ts = Series(np.random.randn(len(rng)), index=rng)

In [475]: ts
```

```
Out[475]:
2006   -0.601544
2007    0.574265
2008   -0.194115
2009    0.202225
Freq: A-DEC

In [476]: ts.asfreq('M', how='start')
Out[476]:
2006-01   -0.601544
2007-01    0.574265
2008-01   -0.194115
2009-01    0.202225
Freq: M

In [477]: ts.asfreq('B', how='end')
Out[477]:
2006-12-29   -0.601544
2007-12-31    0.574265
2008-12-31   -0.194115
2009-12-31    0.202225
Freq: B
```

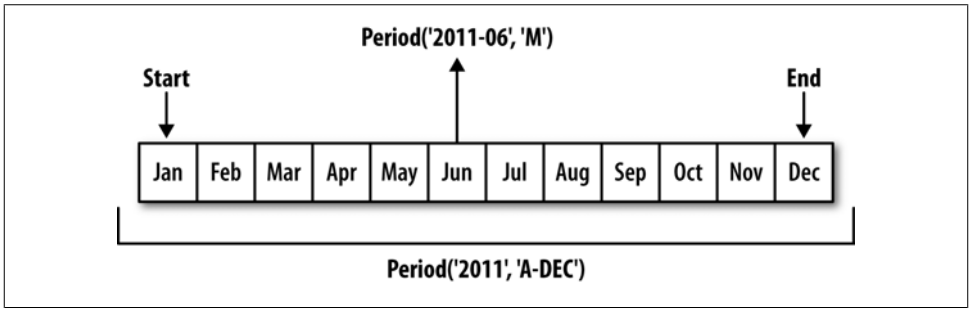


Figure 10-1. Period frequency conversion illustration

Quarterly Period Frequencies

Quarterly data is standard in accounting, finance, and other fields. Much quarterly data is reported relative to a *fiscal year end*, typically the last calendar or business day of one of the 12 months of the year. As such, the period `2012Q4` has a different meaning depending on fiscal year end. pandas supports all 12 possible quarterly frequencies as `Q-JAN` through `Q-DEC`:

```
In [478]: p = pd.Period('2012Q4', freq='Q-JAN')

In [479]: p
Out[479]: Period('2012Q4', 'Q-JAN')
```

In the case of fiscal year ending in January, `2012Q4` runs from November through January, which you can check by converting to daily frequency. See Figure 10-2 for an illustration:

```
In [480]: p.asfreq('D', 'start')
Out[480]: Period('2011-11-01', 'D')

In [481]: p.asfreq('D', 'end')
Out[481]: Period('2012-01-31', 'D')
```

Thus, it's possible to do period arithmetic very easily; for example, to get the timestamp at 4PM on the 2nd to last business day of the quarter, you could do:

```
In [482]: p4pm = (p.asfreq('B', 'e') - 1).asfreq('T', 's') + 16 * 60

In [483]: p4pm
Out[483]: Period('2012-01-30 16:00', 'T')

In [484]: p4pm.to_timestamp()
Out[484]: <Timestamp: 2012-01-30 16:00:00>
```

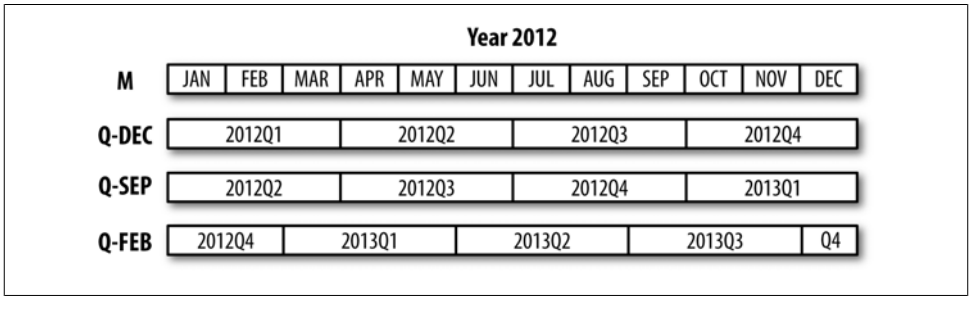


Figure 10-2. Different quarterly frequency conventions

Generating quarterly ranges works as you would expect using `period_range`. Arithmetic is identical, too:

```
In [485]: rng = pd.period_range('2011Q3', '2012Q4', freq='Q-JAN')

In [486]: ts = Series(np.arange(len(rng)), index=rng)

In [487]: ts
Out[487]:
2011Q3    0
2011Q4    1
2012Q1    2
2012Q2    3
2012Q3    4
2012Q4    5
Freq: Q-JAN

In [488]: new_rng = (rng.asfreq('B', 'e') - 1).asfreq('T', 's') + 16 * 60

In [489]: ts.index = new_rng.to_timestamp()

In [490]: ts
Out[490]:
2010-10-28 16:00:00    0
2011-01-28 16:00:00    1
2011-04-28 16:00:00    2
2011-07-28 16:00:00    3
2011-10-28 16:00:00    4
2012-01-30 16:00:00    5
```

Converting Timestamps to Periods (and Back)

Series and DataFrame objects indexed by timestamps can be converted to periods using the `to_period` method:

```
In [491]: rng = pd.date_range('1/1/2000', periods=3, freq='M')

In [492]: ts = Series(randn(3), index=rng)

In [493]: pts = ts.to_period()

In [494]: ts                    In [495]: pts
Out[494]:                       Out[495]:
2000-01-31   -0.505124          2000-01   -0.505124
2000-02-29    2.954439          2000-02    2.954439
2000-03-31   -2.630247          2000-03   -2.630247
Freq: M                         Freq: M
```

Since periods always refer to non-overlapping timespans, a timestamp can only belong to a single period for a given frequency. While the frequency of the new `PeriodIndex` is inferred from the timestamps by default, you can specify any frequency you want. There is also no problem with having duplicate periods in the result:

```
In [496]: rng = pd.date_range('1/29/2000', periods=6, freq='D')

In [497]: ts2 = Series(randn(6), index=rng)

In [498]: ts2.to_period('M')
Out[498]:
2000-01   -0.352453
2000-01   -0.477808
2000-01    0.161594
2000-02    1.686833
2000-02    0.821965
2000-02   -0.667406
Freq: M
```

To convert back to timestamps, use `to_timestamp`:

```
In [499]: pts = ts.to_period()

In [500]: pts
Out[500]:
2000-01   -0.505124
2000-02    2.954439
2000-03   -2.630247
Freq: M

In [501]: pts.to_timestamp(how='end')
Out[501]:
2000-01-31   -0.505124
2000-02-29    2.954439
2000-03-31   -2.630247
Freq: M
```

Creating a PeriodIndex from Arrays

Fixed frequency data sets are sometimes stored with timespan information spread across multiple columns. For example, in this macroeconomic data set, the year and quarter are in different columns:

```
In [502]: data = pd.read_csv('ch08/macrodata.csv')

In [503]: data.year
Out[503]:
0    1959
1    1959
2    1959
3    1959
...
199    2008
200    2009
201    2009
202    2009
Name: year, Length: 203

In [504]: data.quarter
Out[504]:
0    1
1    2
2    3
3    4
...
199    4
200    1
201    2
202    3
Name: quarter, Length: 203
```

By passing these arrays to `PeriodIndex` with a frequency, they can be combined to form an index for the DataFrame:

```
In [505]: index = pd.PeriodIndex(year=data.year, quarter=data.quarter, freq='Q-DEC')

In [506]: index
Out[506]:
<class 'pandas.tseries.period.PeriodIndex'>
freq: Q-DEC
[1959Q1, ..., 2009Q3]
length: 203

In [507]: data.index = index

In [508]: data.infl
Out[508]:
1959Q1    0.00
1959Q2    2.34
1959Q3    2.74
1959Q4    0.27
...
2008Q4   -8.79
2009Q1    0.94
2009Q2    3.37
2009Q3    3.56
Freq: Q-DEC, Name: infl, Length: 203
```

Resampling and Frequency Conversion

Resampling refers to the process of converting a time series from one frequency to another. Aggregating higher frequency data to lower frequency is called *downsampling*, while converting lower frequency to higher frequency is called *upsampling*. Not

all resampling falls into either of these categories; for example, converting `W-WED` (weekly on Wednesday) to `W-FRI` is neither upsampling nor downstampling.

pandas objects are equipped with a `resample` method, which is the workhorse function for all frequency conversion:

```
In [509]: rng = pd.date_range('1/1/2000', periods=100, freq='D')

In [510]: ts = Series(randn(len(rng)), index=rng)

In [511]: ts.resample('M', how='mean')
Out[511]:
2000-01-31    0.170876
2000-02-29    0.165020
2000-03-31    0.095451
2000-04-30    0.363566
Freq: M

In [512]: ts.resample('M', how='mean', kind='period')
Out[512]:
2000-01    0.170876
2000-02    0.165020
2000-03    0.095451
2000-04    0.363566
Freq: M
```

`resample` is a flexible and high-performance method that can be used to process very large time series. I'll illustrate its semantics and use through a series of examples.

Table 10-5. Resample method arguments

Argument	Description
`freq`	String or DateOffset indicating desired resampled frequency, e.g. 'M', '5min', or Second(15)
`how='mean'`	Function name or array function producing aggregated value, for example `'mean'`, `'ohlc'`, `np.max`. Defaults to `'mean'`. Other common values: `'first', 'last', 'median', 'ohlc', 'max', 'min'`.
`axis=0`	Axis to resample on, default axis=0
`fill_method=None`	How to interpolate when upsampling, as in `'ffill'` or `'bfill'`. By default does no interpolation.
`closed='right'`	In downsampling, which end of each interval is closed (inclusive), `'right'` or `'left'`. Defaults to `'right'`
`label='right'`	In downsampling, how to label the aggregated result, with the `'right'` or `'left'` bin edge. For example, the 9:30 to 9:35 5-minute interval could be labeled `9:30` or `9:35`. Defaults to `'right'` (or 9:35, in this example).
`loffset=None`	Time adjustment to the bin labels, such as `'-1s'` / `Second(-1)` to shift the aggregate labels one second earlier
`limit=None`	When forward or backward filling, the maximum number of periods to fill

Argument	Description
`kind=None`	Aggregate to periods (`'period'`) or timestamps (`'timestamp'`); defaults to kind of index the time series has
`convention=None`	When resampling periods, the convention (`'start'` or `'end'`) for converting the low frequency period to high frequency. Defaults to `'end'`

Downsampling

Aggregating data to a regular, lower frequency is a pretty normal time series task. The data you're aggregating doesn't need to be fixed frequently; the desired frequency defines *bin edges* that are used to slice the time series into pieces to aggregate. For example, to convert to monthly, `'M'` or `'BM'`, the data need to be chopped up into one month intervals. Each interval is said to be *half-open*; a data point can only belong to one interval, and the union of the intervals must make up the whole time frame. There are a couple things to think about when using `resample` to downsample data:

- Which side of each interval is *closed*
- How to label each aggregated bin, either with the start of the interval or the end

To illustrate, let's look at some one-minute data:

```
In [513]: rng = pd.date_range('1/1/2000', periods=12, freq='T')

In [514]: ts = Series(np.arange(12), index=rng)

In [515]: ts
Out[515]:
2000-01-01 00:00:00     0
2000-01-01 00:01:00     1
2000-01-01 00:02:00     2
2000-01-01 00:03:00     3
2000-01-01 00:04:00     4
2000-01-01 00:05:00     5
2000-01-01 00:06:00     6
2000-01-01 00:07:00     7
2000-01-01 00:08:00     8
2000-01-01 00:09:00     9
2000-01-01 00:10:00    10
2000-01-01 00:11:00    11
Freq: T
```

Suppose you wanted to aggregate this data into five-minute chunks or *bars* by taking the sum of each group:

```
In [516]: ts.resample('5min', how='sum')
Out[516]:
2000-01-01 00:00:00     0
2000-01-01 00:05:00    15
2000-01-01 00:10:00    40
2000-01-01 00:15:00    11
Freq: 5T
```

The frequency you pass defines bin edges in five-minute increments. By default, the *right* bin edge is inclusive, so the `00:05` value is included in the `00:00` to `00:05` interval.[1] Passing `closed='left'` changes the interval to be closed on the left:

```
In [517]: ts.resample('5min', how='sum', closed='left')
Out[517]:
2000-01-01 00:05:00    10
2000-01-01 00:10:00    35
2000-01-01 00:15:00    21
Freq: 5T
```

As you can see, the resulting time series is labeled by the timestamps from the right side of each bin. By passing `label='left'` you can label them with the left bin edge:

```
In [518]: ts.resample('5min', how='sum', closed='left', label='left')
Out[518]:
2000-01-01 00:00:00    10
2000-01-01 00:05:00    35
2000-01-01 00:10:00    21
Freq: 5T
```

See Figure 10-3 for an illustration of minutely data being resampled to five-minute.

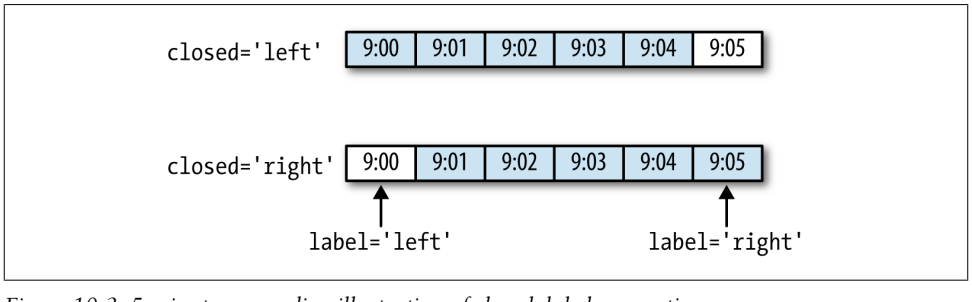


Figure 10-3. 5-minute resampling illustration of closed, label conventions

Lastly, you might want to shift the result index by some amount, say subtracting one second from the right edge to make it more clear which interval the timestamp refers to. To do this, pass a string or date offset to `loffset`:

```
In [519]: ts.resample('5min', how='sum', loffset='-1s')
Out[519]:
1999-12-31 23:59:59     0
2000-01-01 00:04:59    15
2000-01-01 00:09:59    40
2000-01-01 00:14:59    11
Freq: 5T
```

1. The choice of `closed='right', label='right'` as the default might seem a bit odd to some users. In practice the choice is somewhat arbitrary; for some target frequencies, `closed='left'` is preferable, while for others `closed='right'` makes more sense. The important thing is that you keep in mind exactly how you are segmenting the data.

This also could have been accomplished by calling the `shift` method on the result without the `loffset`.

Open-High-Low-Close (OHLC) resampling

In finance, an ubiquitous way to aggregate a time series is to compute four values for each bucket: the first (open), last (close), maximum (high), and minimal (low) values. By passing `how='ohlc'` you will obtain a DataFrame having columns containing these four aggregates, which are efficiently computed in a single sweep of the data:

```
In [520]: ts.resample('5min', how='ohlc')
Out[520]:
                     open  high  low  close
2000-01-01 00:00:00     0     0    0      0
2000-01-01 00:05:00     1     5    1      5
2000-01-01 00:10:00     6    10    6     10
2000-01-01 00:15:00    11    11   11     11
```

Resampling with GroupBy

An alternate way to downsample is to use pandas's `groupby` functionality. For example, you can group by month or weekday by passing a function that accesses those fields on the time series's index:

```
In [521]: rng = pd.date_range('1/1/2000', periods=100, freq='D')

In [522]: ts = Series(np.arange(100), index=rng)

In [523]: ts.groupby(lambda x: x.month).mean()
Out[523]:
1    15
2    45
3    75
4    95

In [524]: ts.groupby(lambda x: x.weekday).mean()
Out[524]:
0    47.5
1    48.5
2    49.5
3    50.5
4    51.5
5    49.0
6    50.0
```

Upsampling and Interpolation

When converting from a low frequency to a higher frequency, no aggregation is needed. Let's consider a DataFrame with some weekly data:

```
In [525]: frame = DataFrame(np.random.randn(2, 4),
   .....:                   index=pd.date_range('1/1/2000', periods=2, freq='W-WED'),
   .....:                   columns=['Colorado', 'Texas', 'New York', 'Ohio'])
```

```
In [526]: frame[:5]
Out[526]:
            Colorado     Texas  New York     Ohio
2000-01-05 -0.609657 -0.268837  0.195592  0.85979
2000-01-12 -0.263206  1.141350 -0.101937 -0.07666
```

When resampling this to daily frequency, by default missing values are introduced:

```
In [527]: df_daily = frame.resample('D')

In [528]: df_daily
Out[528]:
            Colorado     Texas  New York     Ohio
2000-01-05 -0.609657 -0.268837  0.195592  0.85979
2000-01-06       NaN       NaN       NaN      NaN
2000-01-07       NaN       NaN       NaN      NaN
2000-01-08       NaN       NaN       NaN      NaN
2000-01-09       NaN       NaN       NaN      NaN
2000-01-10       NaN       NaN       NaN      NaN
2000-01-11       NaN       NaN       NaN      NaN
2000-01-12 -0.263206  1.141350 -0.101937 -0.07666
```

Suppose you wanted to fill forward each weekly value on the non-Wednesdays. The same filling or interpolation methods available in the `fillna` and `reindex` methods are available for resampling:

```
In [529]: frame.resample('D', fill_method='ffill')
Out[529]:
            Colorado     Texas  New York     Ohio
2000-01-05 -0.609657 -0.268837  0.195592  0.85979
2000-01-06 -0.609657 -0.268837  0.195592  0.85979
2000-01-07 -0.609657 -0.268837  0.195592  0.85979
2000-01-08 -0.609657 -0.268837  0.195592  0.85979
2000-01-09 -0.609657 -0.268837  0.195592  0.85979
2000-01-10 -0.609657 -0.268837  0.195592  0.85979
2000-01-11 -0.609657 -0.268837  0.195592  0.85979
2000-01-12 -0.263206  1.141350 -0.101937 -0.07666
```

You can similarly choose to only fill a certain number of periods forward to limit how far to continue using an observed value:

```
In [530]: frame.resample('D', fill_method='ffill', limit=2)
Out[530]:
            Colorado     Texas  New York     Ohio
2000-01-05 -0.609657 -0.268837  0.195592  0.85979
2000-01-06 -0.609657 -0.268837  0.195592  0.85979
2000-01-07 -0.609657 -0.268837  0.195592  0.85979
2000-01-08       NaN       NaN       NaN      NaN
2000-01-09       NaN       NaN       NaN      NaN
2000-01-10       NaN       NaN       NaN      NaN
2000-01-11       NaN       NaN       NaN      NaN
2000-01-12 -0.263206  1.141350 -0.101937 -0.07666
```

Notably, the new date index need not overlap with the old one at all:

```
In [531]: frame.resample('W-THU', fill_method='ffill')
Out[531]:
            Colorado     Texas  New York     Ohio
2000-01-06 -0.609657 -0.268837  0.195592  0.85979
2000-01-13 -0.263206  1.141350 -0.101937 -0.07666
```

Resampling with Periods

Resampling data indexed by periods is reasonably straightforward and works as you would hope:

```
In [532]: frame = DataFrame(np.random.randn(24, 4),
   .....:                   index=pd.period_range('1-2000', '12-2001', freq='M'),
   .....:                   columns=['Colorado', 'Texas', 'New York', 'Ohio'])

In [533]: frame[:5]
Out[533]:
         Colorado     Texas  New York      Ohio
2000-01  0.120837  1.076607  0.434200  0.056432
2000-02 -0.378890  0.047831  0.341626  1.567920
2000-03 -0.047619 -0.821825 -0.179330 -0.166675
2000-04  0.333219 -0.544615 -0.653635 -2.311026
2000-05  1.612270 -0.806614  0.557884  0.580201

In [534]: annual_frame = frame.resample('A-DEC', how='mean')

In [535]: annual_frame
Out[535]:
      Colorado     Texas  New York      Ohio
2000  0.352070 -0.553642  0.196642 -0.094099
2001  0.158207  0.042967 -0.360755  0.184687
```

Upsampling is more nuanced as you must make a decision about which end of the timespan in the new frequency to place the values before resampling, just like the `asfreq` method. The `convention` argument defaults to `'end'` but can also be `'start'`:

```
# Q-DEC: Quarterly, year ending in December
In [536]: annual_frame.resample('Q-DEC', fill_method='ffill')
Out[536]:
        Colorado     Texas  New York      Ohio
2000Q4  0.352070 -0.553642  0.196642 -0.094099
2001Q1  0.352070 -0.553642  0.196642 -0.094099
2001Q2  0.352070 -0.553642  0.196642 -0.094099
2001Q3  0.352070 -0.553642  0.196642 -0.094099
2001Q4  0.158207  0.042967 -0.360755  0.184687

In [537]: annual_frame.resample('Q-DEC', fill_method='ffill', convention='start')
Out[537]:
        Colorado     Texas  New York      Ohio
2000Q1  0.352070 -0.553642  0.196642 -0.094099
2000Q2  0.352070 -0.553642  0.196642 -0.094099
2000Q3  0.352070 -0.553642  0.196642 -0.094099
2000Q4  0.352070 -0.553642  0.196642 -0.094099
2001Q1  0.158207  0.042967 -0.360755  0.184687
```

Since periods refer to timespans, the rules about upsampling and downsampling are more rigid:

- In downsampling, the target frequency must be a *subperiod* of the source frequency.
- In upsampling, the target frequency must be a *superperiod* of the source frequency.

If these rules are not satisfied, an exception will be raised. This mainly affects the quarterly, annual, and weekly frequencies; for example, the timespans defined by `Q-MAR` only line up with `A-MAR, A-JUN, A-SEP,` and `A-DEC`:

```
In [538]: annual_frame.resample('Q-MAR', fill_method='ffill')
Out[538]:
        Colorado     Texas  New York      Ohio
2001Q3  0.352070 -0.553642  0.196642 -0.094099
2001Q4  0.352070 -0.553642  0.196642 -0.094099
2002Q1  0.352070 -0.553642  0.196642 -0.094099
2002Q2  0.352070 -0.553642  0.196642 -0.094099
2002Q3  0.158207  0.042967 -0.360755  0.184687
```

Time Series Plotting

Plots with pandas time series have improved date formatting compared with matplotlib out of the box. As an example, I downloaded some stock price data on a few common US stock from Yahoo! Finance:

```
In [539]: close_px_all = pd.read_csv('ch09/stock_px.csv', parse_dates=True, index_col=0)

In [540]: close_px = close_px_all[['AAPL', 'MSFT', 'XOM']]

In [541]: close_px = close_px.resample('B', fill_method='ffill')

In [542]: close_px
Out[542]:
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 2292 entries, 2003-01-02 00:00:00 to 2011-10-14 00:00:00
Freq: B
Data columns:
AAPL    2292  non-null values
MSFT    2292  non-null values
XOM     2292  non-null values
dtypes: float64(3)
```

Calling `plot` on one of the columns grenerates a simple plot, seen in Figure 10-4.

```
In [544]: close_px['AAPL'].plot()
```

When called on a DataFrame, as you would expect, all of the time series are drawn on a single subplot with a legend indicating which is which. I'll plot only the year 2009 data so you can see how both months and years are formatted on the X axis; see Figure 10-5.

```
In [546]: close_px.ix['2009'].plot()
```

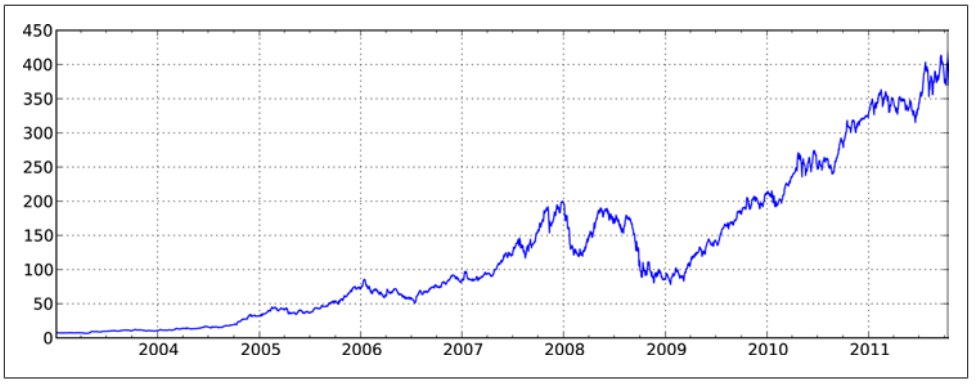


Figure 10-4. AAPL Daily Price

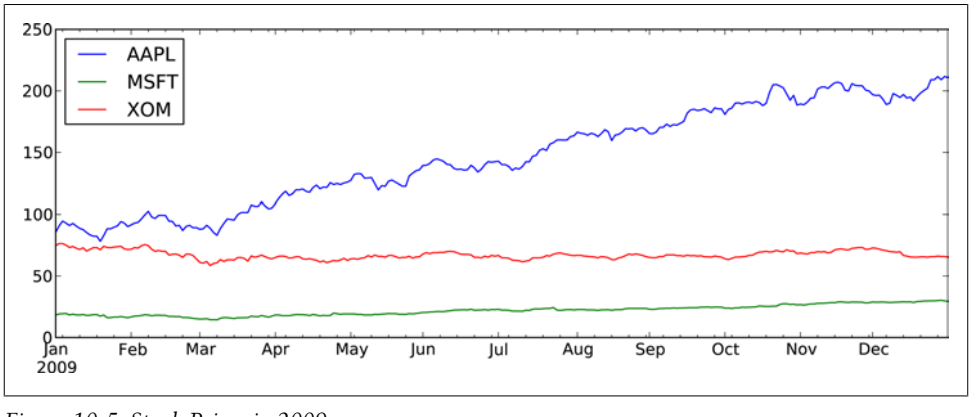


Figure 10-5. Stock Prices in 2009

```
In [548]: close_px['AAPL'].ix['01-2011':'03-2011'].plot()
```

Quarterly frequency data is also more nicely formatted with quarterly markers, something that would be quite a bit more work to do by hand. See Figure 10-7.

```
In [550]: appl_q = close_px['AAPL'].resample('Q-DEC', fill_method='ffill')

In [551]: appl_q.ix['2009':].plot()
```

A last feature of time series plotting in pandas is that by right-clicking and dragging to zoom in and out, the dates will be dynamically expanded or contracted and reformatting depending on the timespan contained in the plot view. This is of course only true when using matplotlib in interactive mode.

Moving Window Functions

A common class of array transformations intended for time series operations are statistics and other functions evaluated over a sliding window or with exponentially de-

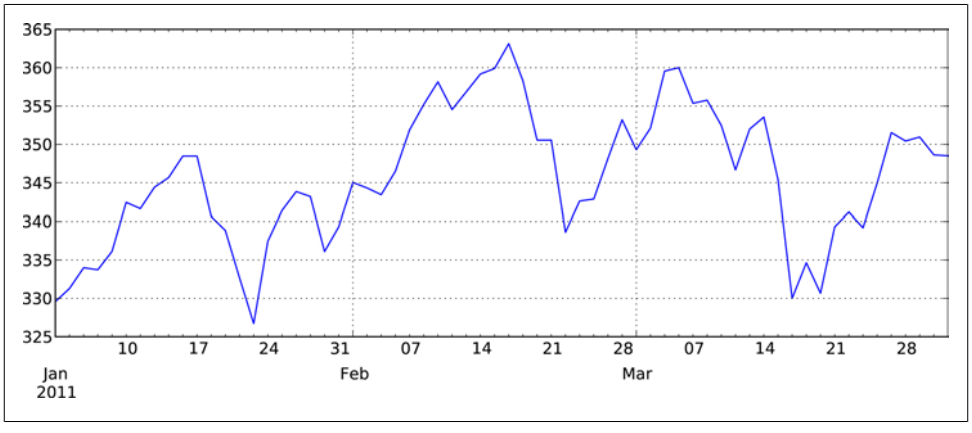


Figure 10-6. Apple Daily Price in 1/2011-3/2011

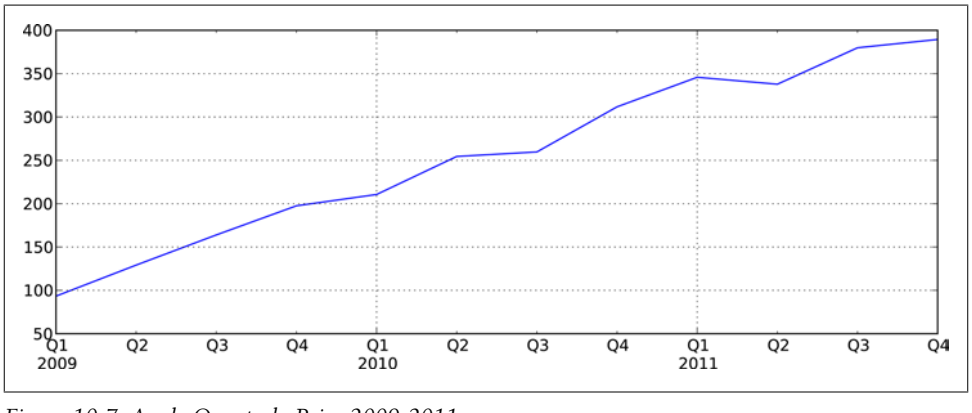


Figure 10-7. Apple Quarterly Price 2009-2011

caying weights. I call these *moving window functions*, even though it includes functions without a fixed-length window like exponentially-weighted moving average. Like other statistical functions, these also automatically exclude missing data.

`rolling_mean` is one of the simplest such functions. It takes a TimeSeries or DataFrame along with a `window` (expressed as a number of periods):

```
In [555]: close_px.AAPL.plot()
Out[555]: <matplotlib.axes.AxesSubplot at 0x1099b3990>

In [556]: pd.rolling_mean(close_px.AAPL, 250).plot()
```

See Figure 10-8 for the plot. By default functions like `rolling_mean` require the indicated number of non-NA observations. This behavior can be changed to account for missing data and, in particular, the fact that you will have fewer than `window` periods of data at the beginning of the time series (see Figure 10-9):

```
In [558]: appl_std250 = pd.rolling_std(close_px.AAPL, 250, min_periods=10)

In [559]: appl_std250[5:12]
Out[559]:
2003-01-09         NaN
2003-01-10         NaN
2003-01-13         NaN
2003-01-14         NaN
2003-01-15    0.077496
2003-01-16    0.074760
2003-01-17    0.112368
Freq: B

In [560]: appl_std250.plot()
```

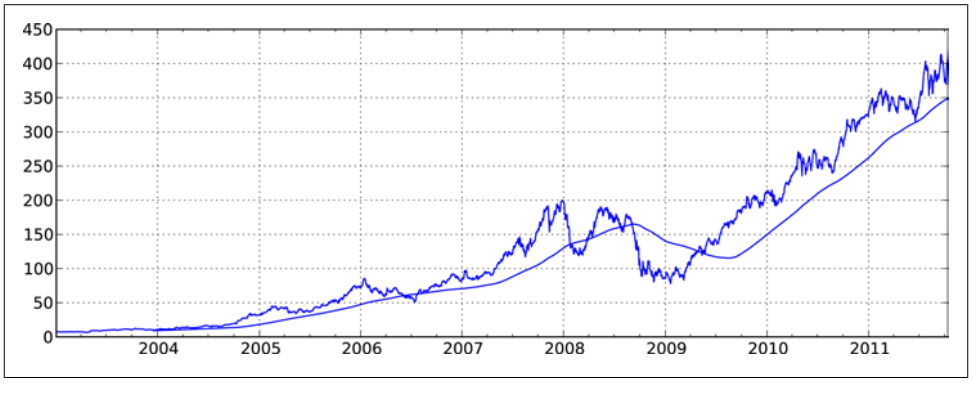


Figure 10-8. Apple Price with 250-day MA

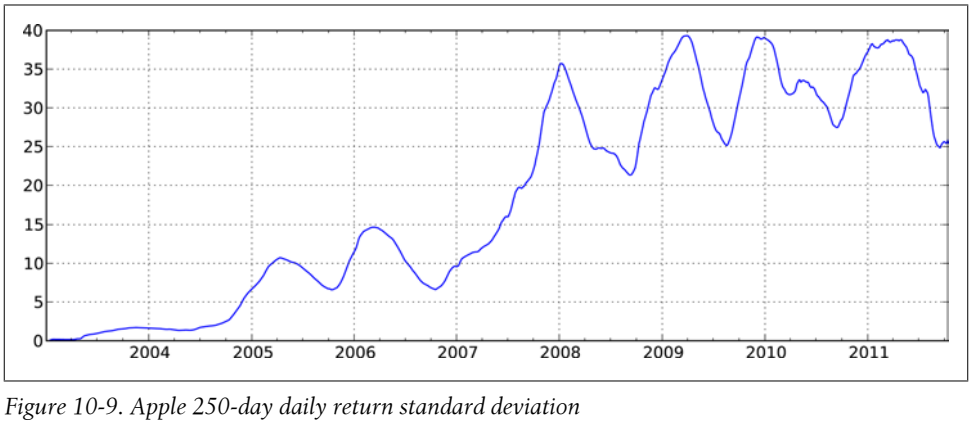


Figure 10-9. Apple 250-day daily return standard deviation

To compute an *expanding window mean*, you can see that an expanding window is just a special case where the window is the length of the time series, but only one or more periods is required to compute a value:

```
# Define expanding mean in terms of rolling_mean
In [561]: expanding_mean = lambda x: rolling_mean(x, len(x), min_periods=1)
```

Calling `rolling_mean` and friends on a DataFrame applies the transformation to each column (see Figure 10-10):

```
In [563]: pd.rolling_mean(close_px, 60).plot(logy=True)
```

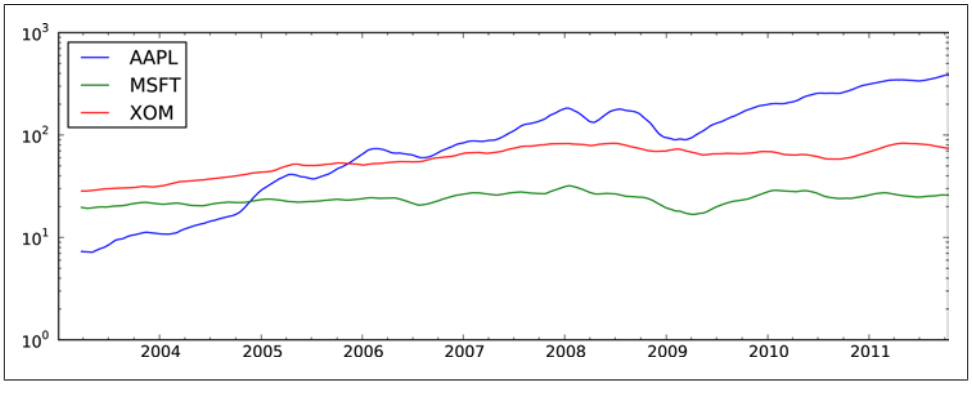


Figure 10-10. Stocks Prices 60-day MA (log Y-axis)

See Table 10-6 for a listing of related functions in pandas.

Table 10-6. Moving window and exponentially-weighted functions

Function	Description
`rolling_count`	Returns number of non-NA observations in each trailing window.
`rolling_sum`	Moving window sum.
`rolling_mean`	Moving window mean.
`rolling_median`	Moving window median.
`rolling_var, rolling_std`	Moving window variance and standard deviation, respectively. Uses n - 1 denominator.
`rolling_skew, rolling_kurt`	Moving window skewness (3rd moment) and kurtosis (4th moment), respectively.
`rolling_min, rolling_max`	Moving window minimum and maximum.
`rolling_quantile`	Moving window score at percentile/sample quantile.
`rolling_corr, rolling_cov`	Moving window correlation and covariance.
`rolling_apply`	Apply generic array function over a moving window.
`ewma`	Exponentially-weighted moving average.
`ewmvar, ewmstd`	Exponentially-weighted moving variance and standard deviation.
`ewmcorr, ewmcov`	Exponentially-weighted moving correlation and covariance.

`bottleneck`, a Python library by Keith Goodman, provides an alternate implementation of `NaN`-friendly moving window functions and may be worth looking at depending on your application.

Exponentially-weighted functions

An alternative to using a static window size with equally-weighted observations is to specify a constant *decay factor* to give more weight to more recent observations. In mathematical terms, if ma_t is the moving average result at time `t` and x is the time series in question, each value in the result is computed as $ma_t = a * ma_{t-1} + (a - 1) * x_t$, where a is the decay factor. There are a couple of ways to specify the decay factor, a popular one is using a *span*, which makes the result comparable to a simple moving window function with window size equal to the span.

Since an exponentially-weighted statistic places more weight on more recent observations, it "adapts" faster to changes compared with the equal-weighted version. Here's an example comparing a 60-day moving average of Apple's stock price with an EW moving average with `span=60` (see Figure 10-11):

```
fig, axes = plt.subplots(nrows=2, ncols=1, sharex=True, sharey=True,
                         figsize=(12, 7))

aapl_px = close_px.AAPL['2005':'2009']

ma60 = pd.rolling_mean(aapl_px, 60, min_periods=50)
ewma60 = pd.ewma(aapl_px, span=60)

aapl_px.plot(style='k-', ax=axes[0])
ma60.plot(style='k--', ax=axes[0])
aapl_px.plot(style='k-', ax=axes[1])
ewma60.plot(style='k--', ax=axes[1])
axes[0].set_title('Simple MA')
axes[1].set_title('Exponentially-weighted MA')
```

Binary Moving Window Functions

Some statistical operators, like correlation and covariance, need to operate on two time series. As an example, financial analysts are often interested in a stock's correlation to a benchmark index like the S&P 500. We can compute that by computing the percent changes and using `rolling_corr` (see Figure 10-12):

```
In [570]: spx_rets = spx_px / spx_px.shift(1) - 1

In [571]: returns = close_px.pct_change()

In [572]: corr = pd.rolling_corr(returns.AAPL, spx_rets, 125, min_periods=100)

In [573]: corr.plot()
```

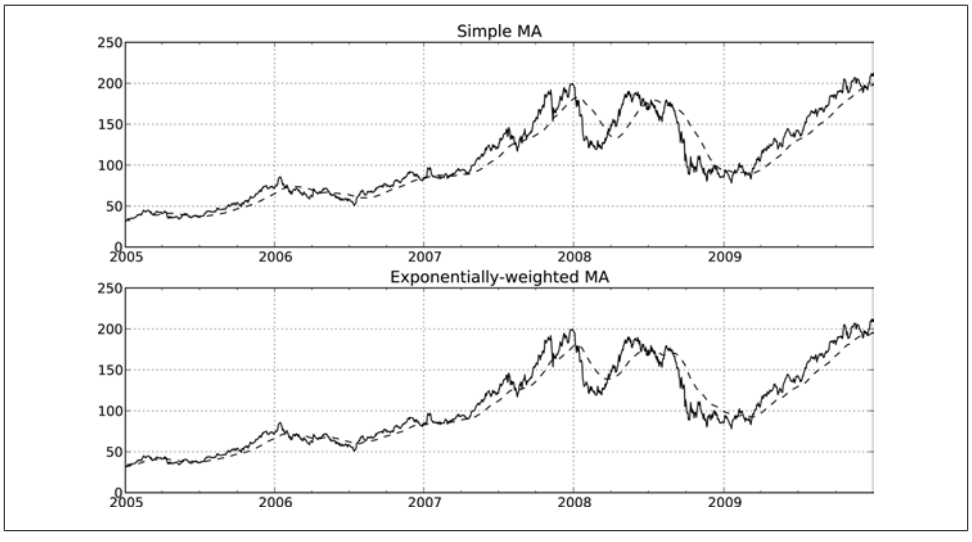


Figure 10-11. Simple moving average versus exponentially-weighted

Figure 10-12. Six-month AAPL return correlation to S&P 500

Suppose you wanted to compute the correlation of the S&P 500 index with many stocks at once. Writing a loop and creating a new DataFrame would be easy but maybe get repetitive, so if you pass a TimeSeries and a DataFrame, a function like `rolling_corr` will compute the correlation of the TimeSeries (`spx_rets` in this case) with each column in the DataFrame. See Figure 10-13 for the plot of the result:

```
In [575]: corr = pd.rolling_corr(returns, spx_rets, 125, min_periods=100)

In [576]: corr.plot()
```

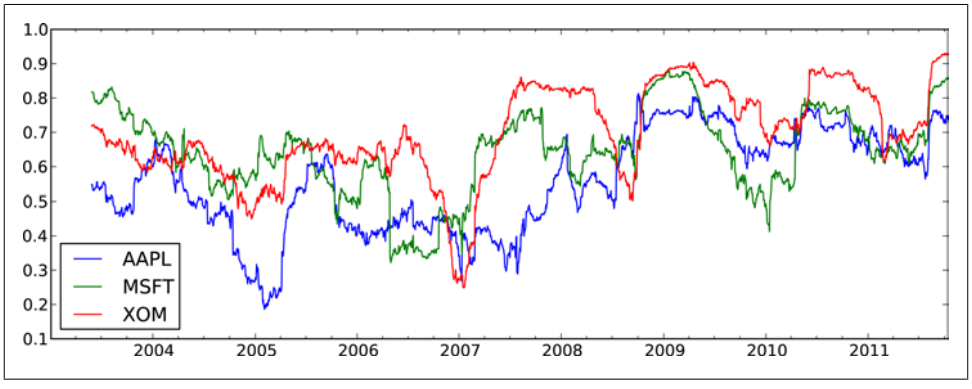


Figure 10-13. Six-month return correlations to S&P 500

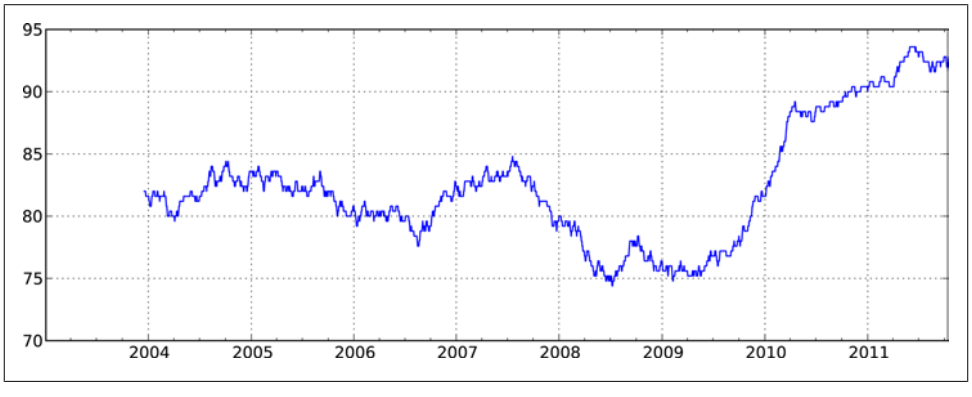


Figure 10-14. Percentile rank of 2% AAPL return over 1 year window

User-Defined Moving Window Functions

The `rolling_apply` function provides a means to apply an array function of your own devising over a moving window. The only requirement is that the function produce a single value (a reduction) from each piece of the array. For example, while we can compute sample quantiles using `rolling_quantile`, we might be interested in the percentile rank of a particular value over the sample. The `scipy.stats.percentileofscore` function does just this:

```
In [578]: from scipy.stats import percentileofscore

In [579]: score_at_2percent = lambda x: percentileofscore(x, 0.02)

In [580]: result = pd.rolling_apply(returns.AAPL, 250, score_at_2percent)

In [581]: result.plot()
```

Performance and Memory Usage Notes

Timestamps and periods are represented as 64-bit integers using NumPy's `datetime64` dtype. This means that for each data point, there is an associated 8 bytes of memory per timestamp. Thus, a time series with 1 million `float64` data points has a memory footprint of approximately 16 megabytes. Since pandas makes every effort to share indexes among time series, creating views on existing time series do not cause any more memory to be used. Additionally, indexes for lower frequencies (daily and up) are stored in a central cache, so that any fixed-frequency index is a view on the date cache. Thus, if you have a large collection of low-frequency time series, the memory footprint of the indexes will not be as significant.

Performance-wise, pandas has been highly optimized for data alignment operations (the behind-the-scenes work of differently indexed `ts1 + ts2`) and resampling. Here is an example of aggregating 10MM data points to OHLC:

```
In [582]: rng = pd.date_range('1/1/2000', periods=10000000, freq='10ms')

In [583]: ts = Series(np.random.randn(len(rng)), index=rng)

In [584]: ts
Out[584]:
2000-01-01 00:00:00          -1.402235
2000-01-01 00:00:00.010000    2.424667
2000-01-01 00:00:00.020000   -1.956042
2000-01-01 00:00:00.030000   -0.897339
...
2000-01-02 03:46:39.960000    0.495530
2000-01-02 03:46:39.970000    0.574766
2000-01-02 03:46:39.980000    1.348374
2000-01-02 03:46:39.990000    0.665034
Freq: 10L, Length: 10000000

In [585]: ts.resample('15min', how='ohlc')
Out[585]:
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 113 entries, 2000-01-01 00:00:00 to 2000-01-02 04:00:00
Freq: 15T
Data columns:
open     113  non-null values
high     113  non-null values
low      113  non-null values
close    113  non-null values
dtypes: float64(4)

In [586]: %timeit ts.resample('15min', how='ohlc')
10 loops, best of 3: 61.1 ms per loop
```

The runtime may depend slightly on the relative size of the aggregated result; higher frequency aggregates unsurprisingly take longer to compute:

```
In [587]: rng = pd.date_range('1/1/2000', periods=10000000, freq='1s')
```

```
In [588]: ts = Series(np.random.randn(len(rng)), index=rng)

In [589]: %timeit ts.resample('15s', how='ohlc')
1 loops, best of 3: 88.2 ms per loop
```

It's possible that by the time you read this, the performance of these algorithms may be even further improved. As an example, there are currently no optimizations for conversions between regular frequencies, but that would be fairly straightforward to do.

CHAPTER 11

Financial and Economic Data Applications

The use of Python in the financial industry has been increasing rapidly since 2005, led largely by the maturation of libraries (like NumPy and pandas) and the availability of skilled Python programmers. Institutions have found that Python is well-suited both as an interactive analysis environment as well as enabling robust systems to be developed often in a fraction of the time it would have taken in Java or C++. Python is also an ideal glue layer; it is easy to build Python interfaces to legacy libraries built in C or C++.

While the field of financial analysis is broad enough to fill an entire book, I hope to show you how the tools in this book can be applied to a number of specific problems in finance. As with other research and analysis domains, too much programming effort is often spent wrangling data rather than solving the core modeling and research problems. I personally got started building pandas in 2008 while grappling with inadequate data tools.

In these examples, I'll use the term *cross-section* to refer to data at a fixed point in time. For example, the closing prices of all the stocks in the S&P 500 index on a particular date form a cross-section. Cross-sectional data at multiple points in time over multiple data items (for example, prices together with volume) form a *panel*. Panel data can either be represented as a hierarchically-indexed DataFrame or using the three-dimensional Panel pandas object.

Data Munging Topics

Many helpful data munging tools for financial applications are spread across the earlier chapters. Here I'll highlight a number of topics as they relate to this problem domain.

CHAPTER 7

Data Wrangling: Clean, Transform, Merge, Reshape

Much of the programming work in data analysis and modeling is spent on data preparation: loading, cleaning, transforming, and rearranging. Sometimes the way that data is stored in files or databases is not the way you need it for a data processing application. Many people choose to do ad hoc processing of data from one form to another using a general purpose programming, like Python, Perl, R, or Java, or UNIX text processing tools like sed or awk. Fortunately, pandas along with the Python standard library provide you with a high-level, flexible, and high-performance set of core manipulations and algorithms to enable you to wrangle data into the right form without much trouble.

If you identify a type of data manipulation that isn't anywhere in this book or elsewhere in the pandas library, feel free to suggest it on the mailing list or GitHub site. Indeed, much of the design and implementation of pandas has been driven by the needs of real world applications.

Combining and Merging Data Sets

Data contained in pandas objects can be combined together in a number of built-in ways:

- `pandas.merge` connects rows in DataFrames based on one or more keys. This will be familiar to users of SQL or other relational databases, as it implements database *join* operations.
- `pandas.concat` glues or stacks together objects along an axis.
- `combine_first` instance method enables splicing together overlapping data to fill in missing values in one object with values from another.

I will address each of these and give a number of examples. They'll be utilized in examples throughout the rest of the book.

Database-style DataFrame Merges

Merge or *join* operations combine data sets by linking rows using one or more *keys*. These operations are central to relational databases. The `merge` function in pandas is the main entry point for using these algorithms on your data.

Let's start with a simple example:

```
In [15]: df1 = DataFrame({'key': ['b', 'b', 'a', 'c', 'a', 'a', 'b'],
   ....:                  'data1': range(7)})

In [16]: df2 = DataFrame({'key': ['a', 'b', 'd'],
   ....:                  'data2': range(3)})

In [17]: df1        In [18]: df2
Out[17]:            Out[18]:
   data1 key           data2 key
0      0   b        0      0   a
1      1   b        1      1   b
2      2   a        2      2   d
3      3   c
4      4   a
5      5   a
6      6   b
```

This is an example of a *many-to-one* merge situation; the data in `df1` has multiple rows labeled `a` and `b`, whereas `df2` has only one row for each value in the `key` column. Calling `merge` with these objects we obtain:

```
In [19]: pd.merge(df1, df2)
Out[19]:
   data1 key  data2
0      2   a      0
1      4   a      0
2      5   a      0
3      0   b      1
4      1   b      1
5      6   b      1
```

Note that I didn't specify which column to join on. If not specified, `merge` uses the overlapping column names as the keys. It's a good practice to specify explicitly, though:

```
In [20]: pd.merge(df1, df2, on='key')
Out[20]:
   data1 key  data2
0      2   a      0
1      4   a      0
2      5   a      0
3      0   b      1
4      1   b      1
5      6   b      1
```

If the column names are different in each object, you can specify them separately:

```
In [21]: df3 = DataFrame({'lkey': ['b', 'b', 'a', 'c', 'a', 'a', 'b'],
   ....:                  'data1': range(7)})
```

```
In [22]: df4 = DataFrame({'rkey': ['a', 'b', 'd'],
   ....:                  'data2': range(3)})

In [23]: pd.merge(df3, df4, left_on='lkey', right_on='rkey')
Out[23]:
   data1 lkey  data2 rkey
0      2    a      0    a
1      4    a      0    a
2      5    a      0    a
3      0    b      1    b
4      1    b      1    b
5      6    b      1    b
```

You probably noticed that the `'c'` and `'d'` values and associated data are missing from the result. By default `merge` does an `'inner'` join; the keys in the result are the intersection. Other possible options are `'left'`, `'right'`, and `'outer'`. The outer join takes the union of the keys, combining the effect of applying both left and right joins:

```
In [24]: pd.merge(df1, df2, how='outer')
Out[24]:
   data1 key  data2
0      2   a      0
1      4   a      0
2      5   a      0
3      0   b      1
4      1   b      1
5      6   b      1
6      3   c    NaN
7    NaN   d      2
```

Many-to-many merges have well-defined though not necessarily intuitive behavior. Here's an example:

```
In [25]: df1 = DataFrame({'key': ['b', 'b', 'a', 'c', 'a', 'b'],
   ....:                  'data1': range(6)})

In [26]: df2 = DataFrame({'key': ['a', 'b', 'a', 'b', 'd'],
   ....:                  'data2': range(5)})

In [27]: df1        In [28]: df2
Out[27]:            Out[28]:
   data1 key           data2 key
0      0   b        0      0   a
1      1   b        1      1   b
2      2   a        2      2   a
3      3   c        3      3   b
4      4   a        4      4   d
5      5   b

In [29]: pd.merge(df1, df2, on='key', how='left')
Out[29]:
    data1 key  data2
0       2   a      0
1       2   a      2
```

```
2       4   a      0
3       4   a      2
4       0   b      1
5       0   b      3
6       1   b      1
7       1   b      3
8       5   b      1
9       5   b      3
10      3   c    NaN
```

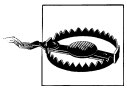
Many-to-many joins form the Cartesian product of the rows. Since there were 3 `'b'` rows in the left DataFrame and 2 in the right one, there are 6 `'b'` rows in the result. The join method only affects the distinct key values appearing in the result:

```
In [30]: pd.merge(df1, df2, how='inner')
Out[30]:
   data1 key  data2
0      2   a      0
1      2   a      2
2      4   a      0
3      4   a      2
4      0   b      1
5      0   b      3
6      1   b      1
7      1   b      3
8      5   b      1
9      5   b      3
```

To merge with multiple keys, pass a list of column names:

```
In [31]: left = DataFrame({'key1': ['foo', 'foo', 'bar'],
   ....:                   'key2': ['one', 'two', 'one'],
   ....:                   'lval': [1, 2, 3]})

In [32]: right = DataFrame({'key1': ['foo', 'foo', 'bar', 'bar'],
   ....:                    'key2': ['one', 'one', 'one', 'two'],
   ....:                    'rval': [4, 5, 6, 7]})

In [33]: pd.merge(left, right, on=['key1', 'key2'], how='outer')
Out[33]:
  key1 key2  lval  rval
0  bar  one     3     6
1  bar  two   NaN     7
2  foo  one     1     4
3  foo  one     1     5
4  foo  two     2   NaN
```

To determine which key combinations will appear in the result depending on the choice of merge method, think of the multiple keys as forming an array of tuples to be used as a single join key (even though it's not actually implemented that way).



When joining columns-on-columns, the indexes on the passed DataFrame objects are discarded.

A last issue to consider in merge operations is the treatment of overlapping column names. While you can address the overlap manually (see the later section on renaming axis labels), `merge` has a `suffixes` option for specifying strings to append to overlapping names in the left and right DataFrame objects:

```
In [34]: pd.merge(left, right, on='key1')
Out[34]:
  key1 key2_x  lval key2_y  rval
0  bar    one     3    one     6
1  bar    one     3    two     7
2  foo    one     1    one     4
3  foo    one     1    one     5
4  foo    two     2    one     4
5  foo    two     2    one     5

In [35]: pd.merge(left, right, on='key1', suffixes=('_left', '_right'))
Out[35]:
  key1 key2_left  lval key2_right  rval
0  bar       one     3        one     6
1  bar       one     3        two     7
2  foo       one     1        one     4
3  foo       one     1        one     5
4  foo       two     2        one     4
5  foo       two     2        one     5
```

See Table 7-1 for an argument reference on `merge`. Joining on index is the subject of the next section.

Table 7-1. merge function arguments

Argument	Description
`left`	DataFrame to be merged on the left side
`right`	DataFrame to be merged on the right side
`how`	One of `'inner'`, `'outer'`, `'left'` or `'right'`. `'inner'` by default
`on`	Column names to join on. Must be found in both DataFrame objects. If not specified and no other join keys given, will use the intersection of the column names in `left` and `right` as the join keys
`left_on`	Columns in `left` DataFrame to use as join keys
`right_on`	Analogous to `left_on` for `left` DataFrame
`left_index`	Use row index in `left` as its join key (or keys, if a MultiIndex)
`right_index`	Analogous to `left_index`
`sort`	Sort merged data lexicographically by join keys; `True` by default. Disable to get better performance in some cases on large datasets
`suffixes`	Tuple of string values to append to column names in case of overlap; defaults to `('_x', '_y')`. For example, if `'data'` in both DataFrame objects, would appear as `'data_x'` and `'data_y'` in result
`copy`	If `False`, avoid copying data into resulting data structure in some exceptional cases. By default always copies

Merging on Index

In some cases, the merge key or keys in a DataFrame will be found in its index. In this case, you can pass `left_index=True` or `right_index=True` (or both) to indicate that the index should be used as the merge key:

```
In [36]: left1 = DataFrame({'key': ['a', 'b', 'a', 'a', 'b', 'c'],
   ....:                    'value': range(6)})

In [37]: right1 = DataFrame({'group_val': [3.5, 7]}, index=['a', 'b'])

In [38]: left1        In [39]: right1
Out[38]:              Out[39]:
  key  value             group_val
0   a      0          a        3.5
1   b      1          b        7.0
2   a      2
3   a      3
4   b      4
5   c      5

In [40]: pd.merge(left1, right1, left_on='key', right_index=True)
Out[40]:
  key  value  group_val
0   a      0        3.5
2   a      2        3.5
3   a      3        3.5
1   b      1        7.0
4   b      4        7.0
```

Since the default merge method is to intersect the join keys, you can instead form the union of them with an outer join:

```
In [41]: pd.merge(left1, right1, left_on='key', right_index=True, how='outer')
Out[41]:
  key  value  group_val
0   a      0        3.5
2   a      2        3.5
3   a      3        3.5
1   b      1        7.0
4   b      4        7.0
5   c      5        NaN
```

With hierarchically-indexed data, things are a bit more complicated:

```
In [42]: lefth = DataFrame({'key1': ['Ohio', 'Ohio', 'Ohio', 'Nevada', 'Nevada'],
   ....:                    'key2': [2000, 2001, 2002, 2001, 2002],
   ....:                    'data': np.arange(5.)})

In [43]: righth = DataFrame(np.arange(12).reshape((6, 2)),
   ....:                    index=[['Nevada', 'Nevada', 'Ohio', 'Ohio', 'Ohio', 'Ohio'],
   ....:                           [2001, 2000, 2000, 2000, 2001, 2002]],
   ....:                    columns=['event1', 'event2'])

In [44]: lefth               In [45]: righth
Out[44]:                     Out[45]:
```

```
   data    key1  key2                    event1  event2
0     0    Ohio  2000        Nevada 2001       0       1
1     1    Ohio  2001               2000       2       3
2     2    Ohio  2002        Ohio   2000       4       5
3     3  Nevada  2001               2000       6       7
4     4  Nevada  2002               2001       8       9
                                    2002      10      11
```

In this case, you have to indicate multiple columns to merge on as a list (pay attention to the handling of duplicate index values):

```
In [46]: pd.merge(lefth, righth, left_on=['key1', 'key2'], right_index=True)
Out[46]:
   data    key1  key2  event1  event2
3     3  Nevada  2001       0       1
0     0    Ohio  2000       4       5
0     0    Ohio  2000       6       7
1     1    Ohio  2001       8       9
2     2    Ohio  2002      10      11

In [47]: pd.merge(lefth, righth, left_on=['key1', 'key2'],
   ....:          right_index=True, how='outer')
Out[47]:
   data    key1  key2  event1  event2
4   NaN  Nevada  2000       2       3
3     3  Nevada  2001       0       1
4     4  Nevada  2002     NaN     NaN
0     0    Ohio  2000       4       5
0     0    Ohio  2000       6       7
1     1    Ohio  2001       8       9
2     2    Ohio  2002      10      11
```

Using the indexes of both sides of the merge is also not an issue:

```
In [48]: left2 = DataFrame([[1., 2.], [3., 4.], [5., 6.]], index=['a', 'c', 'e'],
   ....:                   columns=['Ohio', 'Nevada'])

In [49]: right2 = DataFrame([[7., 8.], [9., 10.], [11., 12.], [13, 14]],
   ....:                    index=['b', 'c', 'd', 'e'], columns=['Missouri', 'Alabama'])

In [50]: left2          In [51]: right2
Out[50]:                Out[51]:
   Ohio  Nevada           Missouri  Alabama
a     1       2        b         7        8
c     3       4        c         9       10
e     5       6        d        11       12
                       e        13       14

In [52]: pd.merge(left2, right2, how='outer', left_index=True, right_index=True)
Out[52]:
   Ohio  Nevada  Missouri  Alabama
a     1       2       NaN      NaN
b   NaN     NaN         7        8
c     3       4         9       10
d   NaN     NaN        11       12
e     5       6        13       14
```

DataFrame has a more convenient `join` instance for merging by index. It can also be used to combine together many DataFrame objects having the same or similar indexes but non-overlapping columns. In the prior example, we could have written:

```
In [53]: left2.join(right2, how='outer')
Out[53]:
   Ohio  Nevada  Missouri  Alabama
a     1       2       NaN      NaN
b   NaN     NaN         7        8
c     3       4         9       10
d   NaN     NaN        11       12
e     5       6        13       14
```

In part for legacy reasons (much earlier versions of pandas), DataFrame's `join` method performs a left join on the join keys. It also supports joining the index of the passed DataFrame on one of the columns of the calling DataFrame:

```
In [54]: left1.join(right1, on='key')
Out[54]:
  key  value  group_val
0   a      0        3.5
1   b      1        7.0
2   a      2        3.5
3   a      3        3.5
4   b      4        7.0
5   c      5        NaN
```

Lastly, for simple index-on-index merges, you can pass a list of DataFrames to `join` as an alternative to using the more general `concat` function described below:

```
In [55]: another = DataFrame([[7., 8.], [9., 10.], [11., 12.], [16., 17.]],
   ....:                     index=['a', 'c', 'e', 'f'], columns=['New York', 'Oregon'])

In [56]: left2.join([right2, another])
Out[56]:
   Ohio  Nevada  Missouri  Alabama  New York  Oregon
a     1       2       NaN      NaN         7       8
c     3       4         9       10         9      10
e     5       6        13       14        11      12

In [57]: left2.join([right2, another], how='outer')
Out[57]:
   Ohio  Nevada  Missouri  Alabama  New York  Oregon
a     1       2       NaN      NaN         7       8
b   NaN     NaN         7        8       NaN     NaN
c     3       4         9       10         9      10
d   NaN     NaN        11       12       NaN     NaN
e     5       6        13       14        11      12
f   NaN     NaN       NaN      NaN        16      17
```

Concatenating Along an Axis

Another kind of data combination operation is alternatively referred to as concatenation, binding, or stacking. NumPy has a `concatenate` function for doing this with raw NumPy arrays:

```
In [58]: arr = np.arange(12).reshape((3, 4))

In [59]: arr
Out[59]:
array([[ 0,  1,  2,  3],
       [ 4,  5,  6,  7],
       [ 8,  9, 10, 11]])

In [60]: np.concatenate([arr, arr], axis=1)
Out[60]:
array([[ 0,  1,  2,  3,  0,  1,  2,  3],
       [ 4,  5,  6,  7,  4,  5,  6,  7],
       [ 8,  9, 10, 11,  8,  9, 10, 11]])
```

In the context of pandas objects such as Series and DataFrame, having labeled axes enable you to further generalize array concatenation. In particular, you have a number of additional things to think about:

- If the objects are indexed differently on the other axes, should the collection of axes be unioned or intersected?
- Do the groups need to be identifiable in the resulting object?
- Does the concatenation axis matter at all?

The `concat` function in pandas provides a consistent way to address each of these concerns. I'll give a number of examples to illustrate how it works. Suppose we have three Series with no index overlap:

```
In [61]: s1 = Series([0, 1], index=['a', 'b'])

In [62]: s2 = Series([2, 3, 4], index=['c', 'd', 'e'])

In [63]: s3 = Series([5, 6], index=['f', 'g'])
```

Calling `concat` with these object in a list glues together the values and indexes:

```
In [64]: pd.concat([s1, s2, s3])
Out[64]:
a    0
b    1
c    2
d    3
e    4
f    5
g    6
```

By default `concat` works along `axis=0`, producing another Series. If you pass `axis=1`, the result will instead be a DataFrame (`axis=1` is the columns):

```
In [65]: pd.concat([s1, s2, s3], axis=1)
Out[65]:
    0   1   2
a   0 NaN NaN
b   1 NaN NaN
c NaN   2 NaN
d NaN   3 NaN
e NaN   4 NaN
f NaN NaN   5
g NaN NaN   6
```

In this case there is no overlap on the other axis, which as you can see is the sorted union (the `'outer'` join) of the indexes. You can instead intersect them by passing `join='inner'`:

```
In [66]: s4 = pd.concat([s1 * 5, s3])

In [67]: pd.concat([s1, s4], axis=1)
Out[67]:
    0  1
a   0  0
b   1  5
f NaN  5
g NaN  6

In [68]: pd.concat([s1, s4], axis=1, join='inner')
Out[68]:
   0  1
a  0  0
b  1  5
```

You can even specify the axes to be used on the other axes with `join_axes`:

```
In [69]: pd.concat([s1, s4], axis=1, join_axes=[['a', 'c', 'b', 'e']])
Out[69]:
    0   1
a   0   0
c NaN NaN
b   1   5
e NaN NaN
```

One issue is that the concatenated pieces are not identifiable in the result. Suppose instead you wanted to create a hierarchical index on the concatenation axis. To do this, use the `keys` argument:

```
In [70]: result = pd.concat([s1, s1, s3], keys=['one', 'two', 'three'])

In [71]: result
Out[71]:
one    a    0
       b    1
two    a    0
       b    1
three  f    5
       g    6

# Much more on the unstack function later
In [72]: result.unstack()
Out[72]:
```

```
        a   b   f   g
one     0   1 NaN NaN
two     0   1 NaN NaN
three NaN NaN   5   6
```

In the case of combining Series along `axis=1`, the `keys` become the DataFrame column headers:

```
In [73]: pd.concat([s1, s2, s3], axis=1, keys=['one', 'two', 'three'])
Out[73]:
   one  two  three
a    0  NaN    NaN
b    1  NaN    NaN
c  NaN    2    NaN
d  NaN    3    NaN
e  NaN    4    NaN
f  NaN  NaN      5
g  NaN  NaN      6
```

The same logic extends to DataFrame objects:

```
In [74]: df1 = DataFrame(np.arange(6).reshape(3, 2), index=['a', 'b', 'c'],
   ....:                 columns=['one', 'two'])

In [75]: df2 = DataFrame(5 + np.arange(4).reshape(2, 2), index=['a', 'c'],
   ....:                 columns=['three', 'four'])

In [76]: pd.concat([df1, df2], axis=1, keys=['level1', 'level2'])
Out[76]:
   level1       level2
      one  two   three  four
a       0    1       5     6
b       2    3     NaN   NaN
c       4    5       7     8
```

If you pass a dict of objects instead of a list, the dict's keys will be used for the `keys` option:

```
In [77]: pd.concat({'level1': df1, 'level2': df2}, axis=1)
Out[77]:
   level1       level2
      one  two   three  four
a       0    1       5     6
b       2    3     NaN   NaN
c       4    5       7     8
```

There are a couple of additional arguments governing how the hierarchical index is created (see Table 7-2):

```
In [78]: pd.concat([df1, df2], axis=1, keys=['level1', 'level2'],
   ....:           names=['upper', 'lower'])
Out[78]:
upper  level1       level2
lower     one  two   three  four
a           0    1       5     6
b           2    3     NaN   NaN
c           4    5       7     8
```

A last consideration concerns DataFrames in which the row index is not meaningful in the context of the analysis:

```
In [79]: df1 = DataFrame(np.random.randn(3, 4), columns=['a', 'b', 'c', 'd'])

In [80]: df2 = DataFrame(np.random.randn(2, 3), columns=['b', 'd', 'a'])

In [81]: df1
Out[81]:
          a         b         c         d
0 -0.204708  0.478943 -0.519439 -0.555730
1  1.965781  1.393406  0.092908  0.281746
2  0.769023  1.246435  1.007189 -1.296221

In [82]: df2
Out[82]:
          b         d         a
0  0.274992  0.228913  1.352917
1  0.886429 -2.001637 -0.371843
```

In this case, you can pass `ignore_index=True`:

```
In [83]: pd.concat([df1, df2], ignore_index=True)
Out[83]:
          a         b         c         d
0 -0.204708  0.478943 -0.519439 -0.555730
1  1.965781  1.393406  0.092908  0.281746
2  0.769023  1.246435  1.007189 -1.296221
3  1.352917  0.274992       NaN  0.228913
4 -0.371843  0.886429       NaN -2.001637
```

Table 7-2. concat function arguments

Argument	Description
`objs`	List or dict of pandas objects to be concatenated. The only required argument
`axis`	Axis to concatenate along; defaults to 0
`join`	One of `'inner', 'outer'`, defaulting to `'outer'`; whether to intersection (inner) or union (outer) together indexes along the other axes
`join_axes`	Specific indexes to use for the other n-1 axes instead of performing union/intersection logic
`keys`	Values to associate with objects being concatenated, forming a hierarchical index along the concatenation axis. Can either be a list or array of arbitrary values, an array of tuples, or a list of arrays (if multiple level arrays passed in `levels`)
`levels`	Specific indexes to use as hierarchical index level or levels if keys passed
`names`	Names for created hierarchical levels if `keys` and / or `levels` passed
`verify_integrity`	Check new axis in concatenated object for duplicates and raise exception if so. By default (`False`) allows duplicates
`ignore_index`	Do not preserve indexes along concatenation `axis`, instead producing a new `range(total_length)` index

Combining Data with Overlap

Another data combination situation can't be expressed as either a merge or concatenation operation. You may have two datasets whose indexes overlap in full or part. As a motivating example, consider NumPy's `where` function, which expressed a vectorized if-else:

```
In [84]: a = Series([np.nan, 2.5, np.nan, 3.5, 4.5, np.nan],
   ....:            index=['f', 'e', 'd', 'c', 'b', 'a'])

In [85]: b = Series(np.arange(len(a), dtype=np.float64),
   ....:            index=['f', 'e', 'd', 'c', 'b', 'a'])

In [86]: b[-1] = np.nan

In [87]: a        In [88]: b        In [89]: np.where(pd.isnull(a), b, a)
Out[87]:          Out[88]:          Out[89]:
f    NaN          f     0           f    0.0
e    2.5          e     1           e    2.5
d    NaN          d     2           d    2.0
c    3.5          c     3           c    3.5
b    4.5          b     4           b    4.5
a    NaN          a   NaN           a    NaN
```

Series has a `combine_first` method, which performs the equivalent of this operation plus data alignment:

```
In [90]: b[:-2].combine_first(a[2:])
Out[90]:
a    NaN
b    4.5
c    3.0
d    2.0
e    1.0
f    0.0
```

With DataFrames, `combine_first` naturally does the same thing column by column, so you can think of it as "patching" missing data in the calling object with data from the object you pass:

```
In [91]: df1 = DataFrame({'a': [1., np.nan, 5., np.nan],
   ....:                  'b': [np.nan, 2., np.nan, 6.],
   ....:                  'c': range(2, 18, 4)})

In [92]: df2 = DataFrame({'a': [5., 4., np.nan, 3., 7.],
   ....:                  'b': [np.nan, 3., 4., 6., 8.]})

In [93]: df1.combine_first(df2)
Out[93]:
   a   b   c
0  1 NaN   2
1  4   2   6
2  5   4  10
3  3   6  14
4  7   8 NaN
```

Reshaping and Pivoting

There are a number of fundamental operations for rearranging tabular data. These are alternatingly referred to as *reshape* or *pivot* operations.

Reshaping with Hierarchical Indexing

Hierarchical indexing provides a consistent way to rearrange data in a DataFrame. There are two primary actions:

- `stack`: this "rotates" or pivots from the columns in the data to the rows
- `unstack`: this pivots from the rows into the columns

I'll illustrate these operations through a series of examples. Consider a small DataFrame with string arrays as row and column indexes:

```
In [94]: data = DataFrame(np.arange(6).reshape((2, 3)),
   ....:                  index=pd.Index(['Ohio', 'Colorado'], name='state'),
   ....:                  columns=pd.Index(['one', 'two', 'three'], name='number'))

In [95]: data
Out[95]:
number    one  two  three
state
Ohio        0    1      2
Colorado    3    4      5
```

Using the `stack` method on this data pivots the columns into the rows, producing a Series:

```
In [96]: result = data.stack()

In [97]: result
Out[97]:
state     number
Ohio      one       0
          two       1
          three     2
Colorado  one       3
          two       4
          three     5
```

From a hierarchically-indexed Series, you can rearrange the data back into a DataFrame with `unstack`:

```
In [98]: result.unstack()
Out[98]:
number    one  two  three
state
Ohio        0    1      2
Colorado    3    4      5
```

By default the innermost level is unstacked (same with `stack`). You can unstack a different level by passing a level number or name:

```
In [99]: result.unstack(0)
Out[99]:
state   Ohio  Colorado
number
one        0         3
```

```
In [100]: result.unstack('state')
Out[100]:
state   Ohio  Colorado
number
one        0         3
```

```
two        1         4            two        1         4
three      2         5            three      2         5
```

Unstacking might introduce missing data if all of the values in the level aren't found in each of the subgroups:

```
In [101]: s1 = Series([0, 1, 2, 3], index=['a', 'b', 'c', 'd'])

In [102]: s2 = Series([4, 5, 6], index=['c', 'd', 'e'])

In [103]: data2 = pd.concat([s1, s2], keys=['one', 'two'])

In [104]: data2.unstack()
Out[104]:
      a   b  c  d   e
one   0   1  2  3 NaN
two NaN NaN  4  5   6
```

Stacking filters out missing data by default, so the operation is easily invertible:

```
In [105]: data2.unstack().stack()
Out[105]:
one  a    0
     b    1
     c    2
     d    3
two  c    4
     d    5
     e    6
```

```
In [106]: data2.unstack().stack(dropna=False)
Out[106]:
one  a     0
     b     1
     c     2
     d     3
     e   NaN
two  a   NaN
     b   NaN
     c     4
     d     5
     e     6
```

When unstacking in a DataFrame, the level unstacked becomes the lowest level in the result:

```
In [107]: df = DataFrame({'left': result, 'right': result + 5},
   .....:                columns=pd.Index(['left', 'right'], name='side'))

In [108]: df
Out[108]:
side             left  right
state    number
Ohio     one        0      5
         two        1      6
         three      2      7
Colorado one        3      8
         two        4      9
         three      5     10
```

```
In [109]: df.unstack('state')
Out[109]:
side    left            right
state   Ohio  Colorado   Ohio  Colorado
number
one        0         3      5         8
two        1         4      6         9
```

```
In [110]: df.unstack('state').stack('side')
Out[110]:
state         Ohio  Colorado
number side
one    left      0         3
       right     5         8
two    left      1         4
```

```
three      2         5      7        10             right     6         9
                                              three  left      2         5
                                                     right     7        10
```

Pivoting "long" to "wide" Format

A common way to store multiple time series in databases and CSV is in so-called *long* or *stacked* format:

```
In [116]: ldata[:10]
Out[116]:
                 date     item     value
0 1959-03-31 00:00:00  realgdp  2710.349
1 1959-03-31 00:00:00     infl     0.000
2 1959-03-31 00:00:00    unemp     5.800
3 1959-06-30 00:00:00  realgdp  2778.801
4 1959-06-30 00:00:00     infl     2.340
5 1959-06-30 00:00:00    unemp     5.100
6 1959-09-30 00:00:00  realgdp  2775.488
7 1959-09-30 00:00:00     infl     2.740
8 1959-09-30 00:00:00    unemp     5.300
9 1959-12-31 00:00:00  realgdp  2785.204
```

Data is frequently stored this way in relational databases like MySQL as a fixed schema (column names and data types) allows the number of distinct values in the `item` column to increase or decrease as data is added or deleted in the table. In the above example `date` and `item` would usually be the primary keys (in relational database parlance), offering both relational integrity and easier joins and programmatic queries in many cases. The downside, of course, is that the data may not be easy to work with in long format; you might prefer to have a DataFrame containing one column per distinct `item` value indexed by timestamps in the `date` column. DataFrame's `pivot` method performs exactly this transformation:

```
In [117]: pivoted = ldata.pivot('date', 'item', 'value')

In [118]: pivoted.head()
Out[118]:
item        infl   realgdp  unemp
date
1959-03-31  0.00  2710.349    5.8
1959-06-30  2.34  2778.801    5.1
1959-09-30  2.74  2775.488    5.3
1959-12-31  0.27  2785.204    5.6
1960-03-31  2.31  2847.699    5.2
```

The first two values passed are the columns to be used as the row and column index, and finally an optional value column to fill the DataFrame. Suppose you had two value columns that you wanted to reshape simultaneously:

```
In [119]: ldata['value2'] = np.random.randn(len(ldata))

In [120]: ldata[:10]
Out[120]:
```

```
                 date     item     value    value2
0 1959-03-31 00:00:00  realgdp  2710.349  1.669025
1 1959-03-31 00:00:00     infl     0.000 -0.438570
2 1959-03-31 00:00:00    unemp     5.800 -0.539741
3 1959-06-30 00:00:00  realgdp  2778.801  0.476985
4 1959-06-30 00:00:00     infl     2.340  3.248944
5 1959-06-30 00:00:00    unemp     5.100 -1.021228
6 1959-09-30 00:00:00  realgdp  2775.488 -0.577087
7 1959-09-30 00:00:00     infl     2.740  0.124121
8 1959-09-30 00:00:00    unemp     5.300  0.302614
9 1959-12-31 00:00:00  realgdp  2785.204  0.523772
```

By omitting the last argument, you obtain a DataFrame with hierarchical columns:

```
In [121]: pivoted = ldata.pivot('date', 'item')

In [122]: pivoted[:5]
Out[122]:
            value                     value2
item         infl   realgdp  unemp      infl   realgdp     unemp
date
1959-03-31   0.00  2710.349    5.8 -0.438570  1.669025 -0.539741
1959-06-30   2.34  2778.801    5.1  3.248944  0.476985 -1.021228
1959-09-30   2.74  2775.488    5.3  0.124121 -0.577087  0.302614
1959-12-31   0.27  2785.204    5.6  0.000940  0.523772  1.343810
1960-03-31   2.31  2847.699    5.2 -0.831154 -0.713544 -2.370232

In [123]: pivoted['value'][:5]
Out[123]:
item        infl   realgdp  unemp
date
1959-03-31  0.00  2710.349    5.8
1959-06-30  2.34  2778.801    5.1
1959-09-30  2.74  2775.488    5.3
1959-12-31  0.27  2785.204    5.6
1960-03-31  2.31  2847.699    5.2
```

Note that `pivot` is just a shortcut for creating a hierarchical index using `set_index` and reshaping with `unstack`:

```
In [124]: unstacked = ldata.set_index(['date', 'item']).unstack('item')

In [125]: unstacked[:7]
Out[125]:
            value                     value2
item         infl   realgdp  unemp      infl   realgdp     unemp
date
1959-03-31   0.00  2710.349    5.8 -0.438570  1.669025 -0.539741
1959-06-30   2.34  2778.801    5.1  3.248944  0.476985 -1.021228
1959-09-30   2.74  2775.488    5.3  0.124121 -0.577087  0.302614
1959-12-31   0.27  2785.204    5.6  0.000940  0.523772  1.343810
1960-03-31   2.31  2847.699    5.2 -0.831154 -0.713544 -2.370232
1960-06-30   0.14  2834.390    5.2 -0.860757 -1.860761  0.560145
1960-09-30   2.70  2839.022    5.6  0.119827 -1.265934 -1.063512
```

Data Transformation

So far in this chapter we've been concerned with rearranging data. Filtering, cleaning, and other tranformations are another class of important operations.

Removing Duplicates

Duplicate rows may be found in a DataFrame for any number of reasons. Here is an example:

```
In [126]: data = DataFrame({'k1': ['one'] * 3 + ['two'] * 4,
   .....:                   'k2': [1, 1, 2, 3, 3, 4, 4]})

In [127]: data
Out[127]:
    k1  k2
0  one   1
1  one   1
2  one   2
3  two   3
4  two   3
5  two   4
6  two   4
```

The DataFrame method `duplicated` returns a boolean Series indicating whether each row is a duplicate or not:

```
In [128]: data.duplicated()
Out[128]:
0    False
1     True
2    False
3    False
4     True
5    False
6     True
```

Relatedly, `drop_duplicates` returns a DataFrame where the `duplicated` array is `True`:

```
In [129]: data.drop_duplicates()
Out[129]:
    k1  k2
0  one   1
2  one   2
3  two   3
5  two   4
```

Both of these methods by default consider all of the columns; alternatively you can specify any subset of them to detect duplicates. Suppose we had an additional column of values and wanted to filter duplicates only based on the `'k1'` column:

```
In [130]: data['v1'] = range(7)

In [131]: data.drop_duplicates(['k1'])
```

```
Out[131]:
    k1  k2  v1
0  one   1   0
3  two   3   3
```

`duplicated` and `drop_duplicates` by default keep the first observed value combination. Passing `take_last=True` will return the last one:

```
In [132]: data.drop_duplicates(['k1', 'k2'], take_last=True)
Out[132]:
    k1  k2  v1
1  one   1   1
2  one   2   2
4  two   3   4
6  two   4   6
```

Transforming Data Using a Function or Mapping

For many data sets, you may wish to perform some transformation based on the values in an array, Series, or column in a DataFrame. Consider the following hypothetical data collected about some kinds of meat:

```
In [133]: data = DataFrame({'food': ['bacon', 'pulled pork', 'bacon', 'Pastrami',
   .....:                            'corned beef', 'Bacon', 'pastrami', 'honey ham',
   .....:                            'nova lox'],
   .....:                   'ounces': [4, 3, 12, 6, 7.5, 8, 3, 5, 6]})

In [134]: data
Out[134]:
          food  ounces
0        bacon     4.0
1  pulled pork     3.0
2        bacon    12.0
3     Pastrami     6.0
4  corned beef     7.5
5        Bacon     8.0
6     pastrami     3.0
7    honey ham     5.0
8     nova lox     6.0
```

Suppose you wanted to add a column indicating the type of animal that each food came from. Let's write down a mapping of each distinct meat type to the kind of animal:

```
meat_to_animal = {
  'bacon': 'pig',
  'pulled pork': 'pig',
  'pastrami': 'cow',
  'corned beef': 'cow',
  'honey ham': 'pig',
  'nova lox': 'salmon'
}
```

The map method on a Series accepts a function or dict-like object containing a mapping, but here we have a small problem in that some of the meats above are capitalized and others are not. Thus, we also need to convert each value to lower case:

```
In [136]: data['animal'] = data['food'].map(str.lower).map(meat_to_animal)

In [137]: data
Out[137]:
          food  ounces  animal
0        bacon     4.0     pig
1  pulled pork     3.0     pig
2        bacon    12.0     pig
3     Pastrami     6.0     cow
4  corned beef     7.5     cow
5        Bacon     8.0     pig
6     pastrami     3.0     cow
7    honey ham     5.0     pig
8     nova lox     6.0  salmon
```

We could also have passed a function that does all the work:

```
In [138]: data['food'].map(lambda x: meat_to_animal[x.lower()])
Out[138]:
0       pig
1       pig
2       pig
3       cow
4       cow
5       pig
6       cow
7       pig
8    salmon
Name: food
```

Using map is a convenient way to perform element-wise transformations and other data cleaning-related operations.

Replacing Values

Filling in missing data with the fillna method can be thought of as a special case of more general value replacement. While map, as you've seen above, can be used to modify a subset of values in an object, replace provides a simpler and more flexible way to do so. Let's consider this Series:

```
In [139]: data = Series([1., -999., 2., -999., -1000., 3.])

In [140]: data
Out[140]:
0       1
1    -999
2       2
3    -999
4   -1000
5       3
```

The `-999` values might be sentinel values for missing data. To replace these with NA values that pandas understands, we can use `replace`, producing a new Series:

```
In [141]: data.replace(-999, np.nan)
Out[141]:
0       1
1     NaN
2       2
3     NaN
4   -1000
5       3
```

If you want to replace multiple values at once, you instead pass a list then the substitute value:

```
In [142]: data.replace([-999, -1000], np.nan)
Out[142]:
0     1
1   NaN
2     2
3   NaN
4   NaN
5     3
```

To use a different replacement for each value, pass a list of substitutes:

```
In [143]: data.replace([-999, -1000], [np.nan, 0])
Out[143]:
0     1
1   NaN
2     2
3   NaN
4     0
5     3
```

The argument passed can also be a dict:

```
In [144]: data.replace({-999: np.nan, -1000: 0})
Out[144]:
0     1
1   NaN
2     2
3   NaN
4     0
5     3
```

Renaming Axis Indexes

Like values in a Series, axis labels can be similarly transformed by a function or mapping of some form to produce new, differently labeled objects. The axes can also be modified in place without creating a new data structure. Here's a simple example:

```
In [145]: data = DataFrame(np.arange(12).reshape((3, 4)),
   .....:                  index=['Ohio', 'Colorado', 'New York'],
   .....:                  columns=['one', 'two', 'three', 'four'])
```

Like a Series, the axis indexes have a `map` method:

```
In [146]: data.index.map(str.upper)
Out[146]: array([OHIO, COLORADO, NEW YORK], dtype=object)
```

You can assign to `index`, modifying the DataFrame in place:

```
In [147]: data.index = data.index.map(str.upper)

In [148]: data
Out[148]:
          one  two  three  four
OHIO        0    1      2     3
COLORADO    4    5      6     7
NEW YORK    8    9     10    11
```

If you want to create a transformed version of a data set without modifying the original, a useful method is `rename`:

```
In [149]: data.rename(index=str.title, columns=str.upper)
Out[149]:
          ONE  TWO  THREE  FOUR
Ohio        0    1      2     3
Colorado    4    5      6     7
New York    8    9     10    11
```

Notably, `rename` can be used in conjunction with a dict-like object providing new values for a subset of the axis labels:

```
In [150]: data.rename(index={'OHIO': 'INDIANA'},
   .....:             columns={'three': 'peekaboo'})
Out[150]:
          one  two  peekaboo  four
INDIANA     0    1         2     3
COLORADO    4    5         6     7
NEW YORK    8    9        10    11
```

`rename` saves having to copy the DataFrame manually and assign to its `index` and `columns` attributes. Should you wish to modify a data set in place, pass `inplace=True`:

```
# Always returns a reference to a DataFrame
In [151]: _ = data.rename(index={'OHIO': 'INDIANA'}, inplace=True)

In [152]: data
Out[152]:
          one  two  three  four
INDIANA     0    1      2     3
COLORADO    4    5      6     7
NEW YORK    8    9     10    11
```

Discretization and Binning

Continuous data is often discretized or otherwised separated into "bins" for analysis. Suppose you have data about a group of people in a study, and you want to group them into discrete age buckets:

```
In [153]: ages = [20, 22, 25, 27, 21, 23, 37, 31, 61, 45, 41, 32]
```

Let's divide these into bins of 18 to 25, 26 to 35, 35 to 60, and finally 60 and older. To do so, you have to use `cut`, a function in pandas:

```
In [154]: bins = [18, 25, 35, 60, 100]

In [155]: cats = pd.cut(ages, bins)

In [156]: cats
Out[156]:
Categorical:
array([(18, 25], (18, 25], (18, 25], (25, 35], (18, 25], (18, 25],
       (35, 60], (25, 35], (60, 100], (35, 60], (35, 60], (25, 35]], dtype=object)
Levels (4): Index([(18, 25], (25, 35], (35, 60], (60, 100]], dtype=object)
```

The object pandas returns is a special `Categorical` object. You can treat it like an array of strings indicating the bin name; internally it contains a `levels` array indicating the distinct category names along with a labeling for the `ages` data in the `labels` attribute:

```
In [157]: cats.labels
Out[157]: array([0, 0, 0, 1, 0, 0, 2, 1, 3, 2, 2, 1])

In [158]: cats.levels
Out[158]: Index([(18, 25], (25, 35], (35, 60], (60, 100]], dtype=object)

In [159]: pd.value_counts(cats)
Out[159]:
(18, 25]     5
(35, 60]     3
(25, 35]     3
(60, 100]    1
```

Consistent with mathematical notation for intervals, a parenthesis means that the side is *open* while the square bracket means it is *closed* (inclusive). Which side is closed can be changed by passing `right=False`:

```
In [160]: pd.cut(ages, [18, 26, 36, 61, 100], right=False)
Out[160]:
Categorical:
array([[18, 26), [18, 26), [18, 26), [26, 36), [18, 26), [18, 26),
       [36, 61), [26, 36), [61, 100), [36, 61), [36, 61), [26, 36)], dtype=object)
Levels (4): Index([[18, 26), [26, 36), [36, 61), [61, 100)], dtype=object)
```

You can also pass your own bin names by passing a list or array to the `labels` option:

```
In [161]: group_names = ['Youth', 'YoungAdult', 'MiddleAged', 'Senior']

In [162]: pd.cut(ages, bins, labels=group_names)
Out[162]:
```

```
Categorical:
array([Youth, Youth, Youth, YoungAdult, Youth, Youth, MiddleAged,
       YoungAdult, Senior, MiddleAged, MiddleAged, YoungAdult], dtype=object)
Levels (4): Index([Youth, YoungAdult, MiddleAged, Senior], dtype=object)
```

If you pass `cut` a integer number of bins instead of explicit bin edges, it will compute equal-length bins based on the minimum and maximum values in the data. Consider the case of some uniformly distributed data chopped into fourths:

```
In [163]: data = np.random.rand(20)

In [164]: pd.cut(data, 4, precision=2)
Out[164]:
Categorical:
array([(0.45, 0.67], (0.23, 0.45], (0.0037, 0.23], (0.45, 0.67],
       (0.67, 0.9], (0.45, 0.67], (0.67, 0.9], (0.23, 0.45], (0.23, 0.45],
       (0.67, 0.9], (0.67, 0.9], (0.67, 0.9], (0.23, 0.45], (0.23, 0.45],
       (0.23, 0.45], (0.67, 0.9], (0.0037, 0.23], (0.0037, 0.23],
       (0.23, 0.45], (0.23, 0.45]], dtype=object)
Levels (4): Index([(0.0037, 0.23], (0.23, 0.45], (0.45, 0.67],
                   (0.67, 0.9]], dtype=object)
```

A closely related function, `qcut`, bins the data based on sample quantiles. Depending on the distribution of the data, using `cut` will not usually result in each bin having the same number of data points. Since `qcut` uses sample quantiles instead, by definition you will obtain roughly equal-size bins:

```
In [165]: data = np.random.randn(1000) # Normally distributed

In [166]: cats = pd.qcut(data, 4) # Cut into quartiles

In [167]: cats
Out[167]:
Categorical:
array([(-0.022, 0.641], [-3.745, -0.635], (0.641, 3.26], ...,
       (-0.635, -0.022], (0.641, 3.26], (-0.635, -0.022]], dtype=object)
Levels (4): Index([[-3.745, -0.635], (-0.635, -0.022], (-0.022, 0.641],
                   (0.641, 3.26]], dtype=object)

In [168]: pd.value_counts(cats)
Out[168]:
[-3.745, -0.635]    250
(0.641, 3.26]       250
(-0.635, -0.022]    250
(-0.022, 0.641]     250
```

Similar to `cut` you can pass your own quantiles (numbers between 0 and 1, inclusive):

```
In [169]: pd.qcut(data, [0, 0.1, 0.5, 0.9, 1.])
Out[169]:
Categorical:
array([(-0.022, 1.302], (-1.266, -0.022], (-0.022, 1.302], ...,
       (-1.266, -0.022], (-0.022, 1.302], (-1.266, -0.022]], dtype=object)
Levels (4): Index([[-3.745, -1.266], (-1.266, -0.022], (-0.022, 1.302],
                   (1.302, 3.26]], dtype=object)
```

We'll return to `cut` and `qcut` later in the chapter on aggregation and group operations, as these discretization functions are especially useful for quantile and group analysis.

Detecting and Filtering Outliers

Filtering or transforming outliers is largely a matter of applying array operations. Consider a DataFrame with some normally distributed data:

```
In [170]: np.random.seed(12345)

In [171]: data = DataFrame(np.random.randn(1000, 4))

In [172]: data.describe()
Out[172]:
                 0            1            2            3
count  1000.000000  1000.000000  1000.000000  1000.000000
mean     -0.067684     0.067924     0.025598    -0.002298
std       0.998035     0.992106     1.006835     0.996794
min      -3.428254    -3.548824    -3.184377    -3.745356
25%      -0.774890    -0.591841    -0.641675    -0.644144
50%      -0.116401     0.101143     0.002073    -0.013611
75%       0.616366     0.780282     0.680391     0.654328
max       3.366626     2.653656     3.260383     3.927528
```

Suppose you wanted to find values in one of the columns exceeding three in magnitude:

```
In [173]: col = data[3]

In [174]: col[np.abs(col) > 3]
Out[174]:
97     3.927528
305   -3.399312
400   -3.745356
Name: 3
```

To select all rows having a value exceeding 3 or -3, you can use the `any` method on a boolean DataFrame:

```
In [175]: data[(np.abs(data) > 3).any(1)]
Out[175]:
           0         1         2         3
5   -0.539741  0.476985  3.248944 -1.021228
97  -0.774363  0.552936  0.106061  3.927528
102 -0.655054 -0.565230  3.176873  0.959533
305 -2.315555  0.457246 -0.025907 -3.399312
324  0.050188  1.951312  3.260383  0.963301
400  0.146326  0.508391 -0.196713 -3.745356
499 -0.293333 -0.242459 -3.056990  1.918403
523 -3.428254 -0.296336 -0.439938 -0.867165
586  0.275144  1.179227 -3.184377  1.369891
808 -0.362528 -3.548824  1.553205 -2.186301
900  3.366626 -2.372214  0.851010  1.332846
```

Values can just as easily be set based on these criteria. Here is code to cap values outside the interval -3 to 3:

```
In [176]: data[np.abs(data) > 3] = np.sign(data) * 3

In [177]: data.describe()
Out[177]:
                0            1            2            3
count  1000.000000  1000.000000  1000.000000  1000.000000
mean     -0.067623     0.068473     0.025153    -0.002081
std       0.995485     0.990253     1.003977     0.989736
min      -3.000000    -3.000000    -3.000000    -3.000000
25%      -0.774890    -0.591841    -0.641675    -0.644144
50%      -0.116401     0.101143     0.002073    -0.013611
75%       0.616366     0.780282     0.680391     0.654328
max       3.000000     2.653656     3.000000     3.000000
```

The ufunc `np.sign` returns an array of 1 and -1 depending on the sign of the values.

Permutation and Random Sampling

Permuting (randomly reordering) a Series or the rows in a DataFrame is easy to do using the `numpy.random.permutation` function. Calling `permutation` with the length of the axis you want to permute produces an array of integers indicating the new ordering:

```
In [178]: df = DataFrame(np.arange(5 * 4).reshape(5, 4))

In [179]: sampler = np.random.permutation(5)

In [180]: sampler
Out[180]: array([1, 0, 2, 3, 4])
```

That array can then be used in `ix`-based indexing or the `take` function:

```
In [181]: df
Out[181]:
    0   1   2   3
0   0   1   2   3
1   4   5   6   7
2   8   9  10  11
3  12  13  14  15
4  16  17  18  19

In [182]: df.take(sampler)
Out[182]:
    0   1   2   3
1   4   5   6   7
0   0   1   2   3
2   8   9  10  11
3  12  13  14  15
4  16  17  18  19
```

To select a random subset without replacement, one way is to slice off the first `k` elements of the array returned by `permutation`, where `k` is the desired subset size. There are much more efficient sampling-without-replacement algorithms, but this is an easy strategy that uses readily available tools:

```
In [183]: df.take(np.random.permutation(len(df))[:3])
Out[183]:
    0   1   2   3
1   4   5   6   7
3  12  13  14  15
4  16  17  18  19
```

To generate a sample *with* replacement, the fastest way is to use `np.random.randint` to draw random integers:

```
In [184]: bag = np.array([5, 7, -1, 6, 4])

In [185]: sampler = np.random.randint(0, len(bag), size=10)

In [186]: sampler
Out[186]: array([4, 4, 2, 2, 2, 0, 3, 0, 4, 1])

In [187]: draws = bag.take(sampler)

In [188]: draws
Out[188]: array([ 4,  4, -1, -1, -1,  5,  6,  5,  4,  7])
```

Computing Indicator/Dummy Variables

Another type of transformation for statistical modeling or machine learning applications is converting a categorical variable into a "dummy" or "indicator" matrix. If a column in a DataFrame has `k` distinct values, you would derive a matrix or DataFrame containing `k` columns containing all 1's and 0's. pandas has a `get_dummies` function for doing this, though devising one yourself is not difficult. Let's return to an earlier example DataFrame:

```
In [189]: df = DataFrame({'key': ['b', 'b', 'a', 'c', 'a', 'b'],
   .....:                 'data1': range(6)})

In [190]: pd.get_dummies(df['key'])
Out[190]:
   a  b  c
0  0  1  0
1  0  1  0
2  1  0  0
3  0  0  1
4  1  0  0
5  0  1  0
```

In some cases, you may want to add a prefix to the columns in the indicator DataFrame, which can then be merged with the other data. `get_dummies` has a prefix argument for doing just this:

```
In [191]: dummies = pd.get_dummies(df['key'], prefix='key')

In [192]: df_with_dummy = df[['data1']].join(dummies)

In [193]: df_with_dummy
Out[193]:
   data1  key_a  key_b  key_c
0      0      0      1      0
1      1      0      1      0
2      2      1      0      0
3      3      0      0      1
4      4      1      0      0
5      5      0      1      0
```

If a row in a DataFrame belongs to multiple categories, things are a bit more complicated. Let's return to the MovieLens 1M dataset from earlier in the book:

```
In [194]: mnames = ['movie_id', 'title', 'genres']

In [195]: movies = pd.read_table('ch07/movies.dat', sep='::', header=None,
   .....:                        names=mnames)

In [196]: movies[:10]
Out[196]:
   movie_id                               title                        genres
0         1                   Toy Story (1995)   Animation|Children's|Comedy
1         2                     Jumanji (1995)  Adventure|Children's|Fantasy
2         3            Grumpier Old Men (1995)                Comedy|Romance
3         4           Waiting to Exhale (1995)                  Comedy|Drama
4         5 Father of the Bride Part II (1995)                        Comedy
5         6                        Heat (1995)         Action|Crime|Thriller
6         7                     Sabrina (1995)                Comedy|Romance
7         8                Tom and Huck (1995)          Adventure|Children's
8         9                Sudden Death (1995)                        Action
9        10                   GoldenEye (1995)     Action|Adventure|Thriller
```

Adding indicator variables for each genre requires a little bit of wrangling. First, we extract the list of unique genres in the dataset (using a nice `set.union` trick):

```
In [197]: genre_iter = (set(x.split('|')) for x in movies.genres)

In [198]: genres = sorted(set.union(*genre_iter))
```

Now, one way to construct the indicator DataFrame is to start with a DataFrame of all zeros:

```
In [199]: dummies = DataFrame(np.zeros((len(movies), len(genres))), columns=genres)
```

Now, iterate through each movie and set entries in each row of `dummies` to 1:

```
In [200]: for i, gen in enumerate(movies.genres):
   .....:     dummies.ix[i, gen.split('|')] = 1
```

Then, as above, you can combine this with `movies`:

```
In [201]: movies_windic = movies.join(dummies.add_prefix('Genre_'))

In [202]: movies_windic.ix[0]
Out[202]:
movie_id                                  1
title                      Toy Story (1995)
genres          Animation|Children's|Comedy
Genre_Action                              0
Genre_Adventure                           0
Genre_Animation                           1
Genre_Children's                          1
Genre_Comedy                              1
Genre_Crime                               0
Genre_Documentary                         0
Genre_Drama                               0
Genre_Fantasy                             0
```

```
Genre_Film-Noir                   0
Genre_Horror                      0
Genre_Musical                     0
Genre_Mystery                     0
Genre_Romance                     0
Genre_Sci-Fi                      0
Genre_Thriller                    0
Genre_War                         0
Genre_Western                     0
Name: 0
```

For much larger data, this method of constructing indicator variables with multiple membership is not especially speedy. A lower-level function leveraging the internals of the DataFrame could certainly be written.

A useful recipe for statistical applications is to combine `get_dummies` with a discretization function like `cut`:

```
In [204]: values = np.random.rand(10)

In [205]: values
Out[205]:
array([ 0.9296,  0.3164,  0.1839,  0.2046,  0.5677,  0.5955,  0.9645,
        0.6532,  0.7489,  0.6536])

In [206]: bins = [0, 0.2, 0.4, 0.6, 0.8, 1]

In [207]: pd.get_dummies(pd.cut(values, bins))
Out[207]:
   (0, 0.2]  (0.2, 0.4]  (0.4, 0.6]  (0.6, 0.8]  (0.8, 1]
0         0           0           0           0         1
1         0           1           0           0         0
2         1           0           0           0         0
3         0           1           0           0         0
4         0           0           1           0         0
5         0           0           1           0         0
6         0           0           0           0         1
7         0           0           0           1         0
8         0           0           0           1         0
9         0           0           0           1         0
```

String Manipulation

Python has long been a popular data munging language in part due to its ease-of-use for string and text processing. Most text operations are made simple with the string object's built-in methods. For more complex pattern matching and text manipulations, regular expressions may be needed. pandas adds to the mix by enabling you to apply string and regular expressions concisely on whole arrays of data, additionally handling the annoyance of missing data.

String Object Methods

In many string munging and scripting applications, built-in string methods are sufficient. As an example, a comma-separated string can be broken into pieces with `split`:

```
In [208]: val = 'a,b,  guido'

In [209]: val.split(',')
Out[209]: ['a', 'b', '  guido']
```

`split` is often combined with `strip` to trim whitespace (including newlines):

```
In [210]: pieces = [x.strip() for x in val.split(',')]

In [211]: pieces
Out[211]: ['a', 'b', 'guido']
```

These substrings could be concatenated together with a two-colon delimiter using addition:

```
In [212]: first, second, third = pieces

In [213]: first + '::' + second + '::' + third
Out[213]: 'a::b::guido'
```

But, this isn't a practical generic method. A faster and more Pythonic way is to pass a list or tuple to the `join` method on the string `'::'`:

```
In [214]: '::'.join(pieces)
Out[214]: 'a::b::guido'
```

Other methods are concerned with locating substrings. Using Python's `in` keyword is the best way to detect a substring, though `index` and `find` can also be used:

```
In [215]: 'guido' in val
Out[215]: True

In [216]: val.index(',')        In [217]: val.find(':')
Out[216]: 1                     Out[217]: -1
```

Note the difference between `find` and `index` is that `index` raises an exception if the string isn't found (versus returning -1):

```
In [218]: val.index(':')
---------------------------------------------------------------------------
ValueError                                Traceback (most recent call last)
<ipython-input-218-280f8b2856ce> in <module>()
----> 1 val.index(':')
ValueError: substring not found
```

Relatedly, `count` returns the number of occurrences of a particular substring:

```
In [219]: val.count(',')
Out[219]: 2
```

`replace` will substitute occurrences of one pattern for another. This is commonly used to delete patterns, too, by passing an empty string:

```
In [220]: val.replace(',', '::')
Out[220]: 'a::b::  guido'

In [221]: val.replace(',', '')
Out[221]: 'ab  guido'
```

Regular expressions can also be used with many of these operations as you'll see below.

Table 7-3. Python built-in string methods

Argument	Description
`count`	Return the number of non-overlapping occurrences of substring in the string.
`endswith, startswith`	Returns True if string ends with suffix (starts with prefix).
`join`	Use string as delimiter for concatenating a sequence of other strings.
`index`	Return position of first character in substring if found in the string. Raises `ValueEr ror` if not found.
`find`	Return position of first character of *first* occurrence of substring in the string. Like `index`, but returns -1 if not found.
`rfind`	Return position of first character of *last* occurrence of substring in the string. Returns -1 if not found.
`replace`	Replace occurrences of string with another string.
`strip, rstrip, lstrip`	Trim whitespace, including newlines; equivalent to `x.strip()` (and `rstrip, lstrip`, respectively) for each element.
`split`	Break string into list of substrings using passed delimiter.
`lower, upper`	Convert alphabet characters to lowercase or uppercase, respectively.
`ljust, rjust`	Left justify or right justify, respectively. Pad opposite side of string with spaces (or some other fill character) to return a string with a minimum width.

Regular expressions

Regular expressions provide a flexible way to search or match string patterns in text. A single expression, commonly called a *regex*, is a string formed according to the regular expression language. Python's built-in `re` module is responsible for applying regular expressions to strings; I'll give a number of examples of its use here.

The art of writing regular expressions could be a chapter of its own and thus is outside the book's scope. There are many excellent tutorials and references on the internet, such as Zed Shaw's *Learn Regex The Hard Way* (*http://regex.learncodethehardway.org/book/*).

The `re` module functions fall into three categories: pattern matching, substitution, and splitting. Naturally these are all related; a regex describes a pattern to locate in the text, which can then be used for many purposes. Let's look at a simple example: suppose I wanted to split a string with a variable number of whitespace characters (tabs, spaces, and newlines). The regex describing one or more whitespace characters is `\s+`:

```
In [222]: import re

In [223]: text = "foo    bar\t baz  \tqux"

In [224]: re.split('\s+', text)
Out[224]: ['foo', 'bar', 'baz', 'qux']
```

When you call `re.split('\s+', text)`, the regular expression is first *compiled*, then its `split` method is called on the passed text. You can compile the regex yourself with `re.compile`, forming a reusable regex object:

```
In [225]: regex = re.compile('\s+')

In [226]: regex.split(text)
Out[226]: ['foo', 'bar', 'baz', 'qux']
```

If, instead, you wanted to get a list of all patterns matching the regex, you can use the `findall` method:

```
In [227]: regex.findall(text)
Out[227]: ['    ', '\t ', '  \t']
```

To avoid unwanted escaping with \ in a regular expression, use *raw* string literals like `r'C:\x'` instead of the equivalent `'C:\\x'`.

Creating a regex object with `re.compile` is highly recommended if you intend to apply the same expression to many strings; doing so will save CPU cycles.

`match` and `search` are closely related to `findall`. While `findall` returns all matches in a string, `search` returns only the first match. More rigidly, `match` *only* matches at the beginning of the string. As a less trivial example, let's consider a block of text and a regular expression capable of identifying most email addresses:

```
text = """Dave dave@google.com
Steve steve@gmail.com
Rob rob@gmail.com
Ryan ryan@yahoo.com
"""
pattern = r'[A-Z0-9._%+-]+@[A-Z0-9.-]+\.[A-Z]{2,4}'

# re.IGNORECASE makes the regex case-insensitive
regex = re.compile(pattern, flags=re.IGNORECASE)
```

Using `findall` on the text produces a list of the e-mail addresses:

```
In [229]: regex.findall(text)
Out[229]: ['dave@google.com', 'steve@gmail.com', 'rob@gmail.com', 'ryan@yahoo.com']
```

`search` returns a special match object for the first email address in the text. For the above regex, the match object can only tell us the start and end position of the pattern in the string:

```
In [230]: m = regex.search(text)

In [231]: m
Out[231]: <_sre.SRE_Match at 0x10a05de00>

In [232]: text[m.start():m.end()]
Out[232]: 'dave@google.com'
```

`regex.match` returns `None`, as it only will match if the pattern occurs at the start of the string:

```
In [233]: print regex.match(text)
None
```

Relatedly, `sub` will return a new string with occurrences of the pattern replaced by the a new string:

```
In [234]: print regex.sub('REDACTED', text)
Dave REDACTED
Steve REDACTED
Rob REDACTED
Ryan REDACTED
```

Suppose you wanted to find email addresses and simultaneously segment each address into its 3 components: username, domain name, and domain suffix. To do this, put parentheses around the parts of the pattern to segment:

```
In [235]: pattern = r'([A-Z0-9._%+-]+)@([A-Z0-9.-]+)\.([A-Z]{2,4})'

In [236]: regex = re.compile(pattern, flags=re.IGNORECASE)
```

A match object produced by this modified regex returns a tuple of the pattern components with its `groups` method:

```
In [237]: m = regex.match('wesm@bright.net')

In [238]: m.groups()
Out[238]: ('wesm', 'bright', 'net')
```

`findall` returns a list of tuples when the pattern has groups:

```
In [239]: regex.findall(text)
Out[239]:
[('dave', 'google', 'com'),
 ('steve', 'gmail', 'com'),
 ('rob', 'gmail', 'com'),
 ('ryan', 'yahoo', 'com')]
```

`sub` also has access to groups in each match using special symbols like `\1, \2`, etc.:

```
In [240]: print regex.sub(r'Username: \1, Domain: \2, Suffix: \3', text)
Dave Username: dave, Domain: google, Suffix: com
Steve Username: steve, Domain: gmail, Suffix: com
Rob Username: rob, Domain: gmail, Suffix: com
Ryan Username: ryan, Domain: yahoo, Suffix: com
```

There is much more to regular expressions in Python, most of which is outside the book's scope. To give you a flavor, one variation on the above email regex gives names to the match groups:

```
regex = re.compile(r"""
    (?P<username>[A-Z0-9._%+-]+)
    @
    (?P<domain>[A-Z0-9.-]+)
    \.
    (?P<suffix>[A-Z]{2,4})""", flags=re.IGNORECASE|re.VERBOSE)
```

The match object produced by such a regex can produce a handy dict with the specified group names:

```
In [242]: m = regex.match('wesm@bright.net')

In [243]: m.groupdict()
Out[243]: {'domain': 'bright', 'suffix': 'net', 'username': 'wesm'}
```

Table 7-4. Regular expression methods

Argument	Description
`findall, finditer`	Return all non-overlapping matching patterns in a string. `findall` returns a list of all patterns while `finditer` returns them one by one from an iterator.
`match`	Match pattern at start of string and optionally segment pattern components into groups. If the pattern matches, returns a match object, otherwise `None`.
`search`	Scan string for match to pattern; returning a match object if so. Unlike `match`, the match can be anywhere in the string as opposed to only at the beginning.
`split`	Break string into pieces at each occurrence of pattern.
`sub, subn`	Replace all (`sub`) or first n occurrences (`subn`) of pattern in string with replacement expression. Use symbols `\1, \2, ...` to refer to match group elements in the replacement string.

Vectorized string functions in pandas

Cleaning up a messy data set for analysis often requires a lot of string munging and regularization. To complicate matters, a column containing strings will sometimes have missing data:

```
In [244]: data = {'Dave': 'dave@google.com', 'Steve': 'steve@gmail.com',
   .....:         'Rob': 'rob@gmail.com', 'Wes': np.nan}

In [245]: data = Series(data)

In [246]: data                  In [247]: data.isnull()
Out[246]:                       Out[247]:
Dave     dave@google.com        Dave     False
Rob        rob@gmail.com        Rob      False
Steve    steve@gmail.com        Steve    False
Wes                  NaN        Wes       True
```

String and regular expression methods can be applied (passing a `lambda` or other function) to each value using `data.map`, but it will fail on the NA. To cope with this, Series has concise methods for string operations that skip NA values. These are accessed through Series's `str` attribute; for example, we could check whether each email address has `'gmail'` in it with `str.contains`:

```
In [248]: data.str.contains('gmail')
Out[248]:
Dave     False
Rob       True
Steve     True
Wes        NaN
```

Regular expressions can be used, too, along with any `re` options like `IGNORECASE`:

```
In [249]: pattern
Out[249]: '([A-Z0-9._%+-]+)@([A-Z0-9.-]+)\\.([A-Z]{2,4})'

In [250]: data.str.findall(pattern, flags=re.IGNORECASE)
Out[250]:
Dave     [('dave', 'google', 'com')]
Rob        [('rob', 'gmail', 'com')]
Steve    [('steve', 'gmail', 'com')]
Wes                              NaN
```

There are a couple of ways to do vectorized element retrieval. Either use `str.get` or index into the `str` attribute:

```
In [251]: matches = data.str.match(pattern, flags=re.IGNORECASE)

In [252]: matches
Out[252]:
Dave     ('dave', 'google', 'com')
Rob        ('rob', 'gmail', 'com')
Steve    ('steve', 'gmail', 'com')
Wes                            NaN

In [253]: matches.str.get(1)
Out[253]:
Dave     google
Rob       gmail
Steve     gmail
Wes         NaN

In [254]: matches.str[0]
Out[254]:
Dave      dave
Rob        rob
Steve    steve
Wes        NaN
```

You can similarly slice strings using this syntax:

```
In [255]: data.str[:5]
Out[255]:
Dave     dave@
Rob      rob@g
Steve    steve
Wes        NaN
```

Table 7-5. Vectorized string methods

Method	Description
`cat`	Concatenate strings element-wise with optional delimiter
`contains`	Return boolean array if each string contains pattern/regex
`count`	Count occurrences of pattern
`endswith, startswith`	Equivalent to `x.endswith(pattern)` or `x.startswith(pattern)` for each element.
`findall`	Compute list of all occurrences of pattern/regex for each string
`get`	Index into each element (retrieve i-th element)
`join`	Join strings in each element of the Series with passed separator
`len`	Compute length of each string
`lower, upper`	Convert cases; equivalent to `x.lower()` or `x.upper()` for each element.
`match`	Use `re.match` with the passed regular expression on each element, returning matched groups as list.
`pad`	Add whitespace to left, right, or both sides of strings
`center`	Equivalent to `pad(side='both')`
`repeat`	Duplicate values; for example `s.str.repeat(3)` equivalent to `x * 3` for each string.
`replace`	Replace occurrences of pattern/regex with some other string
`slice`	Slice each string in the Series.
`split`	Split strings on delimiter or regular expression
`strip, rstrip, lstrip`	Trim whitespace, including newlines; equivalent to `x.strip()` (and `rstrip`, `lstrip`, respectively) for each element.

Example: USDA Food Database

The US Department of Agriculture makes available a database of food nutrient information. Ashley Williams, an English hacker, has made available a version of this database in JSON format (*http://ashleyw.co.uk/project/food-nutrient-database*). The records look like this:

```
{
  "id": 21441,
  "description": "KENTUCKY FRIED CHICKEN, Fried Chicken, EXTRA CRISPY,
Wing, meat and skin with breading",
  "tags": ["KFC"],
  "manufacturer": "Kentucky Fried Chicken",
  "group": "Fast Foods",
  "portions": [
    {
      "amount": 1,
      "unit": "wing, with skin",
      "grams": 68.0
    },
```

```
    ...
  ],
  "nutrients": [
    {
      "value": 20.8,
      "units": "g",
      "description": "Protein",
      "group": "Composition"
    },

    ...
  ]
}
```

Each food has a number of identifying attributes along with two lists of nutrients and portion sizes. Having the data in this form is not particularly amenable for analysis, so we need to do some work to wrangle the data into a better form.

After downloading and extracting the data from the link above, you can load it into Python with any JSON library of your choosing. I'll use the built-in Python `json` module:

```
In [256]: import json

In [257]: db = json.load(open('ch07/foods-2011-10-03.json'))

In [258]: len(db)
Out[258]: 6636
```

Each entry in `db` is a dict containing all the data for a single food. The `'nutrients'` field is a list of dicts, one for each nutrient:

```
In [259]: db[0].keys()
Out[259]:
[u'portions',
 u'description',
 u'tags',
 u'nutrients',
 u'group',
 u'id',
 u'manufacturer']

In [260]: db[0]['nutrients'][0]
Out[260]:
{u'description': u'Protein',
 u'group': u'Composition',
 u'units': u'g',
 u'value': 25.18}

In [261]: nutrients = DataFrame(db[0]['nutrients'])

In [262]: nutrients[:7]
Out[262]:
                    description       group units    value
0                       Protein  Composition     g    25.18
1             Total lipid (fat)  Composition     g    29.20
2  Carbohydrate, by difference  Composition     g     3.06
3                           Ash       Other     g     3.28
4                        Energy      Energy  kcal   376.00
5                         Water  Composition     g    39.28
6                        Energy      Energy    kJ  1573.00
```

When converting a list of dicts to a DataFrame, we can specify a list of fields to extract. We'll take the food names, group, id, and manufacturer:

```
In [263]: info_keys = ['description', 'group', 'id', 'manufacturer']

In [264]: info = DataFrame(db, columns=info_keys)

In [265]: info[:5]
Out[265]:
                          description                   group    id manufacturer
0                     Cheese, caraway  Dairy and Egg Products  1008
1                     Cheese, cheddar  Dairy and Egg Products  1009
2                        Cheese, edam  Dairy and Egg Products  1018
3                        Cheese, feta  Dairy and Egg Products  1019
4  Cheese, mozzarella, part skim milk  Dairy and Egg Products  1028

In [266]: info
Out[266]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 6636 entries, 0 to 6635
Data columns:
description     6636  non-null values
group           6636  non-null values
id              6636  non-null values
manufacturer    5195  non-null values
dtypes: int64(1), object(3)
```

You can see the distribution of food groups with `value_counts`:

```
In [267]: pd.value_counts(info.group)[:10]
Out[267]:
Vegetables and Vegetable Products    812
Beef Products                        618
Baked Products                       496
Breakfast Cereals                    403
Legumes and Legume Products          365
Fast Foods                           365
Lamb, Veal, and Game Products        345
Sweets                               341
Pork Products                        328
Fruits and Fruit Juices              328
```

Now, to do some analysis on all of the nutrient data, it's easiest to assemble the nutrients for each food into a single large table. To do so, we need to take several steps. First, I'll convert each list of food nutrients to a DataFrame, add a column for the food `id`, and append the DataFrame to a list. Then, these can be concatenated together with `concat`:

```
nutrients = []

for rec in db:
    fnuts = DataFrame(rec['nutrients'])
    fnuts['id'] = rec['id']
    nutrients.append(fnuts)

nutrients = pd.concat(nutrients, ignore_index=True)
```

If all goes well, `nutrients` should look like this:

```
In [269]: nutrients
Out[269]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 389355 entries, 0 to 389354
Data columns:
description    389355  non-null values
group          389355  non-null values
units          389355  non-null values
value          389355  non-null values
id             389355  non-null values
dtypes: float64(1), int64(1), object(3)
```

I noticed that, for whatever reason, there are duplicates in this DataFrame, so it makes things easier to drop them:

```
In [270]: nutrients.duplicated().sum()
Out[270]: 14179

In [271]: nutrients = nutrients.drop_duplicates()
```

Since `'group'` and `'description'` is in both DataFrame objects, we can rename them to make it clear what is what:

```
In [272]: col_mapping = {'description' : 'food',
   .....:                'group'       : 'fgroup'}

In [273]: info = info.rename(columns=col_mapping, copy=False)

In [274]: info
Out[274]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 6636 entries, 0 to 6635
Data columns:
food            6636  non-null values
fgroup          6636  non-null values
id              6636  non-null values
manufacturer    5195  non-null values
dtypes: int64(1), object(3)

In [275]: col_mapping = {'description' : 'nutrient',
   .....:                'group' : 'nutgroup'}

In [276]: nutrients = nutrients.rename(columns=col_mapping, copy=False)

In [277]: nutrients
Out[277]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 375176 entries, 0 to 389354
Data columns:
nutrient    375176  non-null values
nutgroup    375176  non-null values
units       375176  non-null values
value       375176  non-null values
```

```
id          375176  non-null values
dtypes: float64(1), int64(1), object(3)
```

With all of this done, we're ready to merge `info` with `nutrients`:

```
In [278]: ndata = pd.merge(nutrients, info, on='id', how='outer')

In [279]: ndata
Out[279]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 375176 entries, 0 to 375175
Data columns:
nutrient        375176  non-null values
nutgroup        375176  non-null values
units           375176  non-null values
value           375176  non-null values
id              375176  non-null values
food            375176  non-null values
fgroup          375176  non-null values
manufacturer    293054  non-null values
dtypes: float64(1), int64(1), object(6)

In [280]: ndata.ix[30000]
Out[280]:
nutrient                       Folic acid
nutgroup                         Vitamins
units                                 mcg
value                                   0
id                                   5658
food            Ostrich, top loin, cooked
fgroup                   Poultry Products
manufacturer
Name: 30000
```

The tools that you need to slice and dice, aggregate, and visualize this dataset will be explored in detail in the next two chapters, so after you get a handle on those methods you might return to this dataset. For example, we could a plot of median values by food group and nutrient type (see Figure 7-1):

```
In [281]: result = ndata.groupby(['nutrient', 'fgroup'])['value'].quantile(0.5)

In [282]: result['Zinc, Zn'].order().plot(kind='barh')
```

With a little cleverness, you can find which food is most dense in each nutrient:

```
by_nutrient = ndata.groupby(['nutgroup', 'nutrient'])

get_maximum = lambda x: x.xs(x.value.idxmax())
get_minimum = lambda x: x.xs(x.value.idxmin())

max_foods = by_nutrient.apply(get_maximum)[['value', 'food']]

# make the food a little smaller
max_foods.food = max_foods.food.str[:50]
```

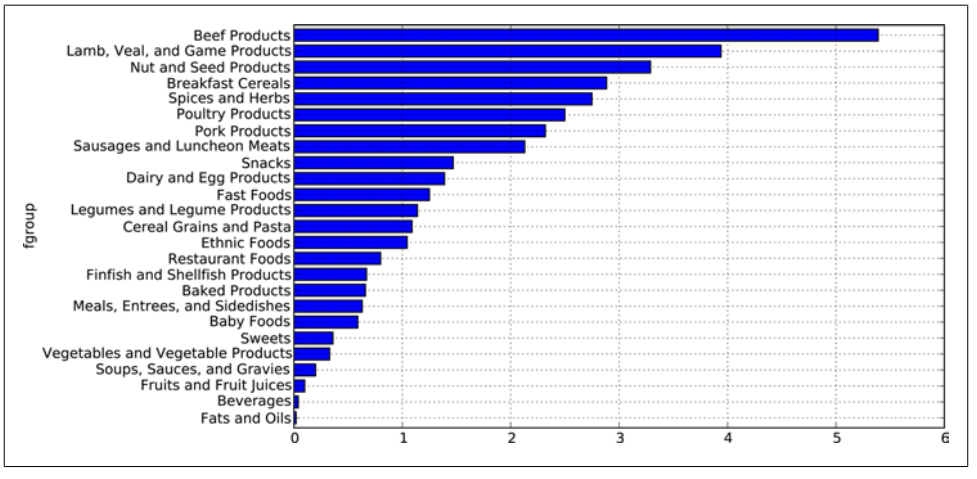


Figure 7-1. Median Zinc values by nutrient group

The resulting DataFrame is a bit too large to display in the book; here is just the `'Amino Acids'` nutrient group:

```
In [284]: max_foods.ix['Amino Acids']['food']
Out[284]:
nutrient
Alanine                            Gelatins, dry powder, unsweetened
Arginine                                Seeds, sesame flour, low-fat
Aspartic acid                                  Soy protein isolate
Cystine               Seeds, cottonseed flour, low fat (glandless)
Glutamic acid                                  Soy protein isolate
Glycine                            Gelatins, dry powder, unsweetened
Histidine                   Whale, beluga, meat, dried (Alaska Native)
Hydroxyproline    KENTUCKY FRIED CHICKEN, Fried Chicken, ORIGINAL R
Isoleucine        Soy protein isolate, PROTEIN TECHNOLOGIES INTERNA
Leucine           Soy protein isolate, PROTEIN TECHNOLOGIES INTERNA
Lysine            Seal, bearded (Oogruk), meat, dried (Alaska Nativ
Methionine                     Fish, cod, Atlantic, dried and salted
Phenylalanine     Soy protein isolate, PROTEIN TECHNOLOGIES INTERNA
Proline                            Gelatins, dry powder, unsweetened
Serine            Soy protein isolate, PROTEIN TECHNOLOGIES INTERNA
Threonine         Soy protein isolate, PROTEIN TECHNOLOGIES INTERNA
Tryptophan         Sea lion, Steller, meat with fat (Alaska Native)
Tyrosine          Soy protein isolate, PROTEIN TECHNOLOGIES INTERNA
Valine            Soy protein isolate, PROTEIN TECHNOLOGIES INTERNA
Name: food
```

CHAPTER 8
Plotting and Visualization

Making plots and static or interactive visualizations is one of the most important tasks in data analysis. It may be a part of the exploratory process; for example, helping identify outliers, needed data transformations, or coming up with ideas for models. For others, building an interactive visualization for the web using a toolkit like d3.js (*http://d3js.org/*) may be the end goal. Python has many visualization tools (see the end of this chapter), but I'll be mainly focused on matplotlib (*http://matplotlib.sourceforge.net*).

matplotlib is a (primarily 2D) desktop plotting package designed for creating publication-quality plots. The project was started by John Hunter in 2002 to enable a MATLAB-like plotting interface in Python. He, Fernando Pérez (of IPython), and others have collaborated for many years since then to make IPython combined with matplotlib a very functional and productive environment for scientific computing. When used in tandem with a GUI toolkit (for example, within IPython), matplotlib has interactive features like zooming and panning. It supports many different GUI backends on all operating systems and additionally can export graphics to all of the common vector and raster graphics formats: PDF, SVG, JPG, PNG, BMP, GIF, etc. I have used it to produce almost all of the graphics outside of diagrams in this book.

matplotlib has a number of add-on toolkits, such as `mplot3d` for 3D plots and `basemap` for mapping and projections. I will give an example using `basemap` to plot data on a map and to read *shapefiles* at the end of the chapter.

To follow along with the code examples in the chapter, make sure you have started IPython in Pylab mode (`ipython --pylab`) or enabled GUI event loop integration with the `%gui` magic.

A Brief matplotlib API Primer

There are several ways to interact with matplotlib. The most common is through *pylab mode* in IPython by running `ipython --pylab`. This launches IPython configured to be able to support the matplotlib GUI backend of your choice (Tk, wxPython, PyQt, Mac

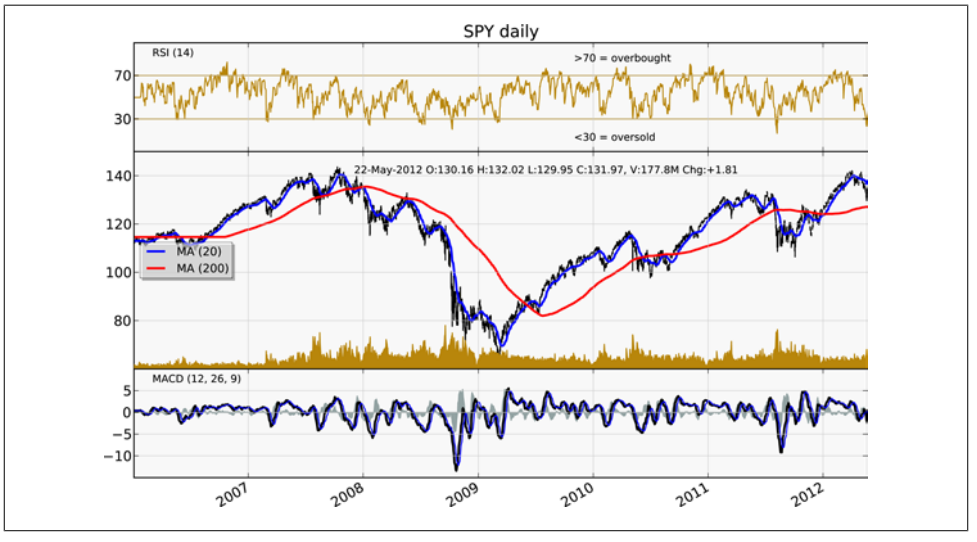


Figure 8-1. A more complex matplotlib financial plot

OS X native, GTK). For most users, the default backend will be sufficient. Pylab mode also imports a large set of modules and functions into IPython to provide a more MATLAB-like interface. You can test that everything is working by making a simple plot:

```
plot(np.arange(10))
```

If everything is set up right, a new window should pop up with a line plot. You can close it by using the mouse or entering `close()`. Matplotlib API functions like `plot` and `close` are all in the `matplotlib.pyplot` module, which is typically imported by convention as:

```
import matplotlib.pyplot as plt
```

While the pandas plotting functions described later deal with many of the mundane details of making plots, should you wish to customize them beyond the function options provided you will need to learn a bit about the matplotlib API.

There is not enough room in the book to give a comprehensive treatment to the breadth and depth of functionality in matplotlib. It should be enough to teach you the ropes to get up and running. The matplotlib gallery and documentation are the best resource for becoming a plotting guru and using advanced features.

Figures and Subplots

Plots in matplotlib reside within a `Figure` object. You can create a new figure with `plt.figure`:

```
In [13]: fig = plt.figure()
```

If you are in pylab mode in IPython, a new empty window should pop up. `plt.figure` has a number of options, notably `figsize` will guarantee the figure has a certain size and aspect ratio if saved to disk. Figures in matplotlib also support a numbering scheme (for example, `plt.figure(2)`) that mimics MATLAB. You can get a reference to the active figure using `plt.gcf()`.

You can't make a plot with a blank figure. You have to create one or more `subplots` using `add_subplot`:

```
In [14]: ax1 = fig.add_subplot(2, 2, 1)
```

This means that the figure should be 2 × 2, and we're selecting the first of 4 subplots (numbered from 1). If you create the next two subplots, you'll end up with a figure that looks like Figure 8-2.

```
In [15]: ax2 = fig.add_subplot(2, 2, 2)

In [16]: ax3 = fig.add_subplot(2, 2, 3)
```

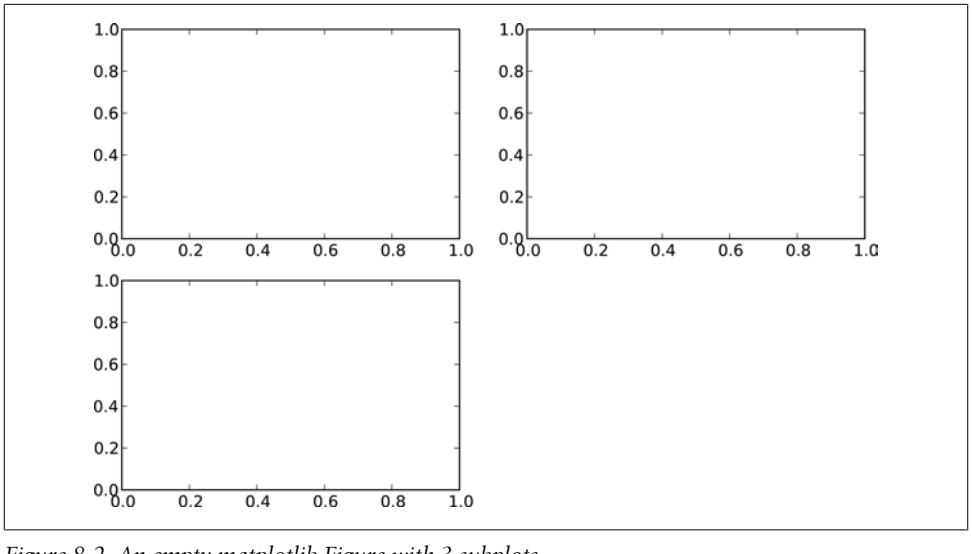


Figure 8-2. An empty matplotlib Figure with 3 subplots

When you issue a plotting command like `plt.plot([1.5, 3.5, -2, 1.6])`, matplotlib draws on the last figure and subplot used (creating one if necessary), thus hiding the figure and subplot creation. Thus, if we run the following command, you'll get something like Figure 8-3:

```
In [17]: from numpy.random import randn

In [18]: plt.plot(randn(50).cumsum(), 'k--')
```

The `'k--'` is a *style* option instructing matplotlib to plot a black dashed line. The objects returned by `fig.add_subplot` above are `AxesSubplot` objects, on which you can directly plot on the other empty subplots by calling each one's instance methods, see Figure 8-4:

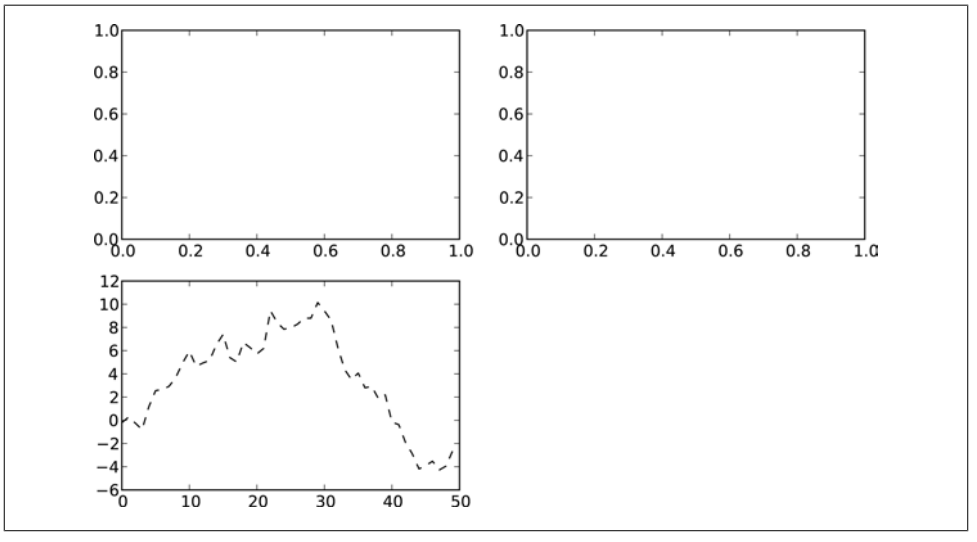


Figure 8-3. Figure after single plot

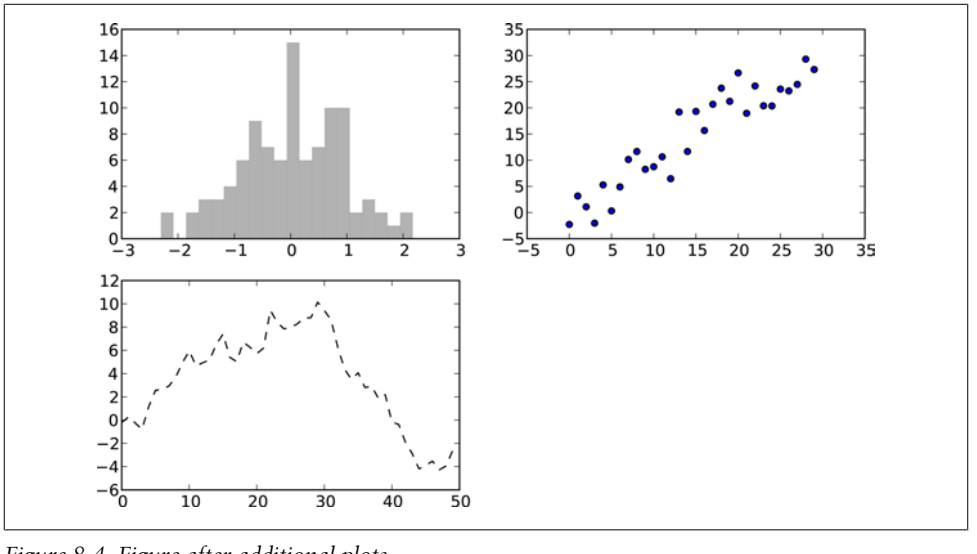


Figure 8-4. Figure after additional plots

```
In [19]: _ = ax1.hist(randn(100), bins=20, color='k', alpha=0.3)

In [20]: ax2.scatter(np.arange(30), np.arange(30) + 3 * randn(30))
```

You can find a comprehensive catalogue of plot types in the matplotlib documentation.

Since creating a figure with multiple subplots according to a particular layout is such a common task, there is a convenience method, `plt.subplots`, that creates a new figure and returns a NumPy array containing the created subplot objects:

```
In [22]: fig, axes = plt.subplots(2, 3)

In [23]: axes
Out[23]:
array([[Axes(0.125,0.536364;0.227941x0.363636),
        Axes(0.398529,0.536364;0.227941x0.363636),
        Axes(0.672059,0.536364;0.227941x0.363636)],
       [Axes(0.125,0.1;0.227941x0.363636),
        Axes(0.398529,0.1;0.227941x0.363636),
        Axes(0.672059,0.1;0.227941x0.363636)]], dtype=object)
```

This is very useful as the `axes` array can be easily indexed like a two-dimensional array; for example, `axes[0, 1]`. You can also indicate that subplots should have the same X or Y axis using `sharex` and `sharey`, respectively. This is especially useful when comparing data on the same scale; otherwise, matplotlib auto-scales plot limits independently. See Table 8-1 for more on this method.

Table 8-1. pyplot.subplots options

Argument	Description
`nrows`	Number of rows of subplots
`ncols`	Number of columns of subplots
`sharex`	All subplots should use the same X-axis ticks (adjusting the `xlim` will affect all subplots)
`sharey`	All subplots should use the same Y-axis ticks (adjusting the `ylim` will affect all subplots)
`subplot_kw`	Dict of keywords for creating the
`**fig_kw`	Additional keywords to `subplots` are used when creating the figure, such as `plt.subplots(2, 2, figsize=(8, 6))`

Adjusting the spacing around subplots

By default matplotlib leaves a certain amount of padding around the outside of the subplots and spacing between subplots. This spacing is all specified relative to the height and width of the plot, so that if you resize the plot either programmatically or manually using the GUI window, the plot will dynamically adjust itself. The spacing can be most easily changed using the `subplots_adjust` `Figure` method, also available as a top-level function:

```
subplots_adjust(left=None, bottom=None, right=None, top=None,
                wspace=None, hspace=None)
```

`wspace` and `hspace` controls the percent of the figure width and figure height, respectively, to use as spacing between subplots. Here is a small example where I shrink the spacing all the way to zero (see Figure 8-5):

```
fig, axes = plt.subplots(2, 2, sharex=True, sharey=True)
for i in range(2):
    for j in range(2):
        axes[i, j].hist(randn(500), bins=50, color='k', alpha=0.5)
plt.subplots_adjust(wspace=0, hspace=0)
```

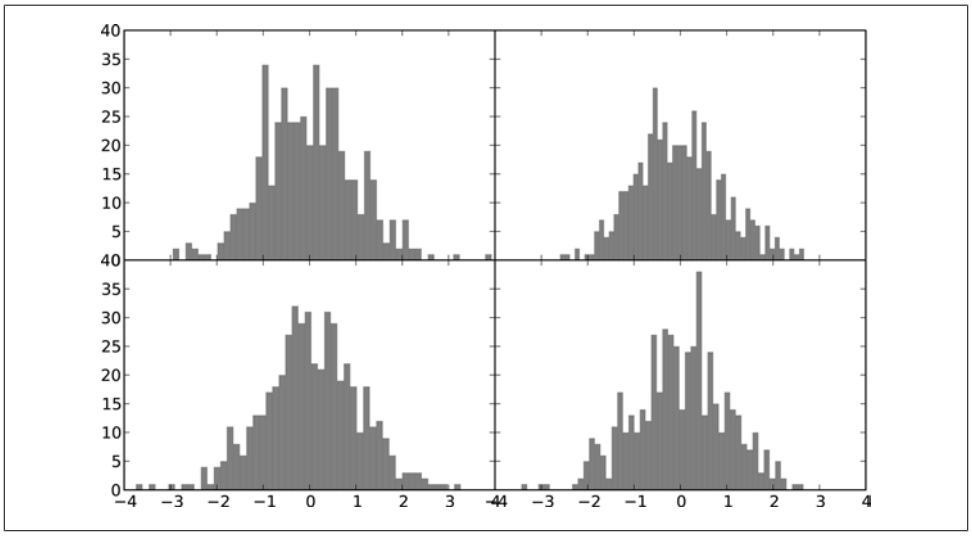


Figure 8-5. Figure with no inter-subplot spacing

You may notice that the axis labels overlap. matplotlib doesn't check whether the labels overlap, so in a case like this you would need to fix the labels yourself by specifying explicit tick locations and tick labels. More on this in the coming sections.

Colors, Markers, and Line Styles

Matplotlib's main `plot` function accepts arrays of X and Y coordinates and optionally a string abbreviation indicating color and line style. For example, to plot `x` versus `y` with green dashes, you would execute:

```
ax.plot(x, y, 'g--')
```

This way of specifying both color and linestyle in a string is provided as a convenience; in practice if you were creating plots programmatically you might prefer not to have to munge strings together to create plots with the desired style. The same plot could also have been expressed more explicitly as:

```
ax.plot(x, y, linestyle='--', color='g')
```

There are a number of color abbreviations provided for commonly-used colors, but any color on the spectrum can be used by specifying its RGB value (for example, `'#CECECE'`). You can see the full set of linestyles by looking at the docstring for `plot`.

Line plots can additionally have *markers* to highlight the actual data points. Since matplotlib creates a continuous line plot, interpolating between points, it can occasionally be unclear where the points lie. The marker can be part of the style string, which must have color followed by marker type and line style (see Figure 8-6):

```
In [28]: plt.plot(randn(30).cumsum(), 'ko--')
```

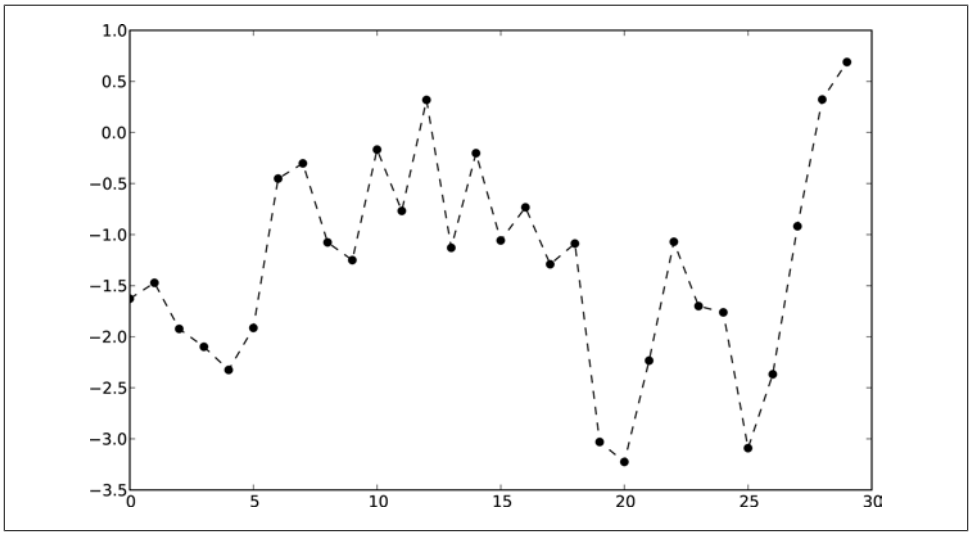


Figure 8-6. Line plot with markers example

This could also have been written more explicitly as:

```
plot(randn(30).cumsum(), color='k', linestyle='dashed', marker='o')
```

For line plots, you will notice that subsequent points are linearly interpolated by default. This can be altered with the `drawstyle` option:

```
In [30]: data = randn(30).cumsum()

In [31]: plt.plot(data, 'k--', label='Default')
Out[31]: [<matplotlib.lines.Line2D at 0x461cdd0>]

In [32]: plt.plot(data, 'k-', drawstyle='steps-post', label='steps-post')
Out[32]: [<matplotlib.lines.Line2D at 0x461f350>]

In [33]: plt.legend(loc='best')
```

Ticks, Labels, and Legends

For most kinds of plot decorations, there are two main ways to do things: using the procedural `pyplot` interface (which will be very familiar to MATLAB users) and the more object-oriented native matplotlib API.

The `pyplot` interface, designed for interactive use, consists of methods like `xlim`, `xticks`, and `xticklabels`. These control the plot range, tick locations, and tick labels, respectively. They can be used in two ways:

- Called with no arguments returns the current parameter value. For example `plt.xlim()` returns the current X axis plotting range

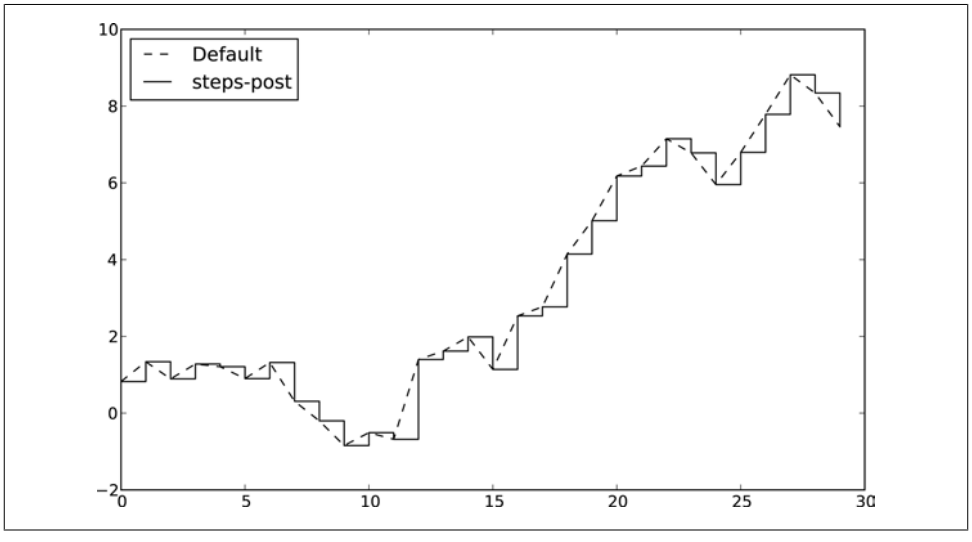


Figure 8-7. Line plot with different drawstyle options

- Called with parameters sets the parameter value. So `plt.xlim([0, 10])`, sets the X axis range to 0 to 10

All such methods act on the active or most recently-created `AxesSubplot`. Each of them corresponds to two methods on the subplot object itself; in the case of `xlim` these are `ax.get_xlim` and `ax.set_xlim`. I prefer to use the subplot instance methods myself in the interest of being explicit (and especially when working with multiple subplots), but you can certainly use whichever you find more convenient.

Setting the title, axis labels, ticks, and ticklabels

To illustrate customizing the axes, I'll create a simple figure and plot of a random walk (see Figure 8-8):

```
In [34]: fig = plt.figure(); ax = fig.add_subplot(1, 1, 1)

In [35]: ax.plot(randn(1000).cumsum())
```

To change the X axis ticks, it's easiest to use `set_xticks` and `set_xticklabels`. The former instructs matplotlib where to place the ticks along the data range; by default these locations will also be the labels. But we can set any other values as the labels using `set_xticklabels`:

```
In [36]: ticks = ax.set_xticks([0, 250, 500, 750, 1000])

In [37]: labels = ax.set_xticklabels(['one', 'two', 'three', 'four', 'five'],
   ....:                             rotation=30, fontsize='small')
```

Lastly, `set_xlabel` gives a name to the X axis and `set_title` the subplot title:

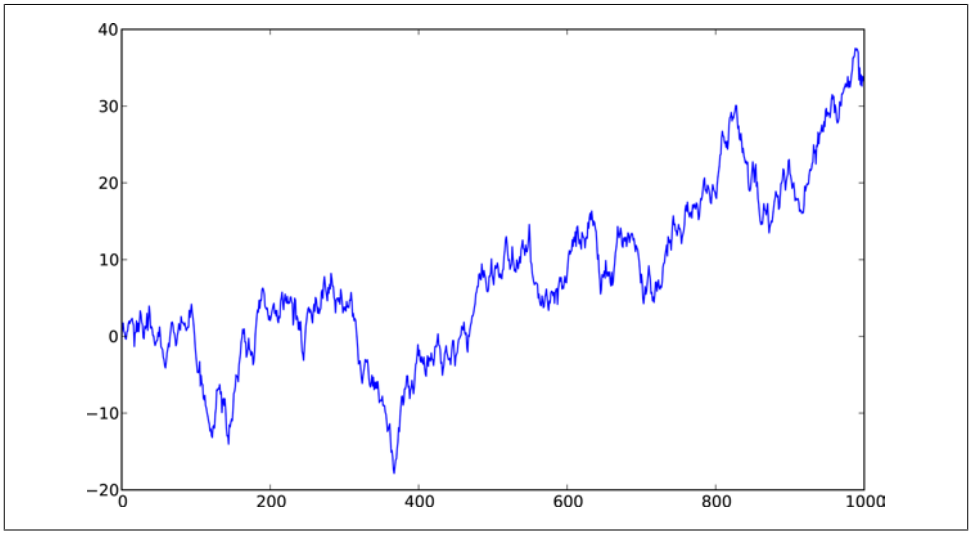


Figure 8-8. Simple plot for illustrating xticks

```
In [38]: ax.set_title('My first matplotlib plot')
Out[38]: <matplotlib.text.Text at 0x7f9190912850>

In [39]: ax.set_xlabel('Stages')
```

See Figure 8-9 for the resulting figure. Modifying the Y axis consists of the same process, substituting `y` for `x` in the above.

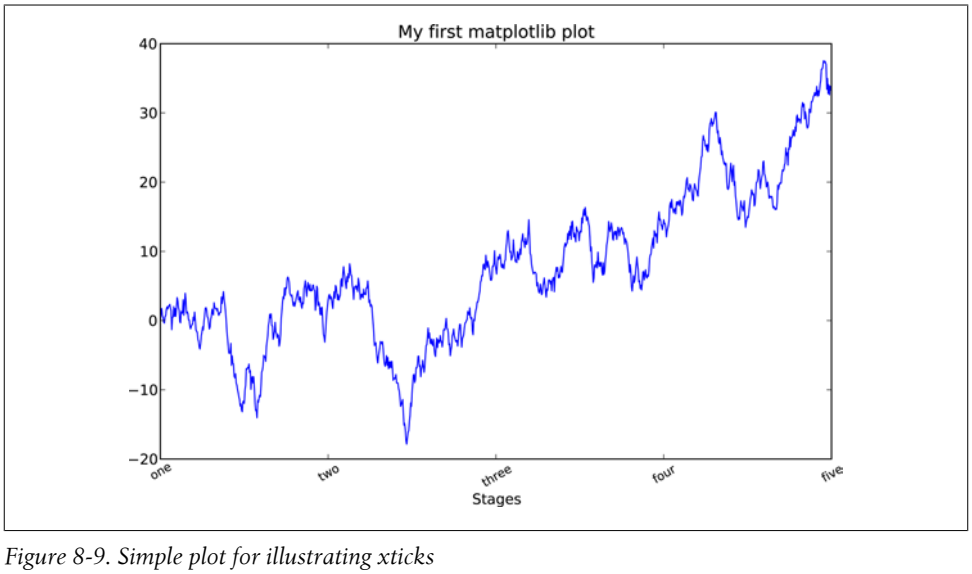


Figure 8-9. Simple plot for illustrating xticks

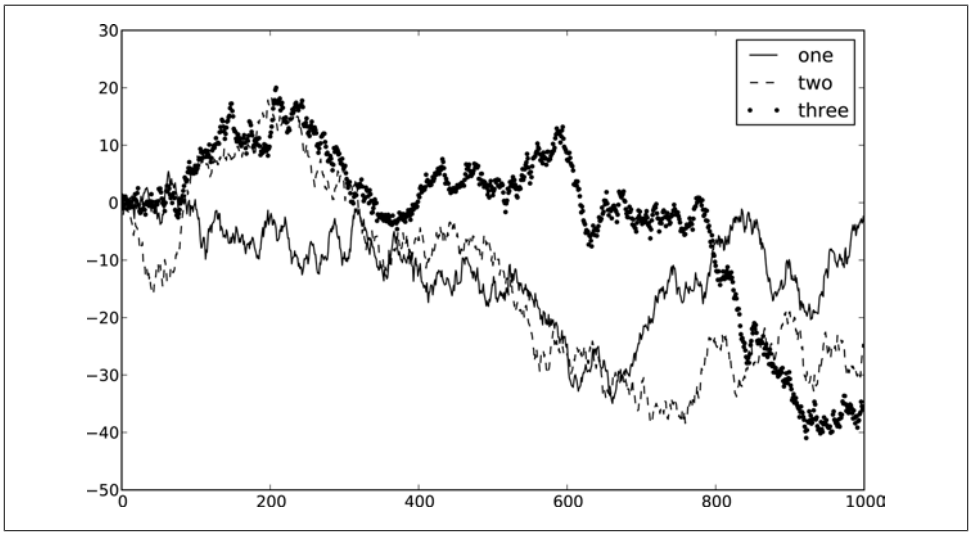


Figure 8-10. Simple plot with 3 lines and legend

Adding legends

Legends are another critical element for identifying plot elements. There are a couple of ways to add one. The easiest is to pass the `label` argument when adding each piece of the plot:

```
In [40]: fig = plt.figure(); ax = fig.add_subplot(1, 1, 1)

In [41]: ax.plot(randn(1000).cumsum(), 'k', label='one')
Out[41]: [<matplotlib.lines.Line2D at 0x4720a90>]

In [42]: ax.plot(randn(1000).cumsum(), 'k--', label='two')
Out[42]: [<matplotlib.lines.Line2D at 0x4720f90>]

In [43]: ax.plot(randn(1000).cumsum(), 'k.', label='three')
Out[43]: [<matplotlib.lines.Line2D at 0x4723550>]
```

Once you've done this, you can either call `ax.legend()` or `plt.legend()` to automatically create a legend:

```
In [44]: ax.legend(loc='best')
```

See Figure 8-10. The `loc` tells matplotlib where to place the plot. If you aren't picky `'best'` is a good option, as it will choose a location that is most out of the way. To exclude one or more elements from the legend, pass no label or `label='_nolegend_'`.

Annotations and Drawing on a Subplot

In addition to the standard plot types, you may wish to draw your own plot annotations, which could consist of text, arrows, or other shapes.

Annotations and text can be added using the `text`, `arrow`, and `annotate` functions. `text` draws text at given coordinates `(x, y)` on the plot with optional custom styling:

```
ax.text(x, y, 'Hello world!',
        family='monospace', fontsize=10)
```

Annotations can draw both text and arrows arranged appropriately. As an example, let's plot the closing S&P 500 index price since 2007 (obtained from Yahoo! Finance) and annotate it with some of the important dates from the 2008-2009 financial crisis. See Figure 8-11 for the result:

```
from datetime import datetime

fig = plt.figure()
ax = fig.add_subplot(1, 1, 1)

data = pd.read_csv('ch08/spx.csv', index_col=0, parse_dates=True)
spx = data['SPX']

spx.plot(ax=ax, style='k-')

crisis_data = [
    (datetime(2007, 10, 11), 'Peak of bull market'),
    (datetime(2008, 3, 12), 'Bear Stearns Fails'),
    (datetime(2008, 9, 15), 'Lehman Bankruptcy')
]

for date, label in crisis_data:
    ax.annotate(label, xy=(date, spx.asof(date) + 50),
                xytext=(date, spx.asof(date) + 200),
                arrowprops=dict(facecolor='black'),
                horizontalalignment='left', verticalalignment='top')

# Zoom in on 2007-2010
ax.set_xlim(['1/1/2007', '1/1/2011'])
ax.set_ylim([600, 1800])

ax.set_title('Important dates in 2008-2009 financial crisis')
```

See the online matplotlib gallery for many more annotation examples to learn from.

Drawing shapes requires some more care. matplotlib has objects that represent many common shapes, referred to as *patches*. Some of these, like `Rectangle` and `Circle` are found in `matplotlib.pyplot`, but the full set is located in `matplotlib.patches`.

To add a shape to a plot, you create the patch object `shp` and add it to a subplot by calling `ax.add_patch(shp)` (see Figure 8-12):

```
fig = plt.figure()
ax = fig.add_subplot(1, 1, 1)

rect = plt.Rectangle((0.2, 0.75), 0.4, 0.15, color='k', alpha=0.3)
circ = plt.Circle((0.7, 0.2), 0.15, color='b', alpha=0.3)
pgon = plt.Polygon([[0.15, 0.15], [0.35, 0.4], [0.2, 0.6]],
                   color='g', alpha=0.5)
```

```
ax.add_patch(rect)
ax.add_patch(circ)
ax.add_patch(pgon)
```

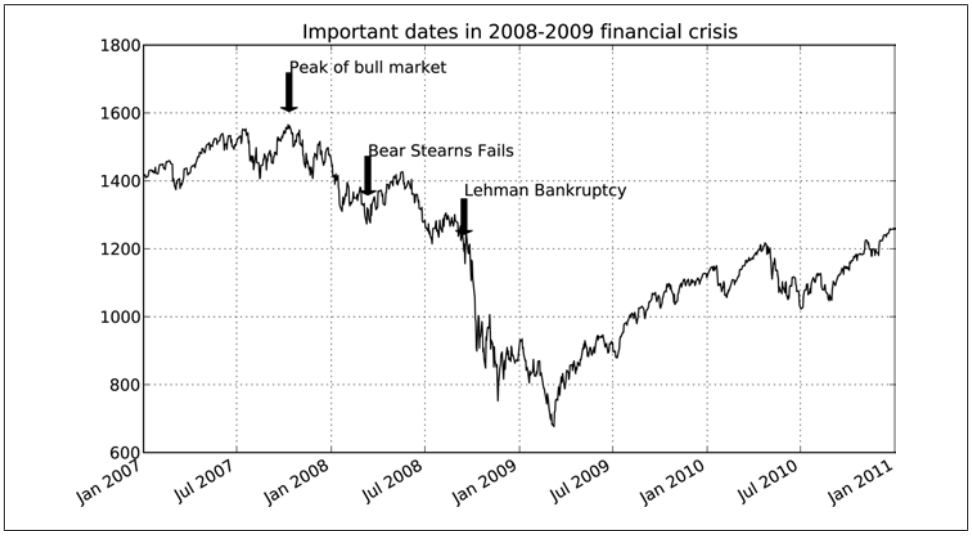


Figure 8-11. Important dates in 2008-2009 financial crisis

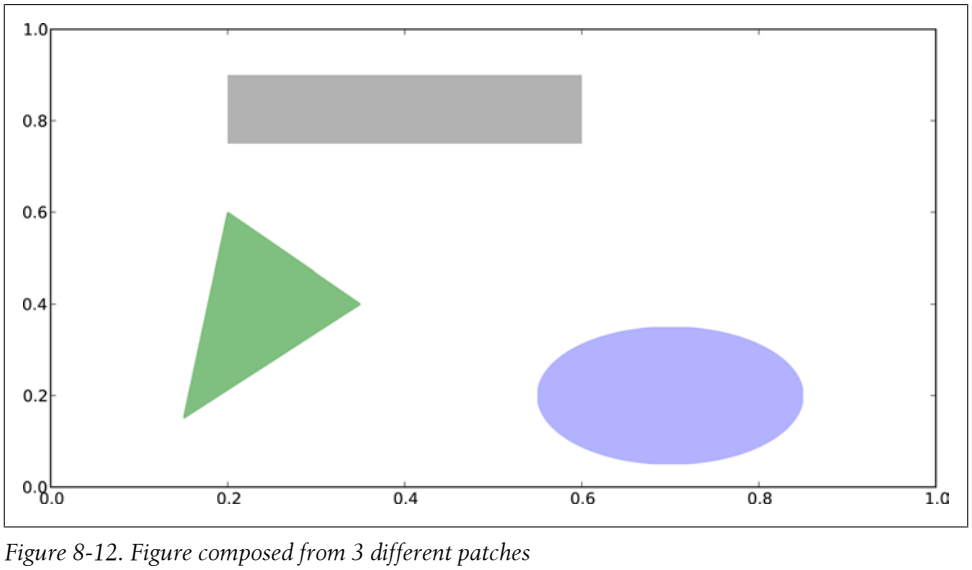


Figure 8-12. Figure composed from 3 different patches

If you look at the implementation of many familiar plot types, you will see that they are assembled from patches.

Saving Plots to File

The active figure can be saved to file using `plt.savefig`. This method is equivalent to the figure object's `savefig` instance method. For example, to save an SVG version of a figure, you need only type:

```
plt.savefig('figpath.svg')
```

The file type is inferred from the file extension. So if you used `.pdf` instead you would get a PDF. There are a couple of important options that I use frequently for publishing graphics: `dpi`, which controls the dots-per-inch resolution, and `bbox_inches`, which can trim the whitespace around the actual figure. To get the same plot as a PNG above with minimal whitespace around the plot and at 400 DPI, you would do:

```
plt.savefig('figpath.png', dpi=400, bbox_inches='tight')
```

`savefig` doesn't have to write to disk; it can also write to any file-like object, such as a `StringIO`:

```
from io import StringIO
buffer = StringIO()
plt.savefig(buffer)
plot_data = buffer.getvalue()
```

For example, this is useful for serving dynamically-generated images over the web.

Table 8-2. Figure.savefig options

Argument	Description
`fname`	String containing a filepath or a Python file-like object. The figure format is inferred from the file extension, e.g. `.pdf` for PDF or `.png` for PNG.
`dpi`	The figure resolution in dots per inch; defaults to 100 out of the box but can be configured
`facecolor, edgecolor`	The color of the figure background outside of the subplots. `'w'` (white), by default
`format`	The explicit file format to use (`'png', 'pdf', 'svg', 'ps', 'eps', ...`)
`bbox_inches`	The portion of the figure to save. If `'tight'` is passed, will attempt to trim the empty space around the figure

matplotlib Configuration

matplotlib comes configured with color schemes and defaults that are geared primarily toward preparing figures for publication. Fortunately, nearly all of the default behavior can be customized via an extensive set of global parameters governing figure size, subplot spacing, colors, font sizes, grid styles, and so on. There are two main ways to interact with the matplotlib configuration system. The first is programmatically from Python using the `rc` method. For example, to set the global default figure size to be 10 x 10, you could enter:

```
plt.rc('figure', figsize=(10, 10))
```

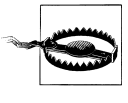
The first argument to `rc` is the component you wish to customize, such as `'figure'`, `'axes'`, `'xtick'`, `'ytick'`, `'grid'`, `'legend'` or many others. After that can follow a sequence of keyword arguments indicating the new parameters. An easy way to write down the options in your program is as a dict:

```
font_options = {'family' : 'monospace',
                'weight' : 'bold',
                'size'   : 'small'}
plt.rc('font', **font_options)
```

For more extensive customization and to see a list of all the options, matplotlib comes with a configuration file `matplotlibrc` in the `matplotlib/mpl-data` directory. If you customize this file and place it in your home directory titled `.matplotlibrc`, it will be loaded each time you use matplotlib.

Plotting Functions in pandas

As you've seen, matplotlib is actually a fairly low-level tool. You assemble a plot from its base components: the data display (the type of plot: line, bar, box, scatter, contour, etc.), legend, title, tick labels, and other annotations. Part of the reason for this is that in many cases the data needed to make a complete plot is spread across many objects. In pandas we have row labels, column labels, and possibly grouping information. This means that many kinds of fully-formed plots that would ordinarily require a lot of matplotlib code can be expressed in one or two concise statements. Therefore, pandas has an increasing number of high-level plotting methods for creating standard visualizations that take advantage of how data is organized in DataFrame objects.



As of this writing, the plotting functionality in pandas is undergoing quite a bit of work. As part of the 2012 Google Summer of Code program, a student is working full time to add features and to make the interface more consistent and usable. Thus, it's possible that this code may fall out-of-date faster than the other things in this book. The online pandas documentation will be the best resource in that event.

Line Plots

Series and DataFrame each have a `plot` method for making many different plot types. By default, they make line plots (see Figure 8-13):

```
In [55]: s = Series(np.random.randn(10).cumsum(), index=np.arange(0, 100, 10))

In [56]: s.plot()
```

The Series object's index is passed to matplotlib for plotting on the X axis, though this can be disabled by passing `use_index=False`. The X axis ticks and limits can be adjusted using the `xticks` and `xlim` options, and Y axis respectively using `yticks` and `ylim`. See

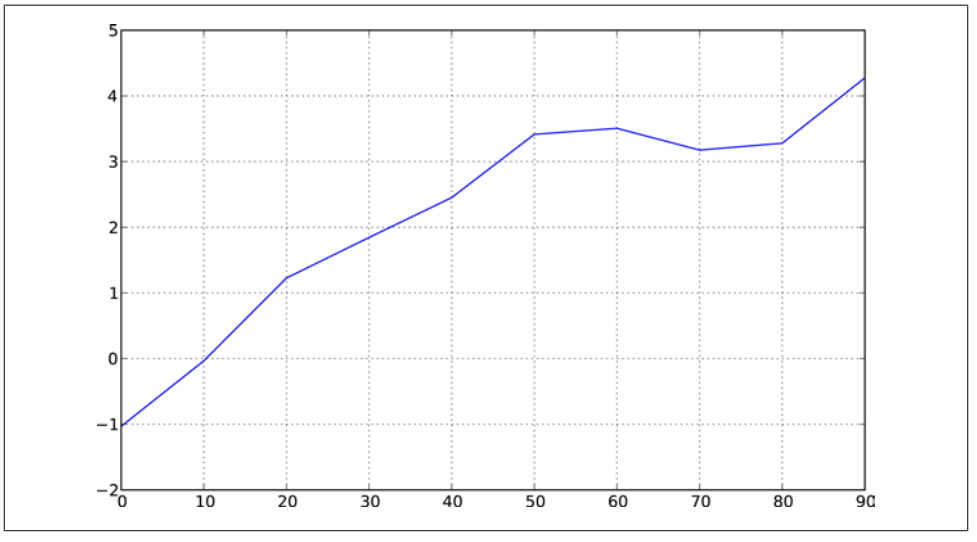


Figure 8-13. Simple Series plot example

Table 8-3 for a full listing of `plot` options. I'll comment on a few more of them throughout this section and leave the rest to you to explore.

Most of pandas's plotting methods accept an optional `ax` parameter, which can be a matplotlib subplot object. This gives you more flexible placement of subplots in a grid layout. There will be more on this in the later section on the matplotlib API.

DataFrame's `plot` method plots each of its columns as a different line on the same subplot, creating a legend automatically (see Figure 8-14):

```
In [57]: df = DataFrame(np.random.randn(10, 4).cumsum(0),
   ....:                columns=['A', 'B', 'C', 'D'],
   ....:                index=np.arange(0, 100, 10))

In [58]: df.plot()
```

Additional keyword arguments to `plot` are passed through to the respective matplotlib plotting function, so you can further customize these plots by learning more about the matplotlib API.

Table 8-3. Series.plot method arguments

Argument	Description
`label`	Label for plot legend
`ax`	matplotlib subplot object to plot on. If nothing passed, uses active matplotlib subplot
`style`	Style string, like `'ko--'`, to be passed to matplotlib.
`alpha`	The plot fill opacity (from 0 to 1)

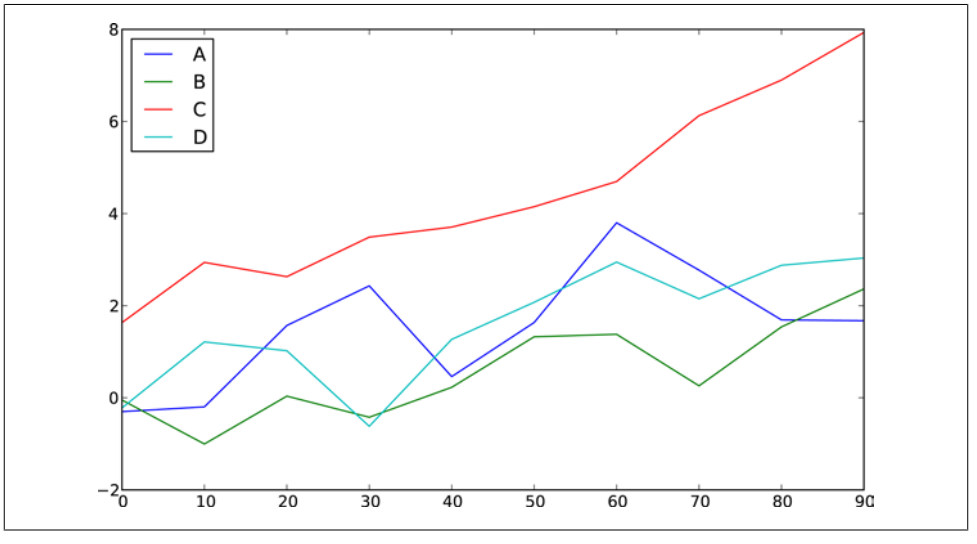


Figure 8-14. Simple DataFrame plot example

Argument	Description
`kind`	Can be `'line', 'bar', 'barh', 'kde'`
`logy`	Use logarithmic scaling on the Y axis
`use_index`	Use the object index for tick labels
`rot`	Rotation of tick labels (0 through 360)
`xticks`	Values to use for X axis ticks
`yticks`	Values to use for Y axis ticks
`xlim`	X axis limits (e.g. `[0, 10]`)
`ylim`	Y axis limits
`grid`	Display axis grid (on by default)

DataFrame has a number of options allowing some flexibility with how the columns are handled; for example, whether to plot them all on the same subplot or to create separate subplots. See Table 8-4 for more on these.

Table 8-4. DataFrame-specific plot arguments

Argument	Description
`subplots`	Plot each DataFrame column in a separate subplot
`sharex`	If `subplots=True`, share the same X axis, linking ticks and limits
`sharey`	If `subplots=True`, share the same Y axis
`figsize`	Size of figure to create as tuple

Argument	Description
`title`	Plot title as string
`legend`	Add a subplot legend (`True` by default)
`sort_columns`	Plot columns in alphabetical order; by default uses existing column order

For time series plotting, see Chapter 10.

Bar Plots

Making bar plots instead of line plots is a simple as passing `kind='bar'` (for vertical bars) or `kind='barh'` (for horizontal bars). In this case, the Series or DataFrame index will be used as the X (`bar`) or Y (`barh`) ticks (see Figure 8-15):

```
In [59]: fig, axes = plt.subplots(2, 1)

In [60]: data = Series(np.random.rand(16), index=list('abcdefghijklmnop'))

In [61]: data.plot(kind='bar', ax=axes[0], color='k', alpha=0.7)
Out[61]: <matplotlib.axes.AxesSubplot at 0x4ee7750>

In [62]: data.plot(kind='barh', ax=axes[1], color='k', alpha=0.7)
```

For more on the `plt.subplots` function and matplotlib axes and figures, see the later section in this chapter.

With a DataFrame, bar plots group the values in each row together in a group in bars, side by side, for each value. See Figure 8-16:

```
In [63]: df = DataFrame(np.random.rand(6, 4),
   ....:                index=['one', 'two', 'three', 'four', 'five', 'six'],
   ....:                columns=pd.Index(['A', 'B', 'C', 'D'], name='Genus'))

In [64]: df
Out[64]:
Genus         A         B         C         D
one    0.301686  0.156333  0.371943  0.270731
two    0.750589  0.525587  0.689429  0.358974
three  0.381504  0.667707  0.473772  0.632528
four   0.942408  0.180186  0.708284  0.641783
five   0.840278  0.909589  0.010041  0.653207
six    0.062854  0.589813  0.811318  0.060217

In [65]: df.plot(kind='bar')
```

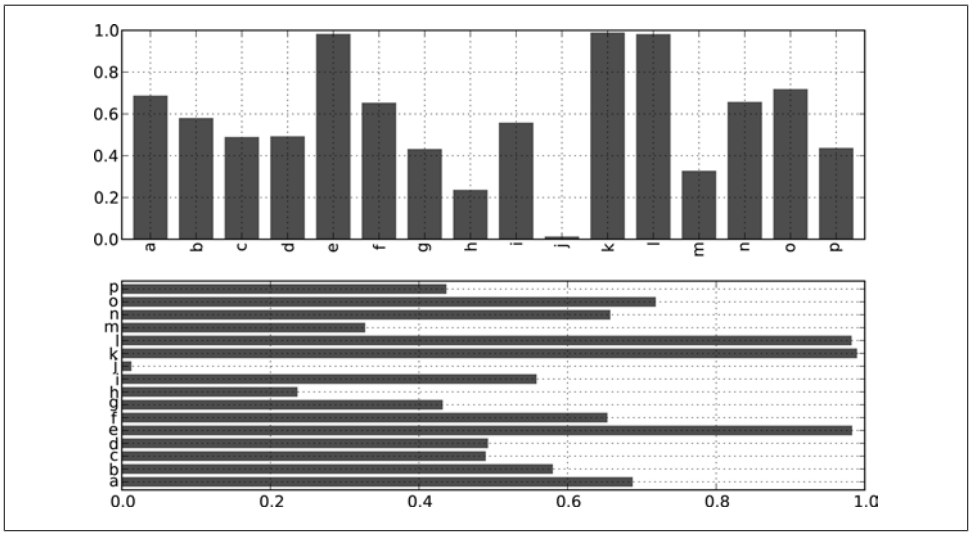


Figure 8-15. Horizonal and vertical bar plot example

Note that the name "Genus" on the DataFrame's columns is used to title the legend.

Stacked bar plots are created from a DataFrame by passing `stacked=True`, resulting in the value in each row being stacked together (see Figure 8-17):

```
In [67]: df.plot(kind='barh', stacked=True, alpha=0.5)
```

A useful recipe for bar plots (as seen in an earlier chapter) is to visualize a Series's value frequency using `value_counts`: `s.value_counts().plot(kind='bar')`

Returning to the tipping data set used earlier in the book, suppose we wanted to make a stacked bar plot showing the percentage of data points for each party size on each day. I load the data using `read_csv` and make a cross-tabulation by day and party size:

```
In [68]: tips = pd.read_csv('ch08/tips.csv')

In [69]: party_counts = pd.crosstab(tips.day, tips.size)

In [70]: party_counts
Out[70]:
size  1   2   3   4  5  6
day
Fri   1  16   1   1  0  0
Sat   2  53  18  13  1  0
Sun   0  39  15  18  3  1
Thur  1  48   4   5  1  3
```

```
# Not many 1- and 6-person parties
In [71]: party_counts = party_counts.ix[:, 2:5]
```

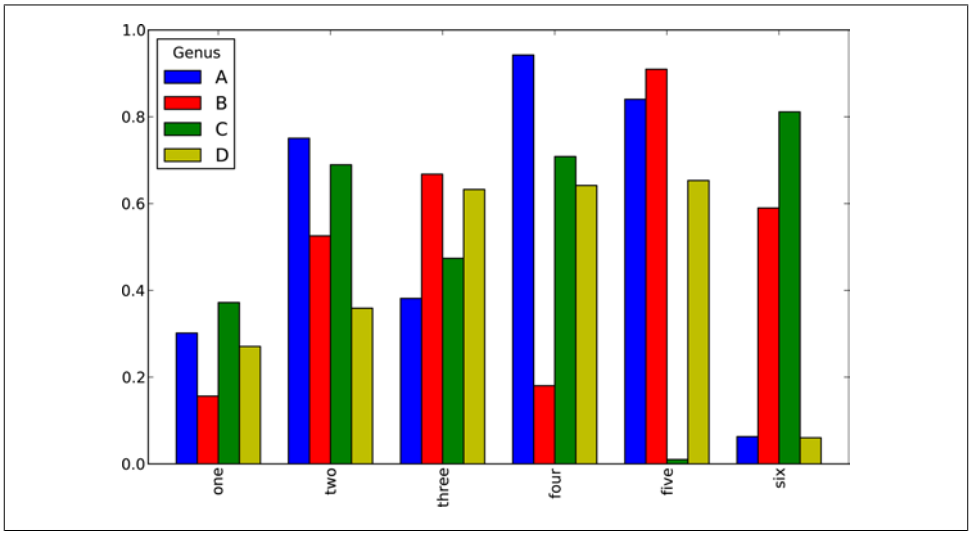


Figure 8-16. DataFrame bar plot example

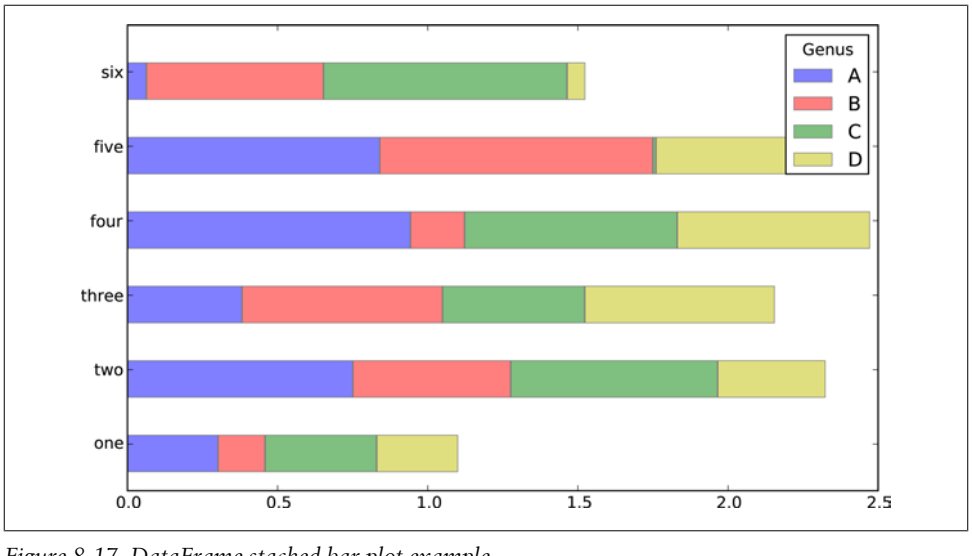


Figure 8-17. DataFrame stacked bar plot example

Then, normalize so that each row sums to 1 (I have to cast to float to avoid integer division issues on Python 2.7) and make the plot (see Figure 8-18):

```
# Normalize to sum to 1
In [72]: party_pcts = party_counts.div(party_counts.sum(1).astype(float), axis=0)
```

```
In [73]: party_pcts
Out[73]:
size         2         3         4         5
day
Fri   0.888889  0.055556  0.055556  0.000000
Sat   0.623529  0.211765  0.152941  0.011765
Sun   0.520000  0.200000  0.240000  0.040000
Thur  0.827586  0.068966  0.086207  0.017241

In [74]: party_pcts.plot(kind='bar', stacked=True)
```

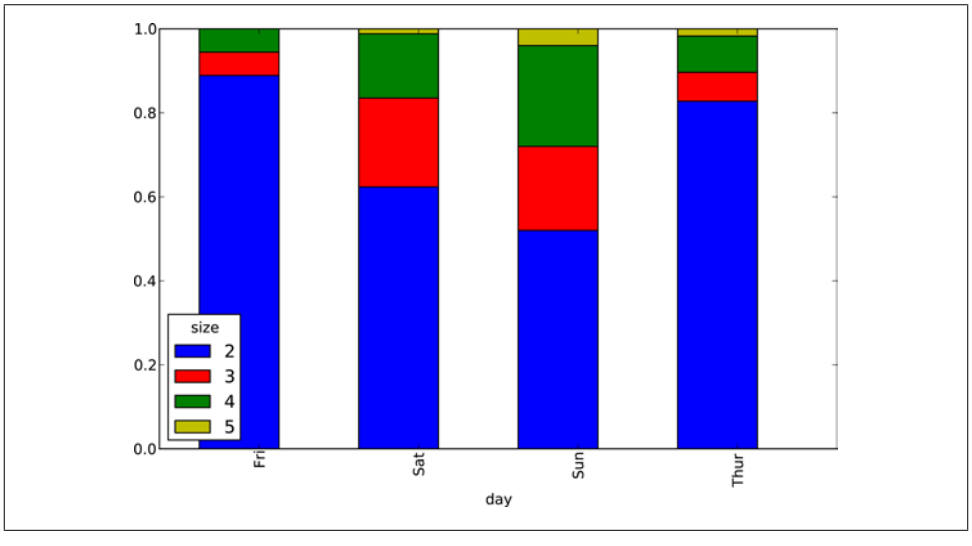


Figure 8-18. Fraction of parties by size on each day

So you can see that party sizes appear to increase on the weekend in this data set.

Histograms and Density Plots

A histogram, with which you may be well-acquainted, is a kind of bar plot that gives a discretized display of value frequency. The data points are split into discrete, evenly spaced bins, and the number of data points in each bin is plotted. Using the tipping data from before, we can make a histogram of tip percentages of the total bill using the `hist` method on the Series (see Figure 8-19):

```
In [76]: tips['tip_pct'] = tips['tip'] / tips['total_bill']

In [77]: tips['tip_pct'].hist(bins=50)
```

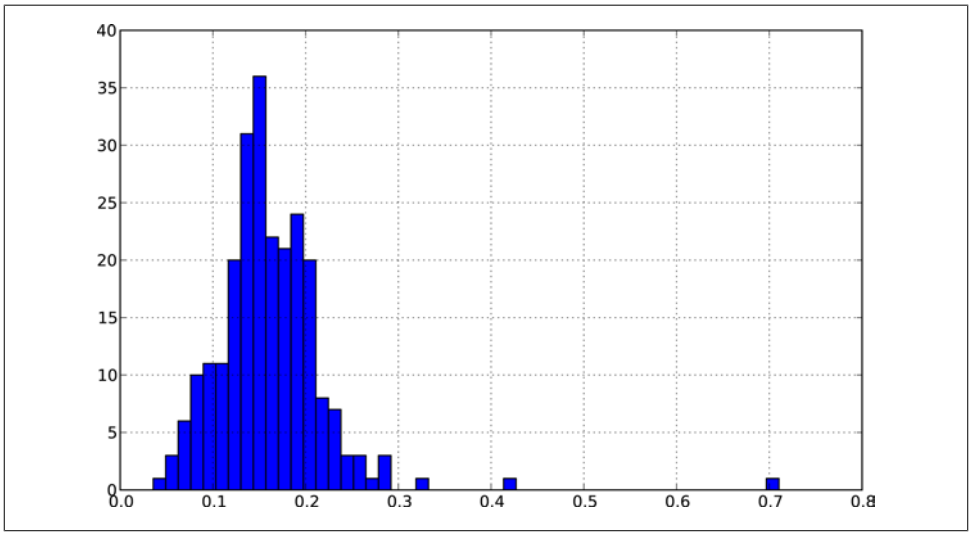


Figure 8-19. Histogram of tip percentages

A related plot type is a *density plot*, which is formed by computing an estimate of a continuous probability distribution that might have generated the observed data. A usual procedure is to approximate this distribution as a mixture of `kernels`, that is, simpler distributions like the normal (Gaussian) distribution. Thus, density plots are also known as KDE (kernel density estimate) plots. Using `plot` with `kind='kde'` makes a density plot using the standard mixture-of-normals KDE (see Figure 8-20):

```
In [79]: tips['tip_pct'].plot(kind='kde')
```

These two plot types are often plotted together; the histogram in normalized form (to give a binned density) with a kernel density estimate plotted on top. As an example, consider a bimodal distribution consisting of draws from two different standard normal distributions (see Figure 8-21):

```
In [81]: comp1 = np.random.normal(0, 1, size=200)  # N(0, 1)

In [82]: comp2 = np.random.normal(10, 2, size=200)  # N(10, 4)

In [83]: values = Series(np.concatenate([comp1, comp2]))

In [84]: values.hist(bins=100, alpha=0.3, color='k', normed=True)
Out[84]: <matplotlib.axes.AxesSubplot at 0x5cd2350>

In [85]: values.plot(kind='kde', style='k--')
```

Scatter Plots

Scatter plots are a useful way of examining the relationship between two one-dimensional data series. matplotlib has a `scatter` plotting method that is the workhorse of

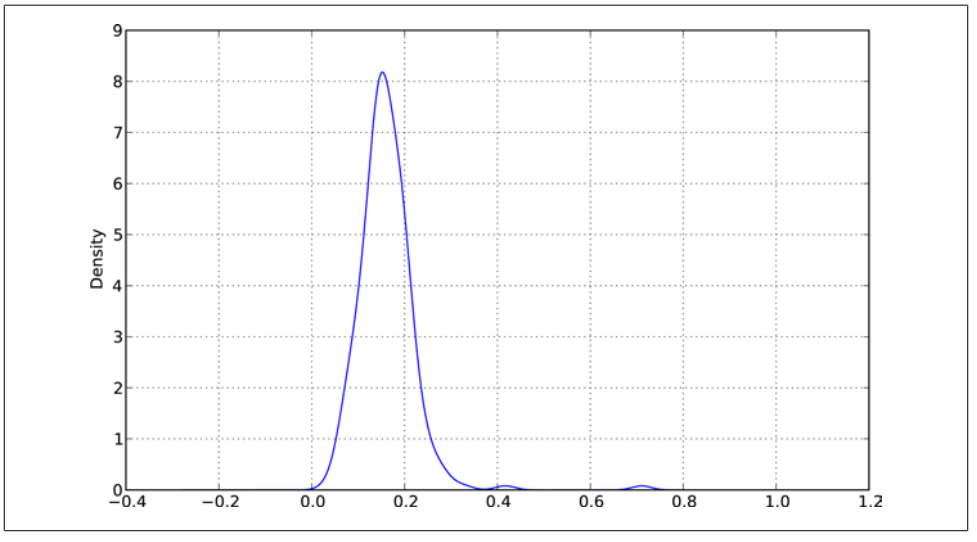


Figure 8-20. Density plot of tip percentages

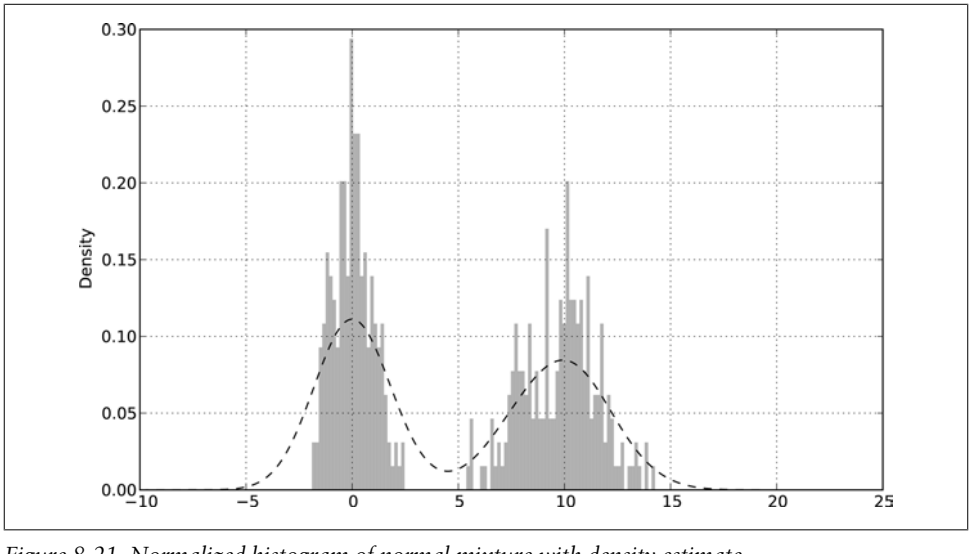


Figure 8-21. Normalized histogram of normal mixture with density estimate

making these kinds of plots. To give an example, I load the `macrodata` dataset from the statsmodels project, select a few variables, then compute log differences:

```
In [86]: macro = pd.read_csv('ch08/macrodata.csv')

In [87]: data = macro[['cpi', 'm1', 'tbilrate', 'unemp']]

In [88]: trans_data = np.log(data).diff().dropna()
```

```
In [89]: trans_data[-5:]
Out[89]:
          cpi        m1  tbilrate     unemp
198 -0.007904  0.045361 -0.396881  0.105361
199 -0.021979  0.066753 -2.277267  0.139762
200  0.002340  0.010286  0.606136  0.160343
201  0.008419  0.037461 -0.200671  0.127339
202  0.008894  0.012202 -0.405465  0.042560
```

It's easy to plot a simple scatter plot using `plt.scatter` (see Figure 8-22):

```
In [91]: plt.scatter(trans_data['m1'], trans_data['unemp'])
Out[91]: <matplotlib.collections.PathCollection at 0x43c31d0>

In [92]: plt.title('Changes in log %s vs. log %s' % ('m1', 'unemp'))
```

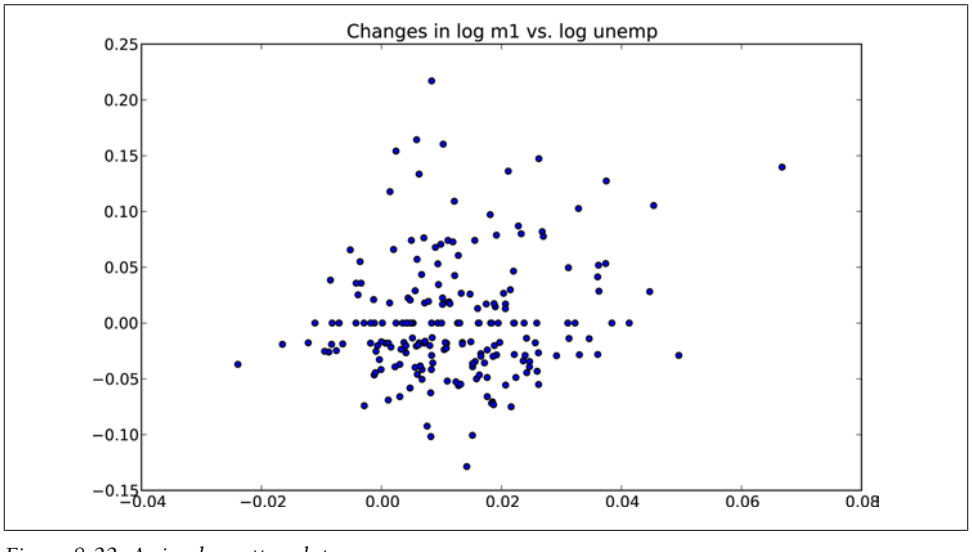


Figure 8-22. A simple scatter plot

In exploratory data analysis it's helpful to be able to look at all the scatter plots among a group of variables; this is known as a *pairs* plot or *scatter plot matrix*. Making such a plot from scratch is a bit of work, so pandas has a `scatter_matrix` function for creating one from a DataFrame. It also supports placing histograms or density plots of each variable along the diagonal. See Figure 8-23 for the resulting plot:

```
In [93]: scatter_matrix(trans_data, diagonal='kde', color='k', alpha=0.3)
```

Plotting Maps: Visualizing Haiti Earthquake Crisis Data

Ushahidi is a non-profit software company that enables crowdsourcing of information related to natural disasters and geopolitical events via text message. Many of these data sets are then published on their website for analysis and visualization. I downloaded

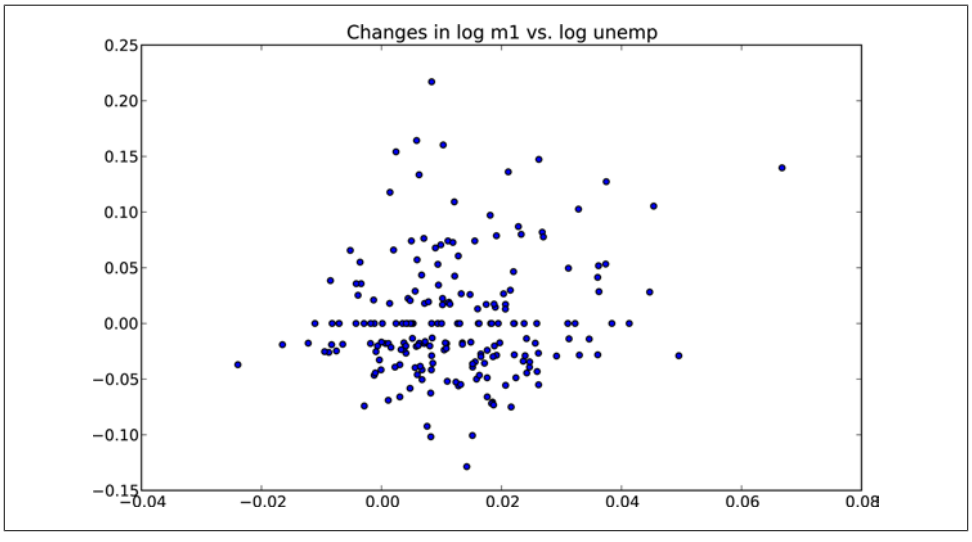


Figure 8-23. Scatter plot matrix of statsmodels macro data

the data collected during the 2010 Haiti earthquake crisis and aftermath, and I'll show you how I prepared the data for analysis and visualization using pandas and other tools we have looked at thus far. After downloading the CSV file from the above link, we can load it into a DataFrame using `read_csv`:

```
In [94]: data = pd.read_csv('ch08/Haiti.csv')

In [95]: data
Out[95]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 3593 entries, 0 to 3592
Data columns:
Serial            3593  non-null values
INCIDENT TITLE    3593  non-null values
INCIDENT DATE     3593  non-null values
LOCATION          3593  non-null values
DESCRIPTION       3593  non-null values
CATEGORY          3587  non-null values
LATITUDE          3593  non-null values
LONGITUDE         3593  non-null values
APPROVED          3593  non-null values
VERIFIED          3593  non-null values
dtypes: float64(2), int64(1), object(7)
```

It's easy now to tinker with this data set to see what kinds of things we might want to do with it. Each row represents a report sent from someone's mobile phone indicating an emergency or some other problem. Each has an associated timestamp and a location as latitude and longitude:

```
In [96]: data[['INCIDENT DATE', 'LATITUDE', 'LONGITUDE']][:10]
Out[96]:
      INCIDENT DATE   LATITUDE   LONGITUDE
```

```
0  05/07/2010 17:26  18.233333  -72.533333
1  28/06/2010 23:06  50.226029    5.729886
2  24/06/2010 16:21  22.278381  114.174287
3  20/06/2010 21:59  44.407062    8.933989
4  18/05/2010 16:26  18.571084  -72.334671
5  26/04/2010 13:14  18.593707  -72.310079
6  26/04/2010 14:19  18.482800  -73.638800
7  26/04/2010 14:27  18.415000  -73.195000
8  15/03/2010 10:58  18.517443  -72.236841
9  15/03/2010 11:00  18.547790  -72.410010
```

The `CATEGORY` field contains a comma-separated list of codes indicating the type of message:

```
In [97]: data['CATEGORY'][:6]
Out[97]:
0          1. Urgences | Emergency, 3. Public Health,
1    1. Urgences | Emergency, 2. Urgences logistiques
2    2. Urgences logistiques | Vital Lines, 8. Autre |
3                             1. Urgences | Emergency,
4                             1. Urgences | Emergency,
5                       5e. Communication lines down,
Name: CATEGORY
```

If you notice above in the data summary, some of the categories are missing, so we might want to drop these data points. Additionally, calling `describe` shows that there are some aberrant locations:

```
In [98]: data.describe()
Out[98]:
            Serial     LATITUDE    LONGITUDE
count  3593.000000  3593.000000  3593.000000
mean   2080.277484    18.611495   -72.322680
std    1171.100360     0.738572     3.650776
min       4.000000    18.041313   -74.452757
25%    1074.000000    18.524070   -72.417500
50%    2163.000000    18.539269   -72.335000
75%    3088.000000    18.561820   -72.293570
max    4052.000000    50.226029   114.174287
```

Cleaning the bad locations and removing the missing categories is now fairly simple:

```
In [99]: data = data[(data.LATITUDE > 18) & (data.LATITUDE < 20) &
   ....:             (data.LONGITUDE > -75) & (data.LONGITUDE < -70)
   ....:             & data.CATEGORY.notnull()]
```

Now we might want to do some analysis or visualization of this data by category, but each category field may have multiple categories. Additionally, each category is given as a code plus an English and possibly also a French code name. Thus, a little bit of wrangling is required to get the data into a more agreeable form. First, I wrote these two functions to get a list of all the categories and to split each category into a code and an English name:

```
def to_cat_list(catstr):
    stripped = (x.strip() for x in catstr.split(','))
```

```
    return [x for x in stripped if x]

def get_all_categories(cat_series):
    cat_sets = (set(to_cat_list(x)) for x in cat_series)
    return sorted(set.union(*cat_sets))

def get_english(cat):
    code, names = cat.split('.')
    if '|' in names:
        names = names.split(' | ')[1]
    return code, names.strip()
```

You can test out that the `get_english` function does what you expect:

```
In [101]: get_english('2. Urgences logistiques | Vital Lines')
Out[101]: ('2', 'Vital Lines')
```

Now, I make a `dict` mapping code to name because we'll use the codes for analysis. We'll use this later when adorning plots (note the use of a generator expression in lieu of a list comprehension):

```
In [102]: all_cats = get_all_categories(data.CATEGORY)

# Generator expression
In [103]: english_mapping = dict(get_english(x) for x in all_cats)

In [104]: english_mapping['2a']
Out[104]: 'Food Shortage'

In [105]: english_mapping['6c']
Out[105]: 'Earthquake and aftershocks'
```

There are many ways to go about augmenting the data set to be able to easily select records by category. One way is to add indicator (or dummy) columns, one for each category. To do that, first extract the unique category codes and construct a DataFrame of zeros having those as its columns and the same index as `data`:

```
def get_code(seq):
    return [x.split('.')[0] for x in seq if x]

all_codes = get_code(all_cats)
code_index = pd.Index(np.unique(all_codes))
dummy_frame = DataFrame(np.zeros((len(data), len(code_index))),
                        index=data.index, columns=code_index)
```

If all goes well, `dummy_frame` should look something like this:

```
In [107]: dummy_frame.ix[:, :6]
Out[107]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 3569 entries, 0 to 3592
Data columns:
1     3569  non-null values
1a    3569  non-null values
1b    3569  non-null values
1c    3569  non-null values
```

```
1d    3569  non-null values
2     3569  non-null values
dtypes: float64(6)
```

As you recall, the trick is then to set the appropriate entries of each row to 1, lastly joining this with `data`:

```
for row, cat in zip(data.index, data.CATEGORY):
    codes = get_code(to_cat_list(cat))
    dummy_frame.ix[row, codes] = 1

data = data.join(dummy_frame.add_prefix('category_'))
```

`data` finally now has new columns like:

```
In [109]: data.ix[:, 10:15]
Out[109]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 3569 entries, 0 to 3592
Data columns:
category_1     3569  non-null values
category_1a    3569  non-null values
category_1b    3569  non-null values
category_1c    3569  non-null values
category_1d    3569  non-null values
dtypes: float64(5)
```

Let's make some plots! As this is spatial data, we'd like to plot the data by category on a map of Haiti. The `basemap` toolkit (*http://matplotlib.github.com/basemap*), an add-on to matplotlib, enables plotting 2D data on maps in Python. `basemap` provides many different globe projections and a means for transforming projecting latitude and longitude coordinates on the globe onto a two-dimensional matplotlib plot. After some trial and error and using the above data as a guideline, I wrote this function which draws a simple black and white map of Haiti:

```
from mpl_toolkits.basemap import Basemap
import matplotlib.pyplot as plt

def basic_haiti_map(ax=None, lllat=17.25, urlat=20.25,
                    lllon=-75, urlon=-71):
    # create polar stereographic Basemap instance.
    m = Basemap(ax=ax, projection='stere',
                lon_0=(urlon + lllon) / 2,
                lat_0=(urlat + lllat) / 2,
                llcrnrlat=lllat, urcrnrlat=urlat,
                llcrnrlon=lllon, urcrnrlon=urlon,
                resolution='f')
    # draw coastlines, state and country boundaries, edge of map.
    m.drawcoastlines()
    m.drawstates()
    m.drawcountries()
    return m
```

The idea, now, is that the returned `Basemap` object, knows how to transform coordinates onto the canvas. I wrote the following code to plot the data observations for a number

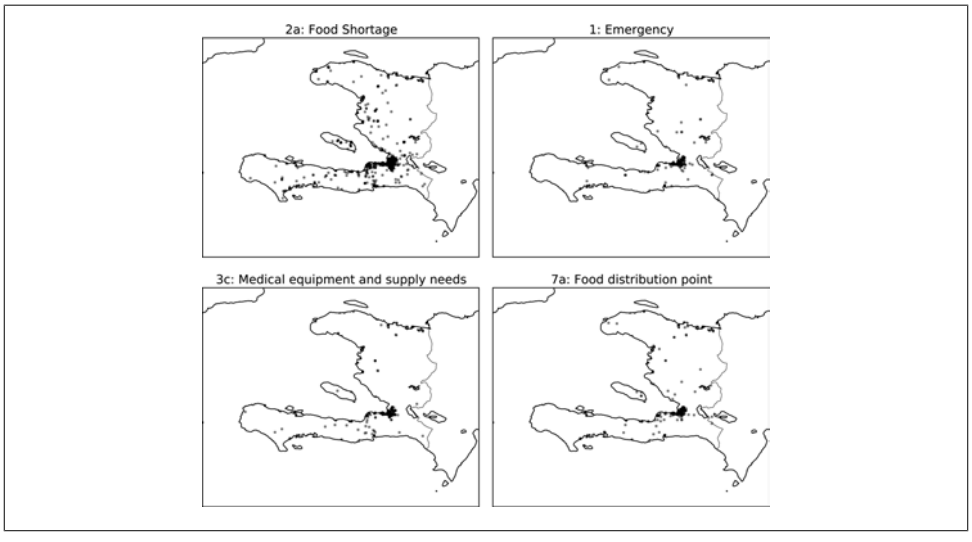


Figure 8-24. Haiti crisis data for 4 categories

of report categories. For each category, I filter down the data set to the coordinates labeled by that category, plot a `Basemap` on the appropriate subplot, transform the coordinates, then plot the points using the `Basemap`'s `plot` method:

```
fig, axes = plt.subplots(nrows=2, ncols=2, figsize=(12, 10))
fig.subplots_adjust(hspace=0.05, wspace=0.05)

to_plot = ['2a', '1', '3c', '7a']

lllat=17.25; urlat=20.25; lllon=-75; urlon=-71

for code, ax in zip(to_plot, axes.flat):
    m = basic_haiti_map(ax, lllat=lllat, urlat=urlat,
                        lllon=lllon, urlon=urlon)

    cat_data = data[data['category_%s' % code] == 1]

    # compute map proj coordinates.
    x, y = m(cat_data.LONGITUDE, cat_data.LATITUDE)

    m.plot(x, y, 'k.', alpha=0.5)
    ax.set_title('%s: %s' % (code, english_mapping[code]))
```

The resulting figure can be seen in Figure 8-24.

It seems from the plot that most of the data is concentrated around the most populous city, Port-au-Prince. `basemap` allows you to overlap additional map data which comes from what are called *shapefiles*. I first downloaded a shapefile with roads in Port-au-Prince (see *http://cegrp.cga.harvard.edu/haiti/?q=resources_data*). The `Basemap` object conveniently has a `readshapefile` method so that, after extracting the road data archive, I added just the following lines to my code:

Figure 8-25. Food shortage reports in Port-au-Prince during the Haiti earthquake crisis

```
shapefile_path = 'ch08/PortAuPrince_Roads/PortAuPrince_Roads'
m.readshapefile(shapefile_path, 'roads')
```

After a little more trial and error with the latitude and longitude boundaries, I was able to make Figure 8-25 for the "Food shortage" category.

Python Visualization Tool Ecosystem

As is common with open source, there are a plethora of options for creating graphics in Python (too many to list). In addition to open source, there are numerous commercial libraries with Python bindings.

In this chapter and throughout the book, I have been primarily concerned with matplotlib as it is the most widely used plotting tool in Python. While it's an important part of the scientific Python ecosystem, matplotlib has plenty of shortcomings when it comes to the creation and display of statistical graphics. MATLAB users will likely find matplotlib familiar, while R users (especially users of the excellent `ggplot2` and `trellis` packages) may be somewhat disappointed (at least as of this writing). It is possible to make beautiful plots for display on the web in matplotlib, but doing so often requires significant effort as the library is designed for the printed page. Aesthetics aside, it is sufficient for most needs. In pandas, I, along with the other developers, have sought to build a convenient user interface that makes it easier to make most kinds of plots commonplace in data analysis.

There are a number of other visualization tools in wide use. I list a few of them here and encourage you to explore the ecosystem.

Chaco

Chaco (*http://code.enthought.com/chaco/*), developed by Enthought, is a plotting toolkit suitable both for static plotting and interactive visualizations. It is especially well-suited for expressing complex visualizations with data interrelationships. Compared with matplotlib, Chaco has much better support for interacting with plot elements and rendering is very fast, making it a good choice for building interactive GUI applications.

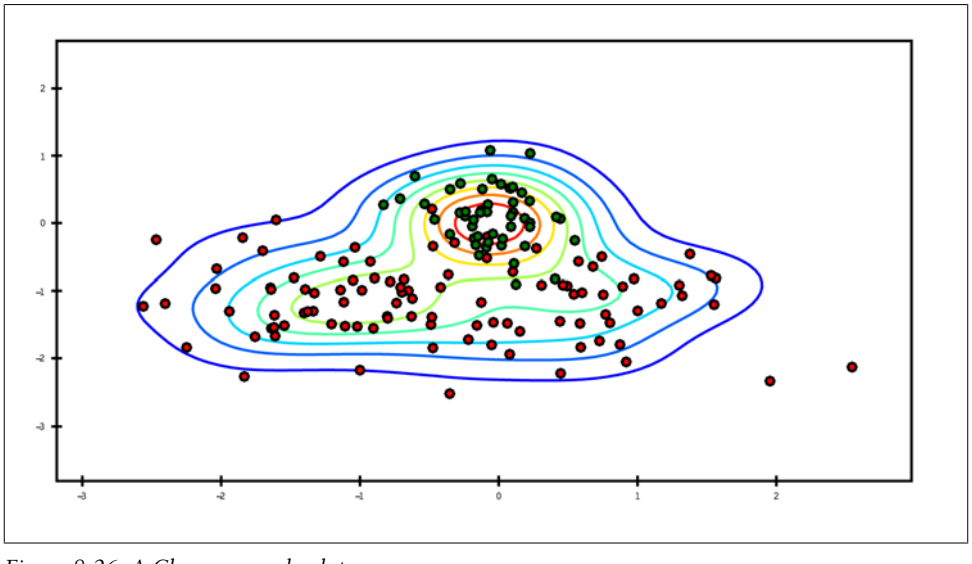


Figure 8-26. A Chaco example plot

mayavi

The mayavi project, developed by Prabhu Ramachandran, Gaël Varoquaux, and others, is a 3D graphics toolkit built on the open source C++ graphics library VTK. mayavi, like matplotlib, integrates with IPython so that it is easy to use interactively. The plots can be panned, rotated, and zoomed using the mouse and keyboard. I used mayavi to make one of the illustrations of broadcasting in Chapter 12. While I don't show any mayavi-using code here, there is plenty of documentation and examples available online. In many cases, I believe it is a good alternative to a technology like WebGL, though the graphics are harder to share in interactive form.

Other Packages

Of course, there are numerous other visualization libraries and applications available in Python: PyQwt, Veusz, gnuplot-py, biggles, and others. I have seen PyQwt put to good use in GUI applications built using the Qt application framework using PyQt. While many of these libraries continue to be under active development (some of them

are part of much larger applications), I have noted in the last few years a general trend toward web-based technologies and away from desktop graphics. I'll say a few more words about this in the next section.

The Future of Visualization Tools?

Visualizations built on web technologies (that is, JavaScript-based) appear to be the inevitable future. Doubtlessly you have used many different kinds of static or interactive visualizations built in Flash or JavaScript over the years. New toolkits (such as d3.js and its numerous off-shoot projects) for building such displays are appearing all the time. In contrast, development in non web-based visualization has slowed significantly in recent years. This holds true of Python as well as other data analysis and statistical computing environments like R.

The development challenge, then, will be in building tighter integration between data analysis and preparation tools, such as pandas, and the web browser. I am hopeful that this will become a fruitful point of collaboration between Python and non-Python users as well.

CHAPTER 9

Data Aggregation and Group Operations

Categorizing a data set and applying a function to each group, whether an aggregation or transformation, is often a critical component of a data analysis workflow. After loading, merging, and preparing a data set, a familiar task is to compute group statistics or possibly *pivot tables* for reporting or visualization purposes. pandas provides a flexible and high-performance `groupby` facility, enabling you to slice and dice, and summarize data sets in a natural way.

One reason for the popularity of relational databases and SQL (which stands for "structured query language") is the ease with which data can be joined, filtered, transformed, and aggregated. However, query languages like SQL are rather limited in the kinds of group operations that can be performed. As you will see, with the expressiveness and power of Python and pandas, we can perform much more complex grouped operations by utilizing any function that accepts a pandas object or NumPy array. In this chapter, you will learn how to:

- Split a pandas object into pieces using one or more keys (in the form of functions, arrays, or DataFrame column names)
- Computing group summary statistics, like count, mean, or standard deviation, or a user-defined function
- Apply a varying set of functions to each column of a DataFrame
- Apply within-group transformations or other manipulations, like normalization, linear regression, rank, or subset selection
- Compute pivot tables and cross-tabulations
- Perform quantile analysis and other data-derived group analyses

Aggregation of time series data, a special use case of `groupby`, is referred to as *resampling* in this book and will receive separate treatment in Chapter 10.

GroupBy Mechanics

Hadley Wickham, an author of many popular packages for the R programming language, coined the term *split-apply-combine* for talking about group operations, and I think that's a good description of the process. In the first stage of the process, data contained in a pandas object, whether a Series, DataFrame, or otherwise, is *split* into groups based on one or more *keys* that you provide. The splitting is performed on a particular axis of an object. For example, a DataFrame can be grouped on its rows (`axis=0`) or its columns (`axis=1`). Once this is done, a function is *applied* to each group, producing a new value. Finally, the results of all those function applications are *combined* into a result object. The form of the resulting object will usually depend on what's being done to the data. See Figure 9-1 for a mockup of a simple group aggregation.

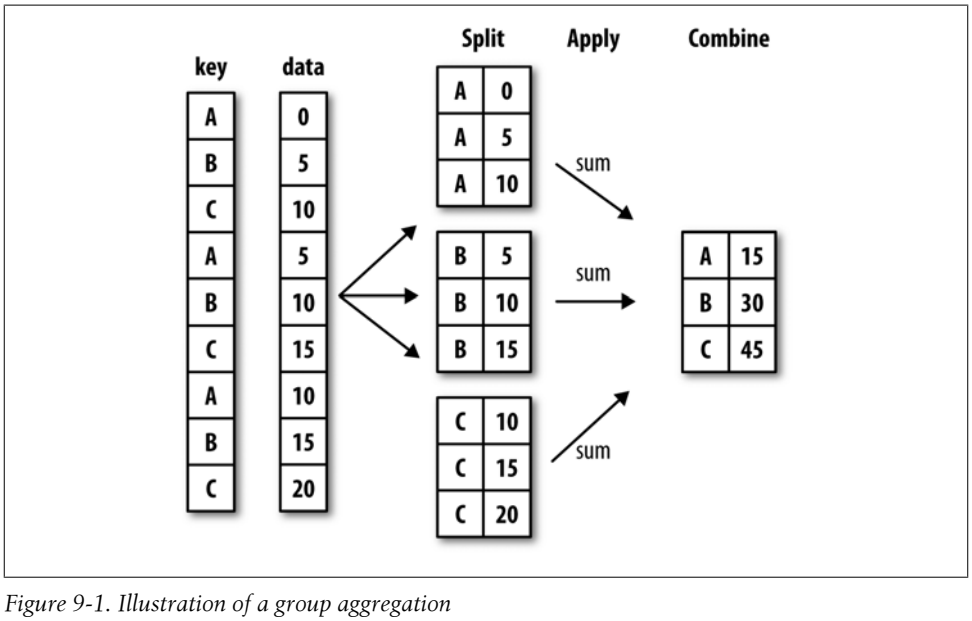


Figure 9-1. Illustration of a group aggregation

Each grouping key can take many forms, and the keys do not have to be all of the same type:

- A list or array of values that is the same length as the axis being grouped
- A value indicating a column name in a DataFrame

- A dict or Series giving a correspondence between the values on the axis being grouped and the group names
- A function to be invoked on the axis index or the individual labels in the index

Note that the latter three methods are all just shortcuts for producing an array of values to be used to split up the object. Don't worry if this all seems very abstract. Throughout this chapter, I will give many examples of all of these methods. To get started, here is a very simple small tabular dataset as a DataFrame:

```
In [13]: df = DataFrame({'key1' : ['a', 'a', 'b', 'b', 'a'],
   ....:                 'key2' : ['one', 'two', 'one', 'two', 'one'],
   ....:                 'data1' : np.random.randn(5),
   ....:                 'data2' : np.random.randn(5)})

In [14]: df
Out[14]:
      data1     data2 key1 key2
0 -0.204708  1.393406    a  one
1  0.478943  0.092908    a  two
2 -0.519439  0.281746    b  one
3 -0.555730  0.769023    b  two
4  1.965781  1.246435    a  one
```

Suppose you wanted to compute the mean of the `data1` column using the groups labels from `key1`. There are a number of ways to do this. One is to access `data1` and call `groupby` with the column (a Series) at `key1`:

```
In [15]: grouped = df['data1'].groupby(df['key1'])

In [16]: grouped
Out[16]: <pandas.core.groupby.SeriesGroupBy at 0x2d78b10>
```

This `grouped` variable is now a *GroupBy* object. It has not actually computed anything yet except for some intermediate data about the group key `df['key1']`. The idea is that this object has all of the information needed to then apply some operation to each of the groups. For example, to compute group means we can call the GroupBy's `mean` method:

```
In [17]: grouped.mean()
Out[17]:
key1
a       0.746672
b      -0.537585
```

Later, I'll explain more about what's going on when you call `.mean()`. The important thing here is that the data (a Series) has been aggregated according to the group key, producing a new Series that is now indexed by the unique values in the `key1` column. The result index has the name `'key1'` because the DataFrame column `df['key1']` did.

If instead we had passed multiple arrays as a list, we get something different:

```
In [18]: means = df['data1'].groupby([df['key1'], df['key2']]).mean()
```

```
In [19]: means
Out[19]:
key1  key2
a     one     0.880536
      two     0.478943
b     one    -0.519439
      two    -0.555730
```

In this case, we grouped the data using two keys, and the resulting Series now has a hierarchical index consisting of the unique pairs of keys observed:

```
In [20]: means.unstack()
Out[20]:
key2       one       two
key1
a     0.880536  0.478943
b    -0.519439 -0.555730
```

In these examples, the group keys are all Series, though they could be any arrays of the right length:

```
In [21]: states = np.array(['Ohio', 'California', 'California', 'Ohio', 'Ohio'])

In [22]: years = np.array([2005, 2005, 2006, 2005, 2006])

In [23]: df['data1'].groupby([states, years]).mean()
Out[23]:
California  2005    0.478943
            2006   -0.519439
Ohio        2005   -0.380219
            2006    1.965781
```

Frequently the grouping information to be found in the same DataFrame as the data you want to work on. In that case, you can pass column names (whether those are strings, numbers, or other Python objects) as the group keys:

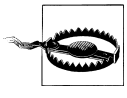
```
In [24]: df.groupby('key1').mean()
Out[24]:
         data1     data2
key1
a     0.746672  0.910916
b    -0.537585  0.525384

In [25]: df.groupby(['key1', 'key2']).mean()
Out[25]:
              data1     data2
key1 key2
a    one   0.880536  1.319920
     two   0.478943  0.092908
b    one  -0.519439  0.281746
     two  -0.555730  0.769023
```

You may have noticed in the first case `df.groupby('key1').mean()` that there is no `key2` column in the result. Because `df['key2']` is not numeric data, it is said to be a *nuisance column*, which is therefore excluded from the result. By default, all of the

numeric columns are aggregated, though it is possible to filter down to a subset as you'll see soon.

Regardless of the objective in using `groupby`, a generally useful GroupBy method is `size` which return a Series containing group sizes:

```
In [26]: df.groupby(['key1', 'key2']).size()
Out[26]:
key1  key2
a     one     2
      two     1
b     one     1
      two     1
```



As of this writing, any missing values in a group key will be excluded from the result. It's possible (and, in fact, quite likely), that by the time you are reading this there will be an option to include the `NA` group in the result.

Iterating Over Groups

The GroupBy object supports iteration, generating a sequence of 2-tuples containing the group name along with the chunk of data. Consider the following small example data set:

```
In [27]: for name, group in df.groupby('key1'):
   ....:     print name
   ....:     print group
   ....:
a
      data1     data2 key1 key2
0 -0.204708  1.393406    a  one
1  0.478943  0.092908    a  two
4  1.965781  1.246435    a  one
b
      data1     data2 key1 key2
2 -0.519439  0.281746    b  one
3 -0.555730  0.769023    b  two
```

In the case of multiple keys, the first element in the tuple will be a tuple of key values:

```
In [28]: for (k1, k2), group in df.groupby(['key1', 'key2']):
   ....:     print k1, k2
   ....:     print group
   ....:
a one
      data1     data2 key1 key2
0 -0.204708  1.393406    a  one
4  1.965781  1.246435    a  one
a two
      data1     data2 key1 key2
1  0.478943  0.092908    a  two
b one
      data1     data2 key1 key2
```

```
2 -0.519439  0.281746    b  one
b two
     data1     data2 key1 key2
3 -0.55573  0.769023    b  two
```

Of course, you can choose to do whatever you want with the pieces of data. A recipe you may find useful is computing a dict of the data pieces as a one-liner:

```
In [29]: pieces = dict(list(df.groupby('key1')))

In [30]: pieces['b']
Out[30]:
      data1     data2 key1 key2
2 -0.519439  0.281746    b  one
3 -0.555730  0.769023    b  two
```

By default `groupby` groups on `axis=0`, but you can group on any of the other axes. For example, we could group the columns of our example `df` here by `dtype` like so:

```
In [31]: df.dtypes
Out[31]:
data1    float64
data2    float64
key1      object
key2      object

In [32]: grouped = df.groupby(df.dtypes, axis=1)

In [33]: dict(list(grouped))
Out[33]:
{dtype('float64'):       data1     data2
0 -0.204708  1.393406
1  0.478943  0.092908
2 -0.519439  0.281746
3 -0.555730  0.769023
4  1.965781  1.246435,
 dtype('object'):   key1 key2
0    a  one
1    a  two
2    b  one
3    b  two
4    a  one}
```

Selecting a Column or Subset of Columns

Indexing a GroupBy object created from a DataFrame with a column name or array of column names has the effect of *selecting those columns* for aggregation. This means that:

```
df.groupby('key1')['data1']
df.groupby('key1')[['data2']]
```

are syntactic sugar for:

```
df['data1'].groupby(df['key1'])
df[['data2']].groupby(df['key1'])
```

Especially for large data sets, it may be desirable to aggregate only a few columns. For example, in the above data set, to compute means for just the `data2` column and get the result as a DataFrame, we could write:

```
In [34]: df.groupby(['key1', 'key2'])[['data2']].mean()
Out[34]:
              data2
key1 key2
a    one   1.319920
     two   0.092908
b    one   0.281746
     two   0.769023
```

The object returned by this indexing operation is a grouped DataFrame if a list or array is passed and a grouped Series is just a single column name that is passed as a scalar:

```
In [35]: s_grouped = df.groupby(['key1', 'key2'])['data2']

In [36]: s_grouped
Out[36]: <pandas.core.groupby.SeriesGroupBy at 0x2e215d0>

In [37]: s_grouped.mean()
Out[37]:
key1  key2
a     one     1.319920
      two     0.092908
b     one     0.281746
      two     0.769023
Name: data2
```

Grouping with Dicts and Series

Grouping information may exist in a form other than an array. Let's consider another example DataFrame:

```
In [38]: people = DataFrame(np.random.randn(5, 5),
   ....:                    columns=['a', 'b', 'c', 'd', 'e'],
   ....:                    index=['Joe', 'Steve', 'Wes', 'Jim', 'Travis'])

In [39]: people.ix[2:3, ['b', 'c']] = np.nan # Add a few NA values

In [40]: people
Out[40]:
               a         b         c         d         e
Joe     1.007189 -1.296221  0.274992  0.228913  1.352917
Steve   0.886429 -2.001637 -0.371843  1.669025 -0.438570
Wes    -0.539741       NaN       NaN -1.021228 -0.577087
Jim     0.124121  0.302614  0.523772  0.000940  1.343810
Travis -0.713544 -0.831154 -2.370232 -1.860761 -0.860757
```

Now, suppose I have a group correspondence for the columns and want to sum together the columns by group:

```
In [41]: mapping = {'a': 'red', 'b': 'red', 'c': 'blue',
   ....:            'd': 'blue', 'e': 'red', 'f' : 'orange'}
```

Now, you could easily construct an array from this dict to pass to `groupby`, but instead we can just pass the dict:

```
In [42]: by_column = people.groupby(mapping, axis=1)

In [43]: by_column.sum()
Out[43]:
          blue       red
Joe     0.503905  1.063885
Steve   1.297183 -1.553778
Wes    -1.021228 -1.116829
Jim     0.524712  1.770545
Travis -4.230992 -2.405455
```

The same functionality holds for Series, which can be viewed as a fixed size mapping. When I used Series as group keys in the above examples, pandas does, in fact, inspect each Series to ensure that its index is aligned with the axis it's grouping:

```
In [44]: map_series = Series(mapping)

In [45]: map_series
Out[45]:
a       red
b       red
c      blue
d      blue
e       red
f    orange

In [46]: people.groupby(map_series, axis=1).count()
Out[46]:
        blue  red
Joe        2    3
Steve      2    3
Wes        1    2
Jim        2    3
Travis     2    3
```

Grouping with Functions

Using Python functions in what can be fairly creative ways is a more abstract way of defining a group mapping compared with a dict or Series. Any function passed as a group key will be called once per index value, with the return values being used as the group names. More concretely, consider the example DataFrame from the previous section, which has people's first names as index values. Suppose you wanted to group by the length of the names; you could compute an array of string lengths, but instead you can just pass the `len` function:

```
In [47]: people.groupby(len).sum()
Out[47]:
          a         b         c         d         e
3  0.591569 -0.993608  0.798764 -0.791374  2.119639
```

```
5  0.886429 -2.001637 -0.371843  1.669025 -0.438570
6 -0.713544 -0.831154 -2.370232 -1.860761 -0.860757
```

Mixing functions with arrays, dicts, or Series is not a problem as everything gets converted to arrays internally:

```
In [48]: key_list = ['one', 'one', 'one', 'two', 'two']

In [49]: people.groupby([len, key_list]).min()
Out[49]:
              a         b         c         d         e
3 one -0.539741 -1.296221  0.274992 -1.021228 -0.577087
  two  0.124121  0.302614  0.523772  0.000940  1.343810
5 one  0.886429 -2.001637 -0.371843  1.669025 -0.438570
6 two -0.713544 -0.831154 -2.370232 -1.860761 -0.860757
```

Grouping by Index Levels

A final convenience for hierarchically-indexed data sets is the ability to aggregate using one of the levels of an axis index. To do this, pass the level number or name using the `level` keyword:

```
In [50]: columns = pd.MultiIndex.from_arrays([['US', 'US', 'US', 'JP', 'JP'],
   ....:                                      [1, 3, 5, 1, 3]], names=['cty', 'tenor'])

In [51]: hier_df = DataFrame(np.random.randn(4, 5), columns=columns)

In [52]: hier_df
Out[52]:
cty          US                            JP
tenor         1         3         5         1         3
0      0.560145 -1.265934  0.119827 -1.063512  0.332883
1     -2.359419 -0.199543 -1.541996 -0.970736 -1.307030
2      0.286350  0.377984 -0.753887  0.331286  1.349742
3      0.069877  0.246674 -0.011862  1.004812  1.327195

In [53]: hier_df.groupby(level='cty', axis=1).count()
Out[53]:
cty  JP  US
0     2   3
1     2   3
2     2   3
3     2   3
```

Data Aggregation

By aggregation, I am generally referring to any data transformation that produces scalar values from arrays. In the examples above I have used several of them, such as `mean`, `count`, `min` and `sum`. You may wonder what is going on when you invoke `mean()` on a GroupBy object. Many common aggregations, such as those found in Table 9-1, have optimized implementations that compute the statistics on the dataset *in place*. However, you are not limited to only this set of methods. You can use aggregations of your

own devising and additionally call any method that is also defined on the grouped object. For example, as you recall `quantile` computes sample quantiles of a Series or a DataFrame's columns [1]:

```
In [54]: df
Out[54]:
      data1     data2 key1 key2
0 -0.204708  1.393406    a  one
1  0.478943  0.092908    a  two
2 -0.519439  0.281746    b  one
3 -0.555730  0.769023    b  two
4  1.965781  1.246435    a  one

In [55]: grouped = df.groupby('key1')

In [56]: grouped['data1'].quantile(0.9)
Out[56]:
key1
a       1.668413
b      -0.523068
```

While `quantile` is not explicitly implemented for GroupBy, it is a Series method and thus available for use. Internally, GroupBy efficiently slices up the Series, calls `piece.quantile(0.9)` for each piece, then assembles those results together into the result object.

To use your own aggregation functions, pass any function that aggregates an array to the `aggregate` or `agg` method:

```
In [57]: def peak_to_peak(arr):
   ....:     return arr.max() - arr.min()

In [58]: grouped.agg(peak_to_peak)
Out[58]:
         data1     data2
key1
a     2.170488  1.300498
b     0.036292  0.487276
```

You'll notice that some methods like `describe` also work, even though they are not aggregations, strictly speaking:

```
In [59]: grouped.describe()
Out[59]:
               data1     data2
key1
a    count  3.000000  3.000000
     mean   0.746672  0.910916
     std    1.109736  0.712217
     min   -0.204708  0.092908
     25%    0.137118  0.669671
     50%    0.478943  1.246435
```

1. Note that `quantile` performs linear interpolation if there is no value at exactly the passed percentile.

```
        75%    1.222362  1.319920
        max    1.965781  1.393406
b       count  2.000000  2.000000
        mean  -0.537585  0.525384
        std    0.025662  0.344556
        min   -0.555730  0.281746
        25%   -0.546657  0.403565
        50%   -0.537585  0.525384
        75%   -0.528512  0.647203
        max   -0.519439  0.769023
```

I will explain in more detail what has happened here in the next major section on group-wise operations and transformations.

You may notice that custom aggregation functions are much slower than the optimized functions found in Table 9-1. This is because there is significant overhead (function calls, data rearrangement) in constructing the intermediate group data chunks.

Table 9-1. Optimized groupby methods

Function name	Description
`count`	Number of non-NA values in the group
`sum`	Sum of non-NA values
`mean`	Mean of non-NA values
`median`	Arithmetic median of non-NA values
`std, var`	Unbiased (n - 1 denominator) standard deviation and variance
`min, max`	Minimum and maximum of non-NA values
`prod`	Product of non-NA values
`first, last`	First and last non-NA values

To illustrate some more advanced aggregation features, I'll use a less trivial dataset, a dataset on restaurant tipping. I obtained it from the R `reshape2` package; it was originally found in Bryant & Smith's 1995 text on business statistics (and found in the book's GitHub repository). After loading it with `read_csv`, I add a tipping percentage column `tip_pct`.

```
In [60]: tips = pd.read_csv('ch08/tips.csv')

# Add tip percentage of total bill
In [61]: tips['tip_pct'] = tips['tip'] / tips['total_bill']

In [62]: tips[:6]
Out[62]:
   total_bill   tip     sex smoker  day    time  size   tip_pct
0       16.99  1.01  Female     No  Sun  Dinner     2  0.059447
1       10.34  1.66    Male     No  Sun  Dinner     3  0.160542
```

```
2       21.01  3.50    Male     No  Sun  Dinner     3  0.166587
3       23.68  3.31    Male     No  Sun  Dinner     2  0.139780
4       24.59  3.61  Female     No  Sun  Dinner     4  0.146808
5       25.29  4.71    Male     No  Sun  Dinner     4  0.186240
```

Column-wise and Multiple Function Application

As you've seen above, aggregating a Series or all of the columns of a DataFrame is a matter of using `aggregate` with the desired function or calling a method like `mean` or `std`. However, you may want to aggregate using a different function depending on the column or multiple functions at once. Fortunately, this is straightforward to do, which I'll illustrate through a number of examples. First, I'll group the `tips` by `sex` and `smoker`:

```
In [63]: grouped = tips.groupby(['sex', 'smoker'])
```

Note that for descriptive statistics like those in Table 9-1, you can pass the name of the function as a string:

```
In [64]: grouped_pct = grouped['tip_pct']

In [65]: grouped_pct.agg('mean')
Out[65]:
sex     smoker
Female  No        0.156921
        Yes       0.182150
Male    No        0.160669
        Yes       0.152771
Name: tip_pct
```

If you pass a list of functions or function names instead, you get back a DataFrame with column names taken from the functions:

```
In [66]: grouped_pct.agg(['mean', 'std', peak_to_peak])
Out[66]:
                   mean       std  peak_to_peak
sex    smoker
Female No      0.156921  0.036421      0.195876
       Yes     0.182150  0.071595      0.360233
Male   No      0.160669  0.041849      0.220186
       Yes     0.152771  0.090588      0.674707
```

You don't need to accept the names that GroupBy gives to the columns; notably `lambda` functions have the name `'<lambda>'` which make them hard to identify (you can see for yourself by looking at a function's `__name__` attribute). As such, if you pass a list of `(name, function)` tuples, the first element of each tuple will be used as the DataFrame column names (you can think of a list of 2-tuples as an ordered mapping):

```
In [67]: grouped_pct.agg([('foo', 'mean'), ('bar', np.std)])
Out[67]:
                     foo       bar
sex    smoker
Female No      0.156921  0.036421
       Yes     0.182150  0.071595
```

```
Male   No      0.160669  0.041849
       Yes     0.152771  0.090588
```

With a DataFrame, you have more options as you can specify a list of functions to apply to all of the columns or different functions per column. To start, suppose we wanted to compute the same three statistics for the `tip_pct` and `total_bill` columns:

```
In [68]: functions = ['count', 'mean', 'max']

In [69]: result = grouped['tip_pct', 'total_bill'].agg(functions)

In [70]: result
Out[70]:
               tip_pct                     total_bill
                 count      mean       max       count       mean    max
sex    smoker
Female No           54  0.156921  0.252672          54  18.105185  35.83
       Yes          33  0.182150  0.416667          33  17.977879  44.30
Male   No           97  0.160669  0.291990          97  19.791237  48.33
       Yes          60  0.152771  0.710345          60  22.284500  50.81
```

As you can see, the resulting DataFrame has hierarchical columns, the same as you would get aggregating each column separately and using `concat` to glue the results together using the column names as the `keys` argument:

```
In [71]: result['tip_pct']
Out[71]:
               count      mean       max
sex    smoker
Female No         54  0.156921  0.252672
       Yes        33  0.182150  0.416667
Male   No         97  0.160669  0.291990
       Yes        60  0.152771  0.710345
```

As above, a list of tuples with custom names can be passed:

```
In [72]: ftuples = [('Durchschnitt', 'mean'), ('Abweichung', np.var)]

In [73]: grouped['tip_pct', 'total_bill'].agg(ftuples)
Out[73]:
                    tip_pct                total_bill
               Durchschnitt  Abweichung  Durchschnitt  Abweichung
sex    smoker
Female No          0.156921    0.001327     18.105185   53.092422
       Yes         0.182150    0.005126     17.977879   84.451517
Male   No          0.160669    0.001751     19.791237   76.152961
       Yes         0.152771    0.008206     22.284500   98.244673
```

Now, suppose you wanted to apply potentially different functions to one or more of the columns. The trick is to pass a dict to `agg` that contains a mapping of column names to any of the function specifications listed so far:

```
In [74]: grouped.agg({'tip' : np.max, 'size' : 'sum'})
Out[74]:
               size   tip
sex    smoker
```

```
Female No       140   5.2
       Yes       74   6.5
Male   No       263   9.0
       Yes      150  10.0

In [75]: grouped.agg({'tip_pct' : ['min', 'max', 'mean', 'std'],
   ....:              'size' : 'sum'})
Out[75]:
                tip_pct                               size
                    min       max      mean       std   sum
sex    smoker
Female No      0.056797  0.252672  0.156921  0.036421   140
       Yes     0.056433  0.416667  0.182150  0.071595    74
Male   No      0.071804  0.291990  0.160669  0.041849   263
       Yes     0.035638  0.710345  0.152771  0.090588   150
```

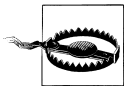
A DataFrame will have hierarchical columns only if multiple functions are applied to at least one column.

Returning Aggregated Data in "unindexed" Form

In all of the examples up until now, the aggregated data comes back with an index, potentially hierarchical, composed from the unique group key combinations observed. Since this isn't always desirable, you can disable this behavior in most cases by passing `as_index=False` to `groupby`:

```
In [76]: tips.groupby(['sex', 'smoker'], as_index=False).mean()
Out[76]:
      sex smoker  total_bill       tip      size   tip_pct
0  Female     No   18.105185  2.773519  2.592593  0.156921
1  Female    Yes   17.977879  2.931515  2.242424  0.182150
2    Male     No   19.791237  3.113402  2.711340  0.160669
3    Male    Yes   22.284500  3.051167  2.500000  0.152771
```

Of course, it's always possible to obtain the result in this format by calling `reset_index` on the result.



Using `groupby` in this way is generally less flexible; results with hierarchical columns, for example, are not currently implemented as the form of the result would have to be somewhat arbitrary.

Group-wise Operations and Transformations

Aggregation is only one kind of group operation. It is a special case in the more general class of data transformations; that is, it accepts functions that reduce a one-dimensional array to a scalar value. In this section, I will introduce you to the `transform` and `apply` methods, which will enable you to do many other kinds of group operations.

Suppose, instead, we wanted to add a column to a DataFrame containing group means for each index. One way to do this is to aggregate, then merge:

```
In [77]: df
Out[77]:
      data1     data2 key1 key2
0 -0.204708  1.393406    a  one
1  0.478943  0.092908    a  two
2 -0.519439  0.281746    b  one
3 -0.555730  0.769023    b  two
4  1.965781  1.246435    a  one

In [78]: k1_means = df.groupby('key1').mean().add_prefix('mean_')

In [79]: k1_means
Out[79]:
      mean_data1  mean_data2
key1
a       0.746672    0.910916
b      -0.537585    0.525384

In [80]: pd.merge(df, k1_means, left_on='key1', right_index=True)
Out[80]:
      data1     data2 key1 key2  mean_data1  mean_data2
0 -0.204708  1.393406    a  one    0.746672    0.910916
1  0.478943  0.092908    a  two    0.746672    0.910916
4  1.965781  1.246435    a  one    0.746672    0.910916
2 -0.519439  0.281746    b  one   -0.537585    0.525384
3 -0.555730  0.769023    b  two   -0.537585    0.525384
```

This works, but is somewhat inflexible. You can think of the operation as transforming the two data columns using the `np.mean` function. Let's look back at the `people` DataFrame from earlier in the chapter and use the `transform` method on GroupBy:

```
In [81]: key = ['one', 'two', 'one', 'two', 'one']

In [82]: people.groupby(key).mean()
Out[82]:
            a         b         c         d         e
one -0.082032 -1.063687 -1.047620 -0.884358 -0.028309
two  0.505275 -0.849512  0.075965  0.834983  0.452620

In [83]: people.groupby(key).transform(np.mean)
Out[83]:
               a         b         c         d         e
Joe    -0.082032 -1.063687 -1.047620 -0.884358 -0.028309
Steve   0.505275 -0.849512  0.075965  0.834983  0.452620
Wes    -0.082032 -1.063687 -1.047620 -0.884358 -0.028309
Jim     0.505275 -0.849512  0.075965  0.834983  0.452620
Travis -0.082032 -1.063687 -1.047620 -0.884358 -0.028309
```

As you may guess, `transform` applies a function to each group, then places the results in the appropriate locations. If each group produces a scalar value, it will be propagated (broadcasted). Suppose instead you wanted to subtract the mean value from each group. To do this, create a demeaning function and pass it to `transform`:

```
In [84]: def demean(arr):
   ....:     return arr - arr.mean()
```

```
In [85]: demeaned = people.groupby(key).transform(demean)

In [86]: demeaned
Out[86]:
              a         b         c         d         e
Joe     1.089221 -0.232534  1.322612  1.113271  1.381226
Steve   0.381154 -1.152125 -0.447807  0.834043 -0.891190
Wes    -0.457709       NaN       NaN -0.136869 -0.548778
Jim    -0.381154  1.152125  0.447807 -0.834043  0.891190
Travis -0.631512  0.232534 -1.322612 -0.976402 -0.832448
```

You can check that `demeaned` now has zero group means:

```
In [87]: demeaned.groupby(key).mean()
Out[87]:
     a  b  c  d  e
one  0 -0  0  0  0
two -0  0  0  0  0
```

As you'll see in the next section, group demeaning can be achieved using `apply` also.

Apply: General split-apply-combine

Like `aggregate`, `transform` is a more specialized function having rigid requirements: the passed function must either produce a scalar value to be broadcasted (like `np.mean`) or a transformed array of the same size. The most general purpose GroupBy method is `apply`, which is the subject of the rest of this section. As in Figure 9-1, `apply` splits the object being manipulated into pieces, invokes the passed function on each piece, then attempts to concatenate the pieces together.

Returning to the tipping data set above, suppose you wanted to select the top five `tip_pct` values by group. First, it's straightforward to write a function that selects the rows with the largest values in a particular column:

```
In [88]: def top(df, n=5, column='tip_pct'):
   ....:     return df.sort_index(by=column)[-n:]

In [89]: top(tips, n=6)
Out[89]:
     total_bill   tip     sex smoker  day    time  size   tip_pct
109       14.31  4.00  Female    Yes  Sat  Dinner     2  0.279525
183       23.17  6.50    Male    Yes  Sun  Dinner     4  0.280535
232       11.61  3.39    Male     No  Sat  Dinner     2  0.291990
67         3.07  1.00  Female    Yes  Sat  Dinner     1  0.325733
178        9.60  4.00  Female    Yes  Sun  Dinner     2  0.416667
172        7.25  5.15    Male    Yes  Sun  Dinner     2  0.710345
```

Now, if we group by `smoker`, say, and call `apply` with this function, we get the following:

```
In [90]: tips.groupby('smoker').apply(top)
Out[90]:
            total_bill   tip     sex smoker   day    time  size   tip_pct
smoker
```

```
No     88        24.71  5.85    Male     No  Thur   Lunch     2  0.236746
       185       20.69  5.00    Male     No   Sun  Dinner     5  0.241663
       51        10.29  2.60  Female     No   Sun  Dinner     2  0.252672
       149        7.51  2.00    Male     No  Thur   Lunch     2  0.266312
       232       11.61  3.39    Male     No   Sat  Dinner     2  0.291990
Yes    109       14.31  4.00  Female    Yes   Sat  Dinner     2  0.279525
       183       23.17  6.50    Male    Yes   Sun  Dinner     4  0.280535
       67         3.07  1.00  Female    Yes   Sat  Dinner     1  0.325733
       178        9.60  4.00  Female    Yes   Sun  Dinner     2  0.416667
       172        7.25  5.15    Male    Yes   Sun  Dinner     2  0.710345
```

What has happened here? The `top` function is called on each piece of the DataFrame, then the results are glued together using `pandas.concat`, labeling the pieces with the group names. The result therefore has a hierarchical index whose inner level contains index values from the original DataFrame.

If you pass a function to `apply` that takes other arguments or keywords, you can pass these after the function:

```
In [91]: tips.groupby(['smoker', 'day']).apply(top, n=1, column='total_bill')
Out[91]:
                 total_bill    tip     sex smoker   day    time  size   tip_pct
smoker day
No     Fri  94        22.75   3.25  Female     No   Fri  Dinner     2  0.142857
       Sat  212       48.33   9.00    Male     No   Sat  Dinner     4  0.186220
       Sun  156       48.17   5.00    Male     No   Sun  Dinner     6  0.103799
       Thur 142       41.19   5.00    Male     No  Thur   Lunch     5  0.121389
Yes    Fri  95        40.17   4.73    Male    Yes   Fri  Dinner     4  0.117750
       Sat  170       50.81  10.00    Male    Yes   Sat  Dinner     3  0.196812
       Sun  182       45.35   3.50    Male    Yes   Sun  Dinner     3  0.077178
       Thur 197       43.11   5.00  Female    Yes  Thur   Lunch     4  0.115982
```

Beyond these basic usage mechanics, getting the most out of `apply` is largely a matter of creativity. What occurs inside the function passed is up to you; it only needs to return a pandas object or a scalar value. The rest of this chapter will mainly consist of examples showing you how to solve various problems using `groupby`.

You may recall above I called `describe` on a GroupBy object:

```
In [92]: result = tips.groupby('smoker')['tip_pct'].describe()

In [93]: result
Out[93]:
smoker
No      count    151.000000
        mean       0.159328
        std        0.039910
        min        0.056797
        25%        0.136906
        50%        0.155625
        75%        0.185014
        max        0.291990
```

```
Yes     count     93.000000
        mean       0.163196
        std        0.085119
        min        0.035638
        25%        0.106771
        50%        0.153846
        75%        0.195059
        max        0.710345

In [94]: result.unstack('smoker')
Out[94]:
smoker          No        Yes
count   151.000000  93.000000
mean      0.159328   0.163196
std       0.039910   0.085119
min       0.056797   0.035638
25%       0.136906   0.106771
50%       0.155625   0.153846
75%       0.185014   0.195059
max       0.291990   0.710345
```

Inside GroupBy, when you invoke a method like `describe`, it is actually just a shortcut for:

```
f = lambda x: x.describe()
grouped.apply(f)
```

Suppressing the group keys

In the examples above, you see that the resulting object has a hierarchical index formed from the group keys along with the indexes of each piece of the original object. This can be disabled by passing `group_keys=False` to `groupby`:

```
In [95]: tips.groupby('smoker', group_keys=False).apply(top)
Out[95]:
     total_bill   tip     sex smoker   day    time  size   tip_pct
88        24.71  5.85    Male     No  Thur   Lunch     2  0.236746
185       20.69  5.00    Male     No   Sun  Dinner     5  0.241663
51        10.29  2.60  Female     No   Sun  Dinner     2  0.252672
149        7.51  2.00    Male     No  Thur   Lunch     2  0.266312
232       11.61  3.39    Male     No   Sat  Dinner     2  0.291990
109       14.31  4.00  Female    Yes   Sat  Dinner     2  0.279525
183       23.17  6.50    Male    Yes   Sun  Dinner     4  0.280535
67         3.07  1.00  Female    Yes   Sat  Dinner     1  0.325733
178        9.60  4.00  Female    Yes   Sun  Dinner     2  0.416667
172        7.25  5.15    Male    Yes   Sun  Dinner     2  0.710345
```

Quantile and Bucket Analysis

As you may recall from Chapter 7, pandas has some tools, in particular `cut` and `qcut`, for slicing data up into buckets with bins of your choosing or by sample quantiles. Combining these functions with `groupby`, it becomes very simple to perform bucket or

quantile analysis on a data set. Consider a simple random data set and an equal-length bucket categorization using `cut`:

```
In [96]: frame = DataFrame({'data1': np.random.randn(1000),
   ....:                    'data2': np.random.randn(1000)})

In [97]: factor = pd.cut(frame.data1, 4)

In [98]: factor[:10]
Out[98]:
Categorical:
array([(-1.23, 0.489], (-2.956, -1.23], (-1.23, 0.489], (0.489, 2.208],
       (-1.23, 0.489], (0.489, 2.208], (-1.23, 0.489], (-1.23, 0.489],
       (0.489, 2.208], (0.489, 2.208]], dtype=object)
Levels (4): Index([(-2.956, -1.23], (-1.23, 0.489], (0.489, 2.208],
                   (2.208, 3.928]], dtype=object)
```

The `Factor` object returned by `cut` can be passed directly to `groupby`. So we could compute a set of statistics for the `data2` column like so:

```
In [99]: def get_stats(group):
   ....:     return {'min': group.min(), 'max': group.max(),
   ....:             'count': group.count(), 'mean': group.mean()}

In [100]: grouped = frame.data2.groupby(factor)

In [101]: grouped.apply(get_stats).unstack()
Out[101]:
                count       max      mean       min
data1
(-1.23, 0.489]     598  3.260383 -0.002051 -2.989741
(-2.956, -1.23]     95  1.670835 -0.039521 -3.399312
(0.489, 2.208]     297  2.954439  0.081822 -3.745356
(2.208, 3.928]      10  1.765640  0.024750 -1.929776
```

These were equal-length buckets; to compute equal-size buckets based on sample quantiles, use `qcut`. I'll pass `labels=False` to just get quantile numbers.

```
# Return quantile numbers
In [102]: grouping = pd.qcut(frame.data1, 10, labels=False)

In [103]: grouped = frame.data2.groupby(grouping)

In [104]: grouped.apply(get_stats).unstack()
Out[104]:
   count       max      mean       min
0    100  1.670835 -0.049902 -3.399312
1    100  2.628441  0.030989 -1.950098
2    100  2.527939 -0.067179 -2.925113
3    100  3.260383  0.065713 -2.315555
4    100  2.074345 -0.111653 -2.047939
5    100  2.184810  0.052130 -2.989741
6    100  2.458842 -0.021489 -2.223506
7    100  2.954439 -0.026459 -3.056990
8    100  2.735527  0.103406 -3.745356
9    100  2.377020  0.220122 -2.064111
```

Example: Filling Missing Values with Group-specific Values

When cleaning up missing data, in some cases you will filter out data observations using `dropna`, but in others you may want to impute (fill in) the NA values using a fixed value or some value derived from the data. `fillna` is the right tool to use; for example here I fill in NA values with the mean:

```
In [105]: s = Series(np.random.randn(6))

In [106]: s[::2] = np.nan

In [107]: s
Out[107]:
0         NaN
1   -0.125921
2         NaN
3   -0.884475
4         NaN
5    0.227290

In [108]: s.fillna(s.mean())
Out[108]:
0   -0.261035
1   -0.125921
2   -0.261035
3   -0.884475
4   -0.261035
5    0.227290
```

Suppose you need the fill value to vary by group. As you may guess, you need only group the data and use `apply` with a function that calls `fillna` on each data chunk. Here is some sample data on some US states divided into eastern and western states:

```
In [109]: states = ['Ohio', 'New York', 'Vermont', 'Florida',
   .....:           'Oregon', 'Nevada', 'California', 'Idaho']

In [110]: group_key = ['East'] * 4 + ['West'] * 4

In [111]: data = Series(np.random.randn(8), index=states)

In [112]: data[['Vermont', 'Nevada', 'Idaho']] = np.nan

In [113]: data
Out[113]:
Ohio          0.922264
New York     -2.153545
Vermont            NaN
Florida      -0.375842
Oregon        0.329939
Nevada             NaN
California    1.105913
Idaho              NaN

In [114]: data.groupby(group_key).mean()
Out[114]:
```

```
East   -0.535707
West    0.717926
```

We can fill the NA values using the group means like so:

```
In [115]: fill_mean = lambda g: g.fillna(g.mean())

In [116]: data.groupby(group_key).apply(fill_mean)
Out[116]:
Ohio          0.922264
New York     -2.153545
Vermont      -0.535707
Florida      -0.375842
Oregon        0.329939
Nevada        0.717926
California    1.105913
Idaho         0.717926
```

In another case, you might have pre-defined fill values in your code that vary by group. Since the groups have a `name` attribute set internally, we can use that:

```
In [117]: fill_values = {'East': 0.5, 'West': -1}

In [118]: fill_func = lambda g: g.fillna(fill_values[g.name])

In [119]: data.groupby(group_key).apply(fill_func)
Out[119]:
Ohio          0.922264
New York     -2.153545
Vermont       0.500000
Florida      -0.375842
Oregon        0.329939
Nevada       -1.000000
California    1.105913
Idaho        -1.000000
```

Example: Random Sampling and Permutation

Suppose you wanted to draw a random sample (with or without replacement) from a large dataset for Monte Carlo simulation purposes or some other application. There are a number of ways to perform the "draws"; some are much more efficient than others. One way is to select the first `K` elements of `np.random.permutation(N)`, where `N` is the size of your complete dataset and `K` the desired sample size. As a more fun example, here's a way to construct a deck of English-style playing cards:

```
# Hearts, Spades, Clubs, Diamonds
suits = ['H', 'S', 'C', 'D']
card_val = (range(1, 11) + [10] * 3) * 4
base_names = ['A'] + range(2, 11) + ['J', 'K', 'Q']
cards = []
for suit in ['H', 'S', 'C', 'D']:
    cards.extend(str(num) + suit for num in base_names)

deck = Series(card_val, index=cards)
```

So now we have a Series of length 52 whose index contains card names and values are the ones used in blackjack and other games (to keep things simple, I just let the ace be 1):

```
In [121]: deck[:13]
Out[121]:
AH      1
2H      2
3H      3
4H      4
5H      5
6H      6
7H      7
8H      8
9H      9
10H    10
JH     10
KH     10
QH     10
```

Now, based on what I said above, drawing a hand of 5 cards from the desk could be written as:

```
In [122]: def draw(deck, n=5):
   .....:     return deck.take(np.random.permutation(len(deck))[:n])

In [123]: draw(deck)
Out[123]:
AD     1
8C     8
5H     5
KC    10
2C     2
```

Suppose you wanted two random cards from each suit. Because the suit is the last character of each card name, we can group based on this and use `apply`:

```
In [124]: get_suit = lambda card: card[-1] # last letter is suit

In [125]: deck.groupby(get_suit).apply(draw, n=2)
Out[125]:
C  2C     2
   3C     3
D  KD    10
   8D     8
H  KH    10
   3H     3
S  2S     2
   4S     4

# alternatively
In [126]: deck.groupby(get_suit, group_keys=False).apply(draw, n=2)
Out[126]:
KC    10
JC    10
AD     1
```

```
5D     5
5H     5
6H     6
7S     7
KS    10
```

Example: Group Weighted Average and Correlation

Under the split-apply-combine paradigm of `groupby`, operations between columns in a DataFrame or two Series, such a group weighted average, become a routine affair. As an example, take this dataset containing group keys, values, and some weights:

```
In [127]: df = DataFrame({'category': ['a', 'a', 'a', 'a', 'b', 'b', 'b', 'b'],
   .....:                 'data': np.random.randn(8),
   .....:                 'weights': np.random.rand(8)})

In [128]: df
Out[128]:
  category      data   weights
0        a  1.561587  0.957515
1        a  1.219984  0.347267
2        a -0.482239  0.581362
3        a  0.315667  0.217091
4        b -0.047852  0.894406
5        b -0.454145  0.918564
6        b -0.556774  0.277825
7        b  0.253321  0.955905
```

The group weighted average by `category` would then be:

```
In [129]: grouped = df.groupby('category')

In [130]: get_wavg = lambda g: np.average(g['data'], weights=g['weights'])

In [131]: grouped.apply(get_wavg)
Out[131]:
category
a           0.811643
b          -0.122262
```

As a less trivial example, consider a data set from Yahoo! Finance containing end of day prices for a few stocks and the S&P 500 index (the `SPX` ticker):

```
In [132]: close_px = pd.read_csv('ch09/stock_px.csv', parse_dates=True, index_col=0)

In [133]: close_px
Out[133]:
<class 'pandas.core.frame.DataFrame'>
DatetimeIndex: 2214 entries, 2003-01-02 00:00:00 to 2011-10-14 00:00:00
Data columns:
AAPL    2214  non-null values
MSFT    2214  non-null values
XOM     2214  non-null values
SPX     2214  non-null values
dtypes: float64(4)
```

```
In [134]: close_px[-4:]
Out[134]:
               AAPL   MSFT    XOM      SPX
2011-10-11  400.29  27.00  76.27  1195.54
2011-10-12  402.19  26.96  77.16  1207.25
2011-10-13  408.43  27.18  76.37  1203.66
2011-10-14  422.00  27.27  78.11  1224.58
```

One task of interest might be to compute a DataFrame consisting of the yearly correlations of daily returns (computed from percent changes) with SPX. Here is one way to do it:

```
In [135]: rets = close_px.pct_change().dropna()

In [136]: spx_corr = lambda x: x.corrwith(x['SPX'])

In [137]: by_year = rets.groupby(lambda x: x.year)

In [138]: by_year.apply(spx_corr)
Out[138]:
          AAPL      MSFT       XOM  SPX
2003  0.541124  0.745174  0.661265    1
2004  0.374283  0.588531  0.557742    1
2005  0.467540  0.562374  0.631010    1
2006  0.428267  0.406126  0.518514    1
2007  0.508118  0.658770  0.786264    1
2008  0.681434  0.804626  0.828303    1
2009  0.707103  0.654902  0.797921    1
2010  0.710105  0.730118  0.839057    1
2011  0.691931  0.800996  0.859975    1
```

There is, of course, nothing to stop you from computing inter-column correlations:

```
# Annual correlation of Apple with Microsoft
In [139]: by_year.apply(lambda g: g['AAPL'].corr(g['MSFT']))
Out[139]:
2003    0.480868
2004    0.259024
2005    0.300093
2006    0.161735
2007    0.417738
2008    0.611901
2009    0.432738
2010    0.571946
2011    0.581987
```

Example: Group-wise Linear Regression

In the same vein as the previous example, you can use `groupby` to perform more complex group-wise statistical analysis, as long as the function returns a pandas object or scalar value. For example, I can define the following `regress` function (using the `statsmodels` econometrics library) which executes an ordinary least squares (OLS) regression on each chunk of data:

```
import statsmodels.api as sm
def regress(data, yvar, xvars):
    Y = data[yvar]
    X = data[xvars]
    X['intercept'] = 1.
    result = sm.OLS(Y, X).fit()
    return result.params
```

Now, to run a yearly linear regression of `AAPL` on `SPX` returns, I execute:

```
In [141]: by_year.apply(regress, 'AAPL', ['SPX'])
Out[141]:
          SPX  intercept
2003  1.195406   0.000710
2004  1.363463   0.004201
2005  1.766415   0.003246
2006  1.645496   0.000080
2007  1.198761   0.003438
2008  0.968016  -0.001110
2009  0.879103   0.002954
2010  1.052608   0.001261
2011  0.806605   0.001514
```

Pivot Tables and Cross-Tabulation

A *pivot table* is a data summarization tool frequently found in spreadsheet programs and other data analysis software. It aggregates a table of data by one or more keys, arranging the data in a rectangle with some of the group keys along the rows and some along the columns. Pivot tables in Python with pandas are made possible using the `groupby` facility described in this chapter combined with reshape operations utilizing hierarchical indexing. DataFrame has a `pivot_table` method, and additionally there is a top-level `pandas.pivot_table` function. In addition to providing a convenience interface to `groupby`, `pivot_table` also can add partial totals, also known as *margins*.

Returning to the tipping data set, suppose I wanted to compute a table of group means (the default `pivot_table` aggregation type) arranged by `sex` and `smoker` on the rows:

```
In [142]: tips.pivot_table(rows=['sex', 'smoker'])
Out[142]:
                size       tip   tip_pct  total_bill
sex    smoker
Female No      2.592593  2.773519  0.156921   18.105185
       Yes     2.242424  2.931515  0.182150   17.977879
Male   No      2.711340  3.113402  0.160669   19.791237
       Yes     2.500000  3.051167  0.152771   22.284500
```

This could have been easily produced using `groupby`. Now, suppose we want to aggregate only `tip_pct` and `size`, and additionally group by `day`. I'll put `smoker` in the table columns and `day` in the rows:

```
In [143]: tips.pivot_table(['tip_pct', 'size'], rows=['sex', 'day'],
   .....:                  cols='smoker')
Out[143]:
```

```
             tip_pct               size
smoker            No       Yes        No       Yes
sex    day
Female Fri   0.165296  0.209129  2.500000  2.000000
       Sat   0.147993  0.163817  2.307692  2.200000
       Sun   0.165710  0.237075  3.071429  2.500000
       Thur  0.155971  0.163073  2.480000  2.428571
Male   Fri   0.138005  0.144730  2.000000  2.125000
       Sat   0.162132  0.139067  2.656250  2.629630
       Sun   0.158291  0.173964  2.883721  2.600000
       Thur  0.165706  0.164417  2.500000  2.300000
```

This table could be augmented to include partial totals by passing `margins=True`. This has the effect of adding `All` row and column labels, with corresponding values being the group statistics for all the data within a single tier. In this below example, the `All` values are means without taking into account smoker vs. non-smoker (the `All` columns) or any of the two levels of grouping on the rows (the `All` row):

```
In [144]: tips.pivot_table(['tip_pct', 'size'], rows=['sex', 'day'],
   .....:                  cols='smoker', margins=True)
Out[144]:
                size                      tip_pct
smoker            No       Yes       All        No       Yes       All
sex    day
Female Fri   2.500000  2.000000  2.111111  0.165296  0.209129  0.199388
       Sat   2.307692  2.200000  2.250000  0.147993  0.163817  0.156470
       Sun   3.071429  2.500000  2.944444  0.165710  0.237075  0.181569
       Thur  2.480000  2.428571  2.468750  0.155971  0.163073  0.157525
Male   Fri   2.000000  2.125000  2.100000  0.138005  0.144730  0.143385
       Sat   2.656250  2.629630  2.644068  0.162132  0.139067  0.151577
       Sun   2.883721  2.600000  2.810345  0.158291  0.173964  0.162344
       Thur  2.500000  2.300000  2.433333  0.165706  0.164417  0.165276
All          2.668874  2.408602  2.569672  0.159328  0.163196  0.160803
```

To use a different aggregation function, pass it to `aggfunc`. For example, `'count'` or `len` will give you a cross-tabulation (count or frequency) of group sizes:

```
In [145]: tips.pivot_table('tip_pct', rows=['sex', 'smoker'], cols='day',
   .....:                  aggfunc=len, margins=True)
Out[145]:
day            Fri  Sat  Sun  Thur  All
sex    smoker
Female No        2   13   14    25   54
       Yes       7   15    4     7   33
Male   No        2   32   43    20   97
       Yes       8   27   15    10   60
All             19   87   76    62  244
```

If some combinations are empty (or otherwise NA), you may wish to pass a `fill_value`:

```
In [146]: tips.pivot_table('size', rows=['time', 'sex', 'smoker'],
   .....:                  cols='day', aggfunc='sum', fill_value=0)
Out[146]:
day                   Fri  Sat  Sun  Thur
time   sex    smoker
Dinner Female No        2   30   43     2
```

```
                Yes       8   33   10     0
        Male    No        4   85  124     0
                Yes      12   71   39     0
Lunch   Female  No        3    0    0    60
                Yes       6    0    0    17
        Male    No        0    0    0    50
                Yes       5    0    0    23
```

See Table 9-2 for a summary of `pivot_table` methods.

Table 9-2. pivot_table options

Function name	Description
`values`	Column name or names to aggregate. By default aggregates all numeric columns
`rows`	Column names or other group keys to group on the rows of the resulting pivot table
`cols`	Column names or other group keys to group on the columns of the resulting pivot table
`aggfunc`	Aggregation function or list of functions; `'mean'` by default. Can be any function valid in a groupby context
`fill_value`	Replace missing values in result table
`margins`	Add row/column subtotals and grand total, False by default

Cross-Tabulations: Crosstab

A cross-tabulation (or *crosstab* for short) is a special case of a pivot table that computes group frequencies. Here is a canonical example taken from the Wikipedia page on cross-tabulation:

```
In [150]: data
Out[150]:
   Sample  Gender    Handedness
0       1  Female  Right-handed
1       2    Male   Left-handed
2       3  Female  Right-handed
3       4    Male  Right-handed
4       5    Male   Left-handed
5       6    Male  Right-handed
6       7  Female  Right-handed
7       8  Female   Left-handed
8       9    Male  Right-handed
9      10  Female  Right-handed
```

As part of some survey analysis, we might want to summarize this data by gender and handedness. You could use `pivot_table` to do this, but the `pandas.crosstab` function is very convenient:

```
In [151]: pd.crosstab(data.Gender, data.Handedness, margins=True)
Out[151]:
Handedness  Left-handed  Right-handed  All
Gender
Female                1             4    5
Male                  2             3    5
All                   3             7   10
```

The first two arguments to `crosstab` can each either be an array or Series or a list of arrays. As in the tips data:

```
In [152]: pd.crosstab([tips.time, tips.day], tips.smoker, margins=True)
Out[152]:
smoker        No  Yes  All
time   day
Dinner Fri     3    9   12
       Sat    45   42   87
       Sun    57   19   76
       Thur    1    0    1
Lunch  Fri     1    6    7
       Thur   44   17   61
All          151   93  244
```

Example: 2012 Federal Election Commission Database

The US Federal Election Commission publishes data on contributions to political campaigns. This includes contributor names, occupation and employer, address, and contribution amount. An interesting dataset is from the 2012 US presidential election (*http://www.fec.gov/disclosurep/PDownload.do*). As of this writing (June 2012), the full dataset for all states is a 150 megabyte CSV file `P00000001-ALL.csv`, which can be loaded with `pandas.read_csv`:

```
In [13]: fec = pd.read_csv('ch09/P00000001-ALL.csv')
```

```
In [14]: fec
Out[14]:
<class 'pandas.core.frame.DataFrame'>
Int64Index: 1001731 entries, 0 to 1001730
Data columns:
cmte_id             1001731  non-null values
cand_id             1001731  non-null values
cand_nm             1001731  non-null values
contbr_nm           1001731  non-null values
contbr_city         1001716  non-null values
contbr_st           1001727  non-null values
contbr_zip          1001620  non-null values
contbr_employer      994314  non-null values
contbr_occupation    994433  non-null values
contb_receipt_amt   1001731  non-null values
contb_receipt_dt    1001731  non-null values
receipt_desc          14166  non-null values
memo_cd               92482  non-null values
memo_text             97770  non-null values
form_tp             1001731  non-null values
file_num            1001731  non-null values
dtypes: float64(1), int64(1), object(14)
```

A sample record in the DataFrame looks like this:

```
In [15]: fec.ix[123456]
Out[15]:
cmte_id                           C00431445
```

```
cand_id                            P80003338
cand_nm                          Obama, Barack
contbr_nm                          ELLMAN, IRA
contbr_city                              TEMPE
contbr_st                                   AZ
contbr_zip                          852816719
contbr_employer      ARIZONA STATE UNIVERSITY
contbr_occupation                    PROFESSOR
contb_receipt_amt                           50
contb_receipt_dt                     01-DEC-11
receipt_desc                               NaN
memo_cd                                    NaN
memo_text                                  NaN
form_tp                                  SA17A
file_num                                 772372
Name: 123456
```

You can probably think of many ways to start slicing and dicing this data to extract informative statistics about donors and patterns in the campaign contributions. I'll spend the next several pages showing you a number of different analyses that apply techniques you have learned about so far.

You can see that there are no political party affiliations in the data, so this would be useful to add. You can get a list of all the unique political candidates using `unique` (note that NumPy suppresses the quotes around the strings in the output):

```
In [16]: unique_cands = fec.cand_nm.unique()

In [17]: unique_cands
Out[17]:
array([Bachmann, Michelle, Romney, Mitt, Obama, Barack,
       Roemer, Charles E. 'Buddy' III, Pawlenty, Timothy,
       Johnson, Gary Earl, Paul, Ron, Santorum, Rick, Cain, Herman,
       Gingrich, Newt, McCotter, Thaddeus G, Huntsman, Jon, Perry, Rick], dtype=object)

In [18]: unique_cands[2]
Out[18]: 'Obama, Barack'
```

An easy way to indicate party affiliation is using a dict:[2]

```
parties = {'Bachmann, Michelle': 'Republican',
           'Cain, Herman': 'Republican',
           'Gingrich, Newt': 'Republican',
           'Huntsman, Jon': 'Republican',
           'Johnson, Gary Earl': 'Republican',
           'McCotter, Thaddeus G': 'Republican',
           'Obama, Barack': 'Democrat',
           'Paul, Ron': 'Republican',
           'Pawlenty, Timothy': 'Republican',
           'Perry, Rick': 'Republican',
           "Roemer, Charles E. 'Buddy' III": 'Republican',
```

2. This makes the simplifying assumption that Gary Johnson is a Republican even though he later became the Libertarian party candidate.

```
            'Romney, Mitt': 'Republican',
            'Santorum, Rick': 'Republican'}
```

Now, using this mapping and the `map` method on Series objects, you can compute an array of political parties from the candidate names:

```
In [20]: fec.cand_nm[123456:123461]
Out[20]:
123456    Obama, Barack
123457    Obama, Barack
123458    Obama, Barack
123459    Obama, Barack
123460    Obama, Barack
Name: cand_nm

In [21]: fec.cand_nm[123456:123461].map(parties)
Out[21]:
123456    Democrat
123457    Democrat
123458    Democrat
123459    Democrat
123460    Democrat
Name: cand_nm

# Add it as a column
In [22]: fec['party'] = fec.cand_nm.map(parties)

In [23]: fec['party'].value_counts()
Out[23]:
Democrat      593746
Republican    407985
```

A couple of data preparation points. First, this data includes both contributions and refunds (negative contribution amount):

```
In [24]: (fec.contb_receipt_amt > 0).value_counts()
Out[24]:
True     991475
False     10256
```

To simplify the analysis, I'll restrict the data set to positive contributions:

```
In [25]: fec = fec[fec.contb_receipt_amt > 0]
```

Since Barack Obama and Mitt Romney are the main two candidates, I'll also prepare a subset that just has contributions to their campaigns:

```
In [26]: fec_mrbo = fec[fec.cand_nm.isin(['Obama, Barack', 'Romney, Mitt'])]
```

Donation Statistics by Occupation and Employer

Donations by occupation is another oft-studied statistic. For example, lawyers (attorneys) tend to donate more money to Democrats, while business executives tend to donate more to Republicans. You have no reason to believe me; you can see for yourself in the data. First, the total number of donations by occupation is easy:

```
In [27]: fec.contbr_occupation.value_counts()[:10]
Out[27]:
RETIRED                                   233990
INFORMATION REQUESTED                      35107
ATTORNEY                                   34286
HOMEMAKER                                  29931
PHYSICIAN                                  23432
INFORMATION REQUESTED PER BEST EFFORTS     21138
ENGINEER                                   14334
TEACHER                                    13990
CONSULTANT                                 13273
PROFESSOR                                  12555
```

You will notice by looking at the occupations that many refer to the same basic job type, or there are several variants of the same thing. Here is a code snippet illustrates a technique for cleaning up a few of them by mapping from one occupation to another; note the "trick" of using `dict.get` to allow occupations with no mapping to "pass through":

```
occ_mapping = {
   'INFORMATION REQUESTED PER BEST EFFORTS' : 'NOT PROVIDED',
   'INFORMATION REQUESTED' : 'NOT PROVIDED',
   'INFORMATION REQUESTED (BEST EFFORTS)' : 'NOT PROVIDED',
   'C.E.O.': 'CEO'
}

# If no mapping provided, return x
f = lambda x: occ_mapping.get(x, x)
fec.contbr_occupation = fec.contbr_occupation.map(f)
```

I'll also do the same thing for employers:

```
emp_mapping = {
   'INFORMATION REQUESTED PER BEST EFFORTS' : 'NOT PROVIDED',
   'INFORMATION REQUESTED' : 'NOT PROVIDED',
   'SELF' : 'SELF-EMPLOYED',
   'SELF EMPLOYED' : 'SELF-EMPLOYED',
}

# If no mapping provided, return x
f = lambda x: emp_mapping.get(x, x)
fec.contbr_employer = fec.contbr_employer.map(f)
```

Now, you can use `pivot_table` to aggregate the data by party and occupation, then filter down to the subset that donated at least $2 million overall:

```
In [34]: by_occupation = fec.pivot_table('contb_receipt_amt',
   ....:                                  rows='contbr_occupation',
   ....:                                  cols='party', aggfunc='sum')

In [35]: over_2mm = by_occupation[by_occupation.sum(1) > 2000000]

In [36]: over_2mm
Out[36]:
party                 Democrat       Republican
contbr_occupation
```

```
ATTORNEY        11141982.97   7477194.430000
CEO              2074974.79   4211040.520000
CONSULTANT       2459912.71   2544725.450000
ENGINEER          951525.55   1818373.700000
EXECUTIVE        1355161.05   4138850.090000
HOMEMAKER        4248875.80  13634275.780000
INVESTOR          884133.00   2431768.920000
LAWYER           3160478.87    391224.320000
MANAGER           762883.22   1444532.370000
NOT PROVIDED     4866973.96  20565473.010000
OWNER            1001567.36   2408286.920000
PHYSICIAN        3735124.94   3594320.240000
PRESIDENT        1878509.95   4720923.760000
PROFESSOR        2165071.08    296702.730000
REAL ESTATE       528902.09   1625902.250000
RETIRED         25305116.38  23561244.489999
SELF-EMPLOYED     672393.40   1640252.540000
```

It can be easier to look at this data graphically as a bar plot (`'barh'` means horizontal bar plot, see Figure 9-2):

```
In [38]: over_2mm.plot(kind='barh')
```

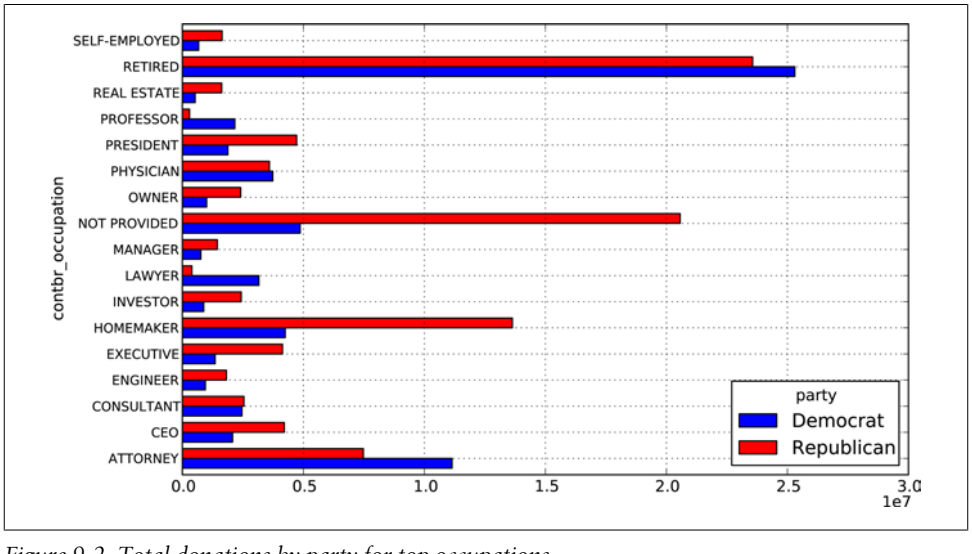


Figure 9-2. Total donations by party for top occupations

You might be interested in the top donor occupations or top companies donating to Obama and Romney. To do this, you can group by candidate name and use a variant of the `top` method from earlier in the chapter:

```
def get_top_amounts(group, key, n=5):
    totals = group.groupby(key)['contb_receipt_amt'].sum()

    # Order totals by key in descending order
    return totals.order(ascending=False)[-n:]
```

Then aggregated by occupation and employer:

```
In [40]: grouped = fec_mrbo.groupby('cand_nm')

In [41]: grouped.apply(get_top_amounts, 'contbr_occupation', n=7)
Out[41]:
cand_nm        contbr_occupation
Obama, Barack  RETIRED              25305116.38
               ATTORNEY             11141982.97
               NOT PROVIDED          4866973.96
               HOMEMAKER             4248875.80
               PHYSICIAN             3735124.94
               LAWYER                3160478.87
               CONSULTANT            2459912.71
Romney, Mitt   RETIRED              11508473.59
               NOT PROVIDED         11396894.84
               HOMEMAKER             8147446.22
               ATTORNEY              5364718.82
               PRESIDENT             2491244.89
               EXECUTIVE             2300947.03
               C.E.O.                1968386.11
Name: contb_receipt_amt

In [42]: grouped.apply(get_top_amounts, 'contbr_employer', n=10)
Out[42]:
cand_nm        contbr_employer
Obama, Barack  RETIRED               22694358.85
               SELF-EMPLOYED         18626807.16
               NOT EMPLOYED           8586308.70
               NOT PROVIDED           5053480.37
               HOMEMAKER              2605408.54
               STUDENT                 318831.45
               VOLUNTEER               257104.00
               MICROSOFT               215585.36
               SIDLEY AUSTIN LLP       168254.00
               REFUSED                 149516.07
Romney, Mitt   NOT PROVIDED          12059527.24
               RETIRED               11506225.71
               HOMEMAKER              8147196.22
               SELF-EMPLOYED          7414115.22
               STUDENT                 496490.94
               CREDIT SUISSE           281150.00
               MORGAN STANLEY          267266.00
               GOLDMAN SACH & CO.      238250.00
               BARCLAYS CAPITAL        162750.00
               H.I.G. CAPITAL          139500.00
Name: contb_receipt_amt
```

Bucketing Donation Amounts

A useful way to analyze this data is to use the `cut` function to discretize the contributor amounts into buckets by contribution size:

```
In [43]: bins = np.array([0, 1, 10, 100, 1000, 10000, 100000, 1000000, 10000000])
```

```
In [44]: labels = pd.cut(fec_mrbo.contb_receipt_amt, bins)

In [45]: labels
Out[45]:
Categorical:contb_receipt_amt
array([(10, 100], (100, 1000], (100, 1000], ..., (1, 10], (10, 100],
       (100, 1000]], dtype=object)
Levels (8): array([(0, 1], (1, 10], (10, 100], (100, 1000], (1000, 10000],
       (10000, 100000], (100000, 1000000], (1000000, 10000000]], dtype=object)
```

We can then group the data for Obama and Romney by name and bin label to get a histogram by donation size:

```
In [46]: grouped = fec_mrbo.groupby(['cand_nm', labels])

In [47]: grouped.size().unstack(0)
Out[47]:
cand_nm              Obama, Barack  Romney, Mitt
contb_receipt_amt
(0, 1]                         493            77
(1, 10]                      40070          3681
(10, 100]                   372280         31853
(100, 1000]                 153991         43357
(1000, 10000]                22284         26186
(10000, 100000]                  2             1
(100000, 1000000]                3           NaN
(1000000, 10000000]              4           NaN
```

This data shows that Obama has received a significantly larger number of small donations than Romney. You can also sum the contribution amounts and normalize within buckets to visualize percentage of total donations of each size by candidate:

```
In [48]: bucket_sums = grouped.contb_receipt_amt.sum().unstack(0)

In [49]: bucket_sums
Out[49]:
cand_nm              Obama, Barack  Romney, Mitt
contb_receipt_amt
(0, 1]                      318.24         77.00
(1, 10]                  337267.62      29819.66
(10, 100]              20288981.41    1987783.76
(100, 1000]            54798531.46   22363381.69
(1000, 10000]          51753705.67   63942145.42
(10000, 100000]           59100.00      12700.00
(100000, 1000000]       1490683.08           NaN
(1000000, 10000000]     7148839.76           NaN

In [50]: normed_sums = bucket_sums.div(bucket_sums.sum(axis=1), axis=0)

In [51]: normed_sums
Out[51]:
cand_nm              Obama, Barack  Romney, Mitt
contb_receipt_amt
(0, 1]                    0.805182      0.194818
(1, 10]                   0.918767      0.081233
(10, 100]                 0.910769      0.089231
```

```
(100, 1000]              0.710176      0.289824
(1000, 10000]            0.447326      0.552674
(10000, 100000]          0.823120      0.176880
(100000, 1000000]        1.000000           NaN
(1000000, 10000000]      1.000000           NaN

In [52]: normed_sums[:-2].plot(kind='barh', stacked=True)
```

I excluded the two largest bins as these are not donations by individuals. See Figure 9-3 for the resulting figure.

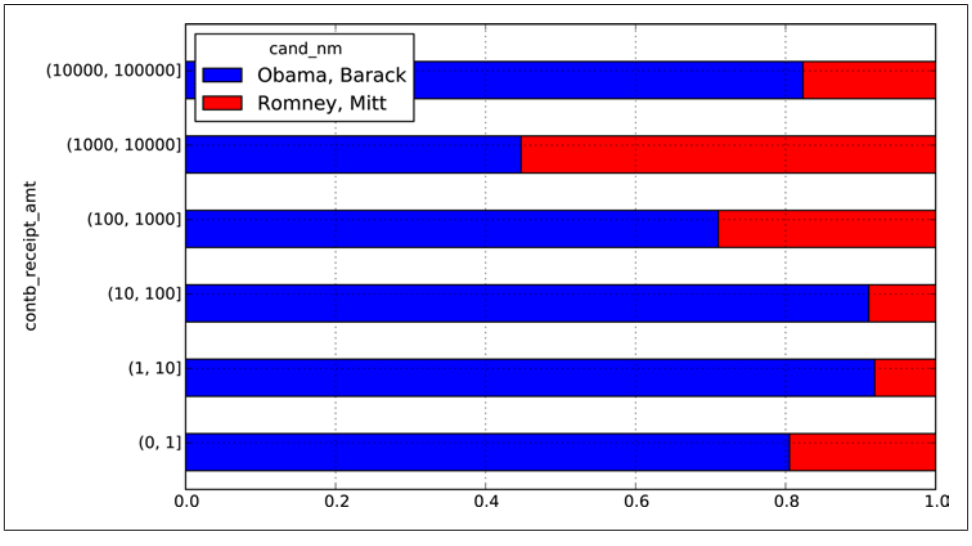


Figure 9-3. Percentage of total donations received by candidates for each donation size

There are of course many refinements and improvements of this analysis. For example, you could aggregate donations by donor name and zip code to adjust for donors who gave many small amounts versus one or more large donations. I encourage you to download it and explore it yourself.

Donation Statistics by State

Aggregating the data by candidate and state is a routine affair:

```
In [53]: grouped = fec_mrbo.groupby(['cand_nm', 'contbr_st'])

In [54]: totals = grouped.contb_receipt_amt.sum().unstack(0).fillna(0)

In [55]: totals = totals[totals.sum(1) > 100000]

In [56]: totals[:10]
Out[56]:
cand_nm    Obama, Barack  Romney, Mitt
contbr_st
```

```
AK            281840.15     86204.24
AL            543123.48    527303.51
AR            359247.28    105556.00
AZ           1506476.98   1888436.23
CA          23824984.24  11237636.60
CO           2132429.49   1506714.12
CT           2068291.26   3499475.45
DC           4373538.80   1025137.50
DE            336669.14     82712.00
FL           7318178.58   8338458.81
```

If you divide each row by the total contribution amount, you get the relative percentage of total donations by state for each candidate:

```
In [57]: percent = totals.div(totals.sum(1), axis=0)

In [58]: percent[:10]
Out[58]:
cand_nm    Obama, Barack  Romney, Mitt
contbr_st
AK              0.765778      0.234222
AL              0.507390      0.492610
AR              0.772902      0.227098
AZ              0.443745      0.556255
CA              0.679498      0.320502
CO              0.585970      0.414030
CT              0.371476      0.628524
DC              0.810113      0.189887
DE              0.802776      0.197224
FL              0.467417      0.532583
```

I thought it would be interesting to look at this data plotted on a map, using ideas from Chapter 8. After locating a shape file for the state boundaries (*http://nationalatlas.gov/atlasftp.html?openChapters=chpbound*) and learning a bit more about matplotlib and its `basemap` toolkit (I was aided by a blog posting from Thomas Lecocq)[3], I ended up with the following code for plotting these relative percentages:

```
from mpl_toolkits.basemap import Basemap, cm
import numpy as np
from matplotlib import rcParams
from matplotlib.collections import LineCollection
import matplotlib.pyplot as plt

from shapelib import ShapeFile
import dbflib

obama = percent['Obama, Barack']

fig = plt.figure(figsize=(12, 12))
ax = fig.add_axes([0.1,0.1,0.8,0.8])

lllat = 21; urlat = 53; lllon = -118; urlon = -62
```

3. *http://www.geophysique.be/2011/01/27/matplotlib-basemap-tutorial-07-shapefiles-unleached/*

```
m = Basemap(ax=ax, projection='stere',
            lon_0=(urlon + lllon) / 2, lat_0=(urlat + lllat) / 2,
            llcrnrlat=lllat, urcrnrlat=urlat, llcrnrlon=lllon,
            urcrnrlon=urlon, resolution='l')
m.drawcoastlines()
m.drawcountries()

shp = ShapeFile('../states/statesp020')
dbf = dbflib.open('../states/statesp020')

for npoly in range(shp.info()[0]):
    # Draw colored polygons on the map
    shpsegs = []
    shp_object = shp.read_object(npoly)
    verts = shp_object.vertices()
    rings = len(verts)
    for ring in range(rings):
        lons, lats = zip(*verts[ring])
        x, y = m(lons, lats)
        shpsegs.append(zip(x,y))
        if ring == 0:
            shapedict = dbf.read_record(npoly)
        name = shapedict['STATE']
    lines = LineCollection(shpsegs,antialiaseds=(1,))

    # state_to_code dict, e.g. 'ALASKA' -> 'AK', omitted
    try:
        per = obama[state_to_code[name.upper()]]
    except KeyError:
        continue

    lines.set_facecolors('k')
    lines.set_alpha(0.75 * per) # Shrink the percentage a bit
    lines.set_edgecolors('k')
    lines.set_linewidth(0.3)
    ax.add_collection(lines)

plt.show()
```

See Figure 9-4 for the result.

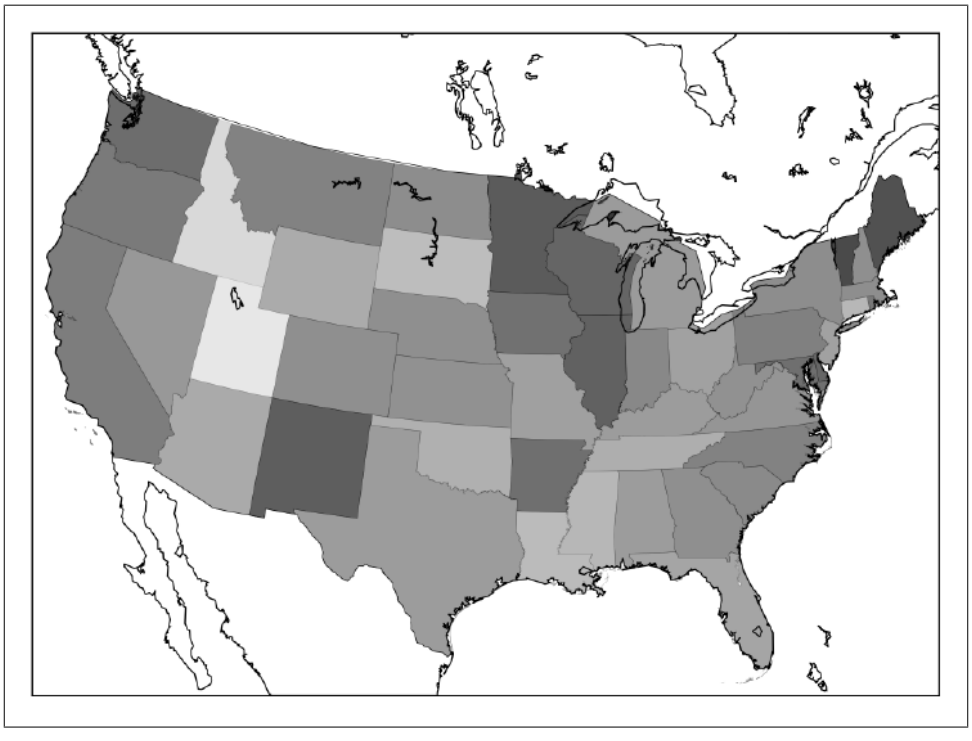


Figure 9-4. US map aggregated donation statistics overlay (darker means more Democratic)

CHAPTER 4

NumPy Basics: Arrays and Vectorized Computation

NumPy, short for Numerical Python, is the fundamental package required for high performance scientific computing and data analysis. It is the foundation on which nearly all of the higher-level tools in this book are built. Here are some of the things it provides:

- `ndarray`, a fast and space-efficient multidimensional array providing vectorized arithmetic operations and sophisticated *broadcasting* capabilities
- Standard mathematical functions for fast operations on entire arrays of data without having to write loops
- Tools for reading / writing array data to disk and working with memory-mapped files
- Linear algebra, random number generation, and Fourier transform capabilities
- Tools for integrating code written in C, C++, and Fortran

The last bullet point is also one of the most important ones from an ecosystem point of view. Because NumPy provides an easy-to-use C API, it is very easy to pass data to external libraries written in a low-level language and also for external libraries to return data to Python as NumPy arrays. This feature has made Python a language of choice for wrapping legacy C/C++/Fortran codebases and giving them a dynamic and easy-to-use interface.

While NumPy by itself does not provide very much high-level data analytical functionality, having an understanding of NumPy arrays and array-oriented computing will help you use tools like pandas much more effectively. If you're new to Python and just looking to get your hands dirty working with data using pandas, feel free to give this chapter a skim. For more on advanced NumPy features like broadcasting, see Chapter 12.

For most data analysis applications, the main areas of functionality I'll focus on are:

- Fast vectorized array operations for data munging and cleaning, subsetting and filtering, transformation, and any other kinds of computations
- Common array algorithms like sorting, unique, and set operations
- Efficient descriptive statistics and aggregating/summarizing data
- Data alignment and relational data manipulations for merging and joining together heterogeneous data sets
- Expressing conditional logic as array expressions instead of loops with `if-elif-else` branches
- Group-wise data manipulations (aggregation, transformation, function application). Much more on this in Chapter 5

While NumPy provides the computational foundation for these operations, you will likely want to use pandas as your basis for most kinds of data analysis (especially for structured or tabular data) as it provides a rich, high-level interface making most common data tasks very concise and simple. pandas also provides some more domain-specific functionality like time series manipulation, which is not present in NumPy.

In this chapter and throughout the book, I use the standard NumPy convention of always using `import numpy as np`. You are, of course, welcome to put `from numpy import *` in your code to avoid having to write `np.`, but I would caution you against making a habit of this.

The NumPy ndarray: A Multidimensional Array Object

One of the key features of NumPy is its N-dimensional array object, or ndarray, which is a fast, flexible container for large data sets in Python. Arrays enable you to perform mathematical operations on whole blocks of data using similar syntax to the equivalent operations between scalar elements:

```
In [8]: data
Out[8]:
array([[ 0.9526, -0.246 , -0.8856],
       [ 0.5639,  0.2379,  0.9104]])

In [9]: data * 10
Out[9]:
array([[ 9.5256, -2.4601, -8.8565],
       [ 5.6385,  2.3794,  9.104 ]])

In [10]: data + data
Out[10]:
array([[ 1.9051, -0.492 , -1.7713],
       [ 1.1277,  0.4759,  1.8208]])
```

An ndarray is a generic multidimensional container for homogeneous data; that is, all of the elements must be the same type. Every array has a `shape`, a tuple indicating the size of each dimension, and a `dtype`, an object describing the *data type* of the array:

```
In [11]: data.shape
Out[11]: (2, 3)
```

```
In [12]: data.dtype
Out[12]: dtype('float64')
```

This chapter will introduce you to the basics of using NumPy arrays, and should be sufficient for following along with the rest of the book. While it's not necessary to have a deep understanding of NumPy for many data analytical applications, becoming proficient in array-oriented programming and thinking is a key step along the way to becoming a scientific Python guru.

Whenever you see "array", "NumPy array", or "ndarray" in the text, with few exceptions they all refer to the same thing: the ndarray object.

Creating ndarrays

The easiest way to create an array is to use the `array` function. This accepts any sequence-like object (including other arrays) and produces a new NumPy array containing the passed data. For example, a list is a good candidate for conversion:

```
In [13]: data1 = [6, 7.5, 8, 0, 1]

In [14]: arr1 = np.array(data1)

In [15]: arr1
Out[15]: array([ 6. ,  7.5,  8. ,  0. ,  1. ])
```

Nested sequences, like a list of equal-length lists, will be converted into a multidimensional array:

```
In [16]: data2 = [[1, 2, 3, 4], [5, 6, 7, 8]]

In [17]: arr2 = np.array(data2)

In [18]: arr2
Out[18]:
array([[1, 2, 3, 4],
       [5, 6, 7, 8]])

In [19]: arr2.ndim
Out[19]: 2

In [20]: arr2.shape
Out[20]: (2, 4)
```

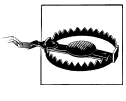
Unless explicitly specified (more on this later), `np.array` tries to infer a good data type for the array that it creates. The data type is stored in a special `dtype` object; for example, in the above two examples we have:

```
In [21]: arr1.dtype
Out[21]: dtype('float64')
```

```
In [22]: arr2.dtype
Out[22]: dtype('int64')
```

In addition to `np.array`, there are a number of other functions for creating new arrays. As examples, `zeros` and `ones` create arrays of 0's or 1's, respectively, with a given length or shape. `empty` creates an array without initializing its values to any particular value. To create a higher dimensional array with these methods, pass a tuple for the shape:

```
In [23]: np.zeros(10)
Out[23]: array([ 0.,  0.,  0.,  0.,  0.,  0.,  0.,  0.,  0.,  0.])

In [24]: np.zeros((3, 6))
Out[24]:
array([[ 0.,  0.,  0.,  0.,  0.,  0.],
       [ 0.,  0.,  0.,  0.,  0.,  0.],
       [ 0.,  0.,  0.,  0.,  0.,  0.]])

In [25]: np.empty((2, 3, 2))
Out[25]:
array([[[  4.94065646e-324,   4.94065646e-324],
        [  3.87491056e-297,   2.46845796e-130],
        [  4.94065646e-324,   4.94065646e-324]],

       [[  1.90723115e+083,   5.73293533e-053],
        [ -2.33568637e+124,  -6.70608105e-012],
        [  4.42786966e+160,   1.27100354e+025]]])
```



It's not safe to assume that `np.empty` will return an array of all zeros. In many cases, as previously shown, it will return uninitialized garbage values.

`arange` is an array-valued version of the built-in Python `range` function:

```
In [26]: np.arange(15)
Out[26]: array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14])
```

See Table 4-1 for a short list of standard array creation functions. Since NumPy is focused on numerical computing, the data type, if not specified, will in many cases be `float64` (floating point).

Table 4-1. Array creation functions

Function	Description
`array`	Convert input data (list, tuple, array, or other sequence type) to an ndarray either by inferring a dtype or explicitly specifying a dtype. Copies the input data by default.
`asarray`	Convert input to ndarray, but do not copy if the input is already an ndarray
`arange`	Like the built-in `range` but returns an ndarray instead of a list.
`ones, ones_like`	Produce an array of all 1's with the given shape and dtype. `ones_like` takes another array and produces a ones array of the same shape and dtype.
`zeros, zeros_like`	Like `ones` and `ones_like` but producing arrays of 0's instead

Function	Description
`empty, empty_like`	Create new arrays by allocating new memory, but do not populate with any values like `ones` and `zeros`
`eye, identity`	Create a square N x N identity matrix (1's on the diagonal and 0's elsewhere)

Data Types for ndarrays

The *data type* or `dtype` is a special object containing the information the ndarray needs to interpret a chunk of memory as a particular type of data:

```
In [27]: arr1 = np.array([1, 2, 3], dtype=np.float64)

In [28]: arr2 = np.array([1, 2, 3], dtype=np.int32)

In [29]: arr1.dtype           In [30]: arr2.dtype
Out[29]: dtype('float64')     Out[30]: dtype('int32')
```

Dtypes are part of what make NumPy so powerful and flexible. In most cases they map directly onto an underlying machine representation, which makes it easy to read and write binary streams of data to disk and also to connect to code written in a low-level language like C or Fortran. The numerical dtypes are named the same way: a type name, like `float` or `int`, followed by a number indicating the number of bits per element. A standard double-precision floating point value (what's used under the hood in Python's `float` object) takes up 8 bytes or 64 bits. Thus, this type is known in NumPy as `float64`. See Table 4-2 for a full listing of NumPy's supported data types.

Don't worry about memorizing the NumPy dtypes, especially if you're a new user. It's often only necessary to care about the general *kind* of data you're dealing with, whether floating point, complex, integer, boolean, string, or general Python object. When you need more control over how data are stored in memory and on disk, especially large data sets, it is good to know that you have control over the storage type.

Table 4-2. NumPy data types

Type	Type Code	Description
`int8, uint8`	`i1, u1`	Signed and unsigned 8-bit (1 byte) integer types
`int16, uint16`	`i2, u2`	Signed and unsigned 16-bit integer types
`int32, uint32`	`i4, u4`	Signed and unsigned 32-bit integer types
`int64, uint64`	`i8, u8`	Signed and unsigned 32-bit integer types
`float16`	`f2`	Half-precision floating point
`float32`	`f4 or f`	Standard single-precision floating point. Compatible with C float
`float64, float128`	`f8 or d`	Standard double-precision floating point. Compatible with C double and Python `float` object

Type	Type Code	Description
float128	f16 or g	Extended-precision floating point
complex64, complex128, complex256	c8, c16, c32	Complex numbers represented by two 32, 64, or 128 floats, respectively
bool	?	Boolean type storing True and False values
object	O	Python object type
string_	S	Fixed-length string type (1 byte per character). For example, to create a string dtype with length 10, use 'S10'.
unicode_	U	Fixed-length unicode type (number of bytes platform specific). Same specification semantics as string_ (e.g. 'U10').

You can explicitly convert or *cast* an array from one dtype to another using ndarray's `astype` method:

```
In [31]: arr = np.array([1, 2, 3, 4, 5])

In [32]: arr.dtype
Out[32]: dtype('int64')

In [33]: float_arr = arr.astype(np.float64)

In [34]: float_arr.dtype
Out[34]: dtype('float64')
```

In this example, integers were cast to floating point. If I cast some floating point numbers to be of integer dtype, the decimal part will be truncated:

```
In [35]: arr = np.array([3.7, -1.2, -2.6, 0.5, 12.9, 10.1])

In [36]: arr
Out[36]: array([  3.7,  -1.2,  -2.6,   0.5,  12.9,  10.1])

In [37]: arr.astype(np.int32)
Out[37]: array([ 3, -1, -2,  0, 12, 10], dtype=int32)
```

Should you have an array of strings representing numbers, you can use `astype` to convert them to numeric form:

```
In [38]: numeric_strings = np.array(['1.25', '-9.6', '42'], dtype=np.string_)

In [39]: numeric_strings.astype(float)
Out[39]: array([  1.25,  -9.6 ,  42.  ])
```

If casting were to fail for some reason (like a string that cannot be converted to `float64`), a `TypeError` will be raised. See that I was a bit lazy and wrote `float` instead of `np.float64`; NumPy is smart enough to alias the Python types to the equivalent dtypes.

You can also use another array's dtype attribute:

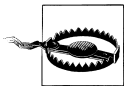
```
In [40]: int_array = np.arange(10)
```

```
In [41]: calibers = np.array([.22, .270, .357, .380, .44, .50], dtype=np.float64)

In [42]: int_array.astype(calibers.dtype)
Out[42]: array([ 0.,  1.,  2.,  3.,  4.,  5.,  6.,  7.,  8.,  9.])
```

There are shorthand type code strings you can also use to refer to a dtype:

```
In [43]: empty_uint32 = np.empty(8, dtype='u4')

In [44]: empty_uint32
Out[44]:
array([       0,        0, 65904672,        0, 64856792,        0,
       39438163,        0], dtype=uint32)
```

Calling `astype` *always* creates a new array (a copy of the data), even if the new dtype is the same as the old dtype.



It's worth keeping in mind that floating point numbers, such as those in `float64` and `float32` arrays, are only capable of approximating fractional quantities. In complex computations, you may accrue some *floating point error*, making comparisons only valid up to a certain number of decimal places.

Operations between Arrays and Scalars

Arrays are important because they enable you to express batch operations on data without writing any `for` loops. This is usually called *vectorization*. Any arithmetic operations between equal-size arrays applies the operation elementwise:

```
In [45]: arr = np.array([[1., 2., 3.], [4., 5., 6.]])

In [46]: arr
Out[46]:
array([[ 1.,  2.,  3.],
       [ 4.,  5.,  6.]])

In [47]: arr * arr
Out[47]:
array([[  1.,   4.,   9.],
       [ 16.,  25.,  36.]])

In [48]: arr - arr
Out[48]:
array([[ 0.,  0.,  0.],
       [ 0.,  0.,  0.]])
```

Arithmetic operations with scalars are as you would expect, propagating the value to each element:

```
In [49]: 1 / arr
Out[49]:
array([[ 1.    ,  0.5   ,  0.3333],
       [ 0.25  ,  0.2   ,  0.1667]])

In [50]: arr ** 0.5
Out[50]:
array([[ 1.    ,  1.4142,  1.7321],
       [ 2.    ,  2.2361,  2.4495]])
```

Operations between differently sized arrays is called *broadcasting* and will be discussed in more detail in Chapter 12. Having a deep understanding of broadcasting is not necessary for most of this book.

Basic Indexing and Slicing

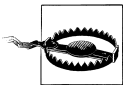
NumPy array indexing is a rich topic, as there are many ways you may want to select a subset of your data or individual elements. One-dimensional arrays are simple; on the surface they act similarly to Python lists:

```
In [51]: arr = np.arange(10)

In [52]: arr
Out[52]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])

In [53]: arr[5]
Out[53]: 5

In [54]: arr[5:8]
Out[54]: array([5, 6, 7])

In [55]: arr[5:8] = 12

In [56]: arr
Out[56]: array([ 0,  1,  2,  3,  4, 12, 12, 12,  8,  9])
```

As you can see, if you assign a scalar value to a slice, as in `arr[5:8] = 12`, the value is propagated (or *broadcasted* henceforth) to the entire selection. An important first distinction from lists is that array slices are *views* on the original array. This means that the data is not copied, and any modifications to the view will be reflected in the source array:

```
In [57]: arr_slice = arr[5:8]

In [58]: arr_slice[1] = 12345

In [59]: arr
Out[59]: array([    0,     1,     2,     3,     4,    12, 12345,    12,     8,     9])

In [60]: arr_slice[:] = 64

In [61]: arr
Out[61]: array([ 0,  1,  2,  3,  4, 64, 64, 64,  8,  9])
```

If you are new to NumPy, you might be surprised by this, especially if they have used other array programming languages which copy data more zealously. As NumPy has been designed with large data use cases in mind, you could imagine performance and memory problems if NumPy insisted on copying data left and right.



If you want a copy of a slice of an ndarray instead of a view, you will need to explicitly copy the array; for example `arr[5:8].copy()`.

With higher dimensional arrays, you have many more options. In a two-dimensional array, the elements at each index are no longer scalars but rather one-dimensional arrays:

```
In [62]: arr2d = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])

In [63]: arr2d[2]
Out[63]: array([7, 8, 9])
```

Thus, individual elements can be accessed recursively. But that is a bit too much work, so you can pass a comma-separated list of indices to select individual elements. So these are equivalent:

```
In [64]: arr2d[0][2]
Out[64]: 3

In [65]: arr2d[0, 2]
Out[65]: 3
```

See Figure 4-1 for an illustration of indexing on a 2D array.

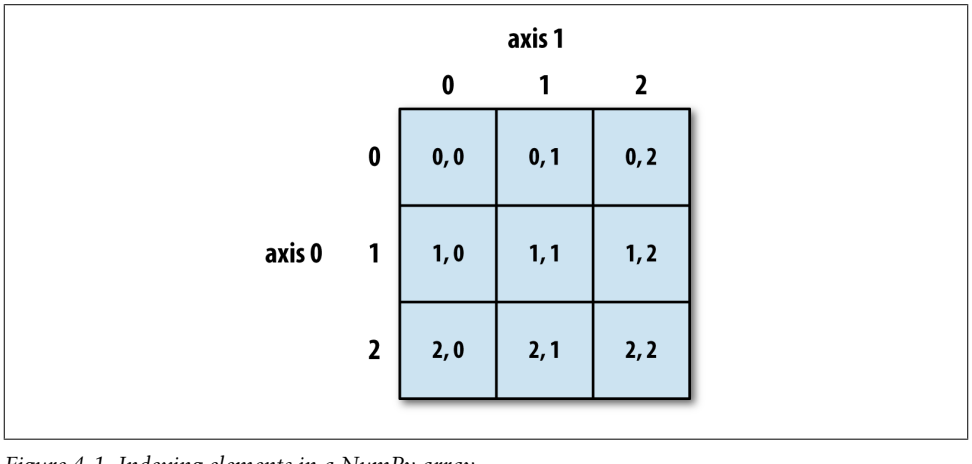


Figure 4-1. Indexing elements in a NumPy array

In multidimensional arrays, if you omit later indices, the returned object will be a lower-dimensional ndarray consisting of all the data along the higher dimensions. So in the 2 × 2 × 3 array `arr3d`

```
In [66]: arr3d = np.array([[[1, 2, 3], [4, 5, 6]], [[7, 8, 9], [10, 11, 12]]])

In [67]: arr3d
Out[67]:
array([[[ 1,  2,  3],
```

```
         [ 4,  5,  6]],
        [[ 7,  8,  9],
         [10, 11, 12]]])
```

`arr3d[0]` is a 2 × 3 array:

```
In [68]: arr3d[0]
Out[68]:
array([[1, 2, 3],
       [4, 5, 6]])
```

Both scalar values and arrays can be assigned to `arr3d[0]`:

```
In [69]: old_values = arr3d[0].copy()

In [70]: arr3d[0] = 42

In [71]: arr3d
Out[71]:
array([[[42, 42, 42],
        [42, 42, 42]],
       [[ 7,  8,  9],
        [10, 11, 12]]])

In [72]: arr3d[0] = old_values

In [73]: arr3d
Out[73]:
array([[[ 1,  2,  3],
        [ 4,  5,  6]],
       [[ 7,  8,  9],
        [10, 11, 12]]])
```

Similarly, `arr3d[1, 0]` gives you all of the values whose indices start with `(1, 0)`, forming a 1-dimensional array:

```
In [74]: arr3d[1, 0]
Out[74]: array([7, 8, 9])
```

Note that in all of these cases where subsections of the array have been selected, the returned arrays are views.

Indexing with slices

Like one-dimensional objects such as Python lists, ndarrays can be sliced using the familiar syntax:

```
In [75]: arr[1:6]
Out[75]: array([ 1,  2,  3,  4, 64])
```

Higher dimensional objects give you more options as you can slice one or more axes and also mix integers. Consider the 2D array above, `arr2d`. Slicing this array is a bit different:

```
In [76]: arr2d
Out[76]:
```

```
In [77]: arr2d[:2]
Out[77]:
```

```
array([[1, 2, 3],         array([[1, 2, 3],
       [4, 5, 6],                [4, 5, 6]])
       [7, 8, 9]])
```

As you can see, it has sliced along axis 0, the first axis. A slice, therefore, selects a range of elements along an axis. You can pass multiple slices just like you can pass multiple indexes:

```
In [78]: arr2d[:2, 1:]
Out[78]:
array([[2, 3],
       [5, 6]])
```

When slicing like this, you always obtain array views of the same number of dimensions. By mixing integer indexes and slices, you get lower dimensional slices:

```
In [79]: arr2d[1, :2]         In [80]: arr2d[2, :1]
Out[79]: array([4, 5])        Out[80]: array([7])
```

See Figure 4-2 for an illustration. Note that a colon by itself means to take the entire axis, so you can slice only higher dimensional axes by doing:

```
In [81]: arr2d[:, :1]
Out[81]:
array([[1],
       [4],
       [7]])
```

Of course, assigning to a slice expression assigns to the whole selection:

```
In [82]: arr2d[:2, 1:] = 0
```

Boolean Indexing

Let's consider an example where we have some data in an array and an array of names with duplicates. I'm going to use here the `randn` function in `numpy.random` to generate some random normally distributed data:

```
In [83]: names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])

In [84]: data = randn(7, 4)

In [85]: names
Out[85]:
array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'],
      dtype='|S4')

In [86]: data
Out[86]:
array([[-0.048 ,  0.5433, -0.2349,  1.2792],
       [-0.268 ,  0.5465,  0.0939, -2.0445],
       [-0.047 , -2.026 ,  0.7719,  0.3103],
       [ 2.1452,  0.8799, -0.0523,  0.0672],
       [-1.0023, -0.1698,  1.1503,  1.7289],
```

```
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174, -0.9297, -1.2564]])
```

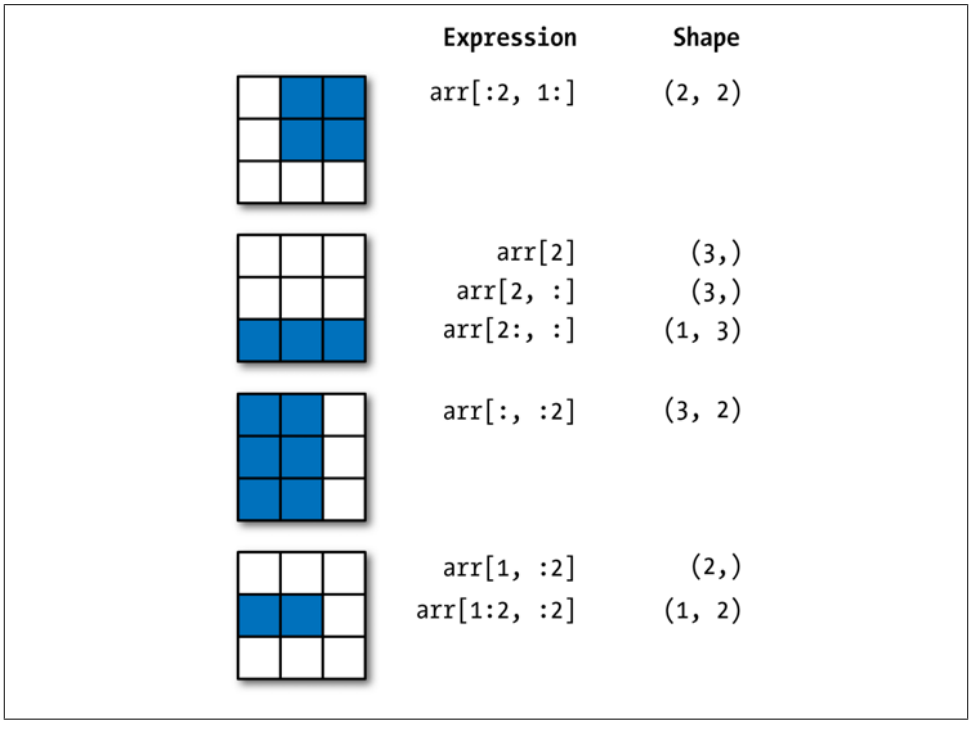


Figure 4-2. Two-dimensional array slicing

Suppose each name corresponds to a row in the `data` array. If we wanted to select all the rows with corresponding name `'Bob'`. Like arithmetic operations, comparisons (such as `==`) with arrays are also vectorized. Thus, comparing `names` with the string `'Bob'` yields a boolean array:

```
In [87]: names == 'Bob'
Out[87]: array([ True, False, False, True, False, False, False], dtype=bool)
```

This boolean array can be passed when indexing the array:

```
In [88]: data[names == 'Bob']
Out[88]:
array([[-0.048 ,  0.5433, -0.2349,  1.2792],
       [ 2.1452,  0.8799, -0.0523,  0.0672]])
```

The boolean array must be of the same length as the axis it's indexing. You can even mix and match boolean arrays with slices or integers (or sequences of integers, more on this later):

```
In [89]: data[names == 'Bob', 2:]
Out[89]:
array([[-0.2349,  1.2792],
```

```
       [-0.0523,  0.0672]])

In [90]: data[names == 'Bob', 3]
Out[90]: array([ 1.2792,  0.0672])
```

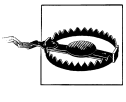
To select everything but `'Bob'`, you can either use `!=` or negate the condition using `-`:

```
In [91]: names != 'Bob'
Out[91]: array([False, True, True, False, True, True, True], dtype=bool)

In [92]: data[-(names == 'Bob')]
Out[92]:
array([[-0.268 ,  0.5465,  0.0939, -2.0445],
       [-0.047 , -2.026 ,  0.7719,  0.3103],
       [-1.0023, -0.1698,  1.1503,  1.7289],
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174, -0.9297, -1.2564]])
```

Selecting two of the three names to combine multiple boolean conditions, use boolean arithmetic operators like `&` (and) and `|` (or):

```
In [93]: mask = (names == 'Bob') | (names == 'Will')

In [94]: mask
Out[94]: array([True, False, True, True, True, False, False], dtype=bool)

In [95]: data[mask]
Out[95]:
array([[-0.048 ,  0.5433, -0.2349,  1.2792],
       [-0.047 , -2.026 ,  0.7719,  0.3103],
       [ 2.1452,  0.8799, -0.0523,  0.0672],
       [-1.0023, -0.1698,  1.1503,  1.7289]])
```

Selecting data from an array by boolean indexing *always* creates a copy of the data, even if the returned array is unchanged.



The Python keywords `and` and `or` do not work with boolean arrays.

Setting values with boolean arrays works in a common-sense way. To set all of the negative values in `data` to 0 we need only do:

```
In [96]: data[data < 0] = 0

In [97]: data
Out[97]:
array([[ 0.    ,  0.5433,  0.    ,  1.2792],
       [ 0.    ,  0.5465,  0.0939,  0.    ],
       [ 0.    ,  0.    ,  0.7719,  0.3103],
       [ 2.1452,  0.8799,  0.    ,  0.0672],
       [ 0.    ,  0.    ,  1.1503,  1.7289],
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174,  0.    ,  0.    ]])
```

Setting whole rows or columns using a 1D boolean array is also easy:

```
In [98]: data[names != 'Joe'] = 7

In [99]: data
Out[99]:
array([[ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 0.    ,  0.5465,  0.0939,  0.    ],
       [ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174,  0.    ,  0.    ]])
```

Fancy Indexing

Fancy indexing is a term adopted by NumPy to describe indexing using integer arrays. Suppose we had a 8 × 4 array:

```
In [100]: arr = np.empty((8, 4))

In [101]: for i in range(8):
   .....:     arr[i] = i

In [102]: arr
Out[102]:
array([[ 0.,  0.,  0.,  0.],
       [ 1.,  1.,  1.,  1.],
       [ 2.,  2.,  2.,  2.],
       [ 3.,  3.,  3.,  3.],
       [ 4.,  4.,  4.,  4.],
       [ 5.,  5.,  5.,  5.],
       [ 6.,  6.,  6.,  6.],
       [ 7.,  7.,  7.,  7.]])
```

To select out a subset of the rows in a particular order, you can simply pass a list or ndarray of integers specifying the desired order:

```
In [103]: arr[[4, 3, 0, 6]]
Out[103]:
array([[ 4.,  4.,  4.,  4.],
       [ 3.,  3.,  3.,  3.],
       [ 0.,  0.,  0.,  0.],
       [ 6.,  6.,  6.,  6.]])
```

Hopefully this code did what you expected! Using negative indices select rows from the end:

```
In [104]: arr[[-3, -5, -7]]
Out[104]:
array([[ 5.,  5.,  5.,  5.],
       [ 3.,  3.,  3.,  3.],
       [ 1.,  1.,  1.,  1.]])
```

Passing multiple index arrays does something slightly different; it selects a 1D array of elements corresponding to each tuple of indices:

```
# more on reshape in Chapter 12
In [105]: arr = np.arange(32).reshape((8, 4))

In [106]: arr
Out[106]:
array([[ 0,  1,  2,  3],
       [ 4,  5,  6,  7],
       [ 8,  9, 10, 11],
       [12, 13, 14, 15],
       [16, 17, 18, 19],
       [20, 21, 22, 23],
       [24, 25, 26, 27],
       [28, 29, 30, 31]])

In [107]: arr[[1, 5, 7, 2], [0, 3, 1, 2]]
Out[107]: array([ 4, 23, 29, 10])
```

Take a moment to understand what just happened: the elements `(1, 0)`, `(5, 3)`, `(7, 1)`, and `(2, 2)` were selected. The behavior of fancy indexing in this case is a bit different from what some users might have expected (myself included), which is the rectangular region formed by selecting a subset of the matrix's rows and columns. Here is one way to get that:

```
In [108]: arr[[1, 5, 7, 2]][:, [0, 3, 1, 2]]
Out[108]:
array([[ 4,  7,  5,  6],
       [20, 23, 21, 22],
       [28, 31, 29, 30],
       [ 8, 11,  9, 10]])
```

Another way is to use the `np.ix_` function, which converts two 1D integer arrays to an indexer that selects the square region:

```
In [109]: arr[np.ix_([1, 5, 7, 2], [0, 3, 1, 2])]
Out[109]:
array([[ 4,  7,  5,  6],
       [20, 23, 21, 22],
       [28, 31, 29, 30],
       [ 8, 11,  9, 10]])
```

Keep in mind that fancy indexing, unlike slicing, always copies the data into a new array.

Transposing Arrays and Swapping Axes

Transposing is a special form of reshaping which similarly returns a view on the underlying data without copying anything. Arrays have the `transpose` method and also the special `T` attribute:

```
In [110]: arr = np.arange(15).reshape((3, 5))

In [111]: arr                        In [112]: arr.T
```

```
Out[111]:
array([[ 0,  1,  2,  3,  4],
       [ 5,  6,  7,  8,  9],
       [10, 11, 12, 13, 14]])
```

```
Out[112]:
array([[ 0,  5, 10],
       [ 1,  6, 11],
       [ 2,  7, 12],
       [ 3,  8, 13],
       [ 4,  9, 14]])
```

When doing matrix computations, you will do this very often, like for example computing the inner matrix product X^TX using `np.dot`:

```
In [113]: arr = np.random.randn(6, 3)

In [114]: np.dot(arr.T, arr)
Out[114]:
array([[ 2.584 ,  1.8753,  0.8888],
       [ 1.8753,  6.6636,  0.3884],
       [ 0.8888,  0.3884,  3.9781]])
```

For higher dimensional arrays, `transpose` will accept a tuple of axis numbers to permute the axes (for extra mind bending):

```
In [115]: arr = np.arange(16).reshape((2, 2, 4))

In [116]: arr
Out[116]:
array([[[ 0,  1,  2,  3],
        [ 4,  5,  6,  7]],
       [[ 8,  9, 10, 11],
        [12, 13, 14, 15]]])

In [117]: arr.transpose((1, 0, 2))
Out[117]:
array([[[ 0,  1,  2,  3],
        [ 8,  9, 10, 11]],
       [[ 4,  5,  6,  7],
        [12, 13, 14, 15]]])
```

Simple transposing with `.T` is just a special case of swapping axes. ndarray has the method `swapaxes` which takes a pair of axis numbers:

```
In [118]: arr
Out[118]:
array([[[ 0,  1,  2,  3],
        [ 4,  5,  6,  7]],

       [[ 8,  9, 10, 11],
        [12, 13, 14, 15]]])
```

```
In [119]: arr.swapaxes(1, 2)
Out[119]:
array([[[ 0,  4],
        [ 1,  5],
        [ 2,  6],
        [ 3,  7]],

       [[ 8, 12],
        [ 9, 13],
        [10, 14],
        [11, 15]]])
```

`swapaxes` similarly returns a view on the data without making a copy.

Universal Functions: Fast Element-wise Array Functions

A universal function, or *ufunc*, is a function that performs elementwise operations on data in ndarrays. You can think of them as fast vectorized wrappers for simple functions that take one or more scalar values and produce one or more scalar results.

Many ufuncs are simple elementwise transformations, like `sqrt` or `exp`:

```
In [120]: arr = np.arange(10)

In [121]: np.sqrt(arr)
Out[121]:
array([ 0.    ,  1.    ,  1.4142,  1.7321,  2.    ,  2.2361,  2.4495,
        2.6458,  2.8284,  3.    ])

In [122]: np.exp(arr)
Out[122]:
array([    1.    ,     2.7183,     7.3891,    20.0855,    54.5982,
         148.4132,   403.4288,  1096.6332,  2980.958 ,  8103.0839])
```

These are referred to as *unary* ufuncs. Others, such as `add` or `maximum`, take 2 arrays (thus, *binary* ufuncs) and return a single array as the result:

```
In [123]: x = randn(8)

In [124]: y = randn(8)

In [125]: x
Out[125]:
array([ 0.0749,  0.0974,  0.2002, -0.2551,  0.4655,  0.9222,  0.446 ,
       -0.9337])

In [126]: y
Out[126]:
array([ 0.267 , -1.1131, -0.3361,  0.6117, -1.2323,  0.4788,  0.4315,
       -0.7147])

In [127]: np.maximum(x, y) # element-wise maximum
Out[127]:
array([ 0.267 ,  0.0974,  0.2002,  0.6117,  0.4655,  0.9222,  0.446 ,
       -0.7147])
```

While not common, a ufunc can return multiple arrays. `modf` is one example, a vectorized version of the built-in Python `divmod`: it returns the fractional and integral parts of a floating point array:

```
In [128]: arr = randn(7) * 5

In [129]: np.modf(arr)
Out[129]:
(array([-0.6808,  0.0636, -0.386 ,  0.1393, -0.8806,  0.9363, -0.883 ]),
 array([-2.,  4., -3.,  5., -3.,  3., -6.]))
```

See Table 4-3 and Table 4-4 for a listing of available ufuncs.

Table 4-3. Unary ufuncs

Function	Description
`abs, fabs`	Compute the absolute value element-wise for integer, floating point, or complex values. Use `fabs` as a faster alternative for non-complex-valued data
`sqrt`	Compute the square root of each element. Equivalent to `arr ** 0.5`
`square`	Compute the square of each element. Equivalent to `arr ** 2`
`exp`	Compute the exponent e^x of each element
`log, log10, log2, log1p`	Natural logarithm (base *e*), log base 10, log base 2, and log(1 + x), respectively
`sign`	Compute the sign of each element: 1 (positive), 0 (zero), or -1 (negative)
`ceil`	Compute the ceiling of each element, i.e. the smallest integer greater than or equal to each element
`floor`	Compute the floor of each element, i.e. the largest integer less than or equal to each element
`rint`	Round elements to the nearest integer, preserving the `dtype`
`modf`	Return fractional and integral parts of array as separate array
`isnan`	Return boolean array indicating whether each value is `NaN` (Not a Number)
`isfinite, isinf`	Return boolean array indicating whether each element is finite (non-`inf`, non-`NaN`) or infinite, respectively
`cos, cosh, sin, sinh, tan, tanh`	Regular and hyperbolic trigonometric functions
`arccos, arccosh, arcsin, arcsinh, arctan, arctanh`	Inverse trigonometric functions
`logical_not`	Compute truth value of `not x` element-wise. Equivalent to `-arr`.

Table 4-4. Binary universal functions

Function	Description
`add`	Add corresponding elements in arrays
`subtract`	Subtract elements in second array from first array
`multiply`	Multiply array elements
`divide, floor_divide`	Divide or floor divide (truncating the remainder)
`power`	Raise elements in first array to powers indicated in second array
`maximum, fmax`	Element-wise maximum. `fmax` ignores `NaN`
`minimum, fmin`	Element-wise minimum. `fmin` ignores `NaN`
`mod`	Element-wise modulus (remainder of division)
`copysign`	Copy sign of values in second argument to values in first argument

Function	Description
`greater, greater_equal, less, less_equal, equal, not_equal`	Perform element-wise comparison, yielding boolean array. Equivalent to infix operators `>, >=, <, <=, ==, !=`
`logical_and, logical_or, logical_xor`	Compute element-wise truth value of logical operation. Equivalent to infix operators `&, |, ^`

Data Processing Using Arrays

Using NumPy arrays enables you to express many kinds of data processing tasks as concise array expressions that might otherwise require writing loops. This practice of replacing explicit loops with array expressions is commonly referred to as *vectorization*. In general, vectorized array operations will often be one or two (or more) orders of magnitude faster than their pure Python equivalents, with the biggest impact in any kind of numerical computations. Later, in Chapter 12, I will explain *broadcasting*, a powerful method for vectorizing computations.

As a simple example, suppose we wished to evaluate the function `sqrt(x^2 + y^2)` across a regular grid of values. The `np.meshgrid` function takes two 1D arrays and produces two 2D matrices corresponding to all pairs of `(x, y)` in the two arrays:

```
In [130]: points = np.arange(-5, 5, 0.01) # 1000 equally spaced points

In [131]: xs, ys = np.meshgrid(points, points)

In [132]: ys
Out[132]:
array([[-5.  , -5.  , -5.  , ..., -5.  , -5.  , -5.  ],
       [-4.99, -4.99, -4.99, ..., -4.99, -4.99, -4.99],
       [-4.98, -4.98, -4.98, ..., -4.98, -4.98, -4.98],
       ...,
       [ 4.97,  4.97,  4.97, ...,  4.97,  4.97,  4.97],
       [ 4.98,  4.98,  4.98, ...,  4.98,  4.98,  4.98],
       [ 4.99,  4.99,  4.99, ...,  4.99,  4.99,  4.99]])
```

Now, evaluating the function is a simple matter of writing the same expression you would write with two points:

```
In [134]: import matplotlib.pyplot as plt

In [135]: z = np.sqrt(xs ** 2 + ys ** 2)

In [136]: z
Out[136]:
array([[ 7.0711,  7.064 ,  7.0569, ...,  7.0499,  7.0569,  7.064 ],
       [ 7.064 ,  7.0569,  7.0499, ...,  7.0428,  7.0499,  7.0569],
       [ 7.0569,  7.0499,  7.0428, ...,  7.0357,  7.0428,  7.0499],
       ...,
       [ 7.0499,  7.0428,  7.0357, ...,  7.0286,  7.0357,  7.0428],
       [ 7.0569,  7.0499,  7.0428, ...,  7.0357,  7.0428,  7.0499],
       [ 7.064 ,  7.0569,  7.0499, ...,  7.0428,  7.0499,  7.0569]])
```

While perhaps not immediately obvious, this `for` loop can be converted into a nested `where` expression:

```
np.where(cond1 & cond2, 0,
         np.where(cond1, 1,
                  np.where(cond2, 2, 3)))
```

In this particular example, we can also take advantage of the fact that boolean values are treated as 0 or 1 in calculations, so this could alternatively be expressed (though a bit more cryptically) as an arithmetic operation:

```
result = 1 * cond1 + 2 * cond2 + 3 * -(cond1 | cond2)
```

Mathematical and Statistical Methods

A set of mathematical functions which compute statistics about an entire array or about the data along an axis are accessible as array methods. Aggregations (often called *reductions*) like `sum`, `mean`, and standard deviation `std` can either be used by calling the array instance method or using the top level NumPy function:

```
In [151]: arr = np.random.randn(5, 4) # normally-distributed data

In [152]: arr.mean()
Out[152]: 0.062814911084854597

In [153]: np.mean(arr)
Out[153]: 0.062814911084854597

In [154]: arr.sum()
Out[154]: 1.2562982216970919
```

Functions like `mean` and `sum` take an optional `axis` argument which computes the statistic over the given axis, resulting in an array with one fewer dimension:

```
In [155]: arr.mean(axis=1)
Out[155]: array([-1.2833,  0.2844,  0.6574,  0.6743, -0.0187])

In [156]: arr.sum(0)
Out[156]: array([-3.1003, -1.6189,  1.4044,  4.5712])
```

Other methods like `cumsum` and `cumprod` do not aggregate, instead producing an array of the intermediate results:

```
In [157]: arr = np.array([[0, 1, 2], [3, 4, 5], [6, 7, 8]])

In [158]: arr.cumsum(0)
Out[158]:
array([[ 0,  1,  2],
       [ 3,  5,  7],
       [ 9, 12, 15]])

In [159]: arr.cumprod(1)
Out[159]:
array([[  0,   0,   0],
       [  3,  12,  60],
       [  6,  42, 336]])
```

See Table 4-5 for a full listing. We'll see many examples of these methods in action in later chapters.

```
Out[205]:
array([[ 1.,  0.,  0.,  0., -0.],
       [ 0.,  1., -0.,  0.,  0.],
       [ 0., -0.,  1.,  0.,  0.],
       [ 0., -0., -0.,  1., -0.],
       [ 0.,  0.,  0.,  0.,  1.]])

In [206]: q, r = qr(mat)

In [207]: r
Out[207]:
array([[ -6.9271,   7.389 ,   6.1227,  -7.1163,  -4.9215],
       [  0.    ,  -3.9735,  -0.8671,   2.9747,  -5.7402],
       [  0.    ,   0.    , -10.2681,   1.8909,   1.6079],
       [  0.    ,   0.    ,   0.    ,  -1.2996,   3.3577],
       [  0.    ,   0.    ,   0.    ,   0.    ,   0.5571]])
```

See Table 4-7 for a list of some of the most commonly-used linear algebra functions.

The scientific Python community is hopeful that there may be a matrix multiplication infix operator implemented someday, providing syntactically nicer alternative to using `np.dot`. But for now this is the way.

Table 4-7. Commonly-used numpy.linalg functions

Function	Description
`diag`	Return the diagonal (or off-diagonal) elements of a square matrix as a 1D array, or convert a 1D array into a square matrix with zeros on the off-diagonal
`dot`	Matrix multiplication
`trace`	Compute the sum of the diagonal elements
`det`	Compute the matrix determinant
`eig`	Compute the eigenvalues and eigenvectors of a square matrix
`inv`	Compute the inverse of a square matrix
`pinv`	Compute the Moore-Penrose pseudo-inverse inverse of a square matrix
`qr`	Compute the QR decomposition
`svd`	Compute the singular value decomposition (SVD)
`solve`	Solve the linear system Ax = b for x, where A is a square matrix
`lstsq`	Compute the least-squares solution to y = Xb

Random Number Generation

The `numpy.random` module supplements the built-in Python `random` with functions for efficiently generating whole arrays of sample values from many kinds of probability

distributions. For example, you can get a 4 by 4 array of samples from the standard normal distribution using `normal`:

```
In [208]: samples = np.random.normal(size=(4, 4))

In [209]: samples
Out[209]:
array([[ 0.1241,  0.3026,  0.5238,  0.0009],
       [ 1.3438, -0.7135, -0.8312, -2.3702],
       [-1.8608, -0.8608,  0.5601, -1.2659],
       [ 0.1198, -1.0635,  0.3329, -2.3594]])
```

Python's built-in `random` module, by contrast, only samples one value at a time. As you can see from this benchmark, `numpy.random` is well over an order of magnitude faster for generating very large samples:

```
In [210]: from random import normalvariate

In [211]: N = 1000000

In [212]: %timeit samples = [normalvariate(0, 1) for _ in xrange(N)]
1 loops, best of 3: 1.33 s per loop

In [213]: %timeit np.random.normal(size=N)
10 loops, best of 3: 57.7 ms per loop
```

See table Table 4-8 for a partial list of functions available in `numpy.random`. I'll give some examples of leveraging these functions' ability to generate large arrays of samples all at once in the next section.

Table 4-8. Partial list of numpy.random functions

Function	Description
`seed`	Seed the random number generator
`permutation`	Return a random permutation of a sequence, or return a permuted range
`shuffle`	Randomly permute a sequence in place
`rand`	Draw samples from a uniform distribution
`randint`	Draw random integers from a given low-to-high range
`randn`	Draw samples from a normal distribution with mean 0 and standard deviation 1 (MATLAB-like interface)
`binomial`	Draw samples a binomial distribution
`normal`	Draw samples from a normal (Gaussian) distribution
`beta`	Draw samples from a beta distribution
`chisquare`	Draw samples from a chi-square distribution
`gamma`	Draw samples from a gamma distribution
`uniform`	Draw samples from a uniform [0, 1) distribution

Example: Random Walks

An illustrative application of utilizing array operations is in the simulation of random walks. Let's first consider a simple random walk starting at 0 with steps of 1 and -1 occurring with equal probability. A pure Python way to implement a single random walk with 1,000 steps using the built-in `random` module:

```
import random
position = 0
walk = [position]
steps = 1000
for i in xrange(steps):
    step = 1 if random.randint(0, 1) else -1
    position += step
    walk.append(position)
```

See Figure 4-4 for an example plot of the first 100 values on one of these random walks.

Figure 4-4. A simple random walk

You might make the observation that `walk` is simply the cumulative sum of the random steps and could be evaluated as an array expression. Thus, I use the `np.random` module to draw 1,000 coin flips at once, set these to 1 and -1, and compute the cumulative sum:

```
In [215]: nsteps = 1000

In [216]: draws = np.random.randint(0, 2, size=nsteps)

In [217]: steps = np.where(draws > 0, 1, -1)

In [218]: walk = steps.cumsum()
```

From this we can begin to extract statistics like the minimum and maximum value along the walk's trajectory:

```
In [219]: walk.min()
Out[219]: -3
```

```
In [220]: walk.max()
Out[220]: 31
```

A more complicated statistic is the *first crossing time*, the step at which the random walk reaches a particular value. Here we might want to know how long it took the random walk to get at least 10 steps away from the origin 0 in either direction. `np.abs(walk) >= 10` gives us a boolean array indicating where the walk has reached or exceeded 10, but we want the index of the *first* 10 or -10. Turns out this can be computed using `argmax`, which returns the first index of the maximum value in the boolean array (`True` is the maximum value):

```
In [221]: (np.abs(walk) >= 10).argmax()
Out[221]: 37
```

Note that using `argmax` here is not always efficient because it always makes a full scan of the array. In this special case once a `True` is observed we know it to be the maximum value.

Simulating Many Random Walks at Once

If your goal was to simulate many random walks, say 5,000 of them, you can generate all of the random walks with minor modifications to the above code. The `numpy.random` functions if passed a 2-tuple will generate a 2D array of draws, and we can compute the cumulative sum across the rows to compute all 5,000 random walks in one shot:

```
In [222]: nwalks = 5000

In [223]: nsteps = 1000

In [224]: draws = np.random.randint(0, 2, size=(nwalks, nsteps)) # 0 or 1

In [225]: steps = np.where(draws > 0, 1, -1)

In [226]: walks = steps.cumsum(1)

In [227]: walks
Out[227]:
array([[  1,   0,   1, ...,   8,   7,   8],
       [  1,   0,  -1, ...,  34,  33,  32],
       [  1,   0,  -1, ...,   4,   5,   4],
       ...,
       [  1,   2,   1, ...,  24,  25,  26],
       [  1,   2,   3, ...,  14,  13,  14],
       [ -1,  -2,  -3, ..., -24, -23, -22]])
```

Now, we can compute the maximum and minimum values obtained over all of the walks:

```
In [228]: walks.max()
Out[228]: 138
```

```
In [229]: walks.min()
Out[229]: -133
```

Out of these walks, let's compute the minimum crossing time to 30 or -30. This is slightly tricky because not all 5,000 of them reach 30. We can check this using the `any` method:

```
In [230]: hits30 = (np.abs(walks) >= 30).any(1)

In [231]: hits30
Out[231]: array([False, True, False, ..., False, True, False], dtype=bool)

In [232]: hits30.sum() # Number that hit 30 or -30
Out[232]: 3410
```

We can use this boolean array to select out the rows of `walks` that actually cross the absolute 30 level and call `argmax` across axis 1 to get the crossing times:

```
In [233]: crossing_times = (np.abs(walks[hits30]) >= 30).argmax(1)

In [234]: crossing_times.mean()
Out[234]: 498.88973607038122
```

Feel free to experiment with other distributions for the steps other than equal sized coin flips. You need only use a different random number generation function, like `normal` to generate normally distributed steps with some mean and standard deviation:

```
In [235]: steps = np.random.normal(loc=0, scale=0.25,
   .....:                          size=(nwalks, nsteps))
```

CHAPTER 5
Getting Started with pandas

pandas will be the primary library of interest throughout much of the rest of the book. It contains high-level data structures and manipulation tools designed to make data analysis fast and easy in Python. pandas is built on top of NumPy and makes it easy to use in NumPy-centric applications.

As a bit of background, I started building pandas in early 2008 during my tenure at AQR, a quantitative investment management firm. At the time, I had a distinct set of requirements that were not well-addressed by any single tool at my disposal:

- Data structures with labeled axes supporting automatic or explicit data alignment. This prevents common errors resulting from misaligned data and working with differently-indexed data coming from different sources.
- Integrated time series functionality.
- The same data structures handle both time series data and non-time series data.
- Arithmetic operations and reductions (like summing across an axis) would pass on the metadata (axis labels).
- Flexible handling of missing data.
- Merge and other relational operations found in popular database databases (SQL-based, for example).

I wanted to be able to do all of these things in one place, preferably in a language well-suited to general purpose software development. Python was a good candidate language for this, but at that time there was not an integrated set of data structures and tools providing this functionality.

Over the last four years, pandas has matured into a quite large library capable of solving a much broader set of data handling problems than I ever anticipated, but it has expanded in its scope without compromising the simplicity and ease-of-use that I desired from the very beginning. I hope that after reading this book, you will find it to be just as much of an indispensable tool as I do.

Throughout the rest of the book, I use the following import conventions for pandas:

```
In [1]: from pandas import Series, DataFrame

In [2]: import pandas as pd
```

Thus, whenever you see `pd.` in code, it's referring to pandas. Series and DataFrame are used so much that I find it easier to import them into the local namespace.

Introduction to pandas Data Structures

To get started with pandas, you will need to get comfortable with its two workhorse data structures: *Series* and *DataFrame*. While they are not a universal solution for every problem, they provide a solid, easy-to-use basis for most applications.

Series

A Series is a one-dimensional array-like object containing an array of data (of any NumPy data type) and an associated array of data labels, called its *index*. The simplest Series is formed from only an array of data:

```
In [4]: obj = Series([4, 7, -5, 3])

In [5]: obj
Out[5]:
0    4
1    7
2   -5
3    3
```

The string representation of a Series displayed interactively shows the index on the left and the values on the right. Since we did not specify an index for the data, a default one consisting of the integers 0 through N - 1 (where N is the length of the data) is created. You can get the array representation and index object of the Series via its values and index attributes, respectively:

```
In [6]: obj.values
Out[6]: array([ 4,  7, -5,  3])

In [7]: obj.index
Out[7]: Int64Index([0, 1, 2, 3])
```

Often it will be desirable to create a Series with an index identifying each data point:

```
In [8]: obj2 = Series([4, 7, -5, 3], index=['d', 'b', 'a', 'c'])

In [9]: obj2
Out[9]:
d    4
b    7
a   -5
c    3
```

```
In [10]: obj2.index
Out[10]: Index([d, b, a, c], dtype=object)
```

Compared with a regular NumPy array, you can use values in the index when selecting single values or a set of values:

```
In [11]: obj2['a']
Out[11]: -5

In [12]: obj2['d'] = 6

In [13]: obj2[['c', 'a', 'd']]
Out[13]:
c    3
a   -5
d    6
```

NumPy array operations, such as filtering with a boolean array, scalar multiplication, or applying math functions, will preserve the index-value link:

```
In [14]: obj2
Out[14]:
d    6
b    7
a   -5
c    3

In [15]: obj2[obj2 > 0]
Out[15]:
d    6
b    7
c    3

In [16]: obj2 * 2
Out[16]:
d    12
b    14
a   -10
c     6

In [17]: np.exp(obj2)
Out[17]:
d     403.428793
b    1096.633158
a       0.006738
c      20.085537
```

Another way to think about a Series is as a fixed-length, ordered dict, as it is a mapping of index values to data values. It can be substituted into many functions that expect a dict:

```
In [18]: 'b' in obj2
Out[18]: True

In [19]: 'e' in obj2
Out[19]: False
```

Should you have data contained in a Python dict, you can create a Series from it by passing the dict:

```
In [20]: sdata = {'Ohio': 35000, 'Texas': 71000, 'Oregon': 16000, 'Utah': 5000}

In [21]: obj3 = Series(sdata)

In [22]: obj3
Out[22]:
Ohio      35000
Oregon    16000
```

```
Texas     71000
Utah       5000
```

When only passing a dict, the index in the resulting Series will have the dict's keys in sorted order.

```
In [23]: states = ['California', 'Ohio', 'Oregon', 'Texas']

In [24]: obj4 = Series(sdata, index=states)

In [25]: obj4
Out[25]:
California      NaN
Ohio          35000
Oregon        16000
Texas         71000
```

In this case, 3 values found in `sdata` were placed in the appropriate locations, but since no value for `'California'` was found, it appears as `NaN` (not a number) which is considered in pandas to mark missing or *NA* values. I will use the terms "missing" or "NA" to refer to missing data. The `isnull` and `notnull` functions in pandas should be used to detect missing data:

```
In [26]: pd.isnull(obj4)
Out[26]:
California     True
Ohio          False
Oregon        False
Texas         False

In [27]: pd.notnull(obj4)
Out[27]:
California    False
Ohio           True
Oregon         True
Texas          True
```

Series also has these as instance methods:

```
In [28]: obj4.isnull()
Out[28]:
California     True
Ohio          False
Oregon        False
Texas         False
```

I discuss working with missing data in more detail later in this chapter.

A critical Series feature for many applications is that it automatically aligns differently-indexed data in arithmetic operations:

```
In [29]: obj3
Out[29]:
Ohio      35000
Oregon    16000
Texas     71000
Utah       5000

In [30]: obj4
Out[30]:
California      NaN
Ohio          35000
Oregon        16000
Texas         71000

In [31]: obj3 + obj4
Out[31]:
California       NaN
Ohio           70000
Oregon         32000
```

```
Texas         142000
Utah             NaN
```

Data alignment features are addressed as a separate topic.

Both the Series object itself and its index have a `name` attribute, which integrates with other key areas of pandas functionality:

```
In [32]: obj4.name = 'population'

In [33]: obj4.index.name = 'state'

In [34]: obj4
Out[34]:
state
California      NaN
Ohio          35000
Oregon        16000
Texas         71000
Name: population
```

A Series's index can be altered in place by assignment:

```
In [35]: obj.index = ['Bob', 'Steve', 'Jeff', 'Ryan']

In [36]: obj
Out[36]:
Bob      4
Steve    7
Jeff    -5
Ryan     3
```

DataFrame

A DataFrame represents a tabular, spreadsheet-like data structure containing an ordered collection of columns, each of which can be a different value type (numeric, string, boolean, etc.). The DataFrame has both a row and column index; it can be thought of as a dict of Series (one for all sharing the same index). Compared with other such DataFrame-like structures you may have used before (like R's `data.frame`), row-oriented and column-oriented operations in DataFrame are treated roughly symmetrically. Under the hood, the data is stored as one or more two-dimensional blocks rather than a list, dict, or some other collection of one-dimensional arrays. The exact details of DataFrame's internals are far outside the scope of this book.

While DataFrame stores the data internally in a two-dimensional format, you can easily represent much higher-dimensional data in a tabular format using hierarchical indexing, a subject of a later section and a key ingredient in many of the more advanced data-handling features in pandas.

There are numerous ways to construct a DataFrame, though one of the most common is from a dict of equal-length lists or NumPy arrays

```
data = {'state': ['Ohio', 'Ohio', 'Ohio', 'Nevada', 'Nevada'],
        'year': [2000, 2001, 2002, 2001, 2002],
        'pop': [1.5, 1.7, 3.6, 2.4, 2.9]}
frame = DataFrame(data)
```

The resulting DataFrame will have its index assigned automatically as with Series, and the columns are placed in sorted order:

```
In [38]: frame
Out[38]:
   pop   state  year
0  1.5    Ohio  2000
1  1.7    Ohio  2001
2  3.6    Ohio  2002
3  2.4  Nevada  2001
4  2.9  Nevada  2002
```

If you specify a sequence of columns, the DataFrame's columns will be exactly what you pass:

```
In [39]: DataFrame(data, columns=['year', 'state', 'pop'])
Out[39]:
   year   state  pop
0  2000    Ohio  1.5
1  2001    Ohio  1.7
2  2002    Ohio  3.6
3  2001  Nevada  2.4
4  2002  Nevada  2.9
```

As with Series, if you pass a column that isn't contained in `data`, it will appear with NA values in the result:

```
In [40]: frame2 = DataFrame(data, columns=['year', 'state', 'pop', 'debt'],
   ....:                    index=['one', 'two', 'three', 'four', 'five'])

In [41]: frame2
Out[41]:
       year   state  pop  debt
one    2000    Ohio  1.5   NaN
two    2001    Ohio  1.7   NaN
three  2002    Ohio  3.6   NaN
four   2001  Nevada  2.4   NaN
five   2002  Nevada  2.9   NaN

In [42]: frame2.columns
Out[42]: Index([year, state, pop, debt], dtype=object)
```

A column in a DataFrame can be retrieved as a Series either by dict-like notation or by attribute:

```
In [43]: frame2['state']        In [44]: frame2.year
Out[43]:                        Out[44]:
one        Ohio                 one      2000
```

```
two        Ohio                two      2001
three      Ohio                three    2002
four     Nevada                four     2001
five     Nevada                five     2002
Name: state                    Name: year
```

Note that the returned Series have the same index as the DataFrame, and their `name` attribute has been appropriately set.

Rows can also be retrieved by position or name by a couple of methods, such as the `ix` indexing field (much more on this later):

```
In [45]: frame2.ix['three']
Out[45]:
year     2002
state    Ohio
pop       3.6
debt      NaN
Name: three
```

Columns can be modified by assignment. For example, the empty `'debt'` column could be assigned a scalar value or an array of values:

```
In [46]: frame2['debt'] = 16.5

In [47]: frame2
Out[47]:
       year   state  pop  debt
one    2000    Ohio  1.5  16.5
two    2001    Ohio  1.7  16.5
three  2002    Ohio  3.6  16.5
four   2001  Nevada  2.4  16.5
five   2002  Nevada  2.9  16.5

In [48]: frame2['debt'] = np.arange(5.)

In [49]: frame2
Out[49]:
       year   state  pop  debt
one    2000    Ohio  1.5     0
two    2001    Ohio  1.7     1
three  2002    Ohio  3.6     2
four   2001  Nevada  2.4     3
five   2002  Nevada  2.9     4
```

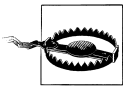
When assigning lists or arrays to a column, the value's length must match the length of the DataFrame. If you assign a Series, it will be instead conformed exactly to the DataFrame's index, inserting missing values in any holes:

```
In [50]: val = Series([-1.2, -1.5, -1.7], index=['two', 'four', 'five'])

In [51]: frame2['debt'] = val

In [52]: frame2
Out[52]:
       year   state  pop  debt
```

```
one    2000    Ohio  1.5   NaN
two    2001    Ohio  1.7  -1.2
three  2002    Ohio  3.6   NaN
four   2001  Nevada  2.4  -1.5
five   2002  Nevada  2.9  -1.7
```

Assigning a column that doesn't exist will create a new column. The `del` keyword will delete columns as with a dict:

```
In [53]: frame2['eastern'] = frame2.state == 'Ohio'

In [54]: frame2
Out[54]:
       year   state  pop  debt eastern
one    2000    Ohio  1.5   NaN    True
two    2001    Ohio  1.7  -1.2    True
three  2002    Ohio  3.6   NaN    True
four   2001  Nevada  2.4  -1.5   False
five   2002  Nevada  2.9  -1.7   False

In [55]: del frame2['eastern']

In [56]: frame2.columns
Out[56]: Index([year, state, pop, debt], dtype=object)
```



The column returned when indexing a DataFrame is a *view* on the underlying data, not a copy. Thus, any in-place modifications to the Series will be reflected in the DataFrame. The column can be explicitly copied using the Series's `copy` method.

Another common form of data is a nested dict of dicts format:

```
In [57]: pop = {'Nevada': {2001: 2.4, 2002: 2.9},
   ....:        'Ohio': {2000: 1.5, 2001: 1.7, 2002: 3.6}}
```

If passed to DataFrame, it will interpret the outer dict keys as the columns and the inner keys as the row indices:

```
In [58]: frame3 = DataFrame(pop)

In [59]: frame3
Out[59]:
      Nevada  Ohio
2000     NaN   1.5
2001     2.4   1.7
2002     2.9   3.6
```

Of course you can always transpose the result:

```
In [60]: frame3.T
Out[60]:
        2000  2001  2002
Nevada   NaN   2.4   2.9
Ohio     1.5   1.7   3.6
```

The keys in the inner dicts are unioned and sorted to form the index in the result. This isn't true if an explicit index is specified:

```
In [61]: DataFrame(pop, index=[2001, 2002, 2003])
Out[61]:
      Nevada  Ohio
2001     2.4   1.7
2002     2.9   3.6
2003     NaN   NaN
```

Dicts of Series are treated much in the same way:

```
In [62]: pdata = {'Ohio': frame3['Ohio'][:-1],
   ....:          'Nevada': frame3['Nevada'][:2]}

In [63]: DataFrame(pdata)
Out[63]:
      Nevada  Ohio
2000     NaN   1.5
2001     2.4   1.7
```

For a complete list of things you can pass the DataFrame constructor, see Table 5-1.

If a DataFrame's `index` and `columns` have their `name` attributes set, these will also be displayed:

```
In [64]: frame3.index.name = 'year'; frame3.columns.name = 'state'

In [65]: frame3
Out[65]:
state  Nevada  Ohio
year
2000      NaN   1.5
2001      2.4   1.7
2002      2.9   3.6
```

Like Series, the `values` attribute returns the data contained in the DataFrame as a 2D ndarray:

```
In [66]: frame3.values
Out[66]:
array([[ nan,  1.5],
       [ 2.4,  1.7],
       [ 2.9,  3.6]])
```

If the DataFrame's columns are different dtypes, the dtype of the values array will be chosen to accomodate all of the columns:

```
In [67]: frame2.values
Out[67]:
array([[2000, Ohio, 1.5, nan],
       [2001, Ohio, 1.7, -1.2],
       [2002, Ohio, 3.6, nan],
       [2001, Nevada, 2.4, -1.5],
       [2002, Nevada, 2.9, -1.7]], dtype=object)
```

Table 5-1. Possible data inputs to DataFrame constructor

Type	Notes
2D ndarray	A matrix of data, passing optional row and column labels
dict of arrays, lists, or tuples	Each sequence becomes a column in the DataFrame. All sequences must be the same length.
NumPy structured/record array	Treated as the "dict of arrays" case
dict of Series	Each value becomes a column. Indexes from each Series are unioned together to form the result's row index if no explicit index is passed.
dict of dicts	Each inner dict becomes a column. Keys are unioned to form the row index as in the "dict of Series" case.
list of dicts or Series	Each item becomes a row in the DataFrame. Union of dict keys or Series indexes become the DataFrame's column labels
List of lists or tuples	Treated as the "2D ndarray" case
Another DataFrame	The DataFrame's indexes are used unless different ones are passed
NumPy MaskedArray	Like the "2D ndarray" case except masked values become NA/missing in the DataFrame result

Index Objects

pandas's Index objects are responsible for holding the axis labels and other metadata (like the axis name or names). Any array or other sequence of labels used when constructing a Series or DataFrame is internally converted to an Index:

```
In [68]: obj = Series(range(3), index=['a', 'b', 'c'])

In [69]: index = obj.index

In [70]: index
Out[70]: Index([a, b, c], dtype=object)

In [71]: index[1:]
Out[71]: Index([b, c], dtype=object)
```

Index objects are immutable and thus can't be modified by the user:

```
In [72]: index[1] = 'd'
---------------------------------------------------------------------------
Exception                                 Traceback (most recent call last)
<ipython-input-72-676fdeb26a68> in <module>()
----> 1 index[1] = 'd'
/Users/wesm/code/pandas/pandas/core/index.pyc in __setitem__(self, key, value)
    302     def __setitem__(self, key, value):
    303         """Disable the setting of values."""
--> 304         raise Exception(str(self.__class__) + ' object is immutable')
    305
    306     def __getitem__(self, key):
Exception: <class 'pandas.core.index.Index'> object is immutable
```

Immutability is important so that Index objects can be safely shared among data structures:

```
In [73]: index = pd.Index(np.arange(3))

In [74]: obj2 = Series([1.5, -2.5, 0], index=index)

In [75]: obj2.index is index
Out[75]: True
```

Table 5-2 has a list of built-in Index classes in the library. With some development effort, Index can even be subclassed to implement specialized axis indexing functionality.

Many users will not need to know much about Index objects, but they're nonetheless an important part of pandas's data model.

Table 5-2. Main Index objects in pandas

Class	Description
`Index`	The most general Index object, representing axis labels in a NumPy array of Python objects.
`Int64Index`	Specialized Index for integer values.
`MultiIndex`	"Hierarchical" index object representing multiple levels of indexing on a single axis. Can be thought of as similar to an array of tuples.
`DatetimeIndex`	Stores nanosecond timestamps (represented using NumPy's `datetime64` dtype).
`PeriodIndex`	Specialized Index for Period data (timespans).

In addition to being array-like, an Index also functions as a fixed-size set:

```
In [76]: frame3
Out[76]:
state  Nevada  Ohio
year
2000      NaN   1.5
2001      2.4   1.7
2002      2.9   3.6

In [77]: 'Ohio' in frame3.columns
Out[77]: True

In [78]: 2003 in frame3.index
Out[78]: False
```

Each Index has a number of methods and properties for set logic and answering other common questions about the data it contains. These are summarized in Table 5-3.

Table 5-3. Index methods and properties

Method	Description
`append`	Concatenate with additional Index objects, producing a new Index
`diff`	Compute set difference as an Index
`intersection`	Compute set intersection
`union`	Compute set union
`isin`	Compute boolean array indicating whether each value is contained in the passed collection
`delete`	Compute new Index with element at index `i` deleted
`drop`	Compute new index by deleting passed values
`insert`	Compute new Index by inserting element at index `i`
`is_monotonic`	Returns `True` if each element is greater than or equal to the previous element
`is_unique`	Returns `True` if the Index has no duplicate values
`unique`	Compute the array of unique values in the Index

Essential Functionality

In this section, I'll walk you through the fundamental mechanics of interacting with the data contained in a Series or DataFrame. Upcoming chapters will delve more deeply into data analysis and manipulation topics using pandas. This book is not intended to serve as exhaustive documentation for the pandas library; I instead focus on the most important features, leaving the less common (that is, more esoteric) things for you to explore on your own.

Reindexing

A critical method on pandas objects is `reindex`, which means to create a new object with the data *conformed* to a new index. Consider a simple example from above:

```
In [79]: obj = Series([4.5, 7.2, -5.3, 3.6], index=['d', 'b', 'a', 'c'])

In [80]: obj
Out[80]:
d    4.5
b    7.2
a   -5.3
c    3.6
```

Calling `reindex` on this Series rearranges the data according to the new index, introducing missing values if any index values were not already present:

```
In [81]: obj2 = obj.reindex(['a', 'b', 'c', 'd', 'e'])

In [82]: obj2
Out[82]:
a   -5.3
```

```
b    7.2
c    3.6
d    4.5
e    NaN

In [83]: obj.reindex(['a', 'b', 'c', 'd', 'e'], fill_value=0)
Out[83]:
a   -5.3
b    7.2
c    3.6
d    4.5
e    0.0
```

For ordered data like time series, it may be desirable to do some interpolation or filling of values when reindexing. The `method` option allows us to do this, using a method such as `ffill` which forward fills the values:

```
In [84]: obj3 = Series(['blue', 'purple', 'yellow'], index=[0, 2, 4])

In [85]: obj3.reindex(range(6), method='ffill')
Out[85]:
0      blue
1      blue
2    purple
3    purple
4    yellow
5    yellow
```

Table 5-4 lists available `method` options. At this time, interpolation more sophisticated than forward- and backfilling would need to be applied after the fact.

Table 5-4. reindex method (interpolation) options

Argument	Description
`ffill` or `pad`	Fill (or carry) values forward
`bfill` or `backfill`	Fill (or carry) values backward

With DataFrame, `reindex` can alter either the (row) index, columns, or both. When passed just a sequence, the rows are reindexed in the result:

```
In [86]: frame = DataFrame(np.arange(9).reshape((3, 3)), index=['a', 'c', 'd'],
   ....:                   columns=['Ohio', 'Texas', 'California'])

In [87]: frame
Out[87]:
   Ohio  Texas  California
a     0      1           2
c     3      4           5
d     6      7           8

In [88]: frame2 = frame.reindex(['a', 'b', 'c', 'd'])

In [89]: frame2
Out[89]:
```

```
   Ohio  Texas  California
a     0      1           2
b   NaN    NaN         NaN
c     3      4           5
d     6      7           8
```

The columns can be reindexed using the `columns` keyword:

```
In [90]: states = ['Texas', 'Utah', 'California']

In [91]: frame.reindex(columns=states)
Out[91]:
   Texas  Utah  California
a      1   NaN           2
c      4   NaN           5
d      7   NaN           8
```

Both can be reindexed in one shot, though interpolation will only apply row-wise (axis 0):

```
In [92]: frame.reindex(index=['a', 'b', 'c', 'd'], method='ffill',
   ....:               columns=states)
Out[92]:
   Texas  Utah  California
a      1   NaN           2
b      1   NaN           2
c      4   NaN           5
d      7   NaN           8
```

As you'll see soon, reindexing can be done more succinctly by label-indexing with `ix`:

```
In [93]: frame.ix[['a', 'b', 'c', 'd'], states]
Out[93]:
   Texas  Utah  California
a      1   NaN           2
b    NaN   NaN         NaN
c      4   NaN           5
d      7   NaN           8
```

Table 5-5. reindex function arguments

Argument	Description
`index`	New sequence to use as index. Can be `Index` instance or any other sequence-like Python data structure. An `Index` will be used exactly as is without any copying
`method`	Interpolation (fill) method, see Table 5-4 for options.
`fill_value`	Substitute value to use when introducing missing data by reindexing
`limit`	When forward- or backfilling, maximum size gap to fill
`level`	Match simple Index on level of MultiIndex, otherwise select subset of
`copy`	Do not copy underlying data if new index is equivalent to old index. `True` by default (i.e. always copy data).

Dropping entries from an axis

Dropping one or more entries from an axis is easy if you have an index array or list without those entries. As that can require a bit of munging and set logic, the `drop` method will return a new object with the indicated value or values deleted from an axis:

```
In [94]: obj = Series(np.arange(5.), index=['a', 'b', 'c', 'd', 'e'])

In [95]: new_obj = obj.drop('c')

In [96]: new_obj
Out[96]:
a    0
b    1
d    3
e    4

In [97]: obj.drop(['d', 'c'])
Out[97]:
a    0
b    1
e    4
```

With DataFrame, index values can be deleted from either axis:

```
In [98]: data = DataFrame(np.arange(16).reshape((4, 4)),
   ....:                  index=['Ohio', 'Colorado', 'Utah', 'New York'],
   ....:                  columns=['one', 'two', 'three', 'four'])

In [99]: data.drop(['Colorado', 'Ohio'])
Out[99]:
          one  two  three  four
Utah        8    9     10    11
New York   12   13     14    15

In [100]: data.drop('two', axis=1)
Out[100]:
          one  three  four
Ohio        0      2     3
Colorado    4      6     7
Utah        8     10    11
New York   12     14    15

In [101]: data.drop(['two', 'four'], axis=1)
Out[101]:
          one  three
Ohio        0      2
Colorado    4      6
Utah        8     10
New York   12     14
```

Indexing, selection, and filtering

Series indexing (`obj[...]`) works analogously to NumPy array indexing, except you can use the Series's index values instead of only integers. Here are some examples this:

```
In [102]: obj = Series(np.arange(4.), index=['a', 'b', 'c', 'd'])

In [103]: obj['b']
Out[103]: 1.0

In [104]: obj[1]
Out[104]: 1.0

In [105]: obj[2:4]
Out[105]:

In [106]: obj[['b', 'a', 'd']]
Out[106]:
```

```
c    2                    b    1
d    3                    a    0
                          d    3

In [107]: obj[[1, 3]]     In [108]: obj[obj < 2]
Out[107]:                 Out[108]:
b    1                    a    0
d    3                    b    1
```

Slicing with labels behaves differently than normal Python slicing in that the endpoint is inclusive:

```
In [109]: obj['b':'c']
Out[109]:
b    1
c    2
```

Setting using these methods works just as you would expect:

```
In [110]: obj['b':'c'] = 5

In [111]: obj
Out[111]:
a    0
b    5
c    5
d    3
```

As you've seen above, indexing into a DataFrame is for retrieving one or more columns either with a single value or sequence:

```
In [112]: data = DataFrame(np.arange(16).reshape((4, 4)),
   .....:                  index=['Ohio', 'Colorado', 'Utah', 'New York'],
   .....:                  columns=['one', 'two', 'three', 'four'])

In [113]: data
Out[113]:
          one  two  three  four
Ohio        0    1      2     3
Colorado    4    5      6     7
Utah        8    9     10    11
New York   12   13     14    15

In [114]: data['two']     In [115]: data[['three', 'one']]
Out[114]:                 Out[115]:
Ohio         1                      three  one
Colorado     5            Ohio          2    0
Utah         9            Colorado      6    4
New York    13            Utah         10    8
Name: two                 New York     14   12
```

Indexing like this has a few special cases. First selecting rows by slicing or a boolean array:

```
In [116]: data[:2]                  In [117]: data[data['three'] > 5]
Out[116]:                           Out[117]:
          one  two  three  four                one  two  three  four
```

```
Ohio        0    1      2     3        Colorado    4    5      6     7
Colorado    4    5      6     7        Utah        8    9     10    11
                                       New York   12   13     14    15
```

This might seem inconsistent to some readers, but this syntax arose out of practicality and nothing more. Another use case is in indexing with a boolean DataFrame, such as one produced by a scalar comparison:

```
In [118]: data < 5
Out[118]:
            one    two  three   four
Ohio       True   True   True   True
Colorado   True  False  False  False
Utah      False  False  False  False
New York  False  False  False  False

In [119]: data[data < 5] = 0

In [120]: data
Out[120]:
          one  two  three  four
Ohio        0    0      0     0
Colorado    0    5      6     7
Utah        8    9     10    11
New York   12   13     14    15
```

This is intended to make DataFrame syntactically more like an ndarray in this case.

For DataFrame label-indexing on the rows, I introduce the special indexing field `ix`. It enables you to select a subset of the rows and columns from a DataFrame with NumPy-like notation plus axis labels. As I mentioned earlier, this is also a less verbose way to do reindexing:

```
In [121]: data.ix['Colorado', ['two', 'three']]
Out[121]:
two      5
three    6
Name: Colorado

In [122]: data.ix[['Colorado', 'Utah'], [3, 0, 1]]
Out[122]:
          four  one  two
Colorado     7    0    5
Utah        11    8    9

In [123]: data.ix[2]        In [124]: data.ix[:'Utah', 'two']
Out[123]:                   Out[124]:
one       8                 Ohio        0
two       9                 Colorado    5
three    10                 Utah        9
four     11                 Name: two
Name: Utah

In [125]: data.ix[data.three > 5, :3]
Out[125]:
```

```
          one  two  three
Colorado    0    5      6
Utah        8    9     10
New York   12   13     14
```

So there are many ways to select and rearrange the data contained in a pandas object. For DataFrame, there is a short summary of many of them in Table 5-6. You have a number of additional options when working with hierarchical indexes as you'll later see.

When designing pandas, I felt that having to type `frame[:, col]` to select a column was too verbose (and error-prone), since column selection is one of the most common operations. Thus I made the design trade-off to push all of the rich label-indexing into `ix`.

Table 5-6. Indexing options with DataFrame

Type	Notes
`obj[val]`	Select single column or sequence of columns from the DataFrame. Special case conveniences: boolean array (filter rows), slice (slice rows), or boolean DataFrame (set values based on some criterion).
`obj.ix[val]`	Selects single row of subset of rows from the DataFrame.
`obj.ix[:, val]`	Selects single column of subset of columns.
`obj.ix[val1, val2]`	Select both rows and columns.
`reindex` method	Conform one or more axes to new indexes.
`xs` method	Select single row or column as a Series by label.
`icol, irow` methods	Select single column or row, respectively, as a Series by integer location.
`get_value, set_value` methods	Select single value by row and column label.

Arithmetic and data alignment

One of the most important pandas features is the behavior of arithmetic between objects with different indexes. When adding together objects, if any index pairs are not the same, the respective index in the result will be the union of the index pairs. Let's look at a simple example:

```
In [126]: s1 = Series([7.3, -2.5, 3.4, 1.5], index=['a', 'c', 'd', 'e'])

In [127]: s2 = Series([-2.1, 3.6, -1.5, 4, 3.1], index=['a', 'c', 'e', 'f', 'g'])

In [128]: s1        In [129]: s2
Out[128]:           Out[129]:
a    7.3            a   -2.1
c   -2.5            c    3.6
d    3.4            e   -1.5
```

```
e    1.5           f    4.0
                   g    3.1
```

Adding these together yields:

```
In [130]: s1 + s2
Out[130]:
a    5.2
c    1.1
d    NaN
e    0.0
f    NaN
g    NaN
```

The internal data alignment introduces NA values in the indices that don't overlap. Missing values propagate in arithmetic computations.

In the case of DataFrame, alignment is performed on both the rows and the columns:

```
In [131]: df1 = DataFrame(np.arange(9.).reshape((3, 3)), columns=list('bcd'),
   .....:                 index=['Ohio', 'Texas', 'Colorado'])

In [132]: df2 = DataFrame(np.arange(12.).reshape((4, 3)), columns=list('bde'),
   .....:                 index=['Utah', 'Ohio', 'Texas', 'Oregon'])

In [133]: df1           In [134]: df2
Out[133]:               Out[134]:
          b  c  d                 b   d   e
Ohio      0  1  2       Utah      0   1   2
Texas     3  4  5       Ohio      3   4   5
Colorado  6  7  8       Texas     6   7   8
                         Oregon    9  10  11
```

Adding these together returns a DataFrame whose index and columns are the unions of the ones in each DataFrame:

```
In [135]: df1 + df2
Out[135]:
           b   c   d   e
Colorado NaN NaN NaN NaN
Ohio       3 NaN   6 NaN
Oregon   NaN NaN NaN NaN
Texas      9 NaN  12 NaN
Utah     NaN NaN NaN NaN
```

Arithmetic methods with fill values

In arithmetic operations between differently-indexed objects, you might want to fill with a special value, like 0, when an axis label is found in one object but not the other:

```
In [136]: df1 = DataFrame(np.arange(12.).reshape((3, 4)), columns=list('abcd'))

In [137]: df2 = DataFrame(np.arange(20.).reshape((4, 5)), columns=list('abcde'))

In [138]: df1           In [139]: df2
Out[138]:               Out[139]:
   a  b   c   d            a   b   c   d   e
```

```
0  0  1   2   3        0   0   1   2   3   4
1  4  5   6   7        1   5   6   7   8   9
2  8  9  10  11        2  10  11  12  13  14
                        3  15  16  17  18  19
```

Adding these together results in NA values in the locations that don't overlap:

```
In [140]: df1 + df2
Out[140]:
    a   b   c   d   e
0   0   2   4   6 NaN
1   9  11  13  15 NaN
2  18  20  22  24 NaN
3 NaN NaN NaN NaN NaN
```

Using the `add` method on `df1`, I pass `df2` and an argument to `fill_value`:

```
In [141]: df1.add(df2, fill_value=0)
Out[141]:
    a   b   c   d   e
0   0   2   4   6   4
1   9  11  13  15   9
2  18  20  22  24  14
3  15  16  17  18  19
```

Relatedly, when reindexing a Series or DataFrame, you can also specify a different fill value:

```
In [142]: df1.reindex(columns=df2.columns, fill_value=0)
Out[142]:
   a  b   c   d  e
0  0  1   2   3  0
1  4  5   6   7  0
2  8  9  10  11  0
```

Table 5-7. Flexible arithmetic methods

Method	Description
`add`	Method for addition (+)
`sub`	Method for subtraction (-)
`div`	Method for division (/)
`mul`	Method for multiplication (*)

Operations between DataFrame and Series

As with NumPy arrays, arithmetic between DataFrame and Series is well-defined. First, as a motivating example, consider the difference between a 2D array and one of its rows:

```
In [143]: arr = np.arange(12.).reshape((3, 4))

In [144]: arr
Out[144]:
array([[  0.,   1.,   2.,   3.],
       [  4.,   5.,   6.,   7.],
```

```
       [  8.,   9.,  10.,  11.]])

In [145]: arr[0]
Out[145]: array([ 0.,  1.,  2.,  3.])

In [146]: arr - arr[0]
Out[146]:
array([[ 0.,  0.,  0.,  0.],
       [ 4.,  4.,  4.,  4.],
       [ 8.,  8.,  8.,  8.]])
```

This is referred to as *broadcasting* and is explained in more detail in Chapter 12. Operations between a DataFrame and a Series are similar:

```
In [147]: frame = DataFrame(np.arange(12.).reshape((4, 3)), columns=list('bde'),
   .....:                   index=['Utah', 'Ohio', 'Texas', 'Oregon'])

In [148]: series = frame.ix[0]

In [149]: frame          In [150]: series
Out[149]:                Out[150]:
        b   d   e        b    0
Utah    0   1   2        d    1
Ohio    3   4   5        e    2
Texas   6   7   8        Name: Utah
Oregon  9  10  11
```

By default, arithmetic between DataFrame and Series matches the index of the Series on the DataFrame's columns, broadcasting down the rows:

```
In [151]: frame - series
Out[151]:
        b  d  e
Utah    0  0  0
Ohio    3  3  3
Texas   6  6  6
Oregon  9  9  9
```

If an index value is not found in either the DataFrame's columns or the Series's index, the objects will be reindexed to form the union:

```
In [152]: series2 = Series(range(3), index=['b', 'e', 'f'])

In [153]: frame + series2
Out[153]:
        b   d   e   f
Utah    0 NaN   3 NaN
Ohio    3 NaN   6 NaN
Texas   6 NaN   9 NaN
Oregon  9 NaN  12 NaN
```

If you want to instead broadcast over the columns, matching on the rows, you have to use one of the arithmetic methods. For example:

```
In [154]: series3 = frame['d']

In [155]: frame      In [156]: series3
```

```
Out[155]:           Out[156]:
        b   d   e   Utah       1
Utah    0   1   2   Ohio       4
Ohio    3   4   5   Texas      7
Texas   6   7   8   Oregon    10
Oregon  9  10  11   Name: d

In [157]: frame.sub(series3, axis=0)
Out[157]:
        b  d  e
Utah   -1  0  1
Ohio   -1  0  1
Texas  -1  0  1
Oregon -1  0  1
```

The axis number that you pass is the *axis to match on*. In this case we mean to match on the DataFrame's row index and broadcast across.

Function application and mapping

NumPy ufuncs (element-wise array methods) work fine with pandas objects:

```
In [158]: frame = DataFrame(np.random.randn(4, 3), columns=list('bde'),
   .....:                   index=['Utah', 'Ohio', 'Texas', 'Oregon'])

In [159]: frame
Out[159]:
               b         d         e
Utah   -0.204708  0.478943 -0.519439
Ohio   -0.555730  1.965781  1.393406
Texas   0.092908  0.281746  0.769023
Oregon  1.246435  1.007189 -1.296221

In [160]: np.abs(frame)
Out[160]:
                b         d         e
Utah     0.204708  0.478943  0.519439
Ohio     0.555730  1.965781  1.393406
Texas    0.092908  0.281746  0.769023
Oregon   1.246435  1.007189  1.296221
```

Another frequent operation is applying a function on 1D arrays to each column or row. DataFrame's `apply` method does exactly this:

```
In [161]: f = lambda x: x.max() - x.min()

In [162]: frame.apply(f)
Out[162]:
b    1.802165
d    1.684034
e    2.689627

In [163]: frame.apply(f, axis=1)
Out[163]:
Utah      0.998382
Ohio      2.521511
Texas     0.676115
Oregon    2.542656
```

Many of the most common array statistics (like `sum` and `mean`) are DataFrame methods, so using `apply` is not necessary.

The function passed to `apply` need not return a scalar value, it can also return a Series with multiple values:

```
In [164]: def f(x):
   .....:     return Series([x.min(), x.max()], index=['min', 'max'])

In [165]: frame.apply(f)
```

```
Out[165]:
            b         d         e
min -0.555730  0.281746 -1.296221
max  1.246435  1.965781  1.393406
```

Element-wise Python functions can be used, too. Suppose you wanted to compute a formatted string from each floating point value in `frame`. You can do this with `applymap`:

```
In [166]: format = lambda x: '%.2f' % x

In [167]: frame.applymap(format)
Out[167]:
            b     d      e
Utah    -0.20  0.48  -0.52
Ohio    -0.56  1.97   1.39
Texas    0.09  0.28   0.77
Oregon   1.25  1.01  -1.30
```

The reason for the name `applymap` is that Series has a `map` method for applying an element-wise function:

```
In [168]: frame['e'].map(format)
Out[168]:
Utah      -0.52
Ohio       1.39
Texas      0.77
Oregon    -1.30
Name: e
```

Sorting and ranking

Sorting a data set by some criterion is another important built-in operation. To sort lexicographically by row or column index, use the `sort_index` method, which returns a new, sorted object:

```
In [169]: obj = Series(range(4), index=['d', 'a', 'b', 'c'])

In [170]: obj.sort_index()
Out[170]:
a    1
b    2
c    3
d    0
```

With a DataFrame, you can sort by index on either axis:

```
In [171]: frame = DataFrame(np.arange(8).reshape((2, 4)), index=['three', 'one'],
   .....:                   columns=['d', 'a', 'b', 'c'])

In [172]: frame.sort_index()
Out[172]:
       d  a  b  c
one    4  5  6  7
three  0  1  2  3

In [173]: frame.sort_index(axis=1)
Out[173]:
       a  b  c  d
three  1  2  3  0
one    5  6  7  4
```

The data is sorted in ascending order by default, but can be sorted in descending order, too:

```
In [174]: frame.sort_index(axis=1, ascending=False)
Out[174]:
       d  c  b  a
three  0  3  2  1
one    4  7  6  5
```

To sort a Series by its values, use its `order` method:

```
In [175]: obj = Series([4, 7, -3, 2])

In [176]: obj.order()
Out[176]:
2   -3
3    2
0    4
1    7
```

Any missing values are sorted to the end of the Series by default:

```
In [177]: obj = Series([4, np.nan, 7, np.nan, -3, 2])

In [178]: obj.order()
Out[178]:
4    -3
5     2
0     4
2     7
1   NaN
3   NaN
```

On DataFrame, you may want to sort by the values in one or more columns. To do so, pass one or more column names to the `by` option:

```
In [179]: frame = DataFrame({'b': [4, 7, -3, 2], 'a': [0, 1, 0, 1]})

In [180]: frame
Out[180]:
   a  b
0  0  4
1  1  7
2  0 -3
3  1  2

In [181]: frame.sort_index(by='b')
Out[181]:
   a  b
2  0 -3
3  1  2
0  0  4
1  1  7
```

To sort by multiple columns, pass a list of names:

```
In [182]: frame.sort_index(by=['a', 'b'])
Out[182]:
   a  b
2  0 -3
0  0  4
3  1  2
1  1  7
```

Ranking is closely related to sorting, assigning ranks from one through the number of valid data points in an array. It is similar to the indirect sort indices produced by `numpy.argsort`, except that ties are broken according to a rule. The `rank` methods for Series and DataFrame are the place to look; by default `rank` breaks ties by assigning each group the mean rank:

```
In [183]: obj = Series([7, -5, 7, 4, 2, 0, 4])

In [184]: obj.rank()
Out[184]:
0    6.5
1    1.0
2    6.5
3    4.5
4    3.0
5    2.0
6    4.5
```

Ranks can also be assigned according to the order they're observed in the data:

```
In [185]: obj.rank(method='first')
Out[185]:
0    6
1    1
2    7
3    4
4    3
5    2
6    5
```

Naturally, you can rank in descending order, too:

```
In [186]: obj.rank(ascending=False, method='max')
Out[186]:
0    2
1    7
2    2
3    4
4    5
5    6
6    4
```

See Table 5-8 for a list of tie-breaking methods available. DataFrame can compute ranks over the rows or the columns:

```
In [187]: frame = DataFrame({'b': [4.3, 7, -3, 2], 'a': [0, 1, 0, 1],
   .....:                    'c': [-2, 5, 8, -2.5]})

In [188]: frame
Out[188]:
   a    b    c
0  0  4.3 -2.0
1  1  7.0  5.0
2  0 -3.0  8.0
3  1  2.0 -2.5

In [189]: frame.rank(axis=1)
Out[189]:
   a  b  c
0  2  3  1
1  1  3  2
2  2  1  3
3  2  3  1
```

Table 5-8. Tie-breaking methods with rank

Method	Description
`'average'`	Default: assign the average rank to each entry in the equal group.
`'min'`	Use the minimum rank for the whole group.
`'max'`	Use the maximum rank for the whole group.
`'first'`	Assign ranks in the order the values appear in the data.

Axis indexes with duplicate values

Up until now all of the examples I've showed you have had unique axis labels (index values). While many pandas functions (like `reindex`) require that the labels be unique, it's not mandatory. Let's consider a small Series with duplicate indices:

```
In [190]: obj = Series(range(5), index=['a', 'a', 'b', 'b', 'c'])

In [191]: obj
Out[191]:
a    0
a    1
b    2
b    3
c    4
```

The index's `is_unique` property can tell you whether its values are unique or not:

```
In [192]: obj.index.is_unique
Out[192]: False
```

Data selection is one of the main things that behaves differently with duplicates. Indexing a value with multiple entries returns a Series while single entries return a scalar value:

```
In [193]: obj['a']    In [194]: obj['c']
Out[193]:             Out[194]: 4
a    0
a    1
```

The same logic extends to indexing rows in a DataFrame:

```
In [195]: df = DataFrame(np.random.randn(4, 3), index=['a', 'a', 'b', 'b'])

In [196]: df
Out[196]:
          0         1         2
a  0.274992  0.228913  1.352917
a  0.886429 -2.001637 -0.371843
b  1.669025 -0.438570 -0.539741
b  0.476985  3.248944 -1.021228

In [197]: df.ix['b']
Out[197]:
          0         1         2
```

```
b  1.669025 -0.438570 -0.539741
b  0.476985  3.248944 -1.021228
```

Summarizing and Computing Descriptive Statistics

pandas objects are equipped with a set of common mathematical and statistical methods. Most of these fall into the category of *reductions* or *summary statistics*, methods that extract a single value (like the sum or mean) from a Series or a Series of values from the rows or columns of a DataFrame. Compared with the equivalent methods of vanilla NumPy arrays, they are all built from the ground up to exclude missing data. Consider a small DataFrame:

```
In [198]: df = DataFrame([[1.4, np.nan], [7.1, -4.5],
   .....:                 [np.nan, np.nan], [0.75, -1.3]],
   .....:                index=['a', 'b', 'c', 'd'],
   .....:                columns=['one', 'two'])

In [199]: df
Out[199]:
    one  two
a  1.40  NaN
b  7.10 -4.5
c   NaN  NaN
d  0.75 -1.3
```

Calling DataFrame's `sum` method returns a Series containing column sums:

```
In [200]: df.sum()
Out[200]:
one    9.25
two   -5.80
```

Passing `axis=1` sums over the rows instead:

```
In [201]: df.sum(axis=1)
Out[201]:
a    1.40
b    2.60
c     NaN
d   -0.55
```

NA values are excluded unless the entire slice (row or column in this case) is NA. This can be disabled using the `skipna` option:

```
In [202]: df.mean(axis=1, skipna=False)
Out[202]:
a      NaN
b    1.300
c      NaN
d   -0.275
```

See Table 5-9 for a list of common options for each reduction method options.

Table 5-9. Options for reduction methods

Method	Description
`axis`	Axis to reduce over. 0 for DataFrame's rows and 1 for columns.
`skipna`	Exclude missing values, `True` by default.
`level`	Reduce grouped by level if the axis is hierarchically-indexed (MultiIndex).

Some methods, like `idxmin` and `idxmax`, return indirect statistics like the index value where the minimum or maximum values are attained:

```
In [203]: df.idxmax()
Out[203]:
one    b
two    d
```

Other methods are *accumulations*:

```
In [204]: df.cumsum()
Out[204]:
    one  two
a  1.40  NaN
b  8.50 -4.5
c   NaN  NaN
d  9.25 -5.8
```

Another type of method is neither a reduction nor an accumulation. `describe` is one such example, producing multiple summary statistics in one shot:

```
In [205]: df.describe()
Out[205]:
            one       two
count  3.000000  2.000000
mean   3.083333 -2.900000
std    3.493685  2.262742
min    0.750000 -4.500000
25%    1.075000 -3.700000
50%    1.400000 -2.900000
75%    4.250000 -2.100000
max    7.100000 -1.300000
```

On non-numeric data, `describe` produces alternate summary statistics:

```
In [206]: obj = Series(['a', 'a', 'b', 'c'] * 4)

In [207]: obj.describe()
Out[207]:
count     16
unique     3
top        a
freq       8
```

See Table 5-10 for a full list of summary statistics and related methods.

Table 5-10. Descriptive and summary statistics

Method	Description
`count`	Number of non-NA values
`describe`	Compute set of summary statistics for Series or each DataFrame column
`min, max`	Compute minimum and maximum values
`argmin, argmax`	Compute index locations (integers) at which minimum or maximum value obtained, respectively
`idxmin, idxmax`	Compute index values at which minimum or maximum value obtained, respectively
`quantile`	Compute sample quantile ranging from 0 to 1
`sum`	Sum of values
`mean`	Mean of values
`median`	Arithmetic median (50% quantile) of values
`mad`	Mean absolute deviation from mean value
`var`	Sample variance of values
`std`	Sample standard deviation of values
`skew`	Sample skewness (3rd moment) of values
`kurt`	Sample kurtosis (4th moment) of values
`cumsum`	Cumulative sum of values
`cummin, cummax`	Cumulative minimum or maximum of values, respectively
`cumprod`	Cumulative product of values
`diff`	Compute 1st arithmetic difference (useful for time series)
`pct_change`	Compute percent changes

Correlation and Covariance

Some summary statistics, like correlation and covariance, are computed from pairs of arguments. Let's consider some DataFrames of stock prices and volumes obtained from Yahoo! Finance:

```
import pandas.io.data as web

all_data = {}
for ticker in ['AAPL', 'IBM', 'MSFT', 'GOOG']:
    all_data[ticker] = web.get_data_yahoo(ticker, '1/1/2000', '1/1/2010')

price = DataFrame({tic: data['Adj Close']
                   for tic, data in all_data.iteritems()})
volume = DataFrame({tic: data['Volume']
                    for tic, data in all_data.iteritems()})
```

I now compute percent changes of the prices:

```
In [209]: returns = price.pct_change()

In [210]: returns.tail()
```

```
Out[210]:
                AAPL      GOOG       IBM      MSFT
Date
2009-12-24  0.034339  0.011117  0.004420  0.002747
2009-12-28  0.012294  0.007098  0.013282  0.005479
2009-12-29 -0.011861 -0.005571 -0.003474  0.006812
2009-12-30  0.012147  0.005376  0.005468 -0.013532
2009-12-31 -0.004300 -0.004416 -0.012609 -0.015432
```

The `corr` method of Series computes the correlation of the overlapping, non-NA, aligned-by-index values in two Series. Relatedly, `cov` computes the covariance:

```
In [211]: returns.MSFT.corr(returns.IBM)
Out[211]: 0.49609291822168838

In [212]: returns.MSFT.cov(returns.IBM)
Out[212]: 0.00021600332437329015
```

DataFrame's `corr` and `cov` methods, on the other hand, return a full correlation or covariance matrix as a DataFrame, respectively:

```
In [213]: returns.corr()
Out[213]:
          AAPL      GOOG       IBM      MSFT
AAPL  1.000000  0.470660  0.410648  0.424550
GOOG  0.470660  1.000000  0.390692  0.443334
IBM   0.410648  0.390692  1.000000  0.496093
MSFT  0.424550  0.443334  0.496093  1.000000

In [214]: returns.cov()
Out[214]:
          AAPL      GOOG       IBM      MSFT
AAPL  0.001028  0.000303  0.000252  0.000309
GOOG  0.000303  0.000580  0.000142  0.000205
IBM   0.000252  0.000142  0.000367  0.000216
MSFT  0.000309  0.000205  0.000216  0.000516
```

Using DataFrame's `corrwith` method, you can compute pairwise correlations between a DataFrame's columns or rows with another Series or DataFrame. Passing a Series returns a Series with the correlation value computed for each column:

```
In [215]: returns.corrwith(returns.IBM)
Out[215]:
AAPL    0.410648
GOOG    0.390692
IBM     1.000000
MSFT    0.496093
```

Passing a DataFrame computes the correlations of matching column names. Here I compute correlations of percent changes with volume:

```
In [216]: returns.corrwith(volume)
Out[216]:
AAPL   -0.057461
GOOG    0.062644
```

```
IBM    -0.007900
MSFT   -0.014175
```

Passing `axis=1` does things row-wise instead. In all cases, the data points are aligned by label before computing the correlation.

Unique Values, Value Counts, and Membership

Another class of related methods extracts information about the values contained in a one-dimensional Series. To illustrate these, consider this example:

```
In [217]: obj = Series(['c', 'a', 'd', 'a', 'a', 'b', 'b', 'c', 'c'])
```

The first function is `unique`, which gives you an array of the unique values in a Series:

```
In [218]: uniques = obj.unique()

In [219]: uniques
Out[219]: array([c, a, d, b], dtype=object)
```

The unique values are not necessarily returned in sorted order, but could be sorted after the fact if needed (`uniques.sort()`). Relatedly, `value_counts` computes a Series containing value frequencies:

```
In [220]: obj.value_counts()
Out[220]:
c    3
a    3
b    2
d    1
```

The Series is sorted by value in descending order as a convenience. `value_counts` is also available as a top-level pandas method that can be used with any array or sequence:

```
In [221]: pd.value_counts(obj.values, sort=False)
Out[221]:
a    3
b    2
c    3
d    1
```

Lastly, `isin` is responsible for vectorized set membership and can be very useful in filtering a data set down to a subset of values in a Series or column in a DataFrame:

```
In [222]: mask = obj.isin(['b', 'c'])

In [223]: mask        In [224]: obj[mask]
Out[223]:             Out[224]:
0     True            0    c
1    False            5    b
2    False            6    b
3    False            7    c
4    False            8    c
5     True
6     True
```

```
7     True
8     True
```

See Table 5-11 for a reference on these methods.

Table 5-11. Unique, value counts, and binning methods

Method	Description
`isin`	Compute boolean array indicating whether each Series value is contained in the passed sequence of values.
`unique`	Compute array of unique values in a Series, returned in the order observed.
`value_counts`	Return a Series containing unique values as its index and frequencies as its values, ordered count in descending order.

In some cases, you may want to compute a histogram on multiple related columns in a DataFrame. Here's an example:

```
In [225]: data = DataFrame({'Qu1': [1, 3, 4, 3, 4],
   .....:                   'Qu2': [2, 3, 1, 2, 3],
   .....:                   'Qu3': [1, 5, 2, 4, 4]})

In [226]: data
Out[226]:
   Qu1  Qu2  Qu3
0    1    2    1
1    3    3    5
2    4    1    2
3    3    2    4
4    4    3    4
```

Passing `pandas.value_counts` to this DataFrame's `apply` function gives:

```
In [227]: result = data.apply(pd.value_counts).fillna(0)

In [228]: result
Out[228]:
   Qu1  Qu2  Qu3
1    1    1    1
2    0    2    1
3    2    2    0
4    2    0    2
5    0    0    1
```

Handling Missing Data

Missing data is common in most data analysis applications. One of the goals in designing pandas was to make working with missing data as painless as possible. For example, all of the descriptive statistics on pandas objects exclude missing data as you've seen earlier in the chapter.

pandas uses the floating point value `NaN` (Not a Number) to represent missing data in both floating as well as in non-floating point arrays. It is just used as a *sentinel* that can be easily detected:

```
In [229]: string_data = Series(['aardvark', 'artichoke', np.nan, 'avocado'])

In [230]: string_data
Out[230]:
0     aardvark
1    artichoke
2          NaN
3      avocado

In [231]: string_data.isnull()
Out[231]:
0    False
1    False
2     True
3    False
```

The built-in Python `None` value is also treated as NA in object arrays:

```
In [232]: string_data[0] = None

In [233]: string_data.isnull()
Out[233]:
0     True
1    False
2     True
3    False
```

I do not claim that pandas's NA representation is optimal, but it is simple and reasonably consistent. It's the best solution, with good all-around performance characteristics and a simple API, that I could concoct in the absence of a true NA data type or bit pattern in NumPy's data types. Ongoing development work in NumPy may change this in the future.

Table 5-12. NA handling methods

Argument	Description
`dropna`	Filter axis labels based on whether values for each label have missing data, with varying thresholds for how much missing data to tolerate.
`fillna`	Fill in missing data with some value or using an interpolation method such as `'ffill'` or `'bfill'`.
`isnull`	Return like-type object containing boolean values indicating which values are missing / NA.
`notnull`	Negation of `isnull`.

Filtering Out Missing Data

You have a number of options for filtering out missing data. While doing it by hand is always an option, `dropna` can be very helpful. On a Series, it returns the Series with only the non-null data and index values:

```
In [234]: from numpy import nan as NA

In [235]: data = Series([1, NA, 3.5, NA, 7])

In [236]: data.dropna()
Out[236]:
```

```
0    1.0
2    3.5
4    7.0
```

Naturally, you could have computed this yourself by boolean indexing:

```
In [237]: data[data.notnull()]
Out[237]:
0    1.0
2    3.5
4    7.0
```

With DataFrame objects, these are a bit more complex. You may want to drop rows or columns which are all NA or just those containing any NAs. `dropna` by default drops any row containing a missing value:

```
In [238]: data = DataFrame([[1., 6.5, 3.], [1., NA, NA],
   .....:                   [NA, NA, NA], [NA, 6.5, 3.]])

In [239]: cleaned = data.dropna()

In [240]: data        In [241]: cleaned
Out[240]:             Out[241]:
    0    1   2           0    1  2
0   1  6.5   3        0  1  6.5  3
1   1  NaN NaN
2 NaN  NaN NaN
3 NaN  6.5   3
```

Passing `how='all'` will only drop rows that are all NA:

```
In [242]: data.dropna(how='all')
Out[242]:
    0    1   2
0   1  6.5   3
1   1  NaN NaN
3 NaN  6.5   3
```

Dropping columns in the same way is only a matter of passing `axis=1`:

```
In [243]: data[4] = NA

In [244]: data            In [245]: data.dropna(axis=1, how='all')
Out[244]:                 Out[245]:
    0    1   2   4            0    1   2
0   1  6.5   3 NaN        0   1  6.5   3
1   1  NaN NaN NaN        1   1  NaN NaN
2 NaN  NaN NaN NaN        2 NaN  NaN NaN
3 NaN  6.5   3 NaN        3 NaN  6.5   3
```

A related way to filter out DataFrame rows tends to concern time series data. Suppose you want to keep only rows containing a certain number of observations. You can indicate this with the `thresh` argument:

```
In [246]: df = DataFrame(np.random.randn(7, 3))

In [247]: df.ix[:4, 1] = NA; df.ix[:2, 2] = NA
```

```
In [248]: df
Out[248]:
          0         1         2
0 -0.577087       NaN       NaN
1  0.523772       NaN       NaN
2 -0.713544       NaN       NaN
3 -1.860761       NaN  0.560145
4 -1.265934       NaN -1.063512
5  0.332883 -2.359419 -0.199543
6 -1.541996 -0.970736 -1.307030
```

```
In [249]: df.dropna(thresh=3)
Out[249]:
          0         1         2
5  0.332883 -2.359419 -0.199543
6 -1.541996 -0.970736 -1.307030
```

Filling in Missing Data

Rather than filtering out missing data (and potentially discarding other data along with it), you may want to fill in the "holes" in any number of ways. For most purposes, the `fillna` method is the workhorse function to use. Calling `fillna` with a constant replaces missing values with that value:

```
In [250]: df.fillna(0)
Out[250]:
          0         1         2
0 -0.577087  0.000000  0.000000
1  0.523772  0.000000  0.000000
2 -0.713544  0.000000  0.000000
3 -1.860761  0.000000  0.560145
4 -1.265934  0.000000 -1.063512
5  0.332883 -2.359419 -0.199543
6 -1.541996 -0.970736 -1.307030
```

Calling `fillna` with a dict you can use a different fill value for each column:

```
In [251]: df.fillna({1: 0.5, 3: -1})
Out[251]:
          0         1         2
0 -0.577087  0.500000       NaN
1  0.523772  0.500000       NaN
2 -0.713544  0.500000       NaN
3 -1.860761  0.500000  0.560145
4 -1.265934  0.500000 -1.063512
5  0.332883 -2.359419 -0.199543
6 -1.541996 -0.970736 -1.307030
```

`fillna` returns a new object, but you can modify the existing object in place:

```
# always returns a reference to the filled object
In [252]: _ = df.fillna(0, inplace=True)

In [253]: df
Out[253]:
          0         1         2
0 -0.577087  0.000000  0.000000
1  0.523772  0.000000  0.000000
2 -0.713544  0.000000  0.000000
3 -1.860761  0.000000  0.560145
```

```
4 -1.265934  0.000000 -1.063512
5  0.332883 -2.359419 -0.199543
6 -1.541996 -0.970736 -1.307030
```

The same interpolation methods available for reindexing can be used with `fillna`:

```
In [254]: df = DataFrame(np.random.randn(6, 3))

In [255]: df.ix[2:, 1] = NA; df.ix[4:, 2] = NA

In [256]: df
Out[256]:
          0         1         2
0  0.286350  0.377984 -0.753887
1  0.331286  1.349742  0.069877
2  0.246674       NaN  1.004812
3  1.327195       NaN -1.549106
4  0.022185       NaN       NaN
5  0.862580       NaN       NaN

In [257]: df.fillna(method='ffill')
Out[257]:
          0         1         2
0  0.286350  0.377984 -0.753887
1  0.331286  1.349742  0.069877
2  0.246674  1.349742  1.004812
3  1.327195  1.349742 -1.549106
4  0.022185  1.349742 -1.549106
5  0.862580  1.349742 -1.549106

In [258]: df.fillna(method='ffill', limit=2)
Out[258]:
          0         1         2
0  0.286350  0.377984 -0.753887
1  0.331286  1.349742  0.069877
2  0.246674  1.349742  1.004812
3  1.327195  1.349742 -1.549106
4  0.022185       NaN -1.549106
5  0.862580       NaN -1.549106
```

With `fillna` you can do lots of other things with a little creativity. For example, you might pass the mean or median value of a Series:

```
In [259]: data = Series([1., NA, 3.5, NA, 7])

In [260]: data.fillna(data.mean())
Out[260]:
0    1.000000
1    3.833333
2    3.500000
3    3.833333
4    7.000000
```

See Table 5-13 for a reference on `fillna`.

Table 5-13. fillna function arguments

Argument	Description
`value`	Scalar value or dict-like object to use to fill missing values
`method`	Interpolation, by default `'ffill'` if function called with no other arguments
`axis`	Axis to fill on, default `axis=0`
`inplace`	Modify the calling object without producing a copy
`limit`	For forward and backward filling, maximum number of consecutive periods to fill

Hierarchical Indexing

Hierarchical indexing is an important feature of pandas enabling you to have multiple (two or more) index *levels* on an axis. Somewhat abstractly, it provides a way for you to work with higher dimensional data in a lower dimensional form. Let's start with a simple example; create a Series with a list of lists or arrays as the index:

```
In [261]: data = Series(np.random.randn(10),
   .....:               index=[['a', 'a', 'a', 'b', 'b', 'b', 'c', 'c', 'd', 'd'],
   .....:                      [1, 2, 3, 1, 2, 3, 1, 2, 2, 3]])

In [262]: data
Out[262]:
a  1    0.670216
   2    0.852965
   3   -0.955869
b  1   -0.023493
   2   -2.304234
   3   -0.652469
c  1   -1.218302
   2   -1.332610
d  2    1.074623
   3    0.723642
```

What you're seeing is a prettified view of a Series with a `MultiIndex` as its index. The "gaps" in the index display mean "use the label directly above":

```
In [263]: data.index
Out[263]:
MultiIndex
[('a', 1) ('a', 2) ('a', 3) ('b', 1) ('b', 2) ('b', 3) ('c', 1)
 ('c', 2) ('d', 2) ('d', 3)]
```

With a hierarchically-indexed object, so-called *partial* indexing is possible, enabling you to concisely select subsets of the data:

```
In [264]: data['b']
Out[264]:
1   -0.023493
2   -2.304234
3   -0.652469

In [265]: data['b':'c']
Out[265]:
b  1   -0.023493
   2   -2.304234
   3   -0.652469
c  1   -1.218302
   2   -1.332610

In [266]: data.ix[['b', 'd']]
Out[266]:
b  1   -0.023493
   2   -2.304234
   3   -0.652469
d  2    1.074623
   3    0.723642
```

Selection is even possible in some cases from an "inner" level:

```
In [267]: data[:, 2]
Out[267]:
a    0.852965
```

```
b   -2.304234
c   -1.332610
d    1.074623
```

Hierarchical indexing plays a critical role in reshaping data and group-based operations like forming a pivot table. For example, this data could be rearranged into a DataFrame using its `unstack` method:

```
In [268]: data.unstack()
Out[268]:
          1         2         3
a  0.670216  0.852965 -0.955869
b -0.023493 -2.304234 -0.652469
c -1.218302 -1.332610       NaN
d       NaN  1.074623  0.723642
```

The inverse operation of `unstack` is `stack`:

```
In [269]: data.unstack().stack()
Out[269]:
a  1    0.670216
   2    0.852965
   3   -0.955869
b  1   -0.023493
   2   -2.304234
   3   -0.652469
c  1   -1.218302
   2   -1.332610
d  2    1.074623
   3    0.723642
```

`stack` and `unstack` will be explored in more detail in Chapter 7.

With a DataFrame, either axis can have a hierarchical index:

```
In [270]: frame = DataFrame(np.arange(12).reshape((4, 3)),
   .....:                   index=[['a', 'a', 'b', 'b'], [1, 2, 1, 2]],
   .....:                   columns=[['Ohio', 'Ohio', 'Colorado'],
   .....:                            ['Green', 'Red', 'Green']])

In [271]: frame
Out[271]:
      Ohio       Colorado
     Green  Red     Green
a 1      0    1         2
  2      3    4         5
b 1      6    7         8
  2      9   10        11
```

The hierarchical levels can have names (as strings or any Python objects). If so, these will show up in the console output (don't confuse the index names with the axis labels!):

```
In [272]: frame.index.names = ['key1', 'key2']

In [273]: frame.columns.names = ['state', 'color']

In [274]: frame
```

```
Out[274]:
state       Ohio       Colorado
color      Green  Red     Green
key1 key2
a    1         0    1         2
     2         3    4         5
b    1         6    7         8
     2         9   10        11
```

With partial column indexing you can similarly select groups of columns:

```
In [275]: frame['Ohio']
Out[275]:
color      Green  Red
key1 key2
a    1         0    1
     2         3    4
b    1         6    7
     2         9   10
```

A `MultiIndex` can be created by itself and then reused; the columns in the above DataFrame with level names could be created like this:

```
MultiIndex.from_arrays([['Ohio', 'Ohio', 'Colorado'], ['Green', 'Red', 'Green']],
                       names=['state', 'color'])
```

Reordering and Sorting Levels

At times you will need to rearrange the order of the levels on an axis or sort the data by the values in one specific level. The `swaplevel` takes two level numbers or names and returns a new object with the levels interchanged (but the data is otherwise unaltered):

```
In [276]: frame.swaplevel('key1', 'key2')
Out[276]:
state       Ohio       Colorado
color      Green  Red     Green
key2 key1
1    a         0    1         2
2    a         3    4         5
1    b         6    7         8
2    b         9   10        11
```

`sortlevel`, on the other hand, sorts the data (stably) using only the values in a single level. When swapping levels, it's not uncommon to also use `sortlevel` so that the result is lexicographically sorted:

```
In [277]: frame.sortlevel(1)
Out[277]:
state       Ohio       Colorado
color      Green  Red     Green
key1 key2
a    1         0    1         2
b    1         6    7         8
a    2         3    4         5
b    2         9   10        11
```

```
In [278]: frame.swaplevel(0, 1).sortlevel(0)
Out[278]:
state       Ohio       Colorado
color      Green  Red     Green
key2 key1
1    a         0    1         2
     b         6    7         8
2    a         3    4         5
     b         9   10        11
```

Data selection performance is much better on hierarchically indexed objects if the index is lexicographically sorted starting with the outermost level, that is, the result of calling `sortlevel(0)` or `sort_index()`.

Summary Statistics by Level

Many descriptive and summary statistics on DataFrame and Series have a `level` option in which you can specify the level you want to sum by on a particular axis. Consider the above DataFrame; we can sum by level on either the rows or columns like so:

```
In [279]: frame.sum(level='key2')
Out[279]:
state   Ohio       Colorado
color  Green  Red     Green
key2
1          6    8        10
2         12   14        16

In [280]: frame.sum(level='color', axis=1)
Out[280]:
color      Green  Red
key1 key2
a    1         2    1
     2         8    4
b    1        14    7
     2        20   10
```

Under the hood, this utilizes pandas's `groupby` machinery which will be discussed in more detail later in the book.

Using a DataFrame's Columns

It's not unusual to want to use one or more columns from a DataFrame as the row index; alternatively, you may wish to move the row index into the DataFrame's columns. Here's an example DataFrame:

```
In [281]: frame = DataFrame({'a': range(7), 'b': range(7, 0, -1),
   .....:                    'c': ['one', 'one', 'one', 'two', 'two', 'two', 'two'],
   .....:                    'd': [0, 1, 2, 0, 1, 2, 3]})

In [282]: frame
Out[282]:
   a  b    c  d
0  0  7  one  0
1  1  6  one  1
2  2  5  one  2
3  3  4  two  0
4  4  3  two  1
5  5  2  two  2
6  6  1  two  3
```

DataFrame's `set_index` function will create a new DataFrame using one or more of its columns as the index:

```
In [283]: frame2 = frame.set_index(['c', 'd'])

In [284]: frame2
Out[284]:
       a  b
c   d
one 0  0  7
    1  1  6
    2  2  5
two 0  3  4
    1  4  3
    2  5  2
    3  6  1
```

By default the columns are removed from the DataFrame, though you can leave them in:

```
In [285]: frame.set_index(['c', 'd'], drop=False)
Out[285]:
       a  b    c  d
c   d
one 0  0  7  one  0
    1  1  6  one  1
    2  2  5  one  2
two 0  3  4  two  0
    1  4  3  two  1
    2  5  2  two  2
    3  6  1  two  3
```

`reset_index`, on the other hand, does the opposite of `set_index`; the hierarchical index levels are are moved into the columns:

```
In [286]: frame2.reset_index()
Out[286]:
     c  d  a  b
0  one  0  0  7
1  one  1  1  6
2  one  2  2  5
3  two  0  3  4
4  two  1  4  3
5  two  2  5  2
6  two  3  6  1
```

Other pandas Topics

Here are some additional topics that may be of use to you in your data travels.

Integer Indexing

Working with pandas objects indexed by integers is something that often trips up new users due to some differences with indexing semantics on built-in Python data

structures like lists and tuples. For example, you would not expect the following code to generate an error:

```
ser = Series(np.arange(3.))
ser[-1]
```

In this case, pandas could "fall back" on integer indexing, but there's not a safe and general way (that I know of) to do this without introducing subtle bugs. Here we have an index containing 0, 1, 2, but inferring what the user wants (label-based indexing or position-based) is difficult::

```
In [288]: ser
Out[288]:
0    0
1    1
2    2
```

On the other hand, with a non-integer index, there is no potential for ambiguity:

```
In [289]: ser2 = Series(np.arange(3.), index=['a', 'b', 'c'])

In [290]: ser2[-1]
Out[290]: 2.0
```

To keep things consistent, if you have an axis index containing indexers, data selection with integers will always be label-oriented. This includes slicing with `ix`, too:

```
In [291]: ser.ix[:1]
Out[291]:
0    0
1    1
```

In cases where you need reliable position-based indexing regardless of the index type, you can use the `iget_value` method from Series and `irow` and `icol` methods from DataFrame:

```
In [292]: ser3 = Series(range(3), index=[-5, 1, 3])

In [293]: ser3.iget_value(2)
Out[293]: 2

In [294]: frame = DataFrame(np.arange(6).reshape(3, 2)), index=[2, 0, 1])

In [295]: frame.irow(0)
Out[295]:
0    0
1    1
Name: 2
```

Panel Data

While not a major topic of this book, pandas has a Panel data structure, which you can think of as a three-dimensional analogue of DataFrame. Much of the development focus of pandas has been in tabular data manipulations as these are easier to reason about,

```
2012-05-31  577.73  12.33  580.86  29.19
2012-06-01  560.99  12.07  570.98  28.45
```

An alternate way to represent panel data, especially for fitting statistical models, is in "stacked" DataFrame form:

```
In [302]: stacked = pdata.ix[:, '5/30/2012':, :].to_frame()

In [303]: stacked
Out[303]:
                     Open    High     Low   Close    Volume  Adj Close
major      minor
2012-05-30 AAPL   569.20  579.99  566.56  579.17  18908200     579.17
           DELL    12.59   12.70   12.46   12.56  19787800      12.56
           GOOG   588.16  591.90  583.53  588.23   1906700     588.23
           MSFT    29.35   29.48   29.12   29.34  41585500      29.34
2012-05-31 AAPL   580.74  581.50  571.46  577.73  17559800     577.73
           DELL    12.53   12.54   12.33   12.33  19955500      12.33
           GOOG   588.72  590.00  579.00  580.86   2968300     580.86
           MSFT    29.30   29.42   28.94   29.19  39134000      29.19
2012-06-01 AAPL   569.16  572.65  560.52  560.99  18606700     560.99
           DELL    12.15   12.30   12.05   12.07  19396700      12.07
           GOOG   571.79  572.65  568.35  570.98   3057900     570.98
           MSFT    28.76   28.96   28.44   28.45  56634300      28.45
```

DataFrame has a related `to_panel` method, the inverse of `to_frame`:

```
In [304]: stacked.to_panel()
Out[304]:
<class 'pandas.core.panel.Panel'>
Dimensions: 6 (items) x 3 (major) x 4 (minor)
Items: Open to Adj Close
Major axis: 2012-05-30 00:00:00 to 2012-06-01 00:00:00
Minor axis: AAPL to MSFT
```

CHAPTER 6

Data Loading, Storage, and File Formats

The tools in this book are of little use if you can't easily import and export data in Python. I'm going to be focused on input and output with pandas objects, though there are of course numerous tools in other libraries to aid in this process. NumPy, for example, features low-level but extremely fast binary data loading and storage, including support for memory-mapped array. See Chapter 12 for more on those.

Input and output typically falls into a few main categories: reading text files and other more efficient on-disk formats, loading data from databases, and interacting with network sources like web APIs.

Reading and Writing Data in Text Format

Python has become a beloved language for text and file munging due to its simple syntax for interacting with files, intuitive data structures, and convenient features like tuple packing and unpacking.

pandas features a number of functions for reading tabular data as a DataFrame object. Table 6-1 has a summary of all of them, though `read_csv` and `read_table` are likely the ones you'll use the most.

Table 6-1. Parsing functions in pandas

Function	Description
`read_csv`	Load delimited data from a file, URL, or file-like object. Use comma as default delimiter
`read_table`	Load delimited data from a file, URL, or file-like object. Use tab (`'\t'`) as default delimiter
`read_fwf`	Read data in fixed-width column format (that is, no delimiters)
`read_clipboard`	Version of `read_table` that reads data from the clipboard. Useful for converting tables from web pages

CHAPTER 4

NumPy Basics: Arrays and Vectorized Computation

NumPy, short for Numerical Python, is the fundamental package required for high performance scientific computing and data analysis. It is the foundation on which nearly all of the higher-level tools in this book are built. Here are some of the things it provides:

- `ndarray`, a fast and space-efficient multidimensional array providing vectorized arithmetic operations and sophisticated *broadcasting* capabilities
- Standard mathematical functions for fast operations on entire arrays of data without having to write loops
- Tools for reading / writing array data to disk and working with memory-mapped files
- Linear algebra, random number generation, and Fourier transform capabilities
- Tools for integrating code written in C, C++, and Fortran

The last bullet point is also one of the most important ones from an ecosystem point of view. Because NumPy provides an easy-to-use C API, it is very easy to pass data to external libraries written in a low-level language and also for external libraries to return data to Python as NumPy arrays. This feature has made Python a language of choice for wrapping legacy C/C++/Fortran codebases and giving them a dynamic and easy-to-use interface.

While NumPy by itself does not provide very much high-level data analytical functionality, having an understanding of NumPy arrays and array-oriented computing will help you use tools like pandas much more effectively. If you're new to Python and just looking to get your hands dirty working with data using pandas, feel free to give this chapter a skim. For more on advanced NumPy features like broadcasting, see Chapter 12.

For most data analysis applications, the main areas of functionality I'll focus on are:

- Fast vectorized array operations for data munging and cleaning, subsetting and filtering, transformation, and any other kinds of computations
- Common array algorithms like sorting, unique, and set operations
- Efficient descriptive statistics and aggregating/summarizing data
- Data alignment and relational data manipulations for merging and joining together heterogeneous data sets
- Expressing conditional logic as array expressions instead of loops with `if-elif-else` branches
- Group-wise data manipulations (aggregation, transformation, function application). Much more on this in Chapter 5

While NumPy provides the computational foundation for these operations, you will likely want to use pandas as your basis for most kinds of data analysis (especially for structured or tabular data) as it provides a rich, high-level interface making most common data tasks very concise and simple. pandas also provides some more domain-specific functionality like time series manipulation, which is not present in NumPy.

In this chapter and throughout the book, I use the standard NumPy convention of always using `import numpy as np`. You are, of course, welcome to put `from numpy import *` in your code to avoid having to write `np.`, but I would caution you against making a habit of this.

The NumPy ndarray: A Multidimensional Array Object

One of the key features of NumPy is its N-dimensional array object, or ndarray, which is a fast, flexible container for large data sets in Python. Arrays enable you to perform mathematical operations on whole blocks of data using similar syntax to the equivalent operations between scalar elements:

```
In [8]: data
Out[8]:
array([[ 0.9526, -0.246 , -0.8856],
       [ 0.5639,  0.2379,  0.9104]])

In [9]: data * 10
Out[9]:
array([[ 9.5256, -2.4601, -8.8565],
       [ 5.6385,  2.3794,  9.104 ]])

In [10]: data + data
Out[10]:
array([[ 1.9051, -0.492 , -1.7713],
       [ 1.1277,  0.4759,  1.8208]])
```

An ndarray is a generic multidimensional container for homogeneous data; that is, all of the elements must be the same type. Every array has a `shape`, a tuple indicating the size of each dimension, and a `dtype`, an object describing the *data type* of the array:

```
In [11]: data.shape
Out[11]: (2, 3)
```

```
In [12]: data.dtype
Out[12]: dtype('float64')
```

This chapter will introduce you to the basics of using NumPy arrays, and should be sufficient for following along with the rest of the book. While it's not necessary to have a deep understanding of NumPy for many data analytical applications, becoming proficient in array-oriented programming and thinking is a key step along the way to becoming a scientific Python guru.

Whenever you see "array", "NumPy array", or "ndarray" in the text, with few exceptions they all refer to the same thing: the ndarray object.

Creating ndarrays

The easiest way to create an array is to use the `array` function. This accepts any sequence-like object (including other arrays) and produces a new NumPy array containing the passed data. For example, a list is a good candidate for conversion:

```
In [13]: data1 = [6, 7.5, 8, 0, 1]

In [14]: arr1 = np.array(data1)

In [15]: arr1
Out[15]: array([ 6. ,  7.5,  8. ,  0. ,  1. ])
```

Nested sequences, like a list of equal-length lists, will be converted into a multidimensional array:

```
In [16]: data2 = [[1, 2, 3, 4], [5, 6, 7, 8]]

In [17]: arr2 = np.array(data2)

In [18]: arr2
Out[18]:
array([[1, 2, 3, 4],
       [5, 6, 7, 8]])

In [19]: arr2.ndim
Out[19]: 2

In [20]: arr2.shape
Out[20]: (2, 4)
```

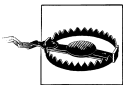
Unless explicitly specified (more on this later), `np.array` tries to infer a good data type for the array that it creates. The data type is stored in a special `dtype` object; for example, in the above two examples we have:

```
In [21]: arr1.dtype
Out[21]: dtype('float64')
```

```
In [22]: arr2.dtype
Out[22]: dtype('int64')
```

In addition to `np.array`, there are a number of other functions for creating new arrays. As examples, `zeros` and `ones` create arrays of 0's or 1's, respectively, with a given length or shape. `empty` creates an array without initializing its values to any particular value. To create a higher dimensional array with these methods, pass a tuple for the shape:

```
In [23]: np.zeros(10)
Out[23]: array([ 0.,  0.,  0.,  0.,  0.,  0.,  0.,  0.,  0.,  0.])

In [24]: np.zeros((3, 6))
Out[24]:
array([[ 0.,  0.,  0.,  0.,  0.,  0.],
       [ 0.,  0.,  0.,  0.,  0.,  0.],
       [ 0.,  0.,  0.,  0.,  0.,  0.]])

In [25]: np.empty((2, 3, 2))
Out[25]:
array([[[  4.94065646e-324,   4.94065646e-324],
        [  3.87491056e-297,   2.46845796e-130],
        [  4.94065646e-324,   4.94065646e-324]],

       [[  1.90723115e+083,   5.73293533e-053],
        [ -2.33568637e+124,  -6.70608105e-012],
        [  4.42786966e+160,   1.27100354e+025]]])
```



It's not safe to assume that `np.empty` will return an array of all zeros. In many cases, as previously shown, it will return uninitialized garbage values.

`arange` is an array-valued version of the built-in Python `range` function:

```
In [26]: np.arange(15)
Out[26]: array([ 0,  1,  2,  3,  4,  5,  6,  7,  8,  9, 10, 11, 12, 13, 14])
```

See Table 4-1 for a short list of standard array creation functions. Since NumPy is focused on numerical computing, the data type, if not specified, will in many cases be `float64` (floating point).

Table 4-1. Array creation functions

Function	Description
`array`	Convert input data (list, tuple, array, or other sequence type) to an ndarray either by inferring a dtype or explicitly specifying a dtype. Copies the input data by default.
`asarray`	Convert input to ndarray, but do not copy if the input is already an ndarray
`arange`	Like the built-in `range` but returns an ndarray instead of a list.
`ones, ones_like`	Produce an array of all 1's with the given shape and dtype. `ones_like` takes another array and produces a ones array of the same shape and dtype.
`zeros, zeros_like`	Like `ones` and `ones_like` but producing arrays of 0's instead

Function	Description
`empty, empty_like`	Create new arrays by allocating new memory, but do not populate with any values like `ones` and `zeros`
`eye, identity`	Create a square N x N identity matrix (1's on the diagonal and 0's elsewhere)

Data Types for ndarrays

The *data type* or `dtype` is a special object containing the information the ndarray needs to interpret a chunk of memory as a particular type of data:

```
In [27]: arr1 = np.array([1, 2, 3], dtype=np.float64)

In [28]: arr2 = np.array([1, 2, 3], dtype=np.int32)

In [29]: arr1.dtype           In [30]: arr2.dtype
Out[29]: dtype('float64')     Out[30]: dtype('int32')
```

Dtypes are part of what make NumPy so powerful and flexible. In most cases they map directly onto an underlying machine representation, which makes it easy to read and write binary streams of data to disk and also to connect to code written in a low-level language like C or Fortran. The numerical dtypes are named the same way: a type name, like `float` or `int`, followed by a number indicating the number of bits per element. A standard double-precision floating point value (what's used under the hood in Python's `float` object) takes up 8 bytes or 64 bits. Thus, this type is known in NumPy as `float64`. See Table 4-2 for a full listing of NumPy's supported data types.

Don't worry about memorizing the NumPy dtypes, especially if you're a new user. It's often only necessary to care about the general *kind* of data you're dealing with, whether floating point, complex, integer, boolean, string, or general Python object. When you need more control over how data are stored in memory and on disk, especially large data sets, it is good to know that you have control over the storage type.

Table 4-2. NumPy data types

Type	Type Code	Description
`int8, uint8`	`i1, u1`	Signed and unsigned 8-bit (1 byte) integer types
`int16, uint16`	`i2, u2`	Signed and unsigned 16-bit integer types
`int32, uint32`	`i4, u4`	Signed and unsigned 32-bit integer types
`int64, uint64`	`i8, u8`	Signed and unsigned 32-bit integer types
`float16`	`f2`	Half-precision floating point
`float32`	`f4 or f`	Standard single-precision floating point. Compatible with C float
`float64, float128`	`f8 or d`	Standard double-precision floating point. Compatible with C double and Python `float` object

Type	Type Code	Description
float128	f16 or g	Extended-precision floating point
complex64, complex128, complex256	c8, c16, c32	Complex numbers represented by two 32, 64, or 128 floats, respectively
bool	?	Boolean type storing True and False values
object	O	Python object type
string_	S	Fixed-length string type (1 byte per character). For example, to create a string dtype with length 10, use 'S10'.
unicode_	U	Fixed-length unicode type (number of bytes platform specific). Same specification semantics as string_ (e.g. 'U10').

You can explicitly convert or *cast* an array from one dtype to another using ndarray's `astype` method:

```
In [31]: arr = np.array([1, 2, 3, 4, 5])

In [32]: arr.dtype
Out[32]: dtype('int64')

In [33]: float_arr = arr.astype(np.float64)

In [34]: float_arr.dtype
Out[34]: dtype('float64')
```

In this example, integers were cast to floating point. If I cast some floating point numbers to be of integer dtype, the decimal part will be truncated:

```
In [35]: arr = np.array([3.7, -1.2, -2.6, 0.5, 12.9, 10.1])

In [36]: arr
Out[36]: array([  3.7,  -1.2,  -2.6,   0.5,  12.9,  10.1])

In [37]: arr.astype(np.int32)
Out[37]: array([ 3, -1, -2,  0, 12, 10], dtype=int32)
```

Should you have an array of strings representing numbers, you can use `astype` to convert them to numeric form:

```
In [38]: numeric_strings = np.array(['1.25', '-9.6', '42'], dtype=np.string_)

In [39]: numeric_strings.astype(float)
Out[39]: array([  1.25,  -9.6 ,  42.  ])
```

If casting were to fail for some reason (like a string that cannot be converted to `float64`), a `TypeError` will be raised. See that I was a bit lazy and wrote `float` instead of `np.float64`; NumPy is smart enough to alias the Python types to the equivalent dtypes.

You can also use another array's dtype attribute:

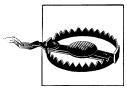
```
In [40]: int_array = np.arange(10)
```

```
In [41]: calibers = np.array([.22, .270, .357, .380, .44, .50], dtype=np.float64)

In [42]: int_array.astype(calibers.dtype)
Out[42]: array([ 0.,  1.,  2.,  3.,  4.,  5.,  6.,  7.,  8.,  9.])
```

There are shorthand type code strings you can also use to refer to a dtype:

```
In [43]: empty_uint32 = np.empty(8, dtype='u4')

In [44]: empty_uint32
Out[44]:
array([       0,        0, 65904672,        0, 64856792,        0,
       39438163,        0], dtype=uint32)
```

Calling `astype` *always* creates a new array (a copy of the data), even if the new dtype is the same as the old dtype.



It's worth keeping in mind that floating point numbers, such as those in `float64` and `float32` arrays, are only capable of approximating fractional quantities. In complex computations, you may accrue some *floating point error*, making comparisons only valid up to a certain number of decimal places.

Operations between Arrays and Scalars

Arrays are important because they enable you to express batch operations on data without writing any `for` loops. This is usually called *vectorization*. Any arithmetic operations between equal-size arrays applies the operation elementwise:

```
In [45]: arr = np.array([[1., 2., 3.], [4., 5., 6.]])

In [46]: arr
Out[46]:
array([[ 1.,  2.,  3.],
       [ 4.,  5.,  6.]])

In [47]: arr * arr
Out[47]:
array([[  1.,   4.,   9.],
       [ 16.,  25.,  36.]])

In [48]: arr - arr
Out[48]:
array([[ 0.,  0.,  0.],
       [ 0.,  0.,  0.]])
```

Arithmetic operations with scalars are as you would expect, propagating the value to each element:

```
In [49]: 1 / arr
Out[49]:
array([[ 1.    ,  0.5   ,  0.3333],
       [ 0.25  ,  0.2   ,  0.1667]])

In [50]: arr ** 0.5
Out[50]:
array([[ 1.    ,  1.4142,  1.7321],
       [ 2.    ,  2.2361,  2.4495]])
```

Operations between differently sized arrays is called *broadcasting* and will be discussed in more detail in Chapter 12. Having a deep understanding of broadcasting is not necessary for most of this book.

Basic Indexing and Slicing

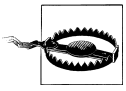
NumPy array indexing is a rich topic, as there are many ways you may want to select a subset of your data or individual elements. One-dimensional arrays are simple; on the surface they act similarly to Python lists:

```
In [51]: arr = np.arange(10)

In [52]: arr
Out[52]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])

In [53]: arr[5]
Out[53]: 5

In [54]: arr[5:8]
Out[54]: array([5, 6, 7])

In [55]: arr[5:8] = 12

In [56]: arr
Out[56]: array([ 0,  1,  2,  3,  4, 12, 12, 12,  8,  9])
```

As you can see, if you assign a scalar value to a slice, as in `arr[5:8] = 12`, the value is propagated (or *broadcasted* henceforth) to the entire selection. An important first distinction from lists is that array slices are *views* on the original array. This means that the data is not copied, and any modifications to the view will be reflected in the source array:

```
In [57]: arr_slice = arr[5:8]

In [58]: arr_slice[1] = 12345

In [59]: arr
Out[59]: array([    0,     1,     2,     3,     4,    12, 12345,    12,     8,     9])

In [60]: arr_slice[:] = 64

In [61]: arr
Out[61]: array([ 0,  1,  2,  3,  4, 64, 64, 64,  8,  9])
```

If you are new to NumPy, you might be surprised by this, especially if they have used other array programming languages which copy data more zealously. As NumPy has been designed with large data use cases in mind, you could imagine performance and memory problems if NumPy insisted on copying data left and right.



If you want a copy of a slice of an ndarray instead of a view, you will need to explicitly copy the array; for example `arr[5:8].copy()`.

With higher dimensional arrays, you have many more options. In a two-dimensional array, the elements at each index are no longer scalars but rather one-dimensional arrays:

```
In [62]: arr2d = np.array([[1, 2, 3], [4, 5, 6], [7, 8, 9]])

In [63]: arr2d[2]
Out[63]: array([7, 8, 9])
```

Thus, individual elements can be accessed recursively. But that is a bit too much work, so you can pass a comma-separated list of indices to select individual elements. So these are equivalent:

```
In [64]: arr2d[0][2]
Out[64]: 3

In [65]: arr2d[0, 2]
Out[65]: 3
```

See Figure 4-1 for an illustration of indexing on a 2D array.

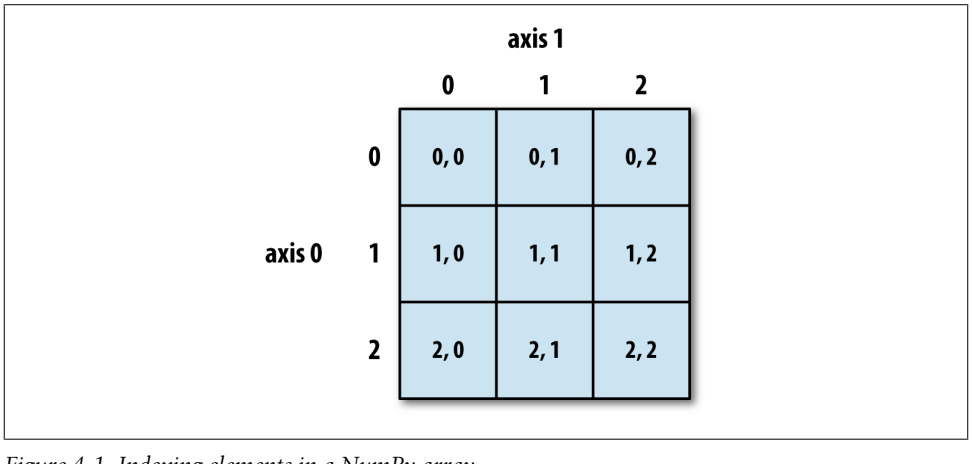


Figure 4-1. Indexing elements in a NumPy array

In multidimensional arrays, if you omit later indices, the returned object will be a lower-dimensional ndarray consisting of all the data along the higher dimensions. So in the 2 × 2 × 3 array `arr3d`

```
In [66]: arr3d = np.array([[[1, 2, 3], [4, 5, 6]], [[7, 8, 9], [10, 11, 12]]])

In [67]: arr3d
Out[67]:
array([[[ 1,  2,  3],
```

```
         [ 4,  5,  6]],
        [[ 7,  8,  9],
         [10, 11, 12]]])
```

`arr3d[0]` is a 2 × 3 array:

```
In [68]: arr3d[0]
Out[68]:
array([[1, 2, 3],
       [4, 5, 6]])
```

Both scalar values and arrays can be assigned to `arr3d[0]`:

```
In [69]: old_values = arr3d[0].copy()

In [70]: arr3d[0] = 42

In [71]: arr3d
Out[71]:
array([[[42, 42, 42],
        [42, 42, 42]],
       [[ 7,  8,  9],
        [10, 11, 12]]])

In [72]: arr3d[0] = old_values

In [73]: arr3d
Out[73]:
array([[[ 1,  2,  3],
        [ 4,  5,  6]],
       [[ 7,  8,  9],
        [10, 11, 12]]])
```

Similarly, `arr3d[1, 0]` gives you all of the values whose indices start with `(1, 0)`, forming a 1-dimensional array:

```
In [74]: arr3d[1, 0]
Out[74]: array([7, 8, 9])
```

Note that in all of these cases where subsections of the array have been selected, the returned arrays are views.

Indexing with slices

Like one-dimensional objects such as Python lists, ndarrays can be sliced using the familiar syntax:

```
In [75]: arr[1:6]
Out[75]: array([ 1,  2,  3,  4, 64])
```

Higher dimensional objects give you more options as you can slice one or more axes and also mix integers. Consider the 2D array above, `arr2d`. Slicing this array is a bit different:

```
In [76]: arr2d
Out[76]:
```

```
In [77]: arr2d[:2]
Out[77]:
```

```
array([[1, 2, 3],         array([[1, 2, 3],
       [4, 5, 6],                [4, 5, 6]])
       [7, 8, 9]])
```

As you can see, it has sliced along axis 0, the first axis. A slice, therefore, selects a range of elements along an axis. You can pass multiple slices just like you can pass multiple indexes:

```
In [78]: arr2d[:2, 1:]
Out[78]:
array([[2, 3],
       [5, 6]])
```

When slicing like this, you always obtain array views of the same number of dimensions. By mixing integer indexes and slices, you get lower dimensional slices:

```
In [79]: arr2d[1, :2]         In [80]: arr2d[2, :1]
Out[79]: array([4, 5])        Out[80]: array([7])
```

See Figure 4-2 for an illustration. Note that a colon by itself means to take the entire axis, so you can slice only higher dimensional axes by doing:

```
In [81]: arr2d[:, :1]
Out[81]:
array([[1],
       [4],
       [7]])
```

Of course, assigning to a slice expression assigns to the whole selection:

```
In [82]: arr2d[:2, 1:] = 0
```

Boolean Indexing

Let's consider an example where we have some data in an array and an array of names with duplicates. I'm going to use here the `randn` function in `numpy.random` to generate some random normally distributed data:

```
In [83]: names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])

In [84]: data = randn(7, 4)

In [85]: names
Out[85]:
array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'],
      dtype='|S4')

In [86]: data
Out[86]:
array([[-0.048 ,  0.5433, -0.2349,  1.2792],
       [-0.268 ,  0.5465,  0.0939, -2.0445],
       [-0.047 , -2.026 ,  0.7719,  0.3103],
       [ 2.1452,  0.8799, -0.0523,  0.0672],
       [-1.0023, -0.1698,  1.1503,  1.7289],
```

```
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174, -0.9297, -1.2564]])
```

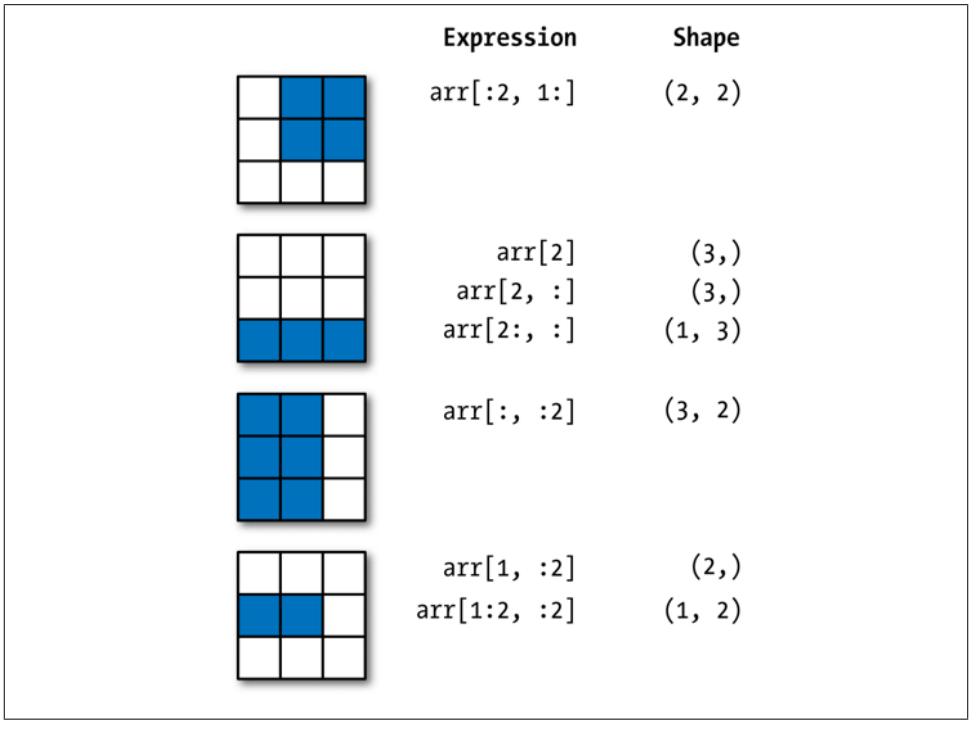


Figure 4-2. Two-dimensional array slicing

Suppose each name corresponds to a row in the `data` array. If we wanted to select all the rows with corresponding name `'Bob'`. Like arithmetic operations, comparisons (such as `==`) with arrays are also vectorized. Thus, comparing `names` with the string `'Bob'` yields a boolean array:

```
In [87]: names == 'Bob'
Out[87]: array([ True, False, False, True, False, False, False], dtype=bool)
```

This boolean array can be passed when indexing the array:

```
In [88]: data[names == 'Bob']
Out[88]:
array([[-0.048 ,  0.5433, -0.2349,  1.2792],
       [ 2.1452,  0.8799, -0.0523,  0.0672]])
```

The boolean array must be of the same length as the axis it's indexing. You can even mix and match boolean arrays with slices or integers (or sequences of integers, more on this later):

```
In [89]: data[names == 'Bob', 2:]
Out[89]:
array([[-0.2349,  1.2792],
```

```
       [-0.0523,  0.0672]])

In [90]: data[names == 'Bob', 3]
Out[90]: array([ 1.2792,  0.0672])
```

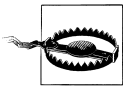
To select everything but `'Bob'`, you can either use `!=` or negate the condition using `-`:

```
In [91]: names != 'Bob'
Out[91]: array([False, True, True, False, True, True, True], dtype=bool)

In [92]: data[-(names == 'Bob')]
Out[92]:
array([[-0.268 ,  0.5465,  0.0939, -2.0445],
       [-0.047 , -2.026 ,  0.7719,  0.3103],
       [-1.0023, -0.1698,  1.1503,  1.7289],
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174, -0.9297, -1.2564]])
```

Selecting two of the three names to combine multiple boolean conditions, use boolean arithmetic operators like `&` (and) and `|` (or):

```
In [93]: mask = (names == 'Bob') | (names == 'Will')

In [94]: mask
Out[94]: array([True, False, True, True, True, False, False], dtype=bool)

In [95]: data[mask]
Out[95]:
array([[-0.048 ,  0.5433, -0.2349,  1.2792],
       [-0.047 , -2.026 ,  0.7719,  0.3103],
       [ 2.1452,  0.8799, -0.0523,  0.0672],
       [-1.0023, -0.1698,  1.1503,  1.7289]])
```

Selecting data from an array by boolean indexing *always* creates a copy of the data, even if the returned array is unchanged.



The Python keywords `and` and `or` do not work with boolean arrays.

Setting values with boolean arrays works in a common-sense way. To set all of the negative values in `data` to 0 we need only do:

```
In [96]: data[data < 0] = 0

In [97]: data
Out[97]:
array([[ 0.    ,  0.5433,  0.    ,  1.2792],
       [ 0.    ,  0.5465,  0.0939,  0.    ],
       [ 0.    ,  0.    ,  0.7719,  0.3103],
       [ 2.1452,  0.8799,  0.    ,  0.0672],
       [ 0.    ,  0.    ,  1.1503,  1.7289],
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174,  0.    ,  0.    ]])
```

Setting whole rows or columns using a 1D boolean array is also easy:

```
In [98]: data[names != 'Joe'] = 7

In [99]: data
Out[99]:
array([[ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 0.    ,  0.5465,  0.0939,  0.    ],
       [ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 7.    ,  7.    ,  7.    ,  7.    ],
       [ 0.1913,  0.4544,  0.4519,  0.5535],
       [ 0.5994,  0.8174,  0.    ,  0.    ]])
```

Fancy Indexing

Fancy indexing is a term adopted by NumPy to describe indexing using integer arrays. Suppose we had a 8 × 4 array:

```
In [100]: arr = np.empty((8, 4))

In [101]: for i in range(8):
   .....:     arr[i] = i

In [102]: arr
Out[102]:
array([[ 0.,  0.,  0.,  0.],
       [ 1.,  1.,  1.,  1.],
       [ 2.,  2.,  2.,  2.],
       [ 3.,  3.,  3.,  3.],
       [ 4.,  4.,  4.,  4.],
       [ 5.,  5.,  5.,  5.],
       [ 6.,  6.,  6.,  6.],
       [ 7.,  7.,  7.,  7.]])
```

To select out a subset of the rows in a particular order, you can simply pass a list or ndarray of integers specifying the desired order:

```
In [103]: arr[[4, 3, 0, 6]]
Out[103]:
array([[ 4.,  4.,  4.,  4.],
       [ 3.,  3.,  3.,  3.],
       [ 0.,  0.,  0.,  0.],
       [ 6.,  6.,  6.,  6.]])
```

Hopefully this code did what you expected! Using negative indices select rows from the end:

```
In [104]: arr[[-3, -5, -7]]
Out[104]:
array([[ 5.,  5.,  5.,  5.],
       [ 3.,  3.,  3.,  3.],
       [ 1.,  1.,  1.,  1.]])
```

Passing multiple index arrays does something slightly different; it selects a 1D array of elements corresponding to each tuple of indices:

```
# more on reshape in Chapter 12
In [105]: arr = np.arange(32).reshape((8, 4))

In [106]: arr
Out[106]:
array([[ 0,  1,  2,  3],
       [ 4,  5,  6,  7],
       [ 8,  9, 10, 11],
       [12, 13, 14, 15],
       [16, 17, 18, 19],
       [20, 21, 22, 23],
       [24, 25, 26, 27],
       [28, 29, 30, 31]])

In [107]: arr[[1, 5, 7, 2], [0, 3, 1, 2]]
Out[107]: array([ 4, 23, 29, 10])
```

Take a moment to understand what just happened: the elements `(1, 0)`, `(5, 3)`, `(7, 1)`, and `(2, 2)` were selected. The behavior of fancy indexing in this case is a bit different from what some users might have expected (myself included), which is the rectangular region formed by selecting a subset of the matrix's rows and columns. Here is one way to get that:

```
In [108]: arr[[1, 5, 7, 2]][:, [0, 3, 1, 2]]
Out[108]:
array([[ 4,  7,  5,  6],
       [20, 23, 21, 22],
       [28, 31, 29, 30],
       [ 8, 11,  9, 10]])
```

Another way is to use the `np.ix_` function, which converts two 1D integer arrays to an indexer that selects the square region:

```
In [109]: arr[np.ix_([1, 5, 7, 2], [0, 3, 1, 2])]
Out[109]:
array([[ 4,  7,  5,  6],
       [20, 23, 21, 22],
       [28, 31, 29, 30],
       [ 8, 11,  9, 10]])
```

Keep in mind that fancy indexing, unlike slicing, always copies the data into a new array.

Transposing Arrays and Swapping Axes

Transposing is a special form of reshaping which similarly returns a view on the underlying data without copying anything. Arrays have the `transpose` method and also the special `T` attribute:

```
In [110]: arr = np.arange(15).reshape((3, 5))

In [111]: arr                        In [112]: arr.T
```

```
Out[111]:
array([[ 0,  1,  2,  3,  4],
       [ 5,  6,  7,  8,  9],
       [10, 11, 12, 13, 14]])
```

```
Out[112]:
array([[ 0,  5, 10],
       [ 1,  6, 11],
       [ 2,  7, 12],
       [ 3,  8, 13],
       [ 4,  9, 14]])
```

When doing matrix computations, you will do this very often, like for example computing the inner matrix product X^TX using `np.dot`:

```
In [113]: arr = np.random.randn(6, 3)

In [114]: np.dot(arr.T, arr)
Out[114]:
array([[ 2.584 ,  1.8753,  0.8888],
       [ 1.8753,  6.6636,  0.3884],
       [ 0.8888,  0.3884,  3.9781]])
```

For higher dimensional arrays, `transpose` will accept a tuple of axis numbers to permute the axes (for extra mind bending):

```
In [115]: arr = np.arange(16).reshape((2, 2, 4))

In [116]: arr
Out[116]:
array([[[ 0,  1,  2,  3],
        [ 4,  5,  6,  7]],
       [[ 8,  9, 10, 11],
        [12, 13, 14, 15]]])

In [117]: arr.transpose((1, 0, 2))
Out[117]:
array([[[ 0,  1,  2,  3],
        [ 8,  9, 10, 11]],
       [[ 4,  5,  6,  7],
        [12, 13, 14, 15]]])
```

Simple transposing with `.T` is just a special case of swapping axes. ndarray has the method `swapaxes` which takes a pair of axis numbers:

```
In [118]: arr
Out[118]:
array([[[ 0,  1,  2,  3],
        [ 4,  5,  6,  7]],

       [[ 8,  9, 10, 11],
        [12, 13, 14, 15]]])
```

```
In [119]: arr.swapaxes(1, 2)
Out[119]:
array([[[ 0,  4],
        [ 1,  5],
        [ 2,  6],
        [ 3,  7]],

       [[ 8, 12],
        [ 9, 13],
        [10, 14],
        [11, 15]]])
```

`swapaxes` similarly returns a view on the data without making a copy.

Universal Functions: Fast Element-wise Array Functions

A universal function, or *ufunc*, is a function that performs elementwise operations on data in ndarrays. You can think of them as fast vectorized wrappers for simple functions that take one or more scalar values and produce one or more scalar results.

Many ufuncs are simple elementwise transformations, like `sqrt` or `exp`:

```
In [120]: arr = np.arange(10)

In [121]: np.sqrt(arr)
Out[121]:
array([ 0.    ,  1.    ,  1.4142,  1.7321,  2.    ,  2.2361,  2.4495,
        2.6458,  2.8284,  3.    ])

In [122]: np.exp(arr)
Out[122]:
array([    1.    ,     2.7183,     7.3891,    20.0855,    54.5982,
         148.4132,   403.4288,  1096.6332,  2980.958 ,  8103.0839])
```

These are referred to as *unary* ufuncs. Others, such as `add` or `maximum`, take 2 arrays (thus, *binary* ufuncs) and return a single array as the result:

```
In [123]: x = randn(8)

In [124]: y = randn(8)

In [125]: x
Out[125]:
array([ 0.0749,  0.0974,  0.2002, -0.2551,  0.4655,  0.9222,  0.446 ,
       -0.9337])

In [126]: y
Out[126]:
array([ 0.267 , -1.1131, -0.3361,  0.6117, -1.2323,  0.4788,  0.4315,
       -0.7147])

In [127]: np.maximum(x, y) # element-wise maximum
Out[127]:
array([ 0.267 ,  0.0974,  0.2002,  0.6117,  0.4655,  0.9222,  0.446 ,
       -0.7147])
```

While not common, a ufunc can return multiple arrays. `modf` is one example, a vectorized version of the built-in Python `divmod`: it returns the fractional and integral parts of a floating point array:

```
In [128]: arr = randn(7) * 5

In [129]: np.modf(arr)
Out[129]:
(array([-0.6808,  0.0636, -0.386 ,  0.1393, -0.8806,  0.9363, -0.883 ]),
 array([-2.,  4., -3.,  5., -3.,  3., -6.]))
```

See Table 4-3 and Table 4-4 for a listing of available ufuncs.

Table 4-3. Unary ufuncs

Function	Description
`abs, fabs`	Compute the absolute value element-wise for integer, floating point, or complex values. Use `fabs` as a faster alternative for non-complex-valued data
`sqrt`	Compute the square root of each element. Equivalent to `arr ** 0.5`
`square`	Compute the square of each element. Equivalent to `arr ** 2`
`exp`	Compute the exponent e^x of each element
`log, log10, log2, log1p`	Natural logarithm (base *e*), log base 10, log base 2, and log(1 + x), respectively
`sign`	Compute the sign of each element: 1 (positive), 0 (zero), or -1 (negative)
`ceil`	Compute the ceiling of each element, i.e. the smallest integer greater than or equal to each element
`floor`	Compute the floor of each element, i.e. the largest integer less than or equal to each element
`rint`	Round elements to the nearest integer, preserving the `dtype`
`modf`	Return fractional and integral parts of array as separate array
`isnan`	Return boolean array indicating whether each value is `NaN` (Not a Number)
`isfinite, isinf`	Return boolean array indicating whether each element is finite (non-`inf`, non-`NaN`) or infinite, respectively
`cos, cosh, sin, sinh, tan, tanh`	Regular and hyperbolic trigonometric functions
`arccos, arccosh, arcsin, arcsinh, arctan, arctanh`	Inverse trigonometric functions
`logical_not`	Compute truth value of `not x` element-wise. Equivalent to `-arr`.

Table 4-4. Binary universal functions

Function	Description
`add`	Add corresponding elements in arrays
`subtract`	Subtract elements in second array from first array
`multiply`	Multiply array elements
`divide, floor_divide`	Divide or floor divide (truncating the remainder)
`power`	Raise elements in first array to powers indicated in second array
`maximum, fmax`	Element-wise maximum. `fmax` ignores `NaN`
`minimum, fmin`	Element-wise minimum. `fmin` ignores `NaN`
`mod`	Element-wise modulus (remainder of division)
`copysign`	Copy sign of values in second argument to values in first argument

Function	Description
`greater, greater_equal, less, less_equal, equal, not_equal`	Perform element-wise comparison, yielding boolean array. Equivalent to infix operators `>, >=, <, <=, ==, !=`
`logical_and, logical_or, logical_xor`	Compute element-wise truth value of logical operation. Equivalent to infix operators `&, |, ^`

Data Processing Using Arrays

Using NumPy arrays enables you to express many kinds of data processing tasks as concise array expressions that might otherwise require writing loops. This practice of replacing explicit loops with array expressions is commonly referred to as *vectorization*. In general, vectorized array operations will often be one or two (or more) orders of magnitude faster than their pure Python equivalents, with the biggest impact in any kind of numerical computations. Later, in Chapter 12, I will explain *broadcasting*, a powerful method for vectorizing computations.

As a simple example, suppose we wished to evaluate the function `sqrt(x^2 + y^2)` across a regular grid of values. The `np.meshgrid` function takes two 1D arrays and produces two 2D matrices corresponding to all pairs of `(x, y)` in the two arrays:

```
In [130]: points = np.arange(-5, 5, 0.01) # 1000 equally spaced points

In [131]: xs, ys = np.meshgrid(points, points)

In [132]: ys
Out[132]:
array([[-5.  , -5.  , -5.  , ..., -5.  , -5.  , -5.  ],
       [-4.99, -4.99, -4.99, ..., -4.99, -4.99, -4.99],
       [-4.98, -4.98, -4.98, ..., -4.98, -4.98, -4.98],
       ...,
       [ 4.97,  4.97,  4.97, ...,  4.97,  4.97,  4.97],
       [ 4.98,  4.98,  4.98, ...,  4.98,  4.98,  4.98],
       [ 4.99,  4.99,  4.99, ...,  4.99,  4.99,  4.99]])
```

Now, evaluating the function is a simple matter of writing the same expression you would write with two points:

```
In [134]: import matplotlib.pyplot as plt

In [135]: z = np.sqrt(xs ** 2 + ys ** 2)

In [136]: z
Out[136]:
array([[ 7.0711,  7.064 ,  7.0569, ...,  7.0499,  7.0569,  7.064 ],
       [ 7.064 ,  7.0569,  7.0499, ...,  7.0428,  7.0499,  7.0569],
       [ 7.0569,  7.0499,  7.0428, ...,  7.0357,  7.0428,  7.0499],
       ...,
       [ 7.0499,  7.0428,  7.0357, ...,  7.0286,  7.0357,  7.0428],
       [ 7.0569,  7.0499,  7.0428, ...,  7.0357,  7.0428,  7.0499],
       [ 7.064 ,  7.0569,  7.0499, ...,  7.0428,  7.0499,  7.0569]])
```

```
In [137]: plt.imshow(z, cmap=plt.cm.gray); plt.colorbar()
Out[137]: <matplotlib.colorbar.Colorbar instance at 0x4e46d40>

In [138]: plt.title("Image plot of $\sqrt{x^2 + y^2}$ for a grid of values")
Out[138]: <matplotlib.text.Text at 0x4565790>
```

See Figure 4-3. Here I used the matplotlib function `imshow` to create an image plot from a 2D array of function values.

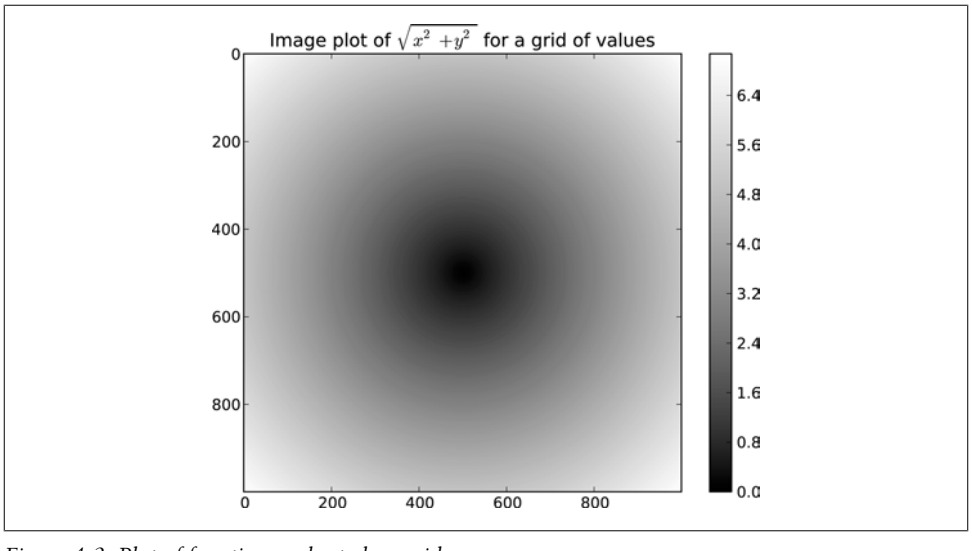


Figure 4-3. Plot of function evaluated on grid

Expressing Conditional Logic as Array Operations

The `numpy.where` function is a vectorized version of the ternary expression `x if condition else y`. Suppose we had a boolean array and two arrays of values:

```
In [140]: xarr = np.array([1.1, 1.2, 1.3, 1.4, 1.5])

In [141]: yarr = np.array([2.1, 2.2, 2.3, 2.4, 2.5])

In [142]: cond = np.array([True, False, True, True, False])
```

Suppose we wanted to take a value from `xarr` whenever the corresponding value in `cond` is `True` otherwise take the value from `yarr`. A list comprehension doing this might look like:

```
In [143]: result = [(x if c else y)
   .....:           for x, y, c in zip(xarr, yarr, cond)]

In [144]: result
Out[144]: [1.1000000000000001, 2.2000000000000002, 1.3, 1.3999999999999999, 2.5]
```

This has multiple problems. First, it will not be very fast for large arrays (because all the work is being done in pure Python). Secondly, it will not work with multidimensional arrays. With `np.where` you can write this very concisely:

```
In [145]: result = np.where(cond, xarr, yarr)

In [146]: result
Out[146]: array([ 1.1,  2.2,  1.3,  1.4,  2.5])
```

The second and third arguments to `np.where` don't need to be arrays; one or both of them can be scalars. A typical use of `where` in data analysis is to produce a new array of values based on another array. Suppose you had a matrix of randomly generated data and you wanted to replace all positive values with 2 and all negative values with -2. This is very easy to do with `np.where`:

```
In [147]: arr = randn(4, 4)

In [148]: arr
Out[148]:
array([[ 0.6372,  2.2043,  1.7904,  0.0752],
       [-1.5926, -1.1536,  0.4413,  0.3483],
       [-0.1798,  0.3299,  0.7827, -0.7585],
       [ 0.5857,  0.1619,  1.3583, -1.3865]])

In [149]: np.where(arr > 0, 2, -2)
Out[149]:
array([[ 2,  2,  2,  2],
       [-2, -2,  2,  2],
       [-2,  2,  2, -2],
       [ 2,  2,  2, -2]])

In [150]: np.where(arr > 0, 2, arr) # set only positive values to 2
Out[150]:
array([[ 2.    ,  2.    ,  2.    ,  2.    ],
       [-1.5926, -1.1536,  2.    ,  2.    ],
       [-0.1798,  2.    ,  2.    , -0.7585],
       [ 2.    ,  2.    ,  2.    , -1.3865]])
```

The arrays passed to `where` can be more than just equal sizes array or scalers.

With some cleverness you can use `where` to express more complicated logic; consider this example where I have two boolean arrays, `cond1` and `cond2`, and wish to assign a different value for each of the 4 possible pairs of boolean values:

```
result = []
for i in range(n):
    if cond1[i] and cond2[i]:
        result.append(0)
    elif cond1[i]:
        result.append(1)
    elif cond2[i]:
        result.append(2)
    else:
        result.append(3)
```

While perhaps not immediately obvious, this `for` loop can be converted into a nested `where` expression:

```
np.where(cond1 & cond2, 0,
         np.where(cond1, 1,
                  np.where(cond2, 2, 3)))
```

In this particular example, we can also take advantage of the fact that boolean values are treated as 0 or 1 in calculations, so this could alternatively be expressed (though a bit more cryptically) as an arithmetic operation:

```
result = 1 * cond1 + 2 * cond2 + 3 * -(cond1 | cond2)
```

Mathematical and Statistical Methods

A set of mathematical functions which compute statistics about an entire array or about the data along an axis are accessible as array methods. Aggregations (often called *reductions*) like `sum`, `mean`, and standard deviation `std` can either be used by calling the array instance method or using the top level NumPy function:

```
In [151]: arr = np.random.randn(5, 4) # normally-distributed data

In [152]: arr.mean()
Out[152]: 0.062814911084854597

In [153]: np.mean(arr)
Out[153]: 0.062814911084854597

In [154]: arr.sum()
Out[154]: 1.2562982216970919
```

Functions like `mean` and `sum` take an optional `axis` argument which computes the statistic over the given axis, resulting in an array with one fewer dimension:

```
In [155]: arr.mean(axis=1)
Out[155]: array([-1.2833,  0.2844,  0.6574,  0.6743, -0.0187])

In [156]: arr.sum(0)
Out[156]: array([-3.1003, -1.6189,  1.4044,  4.5712])
```

Other methods like `cumsum` and `cumprod` do not aggregate, instead producing an array of the intermediate results:

```
In [157]: arr = np.array([[0, 1, 2], [3, 4, 5], [6, 7, 8]])

In [158]: arr.cumsum(0)
Out[158]:
array([[ 0,  1,  2],
       [ 3,  5,  7],
       [ 9, 12, 15]])

In [159]: arr.cumprod(1)
Out[159]:
array([[  0,   0,   0],
       [  3,  12,  60],
       [  6,  42, 336]])
```

See Table 4-5 for a full listing. We'll see many examples of these methods in action in later chapters.

Table 4-5. Basic array statistical methods

Method	Description
`sum`	Sum of all the elements in the array or along an axis. Zero-length arrays have sum 0.
`mean`	Arithmetic mean. Zero-length arrays have NaN mean.
`std, var`	Standard deviation and variance, respectively, with optional degrees of freedom adjustment (default denominator n).
`min, max`	Minimum and maximum.
`argmin, argmax`	Indices of minimum and maximum elements, respectively.
`cumsum`	Cumulative sum of elements starting from 0
`cumprod`	Cumulative product of elements starting from 1

Methods for Boolean Arrays

Boolean values are coerced to 1 (`True`) and 0 (`False`) in the above methods. Thus, `sum` is often used as a means of counting `True` values in a boolean array:

```
In [160]: arr = randn(100)

In [161]: (arr > 0).sum() # Number of positive values
Out[161]: 44
```

There are two additional methods, `any` and `all`, useful especially for boolean arrays. `any` tests whether one or more values in an array is `True`, while `all` checks if every value is `True`:

```
In [162]: bools = np.array([False, False, True, False])

In [163]: bools.any()
Out[163]: True

In [164]: bools.all()
Out[164]: False
```

These methods also work with non-boolean arrays, where non-zero elements evaluate to `True`.

Sorting

Like Python's built-in list type, NumPy arrays can be sorted in-place using the `sort` method:

```
In [165]: arr = randn(8)

In [166]: arr
Out[166]:
array([ 0.6903,  0.4678,  0.0968, -0.1349,  0.9879,  0.0185, -1.3147,
       -0.5425])

In [167]: arr.sort()
```

```
In [168]: arr
Out[168]:
array([-1.3147, -0.5425, -0.1349,  0.0185,  0.0968,  0.4678,  0.6903,
        0.9879])
```

Multidimensional arrays can have each 1D section of values sorted in-place along an axis by passing the axis number to `sort`:

```
In [169]: arr = randn(5, 3)

In [170]: arr
Out[170]:
array([[-0.7139, -1.6331, -0.4959],
       [ 0.8236, -1.3132, -0.1935],
       [-1.6748,  3.0336, -0.863 ],
       [-0.3161,  0.5362, -2.468 ],
       [ 0.9058,  1.1184, -1.0516]])

In [171]: arr.sort(1)

In [172]: arr
Out[172]:
array([[-1.6331, -0.7139, -0.4959],
       [-1.3132, -0.1935,  0.8236],
       [-1.6748, -0.863 ,  3.0336],
       [-2.468 , -0.3161,  0.5362],
       [-1.0516,  0.9058,  1.1184]])
```

The top level method `np.sort` returns a sorted copy of an array instead of modifying the array in place. A quick-and-dirty way to compute the quantiles of an array is to sort it and select the value at a particular rank:

```
In [173]: large_arr = randn(1000)

In [174]: large_arr.sort()

In [175]: large_arr[int(0.05 * len(large_arr))] # 5% quantile
Out[175]: -1.5791023260896004
```

For more details on using NumPy's sorting methods, and more advanced techniques like indirect sorts, see Chapter 12. Several other kinds of data manipulations related to sorting (for example, sorting a table of data by one or more columns) are also to be found in pandas.

Unique and Other Set Logic

NumPy has some basic set operations for one-dimensional ndarrays. Probably the most commonly used one is `np.unique`, which returns the sorted unique values in an array:

```
In [176]: names = np.array(['Bob', 'Joe', 'Will', 'Bob', 'Will', 'Joe', 'Joe'])

In [177]: np.unique(names)
Out[177]:
```

```
array(['Bob', 'Joe', 'Will'],
      dtype='|S4')

In [178]: ints = np.array([3, 3, 3, 2, 2, 1, 1, 4, 4])

In [179]: np.unique(ints)
Out[179]: array([1, 2, 3, 4])
```

Contrast `np.unique` with the pure Python alternative:

```
In [180]: sorted(set(names))
Out[180]: ['Bob', 'Joe', 'Will']
```

Another function, `np.in1d`, tests membership of the values in one array in another, returning a boolean array:

```
In [181]: values = np.array([6, 0, 0, 3, 2, 5, 6])

In [182]: np.in1d(values, [2, 3, 6])
Out[182]: array([ True, False, False,  True,  True, False,  True], dtype=bool)
```

See Table 4-6 for a listing of set functions in NumPy.

Table 4-6. Array set operations

Method	Description
`unique(x)`	Compute the sorted, unique elements in x
`intersect1d(x, y)`	Compute the sorted, common elements in x and y
`union1d(x, y)`	Compute the sorted union of elements
`in1d(x, y)`	Compute a boolean array indicating whether each element of x is contained in y
`setdiff1d(x, y)`	Set difference, elements in x that are not in y
`setxor1d(x, y)`	Set symmetric differences; elements that are in either of the arrays, but not both

File Input and Output with Arrays

NumPy is able to save and load data to and from disk either in text or binary format. In later chapters you will learn about tools in pandas for reading tabular data into memory.

Storing Arrays on Disk in Binary Format

`np.save` and `np.load` are the two workhorse functions for efficiently saving and loading array data on disk. Arrays are saved by default in an uncompressed raw binary format with file extension `.npy`.

```
In [183]: arr = np.arange(10)

In [184]: np.save('some_array', arr)
```

If the file path does not already end in `.npy`, the extension will be appended. The array on disk can then be loaded using `np.load`:

```
In [185]: np.load('some_array.npy')
Out[185]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

You save multiple arrays in a zip archive using `np.savez` and passing the arrays as keyword arguments:

```
In [186]: np.savez('array_archive.npz', a=arr, b=arr)
```

When loading an `.npz` file, you get back a dict-like object which loads the individual arrays lazily:

```
In [187]: arch = np.load('array_archive.npz')

In [188]: arch['b']
Out[188]: array([0, 1, 2, 3, 4, 5, 6, 7, 8, 9])
```

Saving and Loading Text Files

Loading text from files is a fairly standard task. The landscape of file reading and writing functions in Python can be a bit confusing for a newcomer, so I will focus mainly on the `read_csv` and `read_table` functions in pandas. It will at times be useful to load data into vanilla NumPy arrays using `np.loadtxt` or the more specialized `np.genfromtxt`.

These functions have many options allowing you to specify different delimiters, converter functions for certain columns, skipping rows, and other things. Take a simple case of a comma-separated file (CSV) like this:

```
In [191]: !cat array_ex.txt
0.580052,0.186730,1.040717,1.134411
0.194163,-0.636917,-0.938659,0.124094
-0.126410,0.268607,-0.695724,0.047428
-1.484413,0.004176,-0.744203,0.005487
2.302869,0.200131,1.670238,-1.881090
-0.193230,1.047233,0.482803,0.960334
```

This can be loaded into a 2D array like so:

```
In [192]: arr = np.loadtxt('array_ex.txt', delimiter=',')

In [193]: arr
Out[193]:
array([[ 0.5801,  0.1867,  1.0407,  1.1344],
       [ 0.1942, -0.6369, -0.9387,  0.1241],
       [-0.1264,  0.2686, -0.6957,  0.0474],
       [-1.4844,  0.0042, -0.7442,  0.0055],
       [ 2.3029,  0.2001,  1.6702, -1.8811],
       [-0.1932,  1.0472,  0.4828,  0.9603]])
```

`np.savetxt` performs the inverse operation: writing an array to a delimited text file. `genfromtxt` is similar to `loadtxt` but is geared for structured arrays and missing data handling; see Chapter 12 for more on structured arrays.

For more on file reading and writing, especially tabular or spreadsheet-like data, see the later chapters involving pandas and DataFrame objects.

Linear Algebra

Linear algebra, like matrix multiplication, decompositions, determinants, and other square matrix math, is an important part of any array library. Unlike some languages like MATLAB, multiplying two two-dimensional arrays with * is an element-wise product instead of a matrix dot product. As such, there is a function `dot`, both an array method, and a function in the `numpy` namespace, for matrix multiplication:

```
In [194]: x = np.array([[1., 2., 3.], [4., 5., 6.]])

In [195]: y = np.array([[6., 23.], [-1, 7], [8, 9]])

In [196]: x                    In [197]: y
Out[196]:                      Out[197]:
array([[ 1.,  2.,  3.],       array([[  6.,  23.],
       [ 4.,  5.,  6.]])              [ -1.,   7.],
                                      [  8.,   9.]])

In [198]: x.dot(y)  # equivalently np.dot(x, y)
Out[198]:
array([[  28.,   64.],
       [  67.,  181.]])
```

A matrix product between a 2D array and a suitably sized 1D array results in a 1D array:

```
In [199]: np.dot(x, np.ones(3))
Out[199]: array([  6.,  15.])
```

`numpy.linalg` has a standard set of matrix decompositions and things like inverse and determinant. These are implemented under the hood using the same industry-standard Fortran libraries used in other languages like MATLAB and R, such as like BLAS, LAPACK, or possibly (depending on your NumPy build) the Intel MKL:

```
In [201]: from numpy.linalg import inv, qr

In [202]: X = randn(5, 5)

In [203]: mat = X.T.dot(X)

In [204]: inv(mat)
Out[204]:
array([[ 3.0361, -0.1808, -0.6878, -2.8285, -1.1911],
       [-0.1808,  0.5035,  0.1215,  0.6702,  0.0956],
       [-0.6878,  0.1215,  0.2904,  0.8081,  0.3049],
       [-2.8285,  0.6702,  0.8081,  3.4152,  1.1557],
       [-1.1911,  0.0956,  0.3049,  1.1557,  0.6051]])

In [205]: mat.dot(inv(mat))
```

```
Out[205]:
array([[ 1.,  0.,  0.,  0., -0.],
       [ 0.,  1., -0.,  0.,  0.],
       [ 0., -0.,  1.,  0.,  0.],
       [ 0., -0., -0.,  1., -0.],
       [ 0.,  0.,  0.,  0.,  1.]])

In [206]: q, r = qr(mat)

In [207]: r
Out[207]:
array([[ -6.9271,   7.389 ,   6.1227,  -7.1163,  -4.9215],
       [  0.    ,  -3.9735,  -0.8671,   2.9747,  -5.7402],
       [  0.    ,   0.    , -10.2681,   1.8909,   1.6079],
       [  0.    ,   0.    ,   0.    ,  -1.2996,   3.3577],
       [  0.    ,   0.    ,   0.    ,   0.    ,   0.5571]])
```

See Table 4-7 for a list of some of the most commonly-used linear algebra functions.

The scientific Python community is hopeful that there may be a matrix multiplication infix operator implemented someday, providing syntactically nicer alternative to using `np.dot`. But for now this is the way.

Table 4-7. Commonly-used numpy.linalg functions

Function	Description
`diag`	Return the diagonal (or off-diagonal) elements of a square matrix as a 1D array, or convert a 1D array into a square matrix with zeros on the off-diagonal
`dot`	Matrix multiplication
`trace`	Compute the sum of the diagonal elements
`det`	Compute the matrix determinant
`eig`	Compute the eigenvalues and eigenvectors of a square matrix
`inv`	Compute the inverse of a square matrix
`pinv`	Compute the Moore-Penrose pseudo-inverse inverse of a square matrix
`qr`	Compute the QR decomposition
`svd`	Compute the singular value decomposition (SVD)
`solve`	Solve the linear system Ax = b for x, where A is a square matrix
`lstsq`	Compute the least-squares solution to y = Xb

Random Number Generation

The `numpy.random` module supplements the built-in Python `random` with functions for efficiently generating whole arrays of sample values from many kinds of probability

distributions. For example, you can get a 4 by 4 array of samples from the standard normal distribution using `normal`:

```
In [208]: samples = np.random.normal(size=(4, 4))

In [209]: samples
Out[209]:
array([[ 0.1241,  0.3026,  0.5238,  0.0009],
       [ 1.3438, -0.7135, -0.8312, -2.3702],
       [-1.8608, -0.8608,  0.5601, -1.2659],
       [ 0.1198, -1.0635,  0.3329, -2.3594]])
```

Python's built-in `random` module, by contrast, only samples one value at a time. As you can see from this benchmark, `numpy.random` is well over an order of magnitude faster for generating very large samples:

```
In [210]: from random import normalvariate

In [211]: N = 1000000

In [212]: %timeit samples = [normalvariate(0, 1) for _ in xrange(N)]
1 loops, best of 3: 1.33 s per loop

In [213]: %timeit np.random.normal(size=N)
10 loops, best of 3: 57.7 ms per loop
```

See table Table 4-8 for a partial list of functions available in `numpy.random`. I'll give some examples of leveraging these functions' ability to generate large arrays of samples all at once in the next section.

Table 4-8. Partial list of numpy.random functions

Function	Description
`seed`	Seed the random number generator
`permutation`	Return a random permutation of a sequence, or return a permuted range
`shuffle`	Randomly permute a sequence in place
`rand`	Draw samples from a uniform distribution
`randint`	Draw random integers from a given low-to-high range
`randn`	Draw samples from a normal distribution with mean 0 and standard deviation 1 (MATLAB-like interface)
`binomial`	Draw samples a binomial distribution
`normal`	Draw samples from a normal (Gaussian) distribution
`beta`	Draw samples from a beta distribution
`chisquare`	Draw samples from a chi-square distribution
`gamma`	Draw samples from a gamma distribution
`uniform`	Draw samples from a uniform [0, 1) distribution

Example: Random Walks

An illustrative application of utilizing array operations is in the simulation of random walks. Let's first consider a simple random walk starting at 0 with steps of 1 and -1 occurring with equal probability. A pure Python way to implement a single random walk with 1,000 steps using the built-in `random` module:

```
import random
position = 0
walk = [position]
steps = 1000
for i in xrange(steps):
    step = 1 if random.randint(0, 1) else -1
    position += step
    walk.append(position)
```

See Figure 4-4 for an example plot of the first 100 values on one of these random walks.

Figure 4-4. A simple random walk

You might make the observation that `walk` is simply the cumulative sum of the random steps and could be evaluated as an array expression. Thus, I use the `np.random` module to draw 1,000 coin flips at once, set these to 1 and -1, and compute the cumulative sum:

```
In [215]: nsteps = 1000

In [216]: draws = np.random.randint(0, 2, size=nsteps)

In [217]: steps = np.where(draws > 0, 1, -1)

In [218]: walk = steps.cumsum()
```

From this we can begin to extract statistics like the minimum and maximum value along the walk's trajectory:

```
In [219]: walk.min()
Out[219]: -3
```

```
In [220]: walk.max()
Out[220]: 31
```

A more complicated statistic is the *first crossing time*, the step at which the random walk reaches a particular value. Here we might want to know how long it took the random walk to get at least 10 steps away from the origin 0 in either direction. `np.abs(walk) >= 10` gives us a boolean array indicating where the walk has reached or exceeded 10, but we want the index of the *first* 10 or -10. Turns out this can be computed using `argmax`, which returns the first index of the maximum value in the boolean array (`True` is the maximum value):

```
In [221]: (np.abs(walk) >= 10).argmax()
Out[221]: 37
```

Note that using `argmax` here is not always efficient because it always makes a full scan of the array. In this special case once a `True` is observed we know it to be the maximum value.

Simulating Many Random Walks at Once

If your goal was to simulate many random walks, say 5,000 of them, you can generate all of the random walks with minor modifications to the above code. The `numpy.random` functions if passed a 2-tuple will generate a 2D array of draws, and we can compute the cumulative sum across the rows to compute all 5,000 random walks in one shot:

```
In [222]: nwalks = 5000

In [223]: nsteps = 1000

In [224]: draws = np.random.randint(0, 2, size=(nwalks, nsteps)) # 0 or 1

In [225]: steps = np.where(draws > 0, 1, -1)

In [226]: walks = steps.cumsum(1)

In [227]: walks
Out[227]:
array([[  1,   0,   1, ...,   8,   7,   8],
       [  1,   0,  -1, ...,  34,  33,  32],
       [  1,   0,  -1, ...,   4,   5,   4],
       ...,
       [  1,   2,   1, ...,  24,  25,  26],
       [  1,   2,   3, ...,  14,  13,  14],
       [ -1,  -2,  -3, ..., -24, -23, -22]])
```

Now, we can compute the maximum and minimum values obtained over all of the walks:

```
In [228]: walks.max()
Out[228]: 138
```

```
In [229]: walks.min()
Out[229]: -133
```

Out of these walks, let's compute the minimum crossing time to 30 or -30. This is slightly tricky because not all 5,000 of them reach 30. We can check this using the `any` method:

```
In [230]: hits30 = (np.abs(walks) >= 30).any(1)

In [231]: hits30
Out[231]: array([False, True, False, ..., False, True, False], dtype=bool)

In [232]: hits30.sum() # Number that hit 30 or -30
Out[232]: 3410
```

We can use this boolean array to select out the rows of `walks` that actually cross the absolute 30 level and call `argmax` across axis 1 to get the crossing times:

```
In [233]: crossing_times = (np.abs(walks[hits30]) >= 30).argmax(1)

In [234]: crossing_times.mean()
Out[234]: 498.88973607038122
```

Feel free to experiment with other distributions for the steps other than equal sized coin flips. You need only use a different random number generation function, like `normal` to generate normally distributed steps with some mean and standard deviation:

```
In [235]: steps = np.random.normal(loc=0, scale=0.25,
   .....:                          size=(nwalks, nsteps))
```

CHAPTER 5
Getting Started with pandas

pandas will be the primary library of interest throughout much of the rest of the book. It contains high-level data structures and manipulation tools designed to make data analysis fast and easy in Python. pandas is built on top of NumPy and makes it easy to use in NumPy-centric applications.

As a bit of background, I started building pandas in early 2008 during my tenure at AQR, a quantitative investment management firm. At the time, I had a distinct set of requirements that were not well-addressed by any single tool at my disposal:

- Data structures with labeled axes supporting automatic or explicit data alignment. This prevents common errors resulting from misaligned data and working with differently-indexed data coming from different sources.
- Integrated time series functionality.
- The same data structures handle both time series data and non-time series data.
- Arithmetic operations and reductions (like summing across an axis) would pass on the metadata (axis labels).
- Flexible handling of missing data.
- Merge and other relational operations found in popular database databases (SQL-based, for example).

I wanted to be able to do all of these things in one place, preferably in a language well-suited to general purpose software development. Python was a good candidate language for this, but at that time there was not an integrated set of data structures and tools providing this functionality.

Over the last four years, pandas has matured into a quite large library capable of solving a much broader set of data handling problems than I ever anticipated, but it has expanded in its scope without compromising the simplicity and ease-of-use that I desired from the very beginning. I hope that after reading this book, you will find it to be just as much of an indispensable tool as I do.

Throughout the rest of the book, I use the following import conventions for pandas: