

Summary Backpropagation

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Dipelajari dari <https://mattmazur.com/2015/03/17/a-step-by-step-backpropagation-example/>

Desain contoh:
2 input, 2 hidden neuron,
2 output neuron

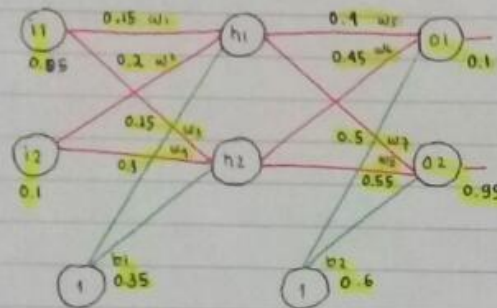
Forward Pass Hidden
layer dan Output layer

Menghitung total error
dengan MSE

Backprop - Step by step

Matmazur

Neural Network dengan 2 input, 2 hidden neuron, 2 output neuron
Hidden dan output memiliki bias.



Ig diolah di atas adalah single training set (1 data sample, 2 attribut)
diberikan input 0,05 dan 0,1, NN ditrain u/ menghasilkan
output 0,01 dan 0,99

Forward Pass

menghitung total net input pd tiap neuron di hidden layer, menerapkan
fungsi aktivasi logistic function, ulangi u/ neuron pd layer output

* net input u/ h1

$$\text{net } h1 = w1 * i1 + w2 * i2 + b1 * 1 = 0.15 * 0.05 + 0.2 * 0.1 + 0.35$$

$$= 0.445 \quad 0.3775$$

* fungsi aktivasi logistik (e = 2,71828)

$$\text{out } h1 = \frac{1}{1 + e^{-\text{net } h1}} = \frac{1}{1 + 0.68557} = 0.5932699921 \quad \text{h1 out}$$

$$\text{net } h2 = w3 * i1 + w4 * i2 + b2 * 1 = 0.25 * 0.05 + 0.3 * 0.1 + 0.35 * 1$$

$$= 0.3925$$

$$\text{out } h2 = \frac{1}{1 + e^{-0.3925}} = \frac{1}{1.6753663} = 0.59688437826 \quad \text{h2 out}$$

HIDDEN LAYER ↑

OUTPUT LAYER ↓

$$\text{* net } o1 = w5 * h1 + w6 * h2 + b2 * 1 \quad (h1, h2 \text{ out} \rightarrow \text{hasil stlh aktivasi})$$

$$= 0.4 * 0.593269 + 0.45 * 0.596884 + 0.6$$

$$= 1.10590596706$$

$$\text{* out } o1 = \frac{1}{1 + e^{-\text{net } o1}} = \frac{1}{1.33091095198} = 0.75136506955 \quad \text{o1 out}$$

$$\text{* net } o2 = w7 * h1 \text{ out} + w8 * h2 \text{ out} + b2 * 1$$

$$= 0.5 * 0.593269 + 0.55 * 0.596884 + 0.6$$

$$= 1.22492140409$$

$$\text{* out } o2 = \frac{1}{1 + e^{-\text{net } o2}} = \frac{1}{1.29378078938} = 0.77292846532 \quad \text{o2 out}$$

Menghitung Total Error

hitung error untuk tiap output neuron dengan Squared Error

$$E_{\text{total}} = \sum \frac{1}{2} (\text{target} - \text{output})^2$$

$$E = \frac{1}{2} (\text{target} - \text{actual})^2$$

- wikipedia -

* Error o1

$$E_{o1} = \frac{1}{2} (0.01 - 0.75136506955)^2 = \frac{1}{2} * 0.54962216634 = 0.27481108317$$

* Error o2

$$E_{o2} = \frac{1}{2} (0.99 - 0.77292846532)^2 = \frac{1}{2} * 0.04712005116 = 0.02356002558$$

* Total Error

$$E_{\text{total}} = E_{o1} + E_{o2} = 0.29837110875$$

Backward Pass dan
update bobot

Backward Pass

Tujuan dari backpropagation adlh meng-update tiap bobot dlm jaringan/network, sehingga nilai yg dihasilkan model mendekati nilai aslinya, dengan demikian meminimalkan error pd tiap output dan scr keseluruhan arsitektur.

OUTPUT LAYER ↓

* perhatikan w_5

seberapa banyak w_5 mempengaruhi total error,
 perubahan

atau ditulis $\frac{\partial E_{total}}{\partial w_5}$

dibaca "derivatif partial dari E_{total} terhadap w_5 "
atau bisa juga "gradien w_5 "

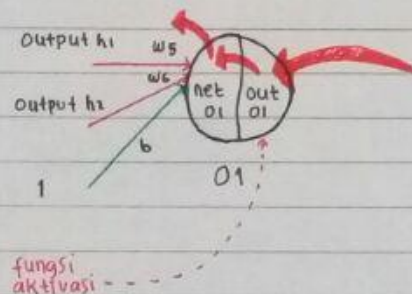
dengan chain-rule dapat ditulis

$$\frac{dz}{dx} = \frac{dy}{dy} \cdot \frac{dy}{dx}$$

- wikipedia -

$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial out_{01}} \times \frac{\partial out_{01}}{\partial net_{01}} \times \frac{\partial net_{01}}{\partial w_5}$$

secara visual jika dilihat neuron pada network:



$$E_{01} = \frac{1}{2} (target_{01} - out_{01})^2$$

$$E_{total} = E_{01} + E_{02}$$

$$\frac{\partial net_{01}}{\partial w_5} \times \frac{\partial out_{01}}{\partial net_{01}} \times \frac{\partial E_{total}}{\partial out_{01}} = \frac{\partial E_{total}}{\partial w_5}$$

Perhitungan turunannya :

$$E_{total} = \frac{1}{2} (target_{01} - out_{01})^2 + \frac{1}{2} (target_{02} - out_{02})^2$$

$$\frac{\partial E_{total}}{\partial out_{01}} = 2 \times \frac{1}{2} (target_{01} - out_{01}) \times (-1) + 0$$

$$= - (target_{01} - out_{01}) \rightarrow \text{dapat juga ditulis}$$

$$= - (0,01 - 0,75136506955) \quad \text{out - target}$$

$$= 0,74136506955$$

$$* out_{01} = \frac{1}{1 + e^{-net_{01}}}$$

$$* \frac{\partial out_{01}}{\partial net_{01}} = out_{01} (1 - out_{01})$$

$$= 0,75136506955 (1 - 0,75136506955)$$

$$= 0,18681560181$$

$$* net_{01} = w_5 * out_{h1} + w_6 * out_{h2} + b_2 * 1$$

$$* \frac{\partial net_{01}}{\partial w_5} = out_{h1}$$

$$= 0,5932699921$$

derivative log function

$$f(x) = \frac{1}{1 + e^{-x}} = \frac{e^x}{1 + e^x}$$

$$\frac{d}{dx} f(x) = \frac{e^x (1 + e^x) - e^x \cdot e^x}{(1 + e^x)^2}$$

$$= \frac{e^x}{(1 + e^x)^2}$$

$$= f(x) (1 - f(x))$$

- wikipedia -

** balik ke chain rule

$$\frac{\partial E_{total}}{\partial w_5} = \frac{\partial E_{total}}{\partial out_{01}} \times \frac{\partial out_{01}}{\partial net_{01}} \times \frac{\partial net_{01}}{\partial w_5}$$

$$= 0,74136506955 \times 0,18681560181 \times 0,5932699921$$

$$= 0,082167041$$

update bobot

dengan $\eta = 0,5$ (learning rate)

$$* w_5' = w_5 - \eta \times \frac{\partial E_{total}}{\partial w_5}$$

$$= 0,4 - (0,5 \times 0,082167041)$$

$$= 0,35891648$$

learning rate,
 $\eta = \eta$ bisa juga
dengan alfa α ,
atau epsilon ϵ .

Backward Pass dan
update bobot (2)

No.

Date

No.

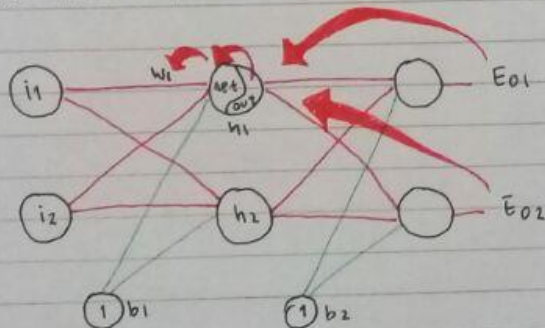
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Hidden layer

Setelah backward pass melalui output layer, sekarang dilanjutkan ke hidden layer, untuk update w_1, w_2, w_3, w_4 .
misal untuk w_1 ,

$$\frac{\partial E_{total}}{\partial w_1} = \frac{\partial E_{total}}{\partial out_{h1}} * \frac{\partial out_{h1}}{\partial net_{h1}} * \frac{\partial net_{h1}}{\partial w_1}$$

secara visual :



$$\frac{\partial net_{h1}}{\partial w_1} * \frac{\partial out_{h1}}{\partial net_{h1}} * \frac{\partial E_{total}}{\partial out_{h1}} = \frac{\partial E_{total}}{\partial w_1}$$

$$\downarrow$$
$$\frac{\partial E_{total}}{\partial out_{h1}} = \frac{\partial E_{01}}{\partial out_{h1}} + \frac{\partial E_{02}}{\partial out_{h1}}$$

Update w_1, w_2, w_3, w_4

Date:

dengan rumus update bobot sebelumnya

Mohon maaf Bu, perhitungannya belum selesai ...

Mohon maaf Bu karena belum lengkap dan berupa foto catatan karena baru faham.
Semoga dapat diterima, terimakasih.