

Motor Trend Analysis

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Executive Summary

You work for Motor Trend, a magazine about the automobile industry. Looking at a data set of a collection of cars, they are interested in exploring the relationship between a set of variables and miles per gallon (MPG) (outcome). They are particularly interested in the following two questions:

- Is an automatic or manual transmission better for MPG.
- Quantify the MPG difference between automatic and manual transmissions.

Load Data

The data was extracted from the 1974 Motor Trend US magazine, and comprises fuel consumption and 10 aspects of automobile design and performance for 32 automobiles (1973–74 models). It consists of 32 observations on 11 variables.

```
library(datasets)
data(mtcars)
names(mtcars)
```

```
## [1] "mpg" "cyl" "disp" "hp" "drat" "wt" "qsec" "vs" "am" "gear"
## [11] "carb"
```

Is an automatic or manual transmission better for MPG?

For automatic:

```
summary(mtcars[mtcars$am==0,])
```

```
##      mpg      cyl      disp      hp
##  Min.   :10.40  Min.   :4.000  Min.   :120.1  Min.   : 62.0
##  1st Qu.:14.95  1st Qu.:6.000  1st Qu.:196.3  1st Qu.:116.5
##  Median :17.30  Median :8.000  Median :275.8  Median :175.0
##  Mean   :17.15  Mean   :6.947  Mean   :290.4  Mean   :160.3
##  3rd Qu.:19.20  3rd Qu.:8.000  3rd Qu.:360.0  3rd Qu.:192.5
##  Max.   :24.40  Max.   :8.000  Max.   :472.0  Max.   :245.0
##      drat      wt      qsec      vs
##  Min.   :2.760  Min.   :2.465  Min.   :15.41  Min.   :0.0000
##  1st Qu.:3.070  1st Qu.:3.438  1st Qu.:17.18  1st Qu.:0.0000
##  Median :3.150  Median :3.520  Median :17.82  Median :0.0000
##  Mean   :3.286  Mean   :3.769  Mean   :18.18  Mean   :0.3684
##  3rd Qu.:3.695  3rd Qu.:3.842  3rd Qu.:19.17  3rd Qu.:1.0000
##  Max.   :3.920  Max.   :5.424  Max.   :22.90  Max.   :1.0000
##      am      gear      carb
##  Min.    :0  Min.   :3.000  Min.   :1.000
##  1st Qu.:0  1st Qu.:3.000  1st Qu.:2.000
##  Median :0  Median :3.000  Median :3.000
##  Mean   :0  Mean   :3.211  Mean   :2.737
```

```
## 3rd Qu.:0    3rd Qu.:3.000    3rd Qu.:4.000
## Max.      :0    Max.      :4.000    Max.      :4.000
```

For manual:

```
summary(mtcars[mtcars$am==1,])
```

```
##      mpg          cyl          disp          hp
## Min.   :15.00    Min.   :4.000    Min.   : 71.1    Min.   : 52.0
## 1st Qu.:21.00    1st Qu.:4.000    1st Qu.: 79.0    1st Qu.: 66.0
## Median :22.80    Median :4.000    Median :120.3    Median :109.0
## Mean   :24.39    Mean   :5.077    Mean   :143.5    Mean   :126.8
## 3rd Qu.:30.40    3rd Qu.:6.000    3rd Qu.:160.0    3rd Qu.:113.0
## Max.   :33.90    Max.   :8.000    Max.   :351.0    Max.   :335.0
##      drat          wt          qsec          vs
## Min.   :3.54    Min.   :1.513    Min.   :14.50    Min.   :0.0000
## 1st Qu.:3.85    1st Qu.:1.935    1st Qu.:16.46    1st Qu.:0.0000
## Median :4.08    Median :2.320    Median :17.02    Median :1.0000
## Mean   :4.05    Mean   :2.411    Mean   :17.36    Mean   :0.5385
## 3rd Qu.:4.22    3rd Qu.:2.780    3rd Qu.:18.61    3rd Qu.:1.0000
## Max.   :4.93    Max.   :3.570    Max.   :19.90    Max.   :1.0000
##      am          gear          carb
## Min.   :1    Min.   :4.000    Min.   :1.000
## 1st Qu.:1    1st Qu.:4.000    1st Qu.:1.000
## Median :1    Median :4.000    Median :2.000
## Mean   :1    Mean   :4.385    Mean   :2.923
## 3rd Qu.:1    3rd Qu.:5.000    3rd Qu.:4.000
## Max.   :1    Max.   :5.000    Max.   :8.000
```

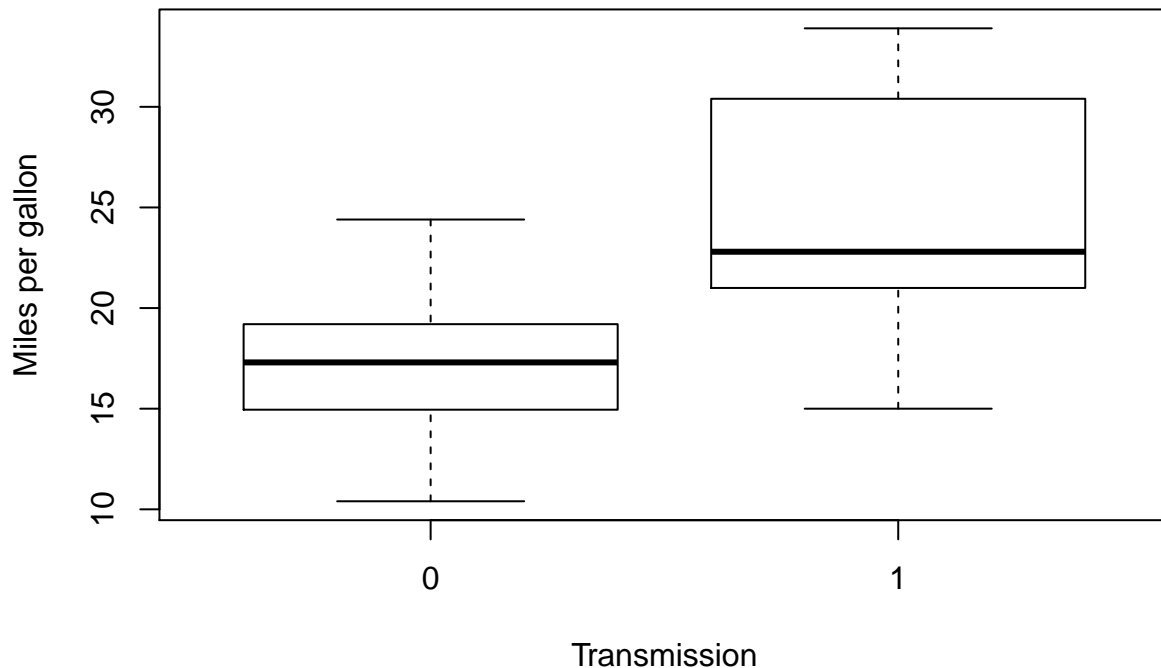
Hence, the mean of mpg is greater for manual (at 24.4) than automatic (at 17.1).

Investigating further..

Quantify the MPG difference between automatic and manual transmissions.

```
boxplot(mpg ~ am, data = mtcars, xlab = "Transmission", ylab = "Miles per gallon", main="Miles per gallon by transmission")
```

Miles per gallon by Transmission Type



Manual (represented by 1) has a higher mean for mpg than automatic (represented by 0).

Hypothesis Testing

```
aggregate(mpg~am, data = mtcars, mean)
```

```
##   am    mpg
## 1  0 17.14737
## 2  1 24.39231
```

The mean transmission for manual is 7.24mpg higher than automatic. Let $\alpha=0.5$.

```
auto <- mtcars[mtcars$am == 0,]
manual <- mtcars[mtcars$am == 1,]
t.test(auto$mpg, manual$mpg)
```

```
##
## Welch Two Sample t-test
##
## data: auto$mpg and manual$mpg
## t = -3.7671, df = 18.332, p-value = 0.001374
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -11.280194 -3.209684
## sample estimates:
## mean of x mean of y
## 17.14737 24.39231
```

Since $p\text{-value} = 0.001374$, we reject the null hypothesis. There is a major difference between mpg of manual and automatic transmissions.

```
m<-lm(mpg~am,data=mtcars)
summary(m)
```

```
##
## Call:
## lm(formula = mpg ~ am, data = mtcars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -9.3923 -3.0923 -0.2974  3.2439  9.5077
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)   17.147      1.125   15.247 1.13e-15 ***
## am              7.245      1.764    4.106 0.000285 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 4.902 on 30 degrees of freedom
## Multiple R-squared:  0.3598, Adjusted R-squared:  0.3385
## F-statistic: 16.86 on 1 and 30 DF,  p-value: 0.000285
```

From the above, we may conclude that automatic run at 17.15mpg, while manual have 7.24 more mpg.

Also, R^2 is 0.36, hence the model only accounts for 36% variance.

Performing multivariate linear regression:

```
model <- lm(mpg~am + wt + hp + cyl, data = mtcars)
anova(m,model)
```

```
## Analysis of Variance Table
##
## Model 1: mpg ~ am
## Model 2: mpg ~ am + wt + hp + cyl
##   Res.Df  RSS Df Sum of Sq    F    Pr(>F)
## 1      30 720.9
## 2      27 170.0  3      550.9 29.166 1.274e-08 ***
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

The final model is below:

```
summary(model)
```

```
##
## Call:
## lm(formula = mpg ~ am + wt + hp + cyl, data = mtcars)
##
## Residuals:
##      Min       1Q   Median       3Q      Max
## -3.4765 -1.8471 -0.5544  1.2758  5.6608
##
## Coefficients:
##              Estimate Std. Error t value Pr(>|t|)
## (Intercept)  36.14654    3.10478   11.642 4.94e-12 ***
## am            1.47805    1.44115    1.026  0.3142
```

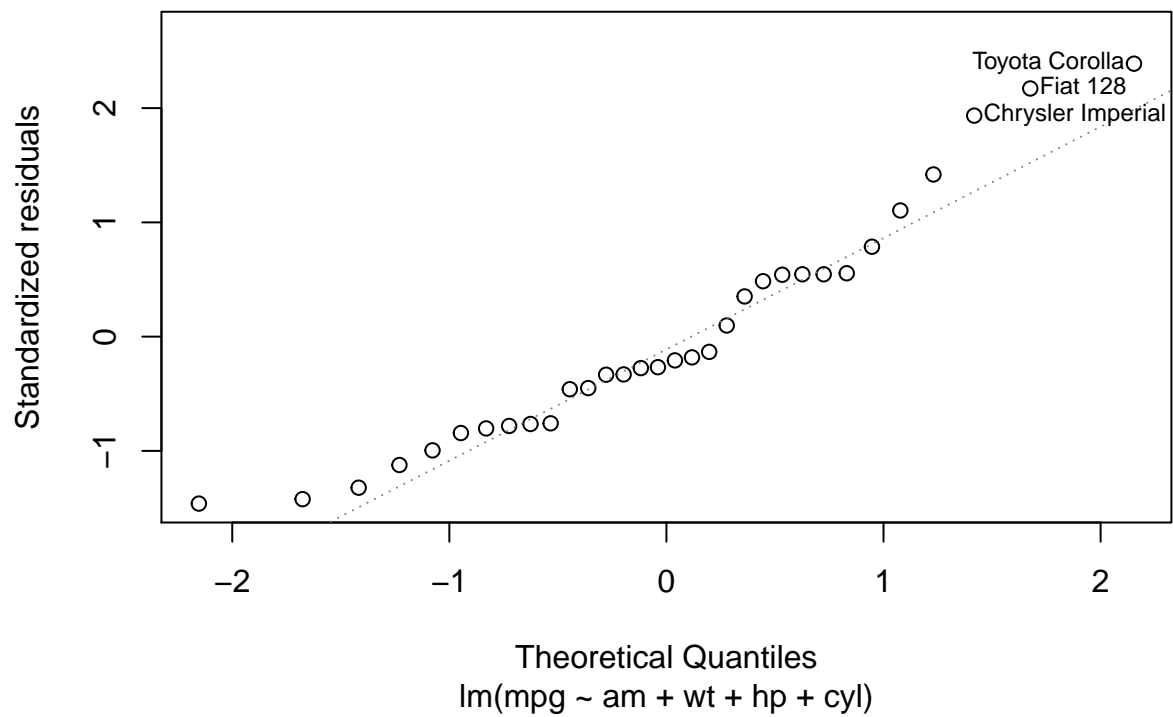
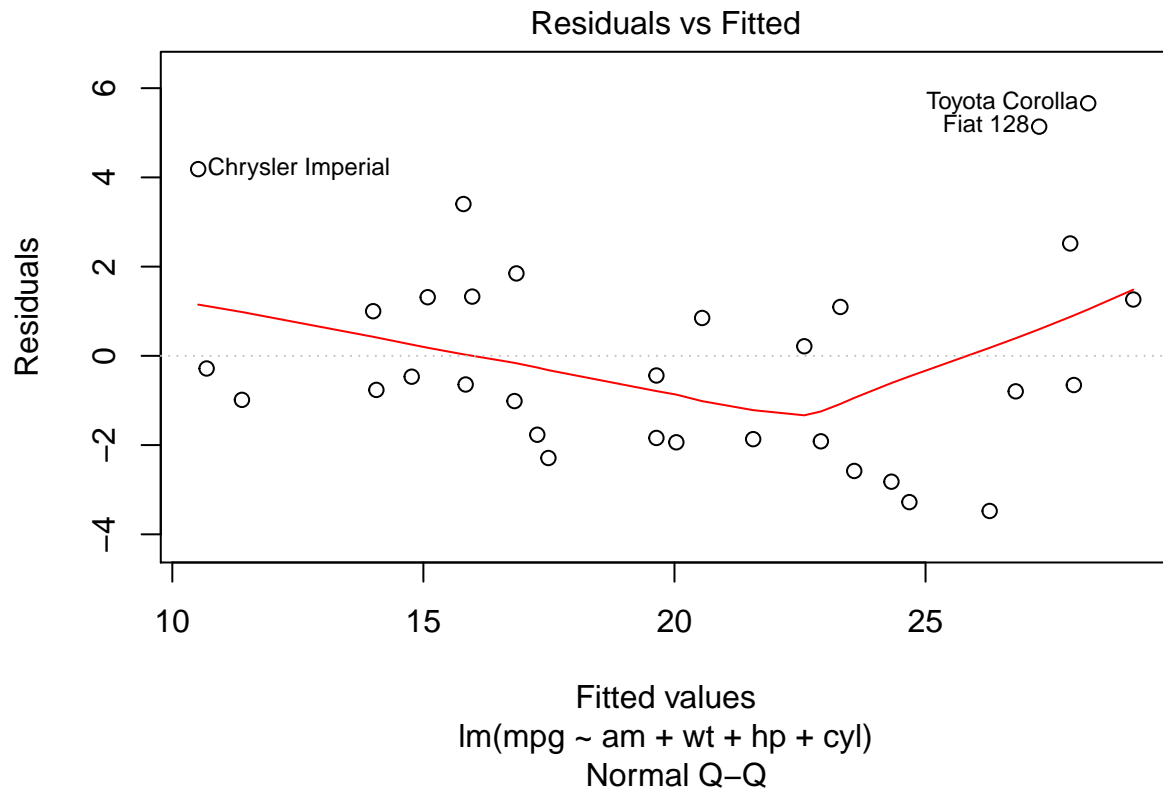
```
## wt          -2.60648    0.91984  -2.834    0.0086 **
## hp          -0.02495    0.01365  -1.828    0.0786 .
## cyl         -0.74516    0.58279  -1.279    0.2119
## ---
## Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.509 on 27 degrees of freedom
## Multiple R-squared:  0.849, Adjusted R-squared:  0.8267
## F-statistic: 37.96 on 4 and 27 DF, p-value: 1.025e-10
```

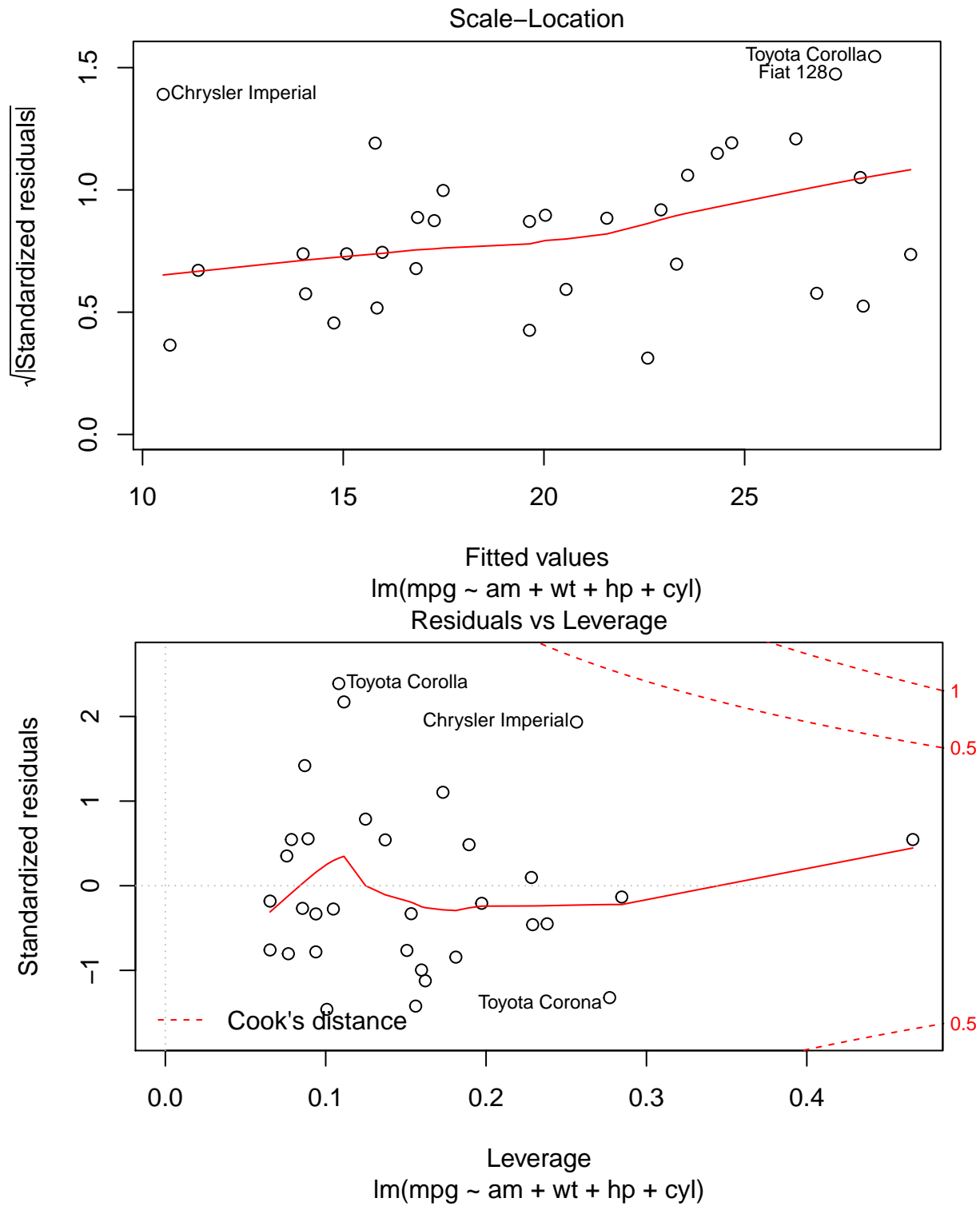
Conclusion

This model explains 84.9% of the variance. It may be concluded that on average, manual transmissions have 1.478 more mpg than automatic.

APPENDIX

```
plot(model)
```





Hence, the residuals are normally distributed, and homoskedastic.