

605.611 - Foundations of Computer Architecture

Assignment 06 - Branching and Jumps

Sabbir Ahmed

March 9, 2021

1. Translate statements 1, 2, and 5 into machine code. Assumes the program loads at 0x0040 0000.

```
1  label_1 :  
2      beq $zero , $zero , label_2  
3      j  label_3  
4      addi $t0 , $t1 , 100  
5      sub $t0 , $t1 , $t2  
6  label_2 :  
7      beq $zero , $zero , label_1  
8  label_3 :  
9      addi $t0 , $t1 , 100
```

Answer: The statements 1, 2, and 5 are

```
1  beq $zero , $zero , label_2  
2  j  label_3  
3  beq $zero , $zero , label_1
```

Putting the program with its address space:

Address	Instruction
0x0040 0000	label_1: beq \$zero, \$zero, label_2
0x0040 0004	j label_3
0x0040 0008	addi \$t0, \$t1, 100
0x0040 000C	sub \$t0, \$t1, \$t2
0x0040 0010	label_2: beq \$zero, \$zero, label_1
0x0040 0014	label_3: addi \$t0, \$t1, 100

The addresses of the labels are as follows:

Address	Instruction
0x0040 0000	label_1
0x0040 0010	label_2
0x0040 0014	label_3

Replacing addresses in absolute jumps:

Address	Instruction
0x0040 0000	beq \$zero, \$zero, label_2
0x0040 0004	j 0x0040 0014
0x0040 0010	beq \$zero, \$zero, label_1

For the relative branches, label_2 is +3 PC (0x0000 0003) from label_1 and label_1 is -5 PC (0xFFFF FFFB) from label_2. Therefore,

Address	Instruction
0x0040 0000	beq \$zero, \$zero, 0x0000 0003
0x0040 0004	j 0x0040 0014
0x0040 0010	beq \$zero, \$zero, 0xFFFF FFFB

(a) beq \$zero, \$zero, 0x0000 0003

$$\text{opcode}(\text{beq}) = 04_{16}$$

$$= 000100_2$$

$$\text{rs}(\$zero) = 00000_2$$

$$\text{rt}(\$zero) = 00000_2$$

$$\text{sign_ext_imm}(3) \Rightarrow 0003_{16}$$

$$\Rightarrow 000100\ 00000\ 00000_2 \mid 0003_{16}$$

$$\Rightarrow 0001\ 0000\ 0000\ 0000 \mid 0003_{16}$$

$$\Rightarrow 10000003_{16}$$

(b) j 0x0040 0014

$$\text{opcode}(\text{j}) = 02_{16}$$

$$= 000010_2$$

$$\text{imm}(0x0040\ 0014) \Rightarrow 0040\ 0014_{16}$$

$$\Rightarrow 000010\ 0000_2 \mid 40\ 0014_{16} \mid 00_2$$

$$\Rightarrow 000010\ 0000\ 0100\ 0000\ 0000\ 0000\ 0001\ 0100\ 00$$

$$\Rightarrow 0000\ 1000\ 0001\ 0000\ 0000\ 0000\ 0000\ 0101\ 0000$$

$$\Rightarrow 08100005_{16}$$

(c) `beq $zero, $zero, 0xFFFF FFFB`

$$\begin{aligned}\text{opcode}(\text{beq}) &= 04_{16} \\ &= 000100_2 \\ \text{rs}(\$zero) &= 00000_2 \\ \text{rt}(\$zero) &= 00000_2 \\ \text{sign_ext_imm}(-5) &\Rightarrow FFFB_{16} \\ &\Rightarrow 000100\ 00000\ 00000_2 \mid FFFB_{16} \\ &\Rightarrow 0001\ 0000\ 0000\ 0000 \mid FFFB_{16} \\ &\Rightarrow 1000FFFB_{16}\end{aligned}$$

6. Explain, in your own words, how a 26 bit address in the `jmp` instruction can access any executable statement in a program. This must be your own words. Copying something from the internet does not count.

Answer: All of the instructions in a MIPS machine allocate 6 bits for their opcodes. This limits 26 bits for the address for the `jmp` instruction. However, the memory is configured in a MIPS machine such that some areas are protected and reserved from the program text, i.e. the kernel space, operating system instructions, etc. The program text is limited to `0x1000 0000`, which leaves a highest address of `0x0fff ffff`. The most significant bit of the addresses are therefore always 0 (in hexadecimal), and 4-bits are regained. The other 2 bits come for the 2 zeros on the least significant bits that account for the word alignment of the addresses.