We specify below the behavior of toAST() and compile() by using the formalization of a subset of Lua semantics, as presented (as Lua Core) in [1]. This subset depicts the notions of lexical scoping, closures and side-effects and is therefore sufficient for our purposes. We extend the Lua Core specification from [1] with a general "binary operator" expression, mimicking Lua operators supported by LuaToAST.

Lua Core syntax is presented as follows:

$$e = b | x | \text{let } x = e \text{ in } e | x := e | e(e) | \text{fun}(x) \{e\} | e \text{ op } e | \text{toAST}(e) | \text{compile}(a)$$

Lua expressions can be base values (b), variables (x), a scoped variable definition (let x = e in e, with e; e as sugar for let  $\_= e$  in e), a variable assignment (x := e), an application (e(e)), a function definition  $(\text{fun}(x)\{e\})$  or an operation on expressions (e op e), with semantics defined by a function Op). We extend this by adding operations to AST(e) and compile (a).

$$v = b \mid \langle \Gamma, x, e \rangle \mid a$$

Lua values can be base values (b), closures  $(\langle \Gamma, x, e \rangle)$  or Lua ASTs (a).

$$a = [\text{base } b] \mid [\text{closure } \langle \Gamma, x, e \rangle] \mid [\text{op } a \ a]$$

A Lua AST may contain nodes that wrap base values ([base b]), closures ([closure  $\langle \Gamma, x, e \rangle$ ]) and operations ([op a a]).

The rules for evaluating Lua expressions over an environment  $\Sigma$ , which is a tuple  $(\Gamma, S)$  containing a namespace  $\Gamma: x \to p$  and a store  $S: p \to v$  (where p are memory positions) are as follows. We use  $\to$  instead of  $\stackrel{L}{\to}$  as in [1]; where rules have the same names, they have the same semantics as those presented in that work.

$$v, \Sigma \to v, \Sigma \text{ (LVAL)}$$

$$\frac{\Sigma = (\Gamma, S)}{x, \Sigma \to S(\Gamma(x)), \Sigma} \text{ (LVAR)}$$

$$\frac{e_1, \Sigma_1 \to v_1, (\Gamma_2, S_2)}{\text{let } x = e_1 \text{ in } e_2, \Sigma_1 \to v_2, (\Gamma_3, S_3)} \text{ (LLET)}$$

$$\frac{e_1, \Sigma_1 \to \langle \Gamma_1, x, e_3 \rangle, \Sigma_2 \quad e_2, \Sigma_2 \to v_1, (\Gamma_3, S_3)}{\text{let } x = e_3, (\Gamma_1[x \leftarrow p], S_3[p \leftarrow v_1]) \to v_2, (\Gamma_4, S_4)} \text{ (LAPP)}$$

$$\frac{e_1, \Sigma_1 \to \langle \Gamma_1, x, e_3 \rangle, \Sigma_2 \quad e_2, \Sigma_2 \to v_1, (\Gamma_3, S_3)}{e_1(e_2), \Sigma_1 \to v_2, (\Gamma_3, S_4)} \text{ (LAPP)}$$

$$\frac{e_1, \Sigma_1 \to v_1, (\Gamma, S) \quad \Gamma(x) = p}{x := e, \Sigma \to v, (\Gamma, S[p \leftarrow v])} \text{ (LASN)}$$

$$\begin{split} \frac{\Sigma &= (\Gamma, S)}{\text{fun}(x)\{e\}, \Sigma \to \langle \Gamma, x, e \rangle, \Sigma} \text{ (LFun)} \\ \frac{e_1, \Sigma_1 \to v_1, \Sigma_2}{e_1 + e_2, \Sigma_1 \to v_3, \Sigma_3} & v_3 &= Op(v_1, v_2) \\ \hline \frac{e_1, \Sigma \to \langle \Gamma, x, e_2 \rangle, \Sigma}{e_1 + e_2, \Sigma_1 \to v_3, \Sigma_3} & \text{(LOP)} \\ \\ \frac{e_1, \Sigma \to \langle \Gamma, x, e_2 \rangle, \Sigma}{\text{toAST}(e_1), \Sigma \to a_1, \Sigma} & \text{(LAST)} \\ \hline \frac{\Sigma &= (\Gamma, S)}{\text{compile}(a_1), \Sigma \to \langle \Gamma, \_, e_1 \rangle, \Sigma} & \text{(LCOMP)} \end{split}$$

The rules for decompiling Lua expressions  $(\stackrel{D}{\rightarrow})$  over an environment  $\Sigma$  are the following:

$$b, \Sigma \xrightarrow{D} [\text{base } b] \text{ (DBASE)}$$

$$\frac{\Sigma = (\Gamma, S, F)}{x, \Sigma \xrightarrow{D} [\text{closure } \langle \Gamma, \_, x \rangle]} \text{ (DVAR)}$$

$$\frac{e_1, \Sigma \xrightarrow{D} a_1 \quad e_2, \Sigma \xrightarrow{D} a_2}{e_1 \text{ op } e_2, \Sigma \xrightarrow{D} [\text{op } a_1 a_2]} \text{ (DOP)}$$

Note that  $\stackrel{D}{\to}$  is defined only for variables, base values and the operator, mirroring the implementation of LuaToAST.

Finally, the rules for compiling Lua ASTs  $\stackrel{C}{\rightarrow}$  over an environment  $\Sigma$  are:

$$[\text{base }b], \Sigma \xrightarrow{C} b, \Sigma \text{ (CBASE)}$$
 
$$\frac{\Sigma = (\Gamma, S) \quad e_1, (\Gamma_1, S) \to v_1, \Sigma_2}{[\text{closure } \langle \Gamma_1, \_, e_1 \rangle], \Sigma \xrightarrow{C} v_1} \text{ (CVAR)}$$
 
$$\frac{a_1, \Sigma \xrightarrow{C} e_1 \quad a_2, \Sigma \xrightarrow{C} e_2}{[\text{op } a_1 \ a_2], \Sigma \xrightarrow{C} e_1 \text{ op } e_2} \text{ (COP)}$$

The evaluation of variables x happens only at compilation time, as evidenced by the evaluation of  $e_1$  using  $\rightarrow$  in rule CVAR.

## References

[1] DeVito et al. "Terra: a multi-stage language for high-performance computing" PLDI'13.