1 01-01 TESTS Biharmonic Tests

## 1 01-01 tests

**Example 1.1.** In this tests we consider:

- $\psi(x) = \exp(x)$
- $\psi_l = 1$
- $\psi_{\rm r} = e$
- $\psi_{ll} = 1$
- $\psi_{\rm rr} = e$
- $g(x) = -\exp(x)$
- in  $\widehat{\psi}_1$  and  $\widehat{\psi}_I$  we reconstruct a polynomial of degree d+1

Table 1: Numerical results of PRO1 scheme to the example 1.1.

|                   |     |                  |                |                  |                |                                    | 1              |                    |                |  |
|-------------------|-----|------------------|----------------|------------------|----------------|------------------------------------|----------------|--------------------|----------------|--|
|                   |     | $\omega = 1 1,1$ |                | $\omega = 1 3,1$ |                | $\omega = 1 3,3$                   |                | $\omega = 1 3, 10$ |                |  |
|                   | I   | $E_{\infty,0}$   | $O_{\infty,0}$ | $E_{\infty,0}$   | $O_{\infty,0}$ | $\overline{\mathrm{E}_{\infty,0}}$ | $O_{\infty,0}$ | $E_{\infty,0}$     | $O_{\infty,0}$ |  |
| $\mathbb{P}_3(4)$ | 20  | 6.89E - 05       | _              | 4.01E - 05       | _              | 4.01E - 05                         | _              | 4.01E - 05         |                |  |
|                   | 40  | 8.09E - 06       | 3.09           | 4.87E - 06       | 3.04           | 4.87E - 06                         | 3.04           | 4.87E - 06         | 3.04           |  |
|                   | 80  | 8.53E - 07       | 3.25           | 4.91E - 07       | 3.31           | 4.91E - 07                         | 3.31           | 4.91E - 07         | 3.31           |  |
|                   | 160 | 7.67E - 08       | 3.48           | 3.66E - 08       | 3.74           | 3.66E - 08                         | 3.74           | 3.66E - 08         | 3.74           |  |
|                   | 200 | 3.38E - 08       | 3.67           | 1.53E - 08       | 3.93           | 1.53E - 08                         | 3.92           | 1.53E - 08         | 3.92           |  |
|                   | 240 | 1.71E - 08       | 3.74           | 7.44E - 09       | 3.94           | 7.44E - 09                         | 3.95           | 7.46E - 09         | 3.94           |  |