



Instruction Selection

Compilers course

Masters in Informatics and Computing Engineering (MIEIC), 3rd Year



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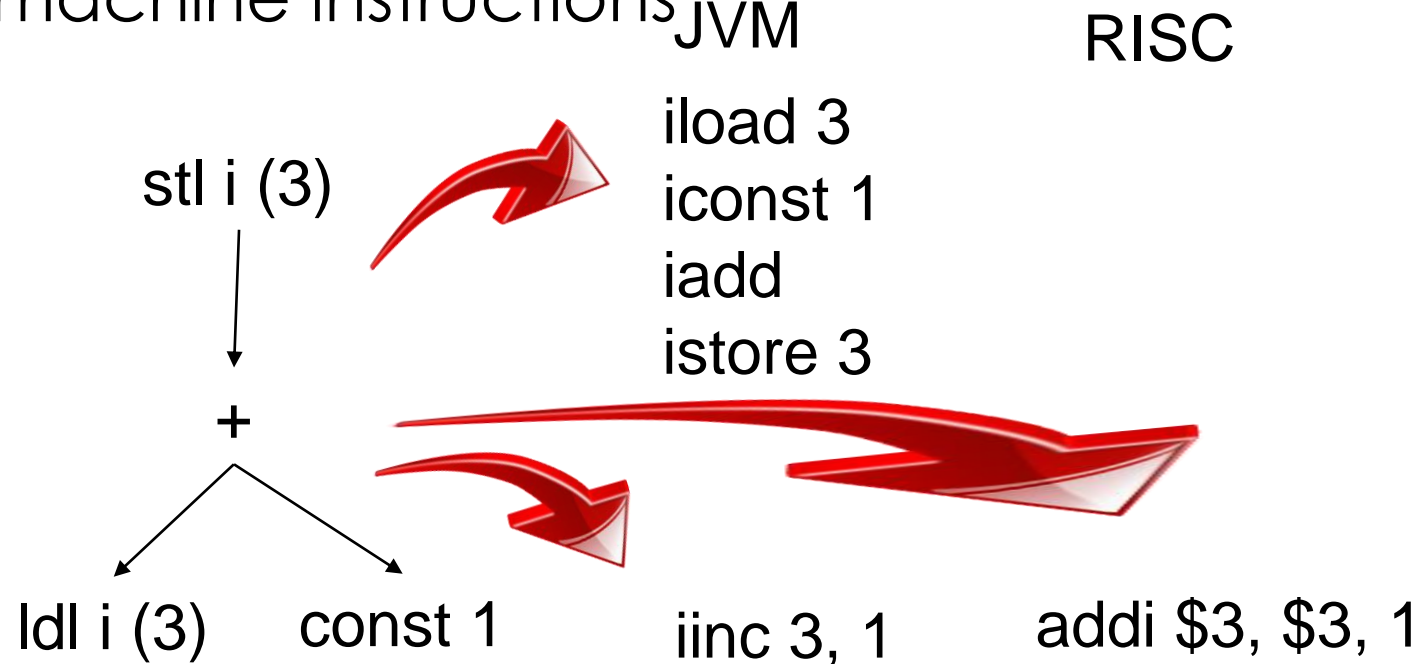
Outline

- Instruction Selection Overview
- Maximal Munch
 - Example
- Dynamic Programming
 - Example
- Other Approaches

Instruction Selection Overview

Problem:

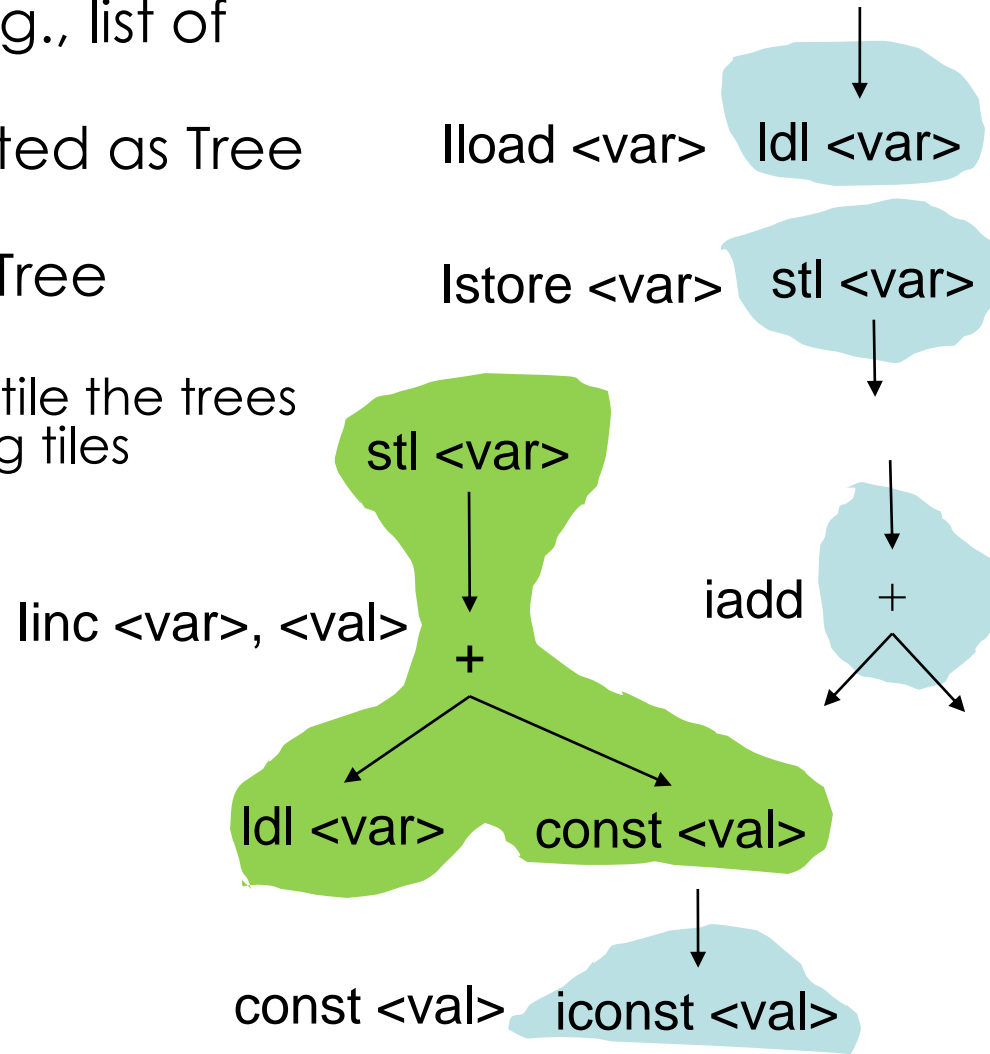
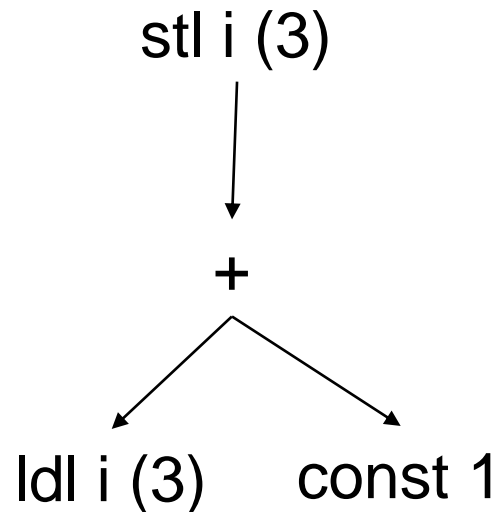
- Find for the operations in the given intermediate representation the appropriate machine instructions



Instruction Selection Overview

From Tree-based IRs (e.g., list of trees):

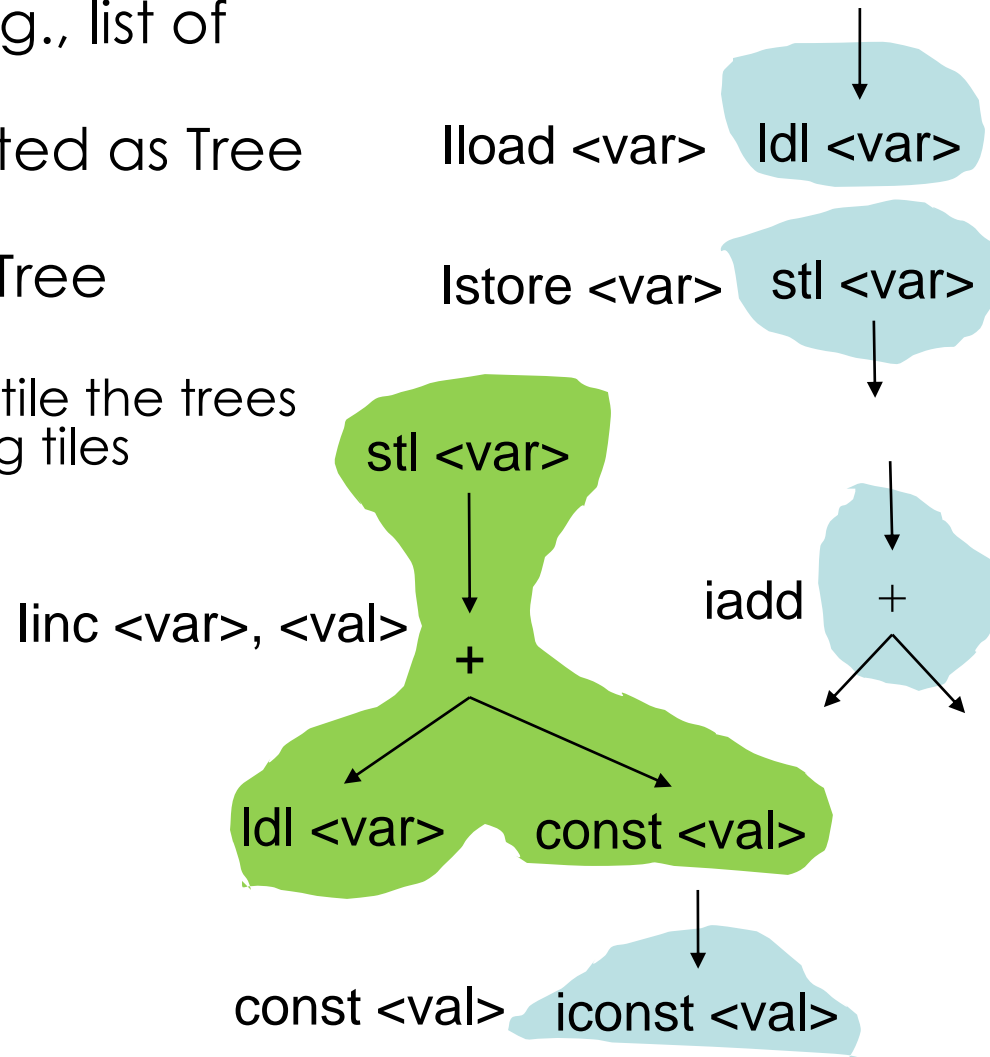
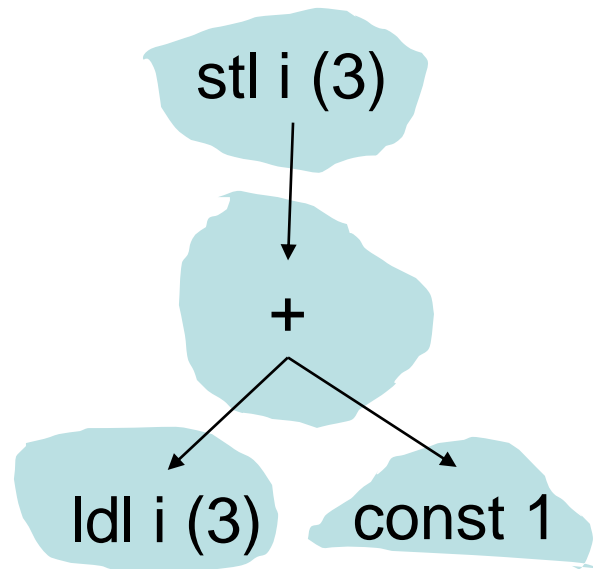
- Instructions represented as Tree Patterns
- Problem resumes to Tree covering/tiling
 - Completely Cover /tile the trees with non-overlapping tiles



Instruction Selection Overview

From Tree-based IRs (e.g., list of trees):

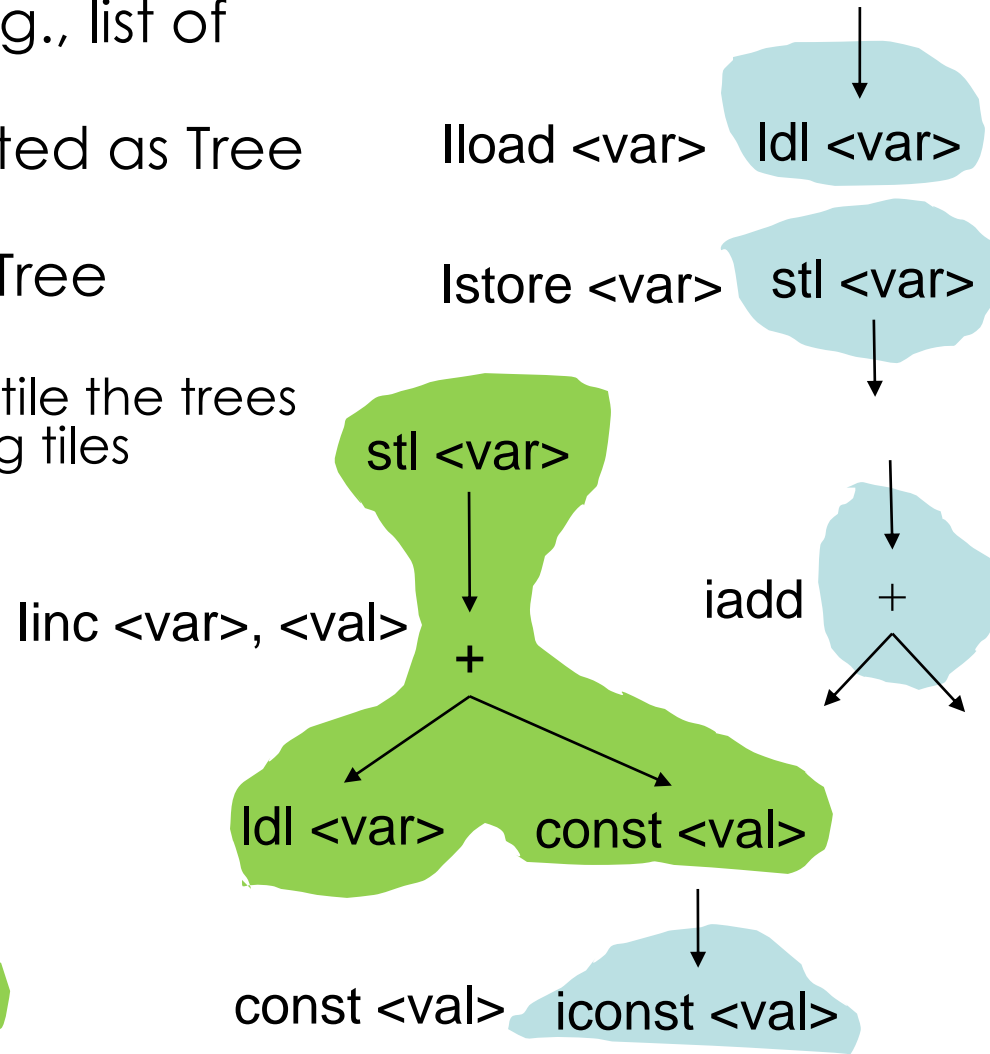
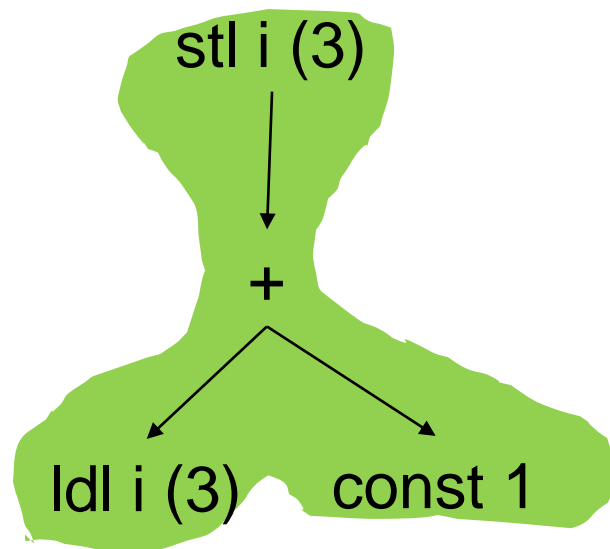
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Instruction Selection Overview

From Tree-based IRs (e.g., list of trees):

- Instructions represented as Tree Patterns
- Problem resumes to Tree covering/tiling
 - Completely Cover /tile the trees with non-overlapping tiles

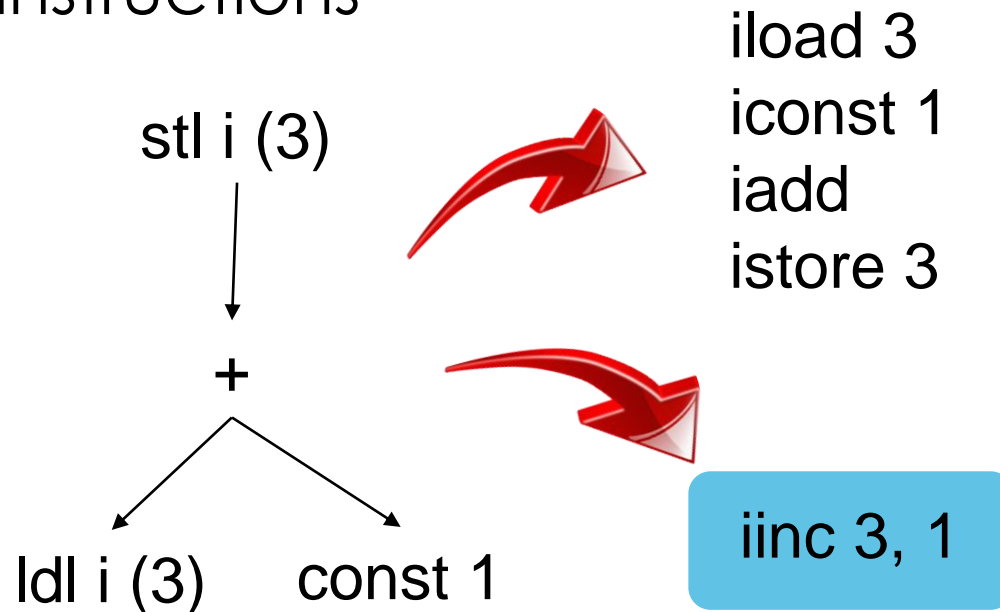


Instruction Selection Overview

Find the best cover/tile

- The one that gives the instruction sequence of least cost
- Least cost == the shortest sequence of instructions

Not always!



Instruction Selection Overview

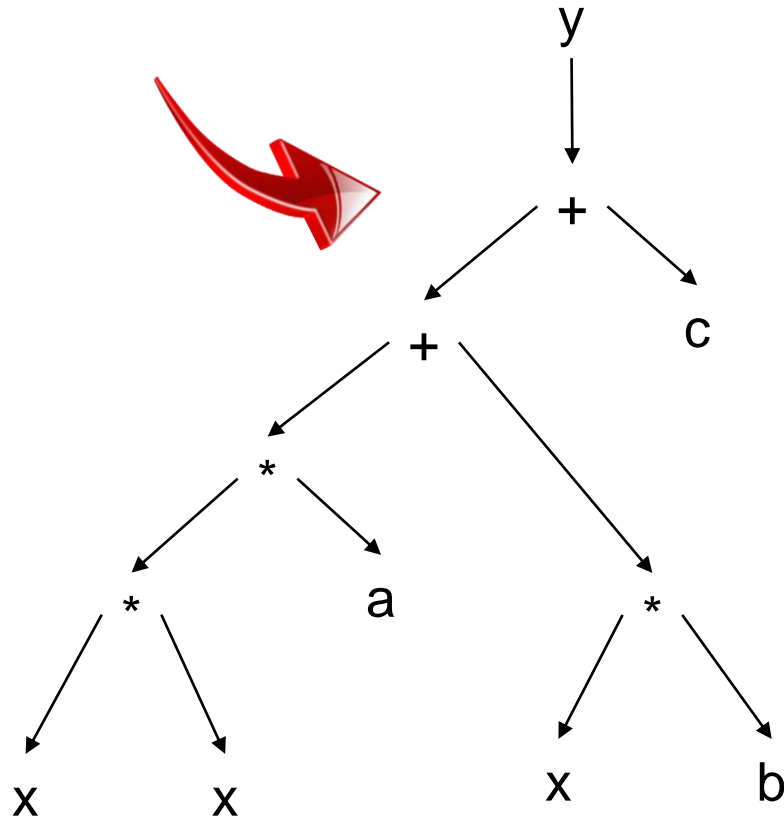
- Each tree pattern can be assigned with a cost
 - Problem is to cover/tile the trees of the program achieving the minimum cost
- However, this simple cost model does not take into account the possible interactions between instructions
- Target machines with reduced instruction set (RISC) have simple tree patterns
 - simple instruction selection algorithms are sufficient

Instruction Selection: Maximal Munch

- A simple algorithm that finds an optimal tiling: Maximal Munch (greedy, top-down pattern match)
 - Starting at the root of the tree
 - Find the largest tile that fits (the tile with most nodes)
 - Cover the root node and the possible nodes with this tile
 - Repeat the algorithm for each subtree of the tile until all the tree is tiled
 - For each tile generates the instructions of that tile
 - code generation is performed in reverse order, least instruction firsts

Instruction Selection: Maximal Munch

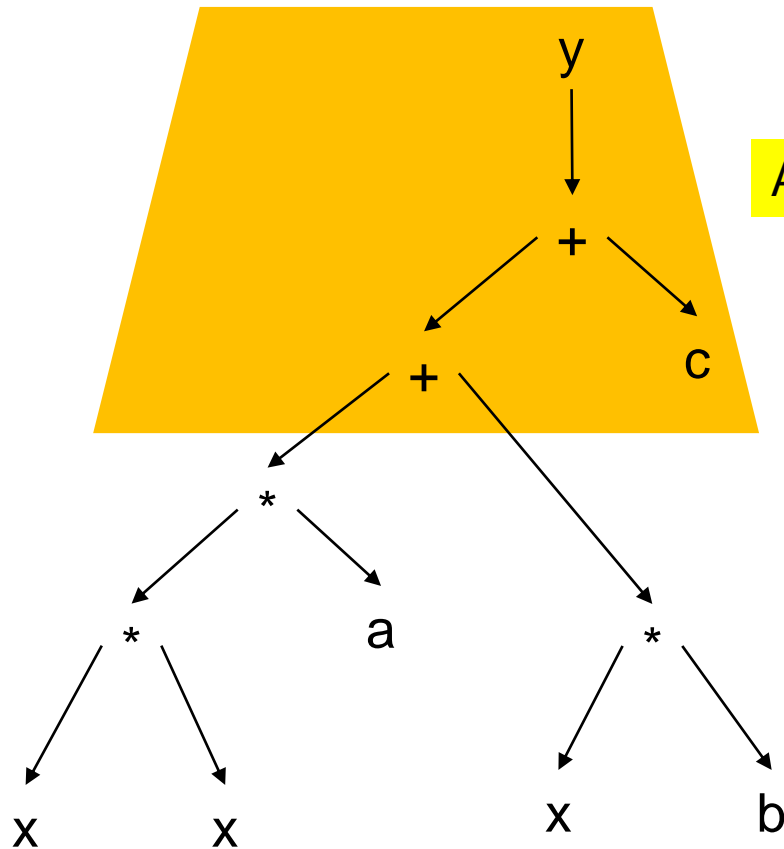
Example: $y = a * x * x + b * x + c$;



Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
ADD3 (A3)	$a \leftarrow b + c + d$	2
MUL2 (M2)	$a \leftarrow b * c$	4
MUL3 (M3)	$a \leftarrow b * c * d$	7
MADD (MA)	$a \leftarrow b * c + d$	4

Instruction Selection: Maximal Munch

➤ $y = a * x * x + b * x + c;$

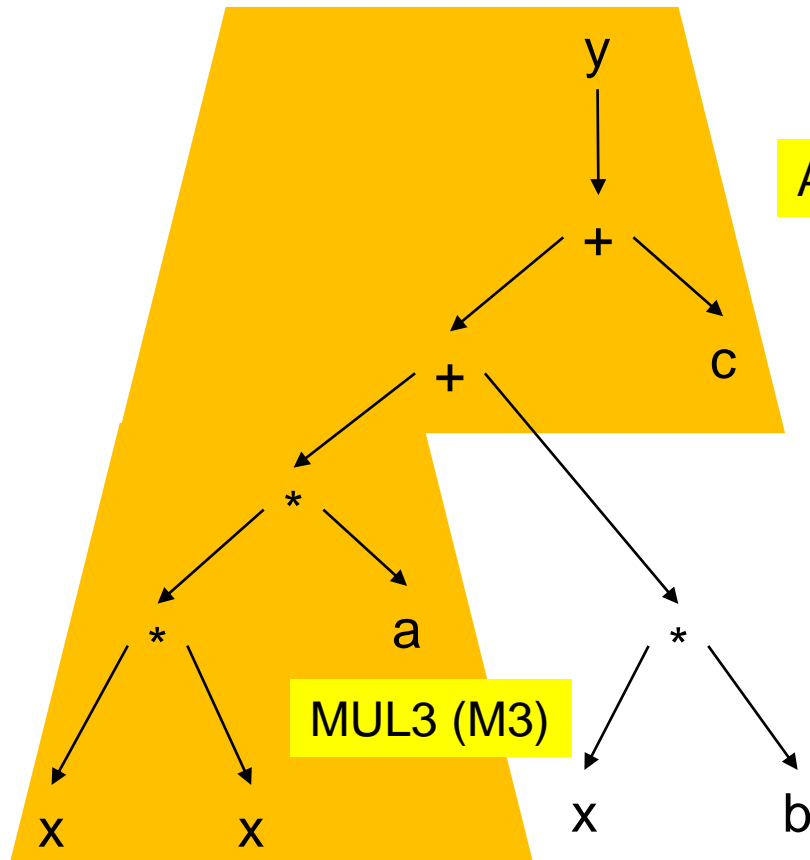


ADD3 (A3)

Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
ADD3 (A3)	$a \leftarrow b + c + d$	2
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Instruction Selection: Maximal Munch

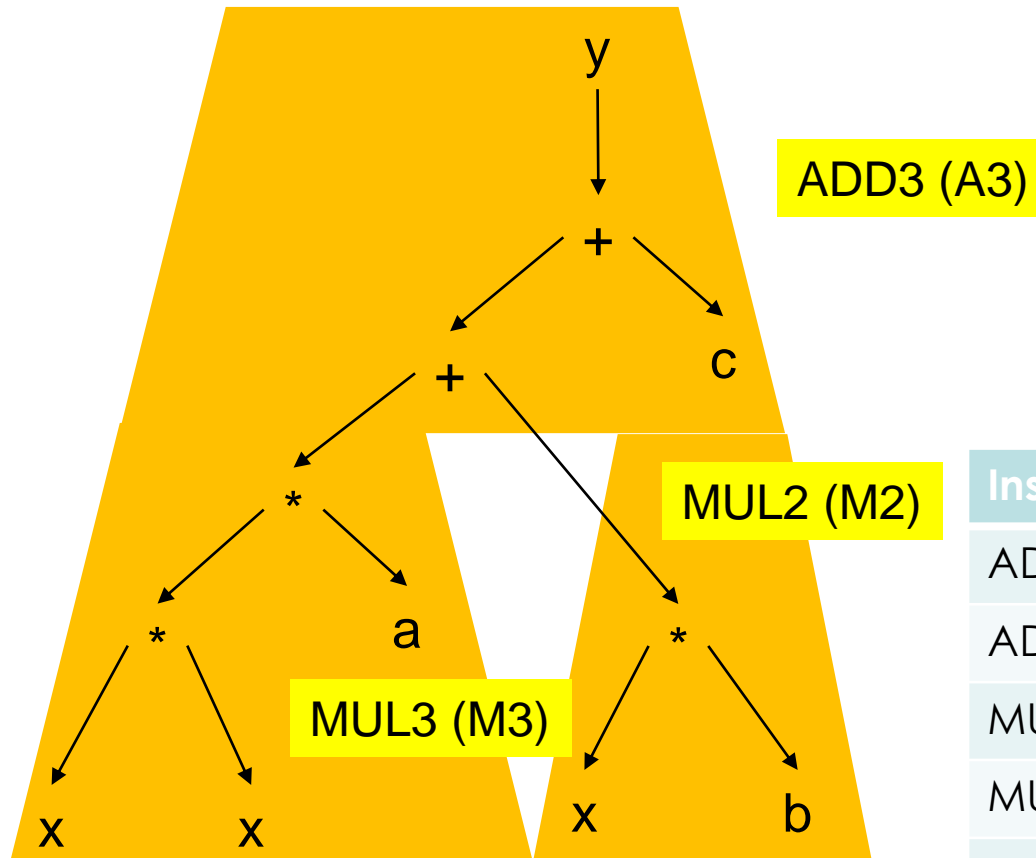
➤ $y = a * x * x + b * x + c;$



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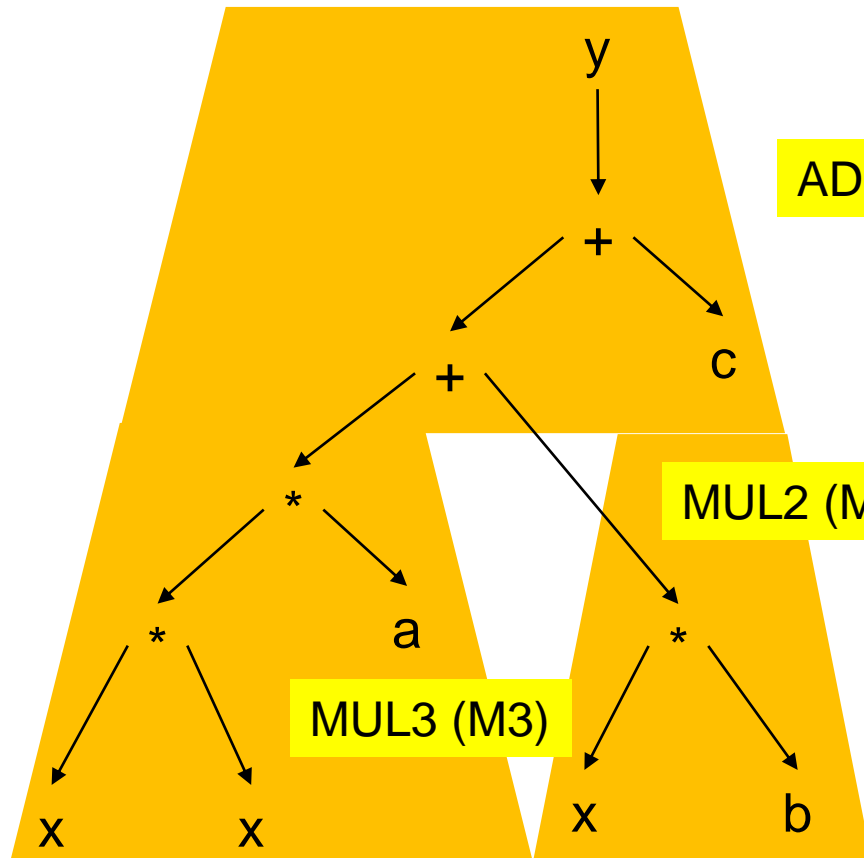
➤ $y = a * x * x + b * x + c;$



Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
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Instruction Selection: Maximal Munch

➤ $y = a * x * x + b * x + c;$



ADD3 (A3)

MUL2 (M2)

MUL3 (M3)

ADD3 (A3)

Cost = 4+7+2
= 13

MUL2 (M2)

MUL3 (M3)

Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
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Instruction Selection: Maximal Munch

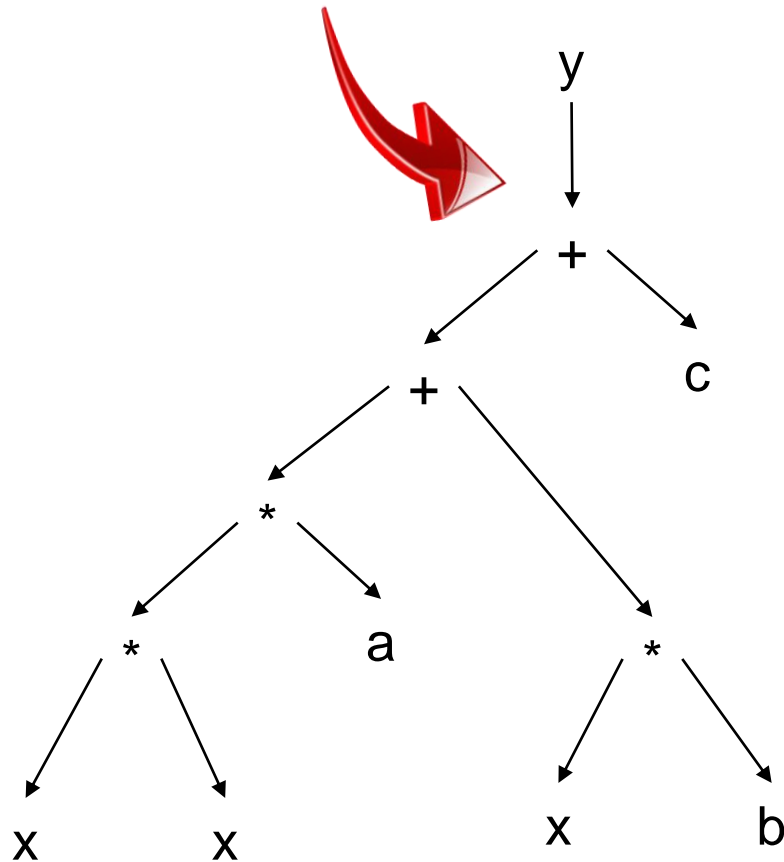
- Maximal Munch does not give the tiling with the minimum cost:
 - It decides locally about the largest pattern to fit, this might prevent the tiling of large patterns in the subtrees
- Gives optimal tiling, i.e., no adjacent tiles can form a tile with lower cost
- One possible solution to achieve minimum cost (i.e., tiling with minimum global cost)
 - Dynamic Programming

Instruction Selection: Dynamic Programming

- Bottom Up Exhaustive Cataloging of Optimum Solutions
- Optimum Solution of Node Based on Optimum Solution of Subnodes
- Delivers the Global Optimum
- Very Efficient
 - Used in, e.g., Twig, and BURG

Dynamic Programming Example

➤ $y = a * x * x + b * x + c;$

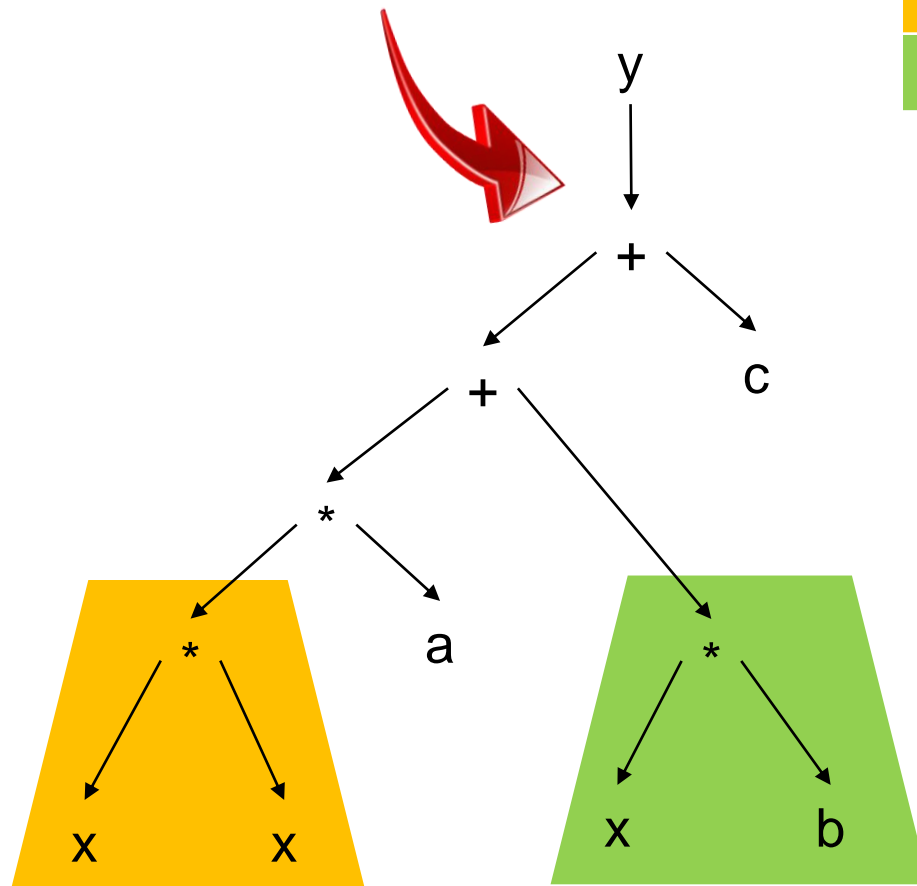


Start at the bottom and tile the first nodes
Select the tiles with minimum costs

Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
ADD3 (A3)	$a \leftarrow b + c + d$	2
MUL2 (M2)	$a \leftarrow b * c$	4
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Dynamic Programming Example

➤ $y = a * x * x + b * x + c;$



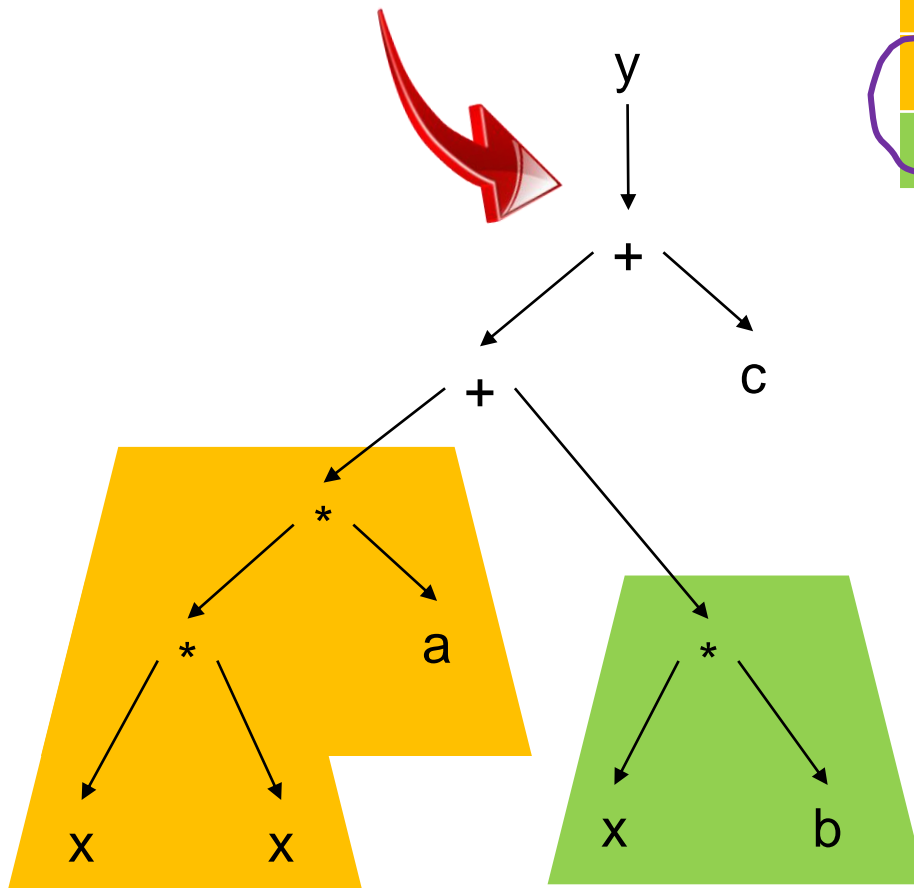
Instructions	Instruction	cost	Leaves cost	total
M2	M2	4	0	4
M2	M2	4	0	4

Go to the next node and tile the subtree with that node as the root

Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
ADD3 (A3)	$a \leftarrow b + c + d$	2
MUL2 (M2)	$a \leftarrow b * c$	4
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Dynamic Programming Example

➤ $y = a * x * x + b * x + c;$



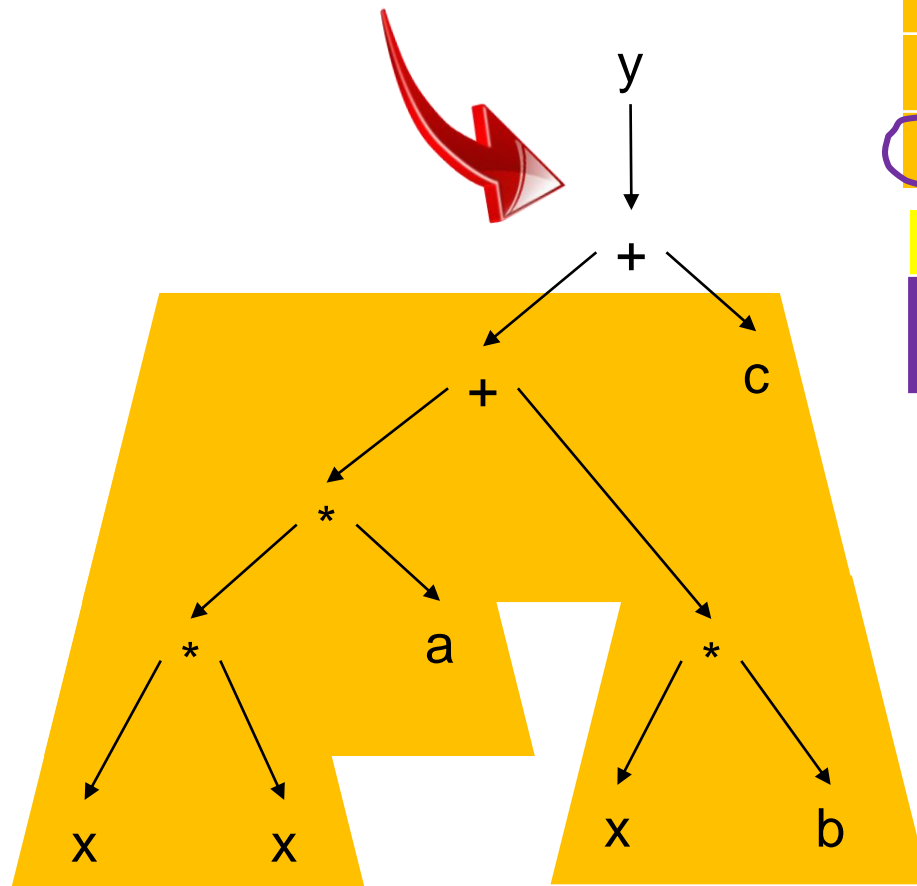
Instructions	Instruction	cost	Leaves cost	total
M2-M2	M2	4	4	8
M3	M3	7	0	7
M2	M2	4	0	4

minimum costs for the subtrees represented as orange and green regions

Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
ADD3 (A3)	$a \leftarrow b + c + d$	2
MUL2 (M2)	$a \leftarrow b * c$	4
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Dynamic Programming Example

➤ $y = a * x * x + b * x + c;$



Instructions	Instruction	cost	Leaves cost	total
M3-A2, M2	A2	1	11	12
M2-MA, M2	MA	4	8	12
M3-MA	MA	4	7	11

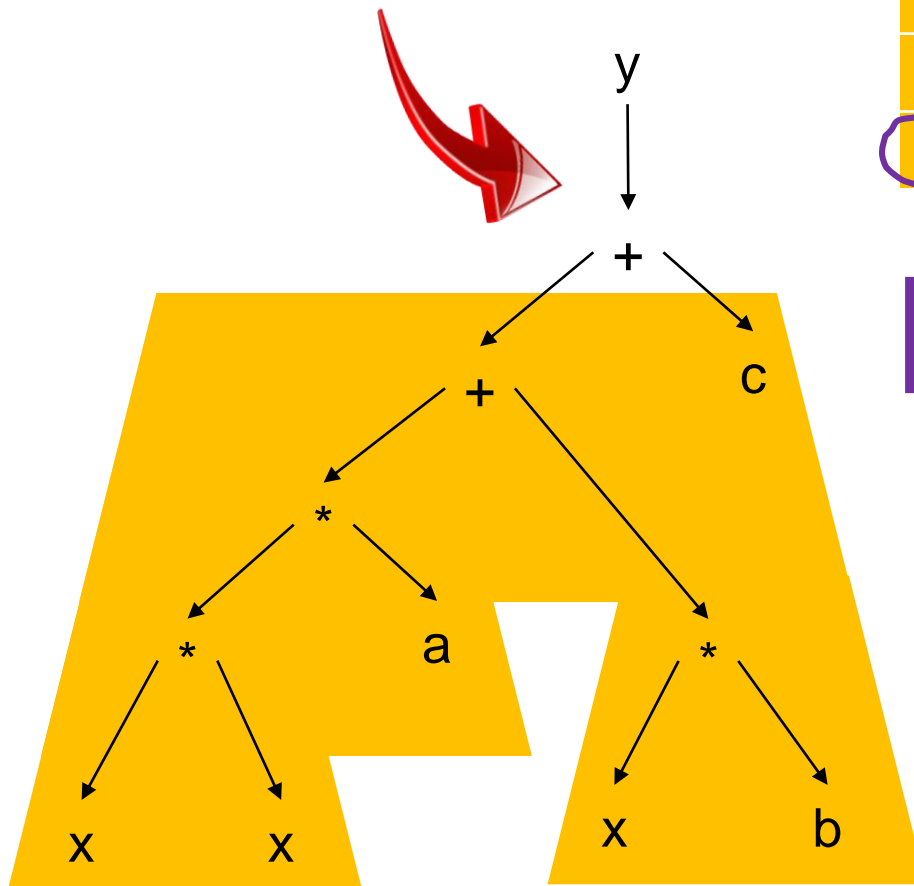
Tile not considered as it uses non-optimal subtree tiles:

M2-M2-A2, M2	A2	1	12	13
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Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
ADD3 (A3)	$a \leftarrow b + c + d$	2
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Dynamic Programming Example

➤ $y = a * x * x + b * x + c;$



Instructions	Instruction	cost	Leaves cost	total
M3-A2, M2	A2	1	11	12
M2-MA, M2	MA	4	8	12
M3-MA	MA	4	7	11

M2-M2-A2,
M2

A2

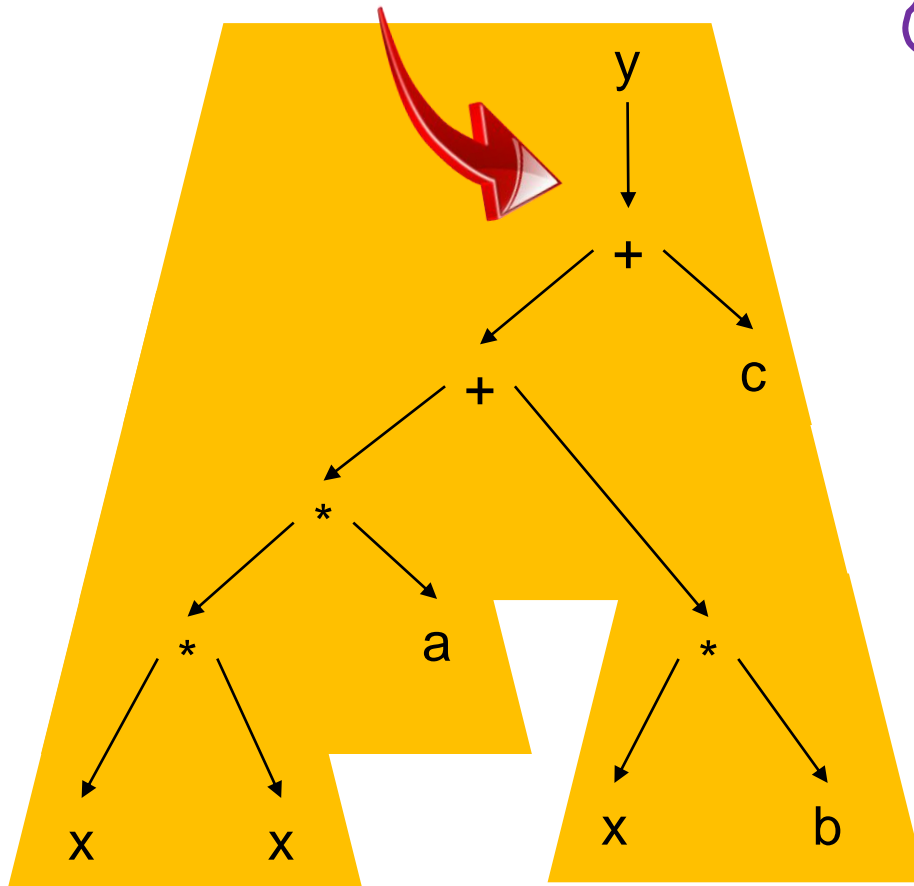
considering the
commutativity of the
addition in MA

13

Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
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Dynamic Programming Example

➤ $y = a * x * x + b * x + c;$

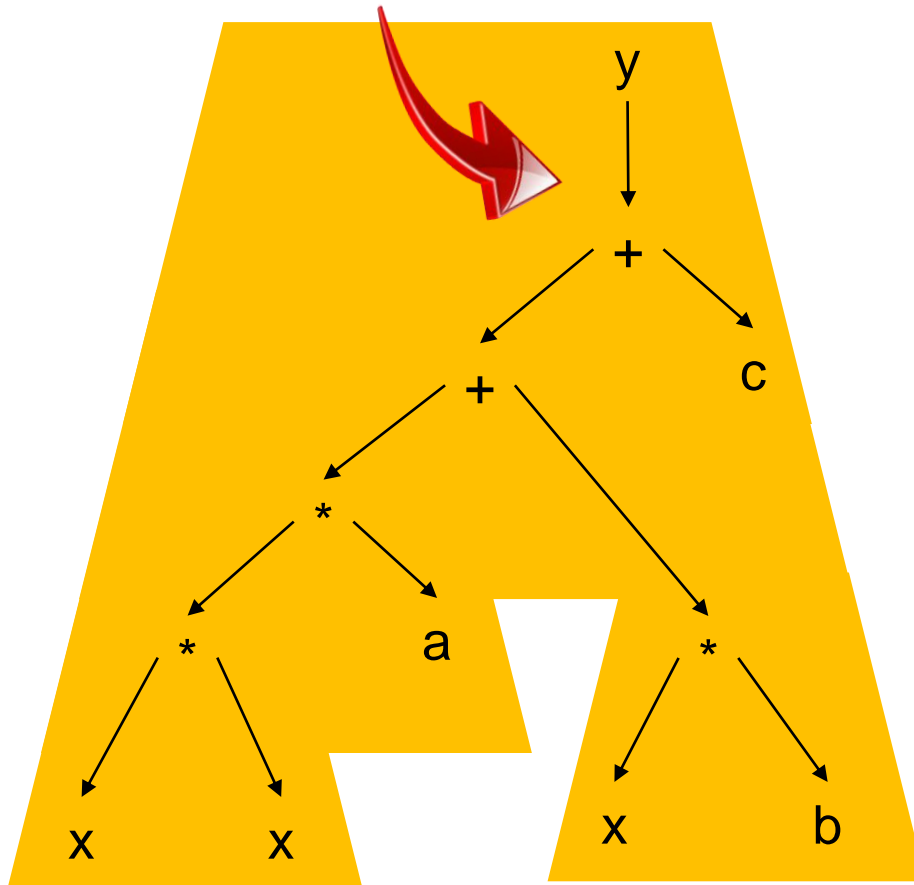


Instructions	Instruction	cost	Leaves cost	total
M3-A3, M2	A3	2	11	13
M3-MA-A2	A2	1	11	12

Instruction	function	cost
ADD2 (A2)	$a \leftarrow b + c$	1
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Dynamic Programming Example

➤ $y = a * x * x + b * x + c;$



Tiles not considered as they use non-optimal subtree tiles:

M2-M2-A2-A2, M2	A2	1	13	14
M2-M2-A3, M2	A3	2	12	14
M3-A2-A2, M2	A2	1	12	13
M2-MA-A2, M2	A2	1	12	13
M2-M2-A2-A2, M2	A2	1	13	14

Instruction	function	cost
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Other Approaches

- Graham-Glanville Parser-Based Approach
- Naive/Canonical Generation
 - Transform each node in the equivalent sequence of machine instructions
 - Can be followed by Peephole optimization

EXERCISE

Exercise

- Consider a microprocessor with the following instructions:
 - $\text{ADD } rd = rs1 + rs2$
 - $\text{ADDI } rd = rs + c$
 - $\text{SUB } rd = rs1 - rs2$
 - $\text{SUBI } rd = rs - c$
 - $\text{MUL } rd = rs1 * rs2$
 - $\text{DIV } rd = rs1 / rs2$
 - $\text{LOAD } rd = M[rs + c]$
 - $\text{STORE } M[rs1 + c] = rs2$
 - $\text{MOVEM } M[rs1] = M[rs2]$
- Where rd, rs identify registers of the architecture (from $r0$ to $r31$ and $r0$ stores the non-modified value 0) and c identifies literals

Exercise

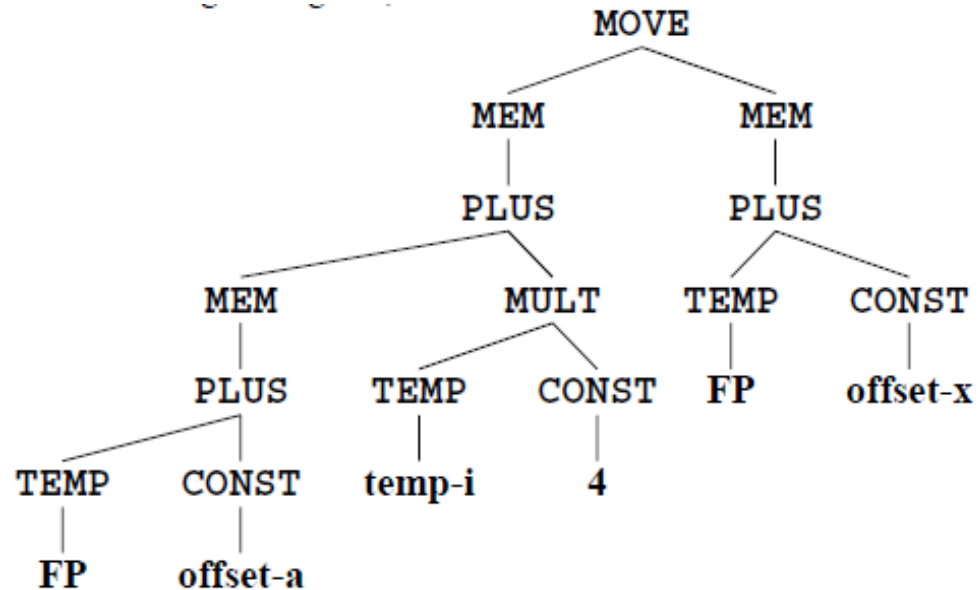
➤ The corresponding Instruction Tree Patterns are the following:

Instruction	Effect	IR Tree Pattern
—	r_i	TEMP r_i
add	$r_i \leftarrow r_j + r_k$	+ / \
mul	$r_i \leftarrow r_j * r_k$	*
sub	$r_i \leftarrow r_j - r_k$	- / \
div	$r_i \leftarrow r_j / r_k$	/ / \
addi	$r_i \leftarrow r_j + c$	+ / \ + CONST CONST CONST c c c
subi	$r_i \leftarrow r_j - c$	- / \ CONST c

Instruction	Effect	IR Tree Pattern
load	$r_i \leftarrow M[r_j + c]$	MEM MEM MEM MEM + + CONST / \ / \ CONST CONST c c c c
store	$M[r_j + c] \leftarrow r_i$	MOVE MOVE MOVE MOVE MEM MEM MEM MEM + + CONST / \ / \ CONST CONST c c c c
movem	$M[r_j] \leftarrow M[r_i]$	MOVE MEM MEM

Exercise

- Consider the input intermediate representation illustrated below for the statement: $a[i] = x$; (assuming i stored in a register identified by r_i , and a and x are frame residents), where FP represents the register with the frame pointer, $offset-a$ and $offset-x$ represent two constants, and $temp-i$ identifies the variable i .



Exercise

- a) Use individual node selection to generate the assembly instructions.
- b) Use the Maximal-Munch algorithm for instruction selection and write the instructions generated.
- c) Use dynamic programming to obtain an optimum solution for instruction selection (considering as goal the minimum number of instructions) and write the instructions generated.