National University of Singapore School of Computing CS1010X: Programming Methodology Semester II, 2022/2023

Recitation 3 Higher Order Functions

Python

1. *lambda* - lambda *params*: expression Creates an anonymous function equivalent to:

```
def function(params):
    return expression
```

Definitions

The following are two higher-order functions discussed in lecture:

```
def sum(term, a, next, b):
    if a > b:
        return 0
    else:
        return term(a) + sum(term, next(a), next, b)

def fold(op, f, n):
    if n == 0:
        return f(0)
    else:
        return op(f(n), fold(op, f, n-1))
```

Note: it is <u>not</u> necessary to memorize these defintions, or even the names of these functions. Definitions of such functions (if they are used) will be given in an Appendix for examinations. What you need to be able to do is to read the definition for such functions and understand what they do and be able to use them.

Problems

1. Evaluate the return values of the following expressions:

```
(a) x = 2
  def f():
    x = 5
    y = x + 5
    return x + y
  f() + x
```

```
(b) x = 2
    y = 3
    def g(x):
        y = x + 5
        x = 7
        return x + y
    g(y)+y

(c) x = 4
    def foo(x):
        return x(3)
    foo(lambda x: x+1)

(d) x = 5
    def bar(x, y):
        return y(x)
    bar(4, lambda x: x**2)
```

2. Write a function my_sum that computes the following sum, for $n \ge 1$:

$$1 \times 2 + 2 \times 3 + \dots + n \times (n+1)$$

- 3. Is the function my_sum as defined above a recursive process or an iterative process? What is the order of growth in time and in space?
- 4. If your answer in Question 2 is a recursive process, re-write my_sum as an iterative process. If your answer in Question 2 is an iterative process, re-write my_sum as a recursive process. What is the new order of growth in time and space?

5. We can also define my_sum in terms of the higher-order function sum. Complete the definition of my_sum below. You cannot change the definition of sum; you may only call it with appropriate arguments.

```
def my_sum(n):
    return sum(<T1>, <T2>, <T3>, <T4>)

T1:

T2:

T4:
```

6. Suppose instead we define my_sum in terms of the higher-order function fold. Complete the definition of my_sum below.

```
def my_sum(n):
    return fold(<T1>, <T2>, <T3>)
T1:
```

T3:

7. Write an iterative version of sum.

8. **Homework:** Write an iterative version of fold.