11

12

13

14

15

16

17

18

19

20

21

22

23

25

26

27

28

29

30

31

32

33

34

35

36

37

38

39

40

41

42

43

44

45

46

47

48

50

51

"HOT" NON-FLARING PLASMA IN ACTIVE REGIONS II. IMPACTS OF TWO-FLUID EFFECTS ON EMISSION FROM IMPULSIVELY HEATED LOOPS

W. T. Barnes and S. J. Bradshaw Department of Physics & Astronomy, Rice University, Houston, TX 77251-1892

P. J. CARGILL

Space and Atmospheric Physics, The Blackett Laboratory, Imperial College, London SW7 2BW and School of Mathematics and Statistics, University of St. Andrews, St. Andrews, Scotland KY16 9SS

*Draft version November 2, 2015**

ABSTRACT

Faint, high-temperature emission in active region cores has long been predicted as a signature of nanoflare heating. However, the detection of such emission has proved difficult due to a combination of the efficiency of thermal conduction, non-equilibrium ionization, and inadequate instrument sensitivity. This second paper in our series on hot non-flaring plasma in active regions aims to show how the assumption of electron-ion equilibrium leads to misleading conclusions regarding the hot emission. We have used an efficient two-fluid hydrodynamic model to carry out a parameter exploration in preferentially heated species, heating event frequency, and the power-law index determining the distribution of event energies. By computing the emission measure distributions and calculating their "hotward" slopes, we have concluded that the assumption of electron-ion equilibrium leads to an understimate of the amount of hot plasma at intermediate and high heating frequencies. Additionally, we find that, while emission due to separate electron and ion heating differs greatly hotward of the peak, the respective coolward emission measure slopes are similar such that a distinction between the heating of one species over another based on this criteria alone is not possible.

1. INTRODUCTION

The nanoflare heating model, first proposed by Parker (1988), has become one of the most favored and contentious coronal heating models (Cargill 1994; Cargill & Klimchuk 2004; Klimchuk 2006). While many theoretical efforts (e.g. Bradshaw et al. 2012; Reep et al. 2013; Cargill 2014) have shown the feasability of nanoflares, the idea has long suffered from a lack observational evidence. The term *nanoflare* has now become synonomous with impulsive heating in the energy range $10^{24}-10^{27}$ erg, with no specific assumption as to what underlying physical mechanism is responsible. However, while we ascribe no particular source (e.g. waves versus reconnection) to this bursty energy release, its origin is almost certainly magnetic.

Cargill (1994) and Cargill & Klimchuk (2004) have predicted that emission measure distributions resulting from nanoflare models should be wide and have a faint, high-temperature (8-10 MK) component and thus a steep hotward slope, the so-called "smoking gun" of nanoflare heating. Unfortunately, observing this high-temperature emission is difficult and in some cases impossible. The reason for this difficulty is twofold. First, thermal conduction is a very efficient cooling mechanism at high temperatures and large spatial temperature gradients. When a loop is heated impulsively, its temperature rises quickly while the increase in density lags behind. By the time the density has increased sufficiently (due to chromospheric evaporation brought about by the response of the transition region to the strong downward coronal heat flux) to allow for an appreciable amount of emission (recalling EM $\propto n^2$), thermal conduction has cooled the loop far below its initial hot temperature, making a direct detection of ~ 10 MK plasma very difficult.

The second reason for this difficulty is non-equilibrium ionization. It is usually assumed that the observed emission lines, because of their known formation temperatures, are a direct indicator of the plasma temperature. However, if the heating timescale is shorter than the ionization equilibration timescale, the time it takes for the ion population to settle into the assumed charge state, an equilibrium assumption can lead to a misdiagnosis of the plasma temperature. This makes signatures of hot, nanoflare-heated plasma especially difficult to detect if the high temperatures persist for less than the ionization timescale (Bradshaw & Cargill 2006; Bradshaw & Klimchuk 2011; Reale & Orlando 2008).

Despite these difficulties, various attempts have been made to observe this faint high-temperature emission. Using the broadband X-Ray Telescope (XRT) (Golub et al. 2007) on board the Hinode spacecraft (Kosugi et al. 2007), Schmelz et al. (2009) and Reale et al. (2009) show a faint hot component in the reconstructed DEM curves. However, since the channels on such broadband instruments can often be polluted by low-temperature emission, the reliability of such measurements depends on the filtering technique used. Additionally, Winebarger et al. (2012) showed that combinations of measurements from XRT and the Extreme-ultraviolet Imaging Spectrometer (EIS) (Culhane et al. 2007), also on Hinode, leave a "blind spot" in the EM -T space conincident with the range where evidence for nanoflare heating is likely to be found.

Unambiguous observational evidence of nanoflare heating must come from pure spectroscopic measurements

91

92

93

94

95

96

97

100

101

102

103

104

105

106

107

108

109

110

111

112

113

114

115

116

117

118

120

121

122

123

124

125

126

127

128

129

130

131

132

133

134

135

136

137

138

139

140

141

142

143

144

145

146

147

148

149

150

151

(see Brosius et al. 2014). Additionally, new instruments $_{152}$ with higher spatial and temporal resolution, such as IRIS $_{153}$ (De Pontieu et al. 2014) and the Hi-C sounding rocket $_{154}$ (Cirtain et al. 2013) have provided encouraging results $_{155}$ for impulsive heating (Testa et al. 2013, 2014). Future $_{156}$ missions like the Marshall Grazing Incidence X-ray Spectrometer (MaGIXS) (Kobayashi et al. 2011; Winebarger $_{158}$ 2014), with a wavelength range of 6-24 Å and a temperature range of 6.2 $<\log T < 7.2$, aim to probe this $_{160}$ previously poorly-resolved portion of the coronal spectrum in hopes of better quantifying the presence of faint, $_{162}$ high-temperature plasma.

One strategy for constraining the nanoflare model is analysis of modelled and observed emission measure distributions for signatures of impulsive heating in active region cores. As with cool emission, hot emission is also often characterized by a power-law relation of the form EM $\propto T^{-b}$. Typically, this power-law fit to the emission measure is done "hotward" of the peak, usually in the 170 range $6.6 \lesssim \log T \lesssim 7.2$. However, measured values of 171 these hotward slopes are poorly constrained due to both 172 the magnitude of emission and the lack of available spectroscopic data in this temperature range. Warren et al. 174 (2012), using spectral measurements from EIS, provided hotward fits for EM reconstructions for a large number of active regions. All measured slopes fell in the range 6.1 < b < 10.3, with large uncertainties on each hotward fit

An often overlooked consequence of impulsive heating in the corona is electron-ion non-equilibrium. In a fullyionized hydrogen plasma like the solar corona, interactions between electrons and ions are governed by binary Coulomb collisions. For $n \sim 10^8 \text{ cm}^{-3}$ and $T \sim 10^7 \text{ K}$, parameters typical of nanoflare heating, the collisional timescale, $\tau_{ei} = 1/\nu_{ei}$, where ν_{ei} is the Coulomb collision frequency (see Equation A6) can be estimated as $\tau_{ei} \approx 8000$ s. Thus, any heating that occurs on a timescale less than 8000 s, such as a nanoflare with a duration of $\tau_H \leq 100$ s, will result in electron-ion nonequilibrium. Chromospheric evaporation, the response from the transition region to the strong coronal heat flux, does lead to an increase in n and thus a decrease in τ_{ei} . However, we maintain that during this initial phase of impulsive heating, $\tau_{ei} \gg \tau_H$ still holds, with 8000 s being an approximate upper bound on τ_{ei} .

Additionally, while it is often assumed that the electrons are the direct recipients of the prescribed heating function, the degree to which the ions or electrons are preferentially heated in the solar corona is unknown. Thus, it is possible that the ions are preferentially heated, for instance, through ion-cyclotron wave resonances (Markovskii & Hollweg 2004). Ion cyclotron waves are excited by plasma instabilities in the lower corona. These waves then propagate upwards through the coronal plasma and wave particle interactions can 203 occur for those ions whose gyrofrequencies have a resonance with the ion-cyclotron wave. Additionally, there 205 is also evidence for ion heating via reconnection, both in laboratory plasmas and in particle-in-cell simulations 207 (Ono et al. 1996; Yoo et al. 2014; Drake & Swisdak 2014). Thus, ion heating in the solar corona should not be dis- 209 counted as a possibility.

In our first paper, Cargill et al. (2016) (Paper I, here-

after), we studied the effect of pulse duration, flux limiting, and non-equilibrium ionization on hot emission from single nanoflares and nanoflare trains. In this second paper in our series on hot emission in active region cores, we use an efficient two-fluid hydrodynamic model to explore the effect of electron and ion heating on nanoflare-heated loops. In particular, we look at how the hot emission is affected by heating preferentially one species or the other as well as how this hot emission can vary with heating frequency and the power-law index that determines the event energy distribution. Additionally, we consider how non-equilbrium ionization may affect hot emission measure slopes in the cases of electron and ion heating as well as the single-fluid case.

Section 2 discusses the numerical model we have used to conduct this study and the parameter space we have investigated. Section 3 shows the resulting emission measure curves and slopes for the electron and ion heating cases as well as the equivalent single-fluid cases. In Section 4, we discuss the implications of two-fluid effects in the context of hot and cool emission measure slopes and the nanoflare heating model. Finally, Section 5 provides some concluding comments on our findings.

2. METHODOLOGY

2.1. Numerical Model

1D hydrodynamic models are excellent tools for computing field-aligned quantities in coronal loops. However, because of the small cell sizes needed to resolve the transition region and consequently small timesteps demanded by thermal conduction, the use of such models in large parameter sweeps is made impractical by long computational runtimes (Bradshaw & Cargill 2013). Thus, in our numerical study, we use a modified form of the popular 0D enthalpy-based thermal evolution of loops (EBTEL) model (Klimchuk et al. 2008; Cargill et al. 2012a,b, 2015). This model, which has been successfully benchmarked against the 1D hydrodynamic HY-DRAD code of Bradshaw & Cargill (2013), computes time-dependent spatially-averaged loop quantities with very low computational overhead and as such is ideal for large parameter space investigations.

We have modified the usual EBTEL equations (see Cargill et al. 2012a) to treat the evolution of the electron and ion populations separately while maintaining the assumption of quasi-neutrality, $n_e = n_i = n$. This amounts to computing spatial averages of the two-fluid hydrodynamic equations over both the transition region and corona. We will reserve a full discussion of this modified EBTEL model for a future paper. The relevant equations can be found in Appendix A.

2.2. Parameter Space

We define our heating function in terms of a series of discrete heating events plus a static background heating rate to ensure that the loop does not drop to unphysically low temperatures and densities between events. All events are modeled as triangular pulses of fixed duration $\tau_H = 100$ s. Thus, for loop half-length L and cross-sectional area A, the total energy per event is $Q_i = LAH_i\tau_H/2$, where H_i is the heating rate amplitude of event i. Each run will consist of N heating events, each with peak amplitude H_i , and a steady background value

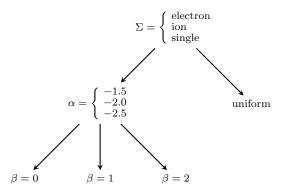


Fig. 1.— Total Parameter space covered. Σ indicates the species that is heated, where "single" indicates a single-fluid model. α is the power-law index and β indicates the scaling in the relationship $Q \propto T_N^{\beta}$, where $\beta = 0$ corresponds to the case where T_N and the event energy are independent. Note that $(3 \alpha \text{ values}) \times (3 \beta \text{ values}) + \text{uniform heating} = 10 \text{ different types of heating func-$

216

217

218

219

227

228

229

230

231

232

233

237

238

239

240

241

242

243

248

of $H_b = 3.4 \times 10^{-6} \text{ erg cm}^{-3} \text{ s}^{-1}$. Observations have suggested that loops in active region cores are maintained at an equilibrium temperature of $T_{peak} \approx 4$ MK (Warren et al. 2011, 2012). The cor- 250 responding heating rate can be estimated using coronal 251 hydrostatics. Neglecting the radiative loss term and let- 252 ting $dF_C/ds \approx \kappa_0 T_{peak}^{7/2}/L^2$, $E_{H,eq}$ can be estimated as

$$E_{H,eq} pprox rac{\kappa_0 T_{peak}^{7/2}}{L^2},$$
 (1) 256

where $\kappa_0 \approx 10^{-6}$ erg K^{-7/2} cm⁻¹ s⁻¹. $E_{H,eq}$ can be ²⁵⁸ interpreted as a time-averaged volumetric heating rate. ²⁵⁹ Thus, to maintain an emission measure peaked about T_{peak} , for triangular pulses, the individual heating rates ²⁶¹ are constrained by

$$E_{H,eq} = \frac{1}{T} \sum_{i=1}^{N} \int_{t_i}^{t_i + \tau_H} dt \ h_i(t) = \frac{\tau_H}{2T} \sum_{i=1}^{N} H_i. \quad (2)$$

where T is the total simulation time. Note that if $H_i = {}^{267}$ H_0 for all i, the uniform heating amplitude H_0 is just ²⁶⁸ $H_0 = 2TE_{H,eq}/N\tau_H$. Thus, for L = 40 Mm, $A = 10^{14}$ ²⁶⁹ cm², the total amount of energy injected into the loop by ²⁷⁰ one heating event for a loop heated by N=20 nanoflares ²⁷¹ in T=80000 s is $Q=LATE_{H,eq}/N\approx 1.3\times 10^{25}$ erg, ²⁷² consistent with the energy budget of the Parker nanoflare ²⁷³ model.

Determining the heating frequency in active region 275 cores will help to place constraints on the source(s) of 276 heat in the corona. We define the heating frequency in 277 terms of the waiting time, T_N , between successive heating events. Following Cargill (2014), the range of waiting ²⁷⁹ times is $250 \le T_N \le 5000$ s in increments of 250 s, for 280 a total of 20 different possible heating frequencies. Ad- $^{\scriptscriptstyle 281}$ ditionally, T_N can be written as $T_N = (T - N\tau_H)/N$, 282 where we fix T=80000 s. Note that because T and τ_H ²⁸³ are fixed, as T_N increases, N decreases. Correspondingly, Q_i , the energy injected per event, increases according to Equation 2 such that the total energy injected per run is 285 constant, regardless of T_N .

We compute the peak heating rate per event in two 287 different ways: 1) the heating rate is uniform such that 288

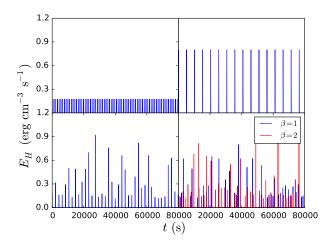


Fig. 2.— Top left: uniform heating amplitudes for $T_N = 1000$ s; Top right: uniform heating amplitudes for $T_N = 5000 \text{ s}$; Bottom left: power-law distributed heating amplitudes for $\alpha = -1.5$, $T_N = 2000 \text{ s}$; **Bottom right:** power-law distributed amplitudes for $\alpha = -1.5$ where the wait times depend on the event energies and the mean wait time for both values of β is $\langle T_N \rangle = 2000$ s.

 $H_i = H_0$ for all i and 2) H_i is chosen from a power-law distribution with index α where $\alpha = -1.5, -2.0, \text{ or } -2.5.$ For the second case, it should be noted that, when $T_N \approx$ 5000s, $N\sim20$ events, meaning a single run does not accurately represent the distribution of index α . Thus, a sufficiently large number of runs, N_R , are computed for each T_N to ensure that the total number of events is $N_{tot} = N \times N_R \sim 10^4$ such that the distribution is wellrepresented. Figure 1 shows the parameter space we will explore. For each set of parameters and waiting time T_N , we compute the resulting emission measure distribution for N events in a period T. This procedure is repeated

 N_R times until $N \times N_R \sim 10^4$ is satisfied. According to the nanoflare heating model of Parker (1988), turbulent loop footpoint motions twist and stress the field, leading to a buildup and subsequent release of energy. Following Cargill (2014), we let $Q_i \propto T_{N,i}^{\beta}$, where $Q_i, T_{N,i}$ are the total energy and waiting time following event i, respectively, and $\beta = 1, 2$ such that the event energy scales either linearly or quadratically with the waiting time. The reasoning for such an expression is as follows. Bursty, nanoflare heating is thought to arise from the stressing and subsequent relaxation of the coronal field. If a sufficient amount of time has elapsed since the last energy release event, the field will have had enough time to "wind up" such that the subsequent energy release is large. Conversely, if only a small amount of time has elapsed since the last event, the field will have not had time to become as stressed, resulting in a lower energy event. Thus, this scaling provides a way to incorporate a more physically motivated heating function into a hydrodynamic model which cannot self-consistently determine the heat input based on the evolving magnetic field. Figure 2 shows the various heating functions used for several example T_N values.

2.3. Emission Measure Distributions

In our 0D model, the emission measure is calculated using the familiar expression EM = $n^2(2L)$, where L is the loop half-length. We consider a temperature range

290

291

292

293

294

295

296

297

298

299

300

301

302

303

304

305

306

307

308

309

310

311

312

313

314

315

316

317

318

319

320

321

322

323

324

325

326

327

328

329

330

331

332

333

334

335

336

337

338

339

340

341

342

343

344

345

346

347

of $4.0 \le \log T \le 8.5$ with bin sizes of $\Delta \log T = 0.01$. At 351 each iteration i, the coronal temperature range $[T_0, T_a]$ is 352 calculated from T_e (see Appendix A). For each bin that 353 falls within $[T_0, T_a]$, $\bar{n}_i^2(2L)$ is added to that bin, where 354 \bar{n}_i is the spatially-averaged number density at iteration i. 355 The emission measure in each bin is then averaged over 356 the entire simulation period. When measured observa- 357 tionally, EM(T) is a line-of-sight quantity. Assuming an 358 aspect ratio (i.e. ratio of loop length to loop width) of 10, 359 we apply a correction factor 1/10 to all calculated EM ³⁶⁰ curves. We do not attempt to apply an advanced forward ³⁶¹ modeling treatment here and instead reserve such an approach for a future paper. However, while effects due to ³⁶³ non-equilibrium ionization are neglected in our parame- 364 ter space exploration, in Subsection 3.3 we consider the 365 emission measure due to T_{eff} , the effective temperature ³⁶⁶ due to non-equilibrium ionization, for several test cases ³⁶⁷ in order to diagnose how this might affect our calculated 368 emission measure slopes.

3. RESULTS

For each species, type of power-law heating function, 372 and waiting time T_N , N_R emission measure curves are 373 calculated. Because drawing event amplitudes from a 374 power-law distribution introduces random fluctuations 375 into our model, we must be sure to account for the full 376 range of effects due to the distribution. This is especially 377 true in the low-frequency regime, when $T_N \geq \tau_{cool}$, the 378 cooling timescale, and there are fewer events per run. In 379 this case, one or two especially strong heating events can 380 lead to an extremely enhanced hotward emission measure; conversely, a run with only small events will lead 382 to a diminished hotward slope. Thus, the mean EM curve 383 of each set of N_R runs can be said to reasonably represent the expected hot emission for a given T_N .

To characterize the emission measure, we compute the 386 slopes on both the cool and hot sides of the peak. To 387 be consistent with past observational and computational 388 studies of cool emission (see Bradshaw et al. 2012, and 389 references therein), we fit the cool slope on the interval 390 $6.0 \leq \log T \leq 6.6$. Contrastingly, past studies of hot 391 emission are less abundant; thus, the "hot" region where 392 EM is known to follow a power-law is far less constrained. 393 In order to best describe the steepness of the emission 394 measure hotward of the peak, we choose to fit EM be- 395 tween the temperatures at which the emission measure 396 is 99% and 92% of the peak value. We have no physi- $_{397}$ cal reason for choosing these particular bounds, but note 398 that on this interval, the mean hotward emission is reasonably well described by a linear relationship. Fitting 400 too close to the wide peak leads to misleadingly shal- 401 low slopes while fitting too close to the steep drop near 402 $\log T \sim 7.5$ results in steep slopes not particularly representative of the hotward emission. We perform the 404 fit using the Levenberg-Marquardt algorithm for least- 405 squares curve fitting as implemented in the SciPy scien- 406 tific Python package (van der Walt et al. 2011).

3.1. Separate Electron and Ion Heating

Figure 3 and Figure 4 show the results of our emission measure study for the two distinct cases where only the electrons are heated and only the ions are heated with $\alpha = -2.5, \beta = 1$ for a loop half-length of 40 Mm, consistent with Paper I. The panels on the left show the mean

EM for all T_N , where the average is taken over all N_R runs. There is an artifical spacing of $\Delta \log \mathrm{EM} = 0.2$ between each curve so that they can be easily distinguished from each other. The blue (red) lines indicate the cool (hot) power-law fits, where the slopes of the lines are the averages taken over all N_R runs. We note that EM, for all T_N , peaks at approximately 4 MK ($10^{6.6}$ K), consistent with the constraints laid out in Subsection 2.2. The top right panels show these average slope values as a function of T_N . The error bars indicate one standard deviation as calculated from the distribution of all N_R runs.

Lastly, the bottom right panels show the first derivative as a function of temperature, $d \log \mathrm{EM}/d \log T$, computed using central differences. The color scheme and line styles correspond to the emission mesure curves in the left panel. As in Paper I, we compute the derivative in an effort to better assess at what temperatures the emission measure is not well described by a power-law.

We first briefly consider the calculated cool emission measure slopes. Looking at the top right panels of Figure 3 and Figure 4, we note that in the cases of electron and ion heating, the cool emission measure slopes are consistent with both observational and modelling studies of cool emission in active region cores, having values that fall within the range $2 \le a \le 5$ (Bradshaw et al. 2012, and references therein). Furthermore, the cool slopes computed using our new modified EBTEL model, with a heating function of the form $Q \propto T_N^{\beta}$, are consistent with those values reported in Cargill (2014) and show a dependence on the waiting time T_N .

Additionally, looking at the bottom right panels of Figure 3 and Figure 4, we see that, within the range $6.0 \le \log T \le 6.6$, a linear approximation of EM on a loglog scale is reasonable, where $2 \lesssim d \log \text{EM}/d \log T \lesssim 3$. Comparing the cases of electron and ion heating for both the cool slopes and $d \log \text{EM}/d \log T$ on $6.0 \le \log T \le 6.6$, there are no substantial differences for all values of T_N considered.

This is not the case for the hot emission measure. Looking first at the case of electron heating in Figure 3, we note that there is a pronounced "hot shoulder" in the emission measure (left panel) just above 10^7 K for $T_N \gtrsim 2000$ s. This feature is even more evident when looking at the derivative of EM in the bottom right panel of Figure 3. The peak between 10^7 and $10^{7.5}$ K shows how the EM flattens out around 10^7 K, indicating an enhanced hot emission measure. Considering the large range of values of $d \log EM/d \log T$ on the interval over which the fit was performed, we acknowledge that a single power-law is not a good description of the hot emission measure in the case of electron heating.

Contrastingly, we have not calculated the hot emission measure slopes for the case of ion heating. Looking at the left panel of Figure 4, for $T_N \gtrsim 1000$ s, the EM peak is wide with a steep drop near 10^7 K. There is no substantial emission measure component above 10^7 K and, consequently, no hot shoulder as in the electron heating case. Applying the fitting procedure outlined above to the hot emission in the case of ion heating yields meaningful results for only a few short T_N . Thus, as in the case of electron heating, the resulting hot emission measure from ion heating is not well described by a power-law.

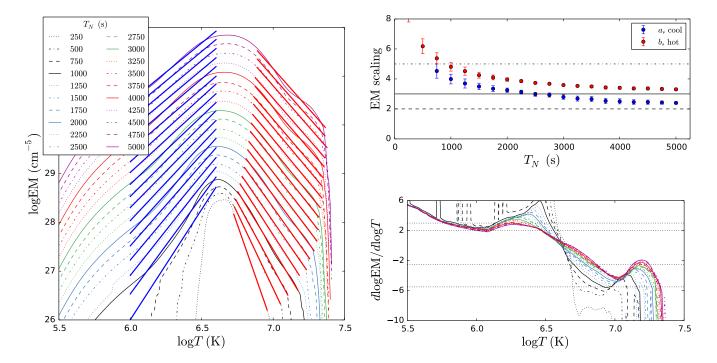


Fig. 3.— $\alpha = -2.5$, $\beta = 1$, L = 40 Mm, electron heating. **Left:** log EM as a function of log T for all values of T_N . There is an artificial spacing of $\Delta \log \mathrm{EM} = 0.2$ between each curve. The bold blue (red) lines on either side of the peak show the linear fit to the cool (hot) emission. **Top right:** Average slopes from power-law fits to all N_R curves as a function of T_N . The error bars indicate one standard deviation from the distribution of N_R fits. In the case of hot slopes, the absolute value is shown. The dashed, solid, and dot-dashed reference lines are placed at 2, 3, and 5 respectively. **Bottom right:** Derivative of log EM with respect to $\log T$. The dotted reference lines are placed at -5.5, -2.5, 2, and 3. The legend is the same as the left panel.

The lower right panel of Figure 4 further highlights this ⁴⁴⁵ by showing that around 10^7 K, $d \log \text{EM}/d \log T \rightarrow -\infty$. ⁴⁴⁶

3.2. Single-fluid

Figure 5 shows the same results as Figure 3 and Figure 4, but for the single-fluid case in which electronion equilibrium is assumed at all times. To compute these EM curves, we have used the original, single-fluid EBTEL model as described in Klimchuk et al. (2008) and Cargill et al. (2012a). The equivalent parameter space that was investigated with the modified two-fluid EBTEL model is explored with the single-fluid EBTEL code as well.

We compute the hot and cool emission measure slopes in the same manner as the electron and ion heating cases. We first note that the cool emission measure slopes are comparable to those in both the electron and ion heating cases. In particular, we find $2 \lesssim a \lesssim 5$ for all values of T_N as expected. Again, we confirm the validity of our linear fit to the cool emission by computing the derivative $d \log EM/d \log T$ in the lower right panel of Figure 5. For $T_N \gtrsim 2000$ s, the slope is bounded between 2 and 3 on 466 the interval $6.0 \leq \log T \leq 6.6$.

The hot emission measure in the single-fluid case dif- $_{468}$ fers significantly from the two-fluid case. In contrast to $_{469}$ the electron heating case in Figure 3, the EM curves in $_{470}$ the left panel of Figure 5 show no hot shoulder. This is $_{471}$ further confirmed by the lower right panel; the deriva- $_{472}$ tive, in contrast to the electron heating case, shows no $_{473}$ peak near 10^7 K. For low T_N , $d\log {\rm EM}/d\log T$ is mono- $_{474}$ tonically decreasing for $\log T \gtrsim 6.6$. For $T_N \ge 3000$ s, $_{475}$ $d\log {\rm EM}/d\log T$ is relatively flat for $\log T \ge 7.0$, indi- $_{476}$

cating that a linear fit is a good description for the hot emission in this region. This is confirmed by noting the agreement between the fit lines and the EM curves in the left panel.

Comparing the top right panels of Figure 5 and Figure 3 further highlights the enhanced hot emission in the electron case. For high T_N , the hot emission slopes in the electron case converge to a value just above 3; for the single-fluid case, the hot slopes converge to approximately 4.5. Thus, while a single power-law is not a good descriptor of the hot emission in the case of electron heating, the slope still captures the enhanced hot shoulder relative to the weaker hot emission of the single-fluid case. Additionally, comparing the single-fluid case to the ion heating case in Figure 4, it is obvious that the single-fluid case shows a great deal more hot emission as the EM curves in the left panel of Figure 5 extend well above 10^7 K while those in the left panel of Figure 4 show a steep cutoff at temperatures just above the peak.

3.3. Non-equilibrium Ionization Effects

As mentioned in Section 1, non-equilibrium ionization (NEI) can make it difficult to observe emission signatures from nanoflare-heated plasma because the heating timescale is shorter than the ionization timescale such that the charge state of the plasma is not representative of the plasma temperature. In order to diagnose how NEI might affect hot emission measure slopes, we use n and T_e profiles from our modified EBTEL code along with the method outlined by Bradshaw (2009) to compute T_{eff} , the temperature that would be measured based on the actual ionization states. An effective emission measure

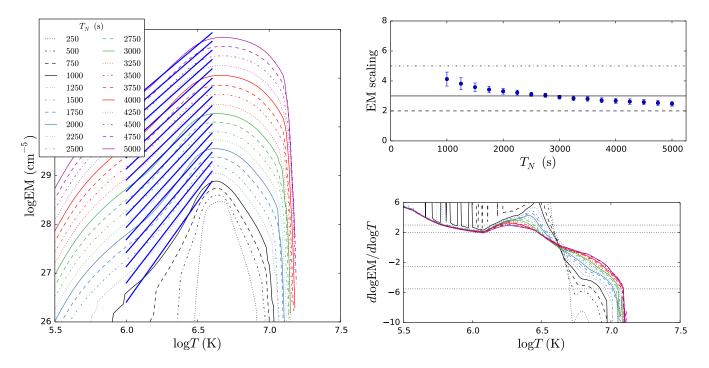
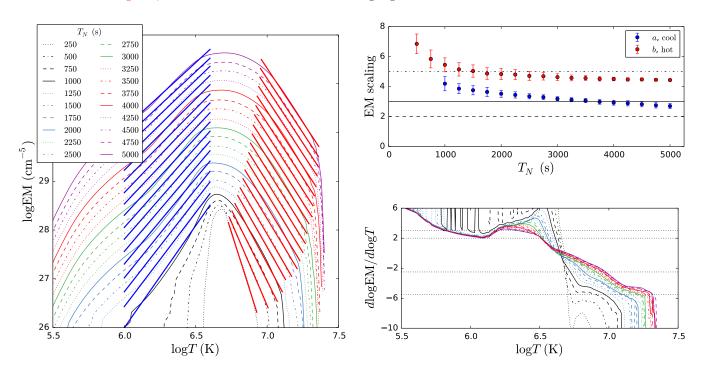


Fig. 4.— Same as Figure 3, but for the case in which all of the heating is given to the ions.



 $Fig. \ 5. \\ -- Same \ as \ {\color{red} Figure \ 3}, \ but \ for \ the \ single-fluid \ case \ in \ which \ electron-ion \ equilibrium \ is \ assumed.$

distribution, ${\rm EM}_{eff}$, can then be calculated. Following 485 Paper I, we use iron (Fe) and the ionization states Fe IX $_{486}$ through FeXXV.

As the calculation of T_{eff} is significantly more expensive than an EBTEL calculation, we do not compute 489 EM $_{eff}$ for the entire parameter space and instead consider only a small number of single-pulse test cases of 491 duration $\tau_H=100$ s and peak heating rate $H_0=0.8$ 492

erg cm $^{-3}$ s $^{-1}.$ Figure 6 shows temperature and density profiles (left column) and emission measure distributions (right column) for the cases where NEI is (dashed) and is not (solid) included. These profiles are computed for all preferentially-heated species (electron, ion, single-fluid). For all three species, we note that including NEI in the calculation of the cool slope makes essentially no difference .

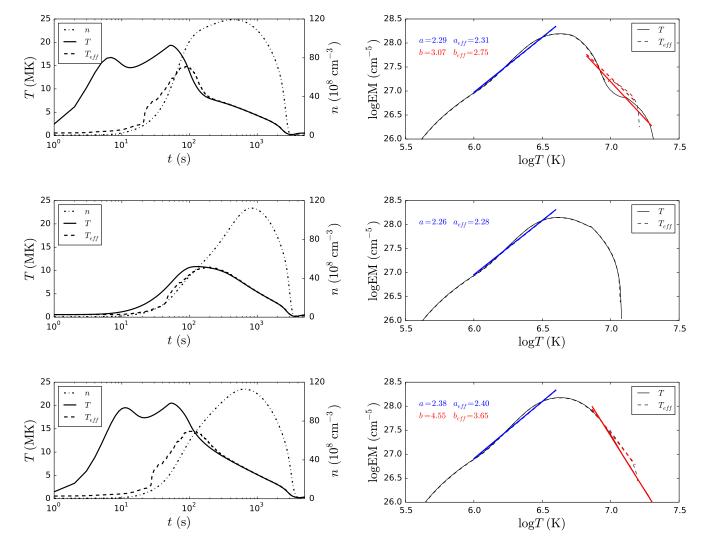


Fig. 6.— Non-equilibrium ionization T (solid), T_{eff} (dashed) and n (dot-dashed), profiles (**left column**) and EM distributions (**right column**) for electron heating (**top row**), ion heating (**middle row**), and the single-fluid case (**bottom row**). In all cases, L=40 Mm and the loop is subject to a single pulse of energy $Q\approx 10^{25}$ erg with a duration of $\tau_H=100$ s. The values printed on the EM plots are the resulting emission measure slopes for the cool (blue) and hot (red) slopes for the cases of EM and EM_{eff}.

As in Figure 4, we do not compute the hot slope for 512 the case of ion heating. Looking at the right panel in the middle row of Figure 6, we see that the inclusion of NEI in the case of ion heating has little to no effect on the emission measure. This is confirmed by the left panel of the middle row which shows that the difference between T and T_{eff} is relatively small and only occurs at low densities. Conversely, in the single-fluid and electron-heating cases, T and T_{eff} differ greatly during the heating phase and NEI has two distinct effects on the EM: it leads to an overestimation of the amount of emission in the midrange hot temperatures (7.0 $\lesssim \log T \lesssim$ 7.2) and causes a steeper cutoff in the emission at lower temperatures (before $\log T \approx 7.25$) compared to the case where NEI is not included. Interestingly, in both the electron-heating (first row) and single-fluid (third row) cases, $b_{eff} < b$ though we note that in the electron-heating case (first row), a linear fit does not adequately describe the hot side of the EM distribution.

493

494

495

496

497

498

499

500

501

502

503

504

505

506

507

508

509

510

511

3.4. Full Parameter Space Comparison

To compare the effects of varying α , β , and T_N for each species (i.e. electron, ion, single-fluid), we construct histograms of hot and cool emission measure slopes for each parameter space point. Recall that in the case where the distributions of heating event energies are non-uniform, we have N_R emission measure slopes to properly account for the statistical spread in hot emission measure slopes due to power-law distributions.

As seen in Figure 7, these histograms, denoted by type of slope (i.e. hot or cool) and species, are constructed in one of two ways: each distinct histogram (denoted by linestyle and/or color) is either representative of a distinct heating function (e.g. top row of Figure 7) or a distinct value of T_N (e.g. bottom row of Figure 7). In the four panels of Figure 7, we choose to separate the cool emission measure slopes by type of heating function and the hot emission measure slopes by T_N . This means, for example, that the dot-dashed blue $\alpha = -1.5, \beta = 1$ histogram in the upper left panel of Figure 7 encapsu-

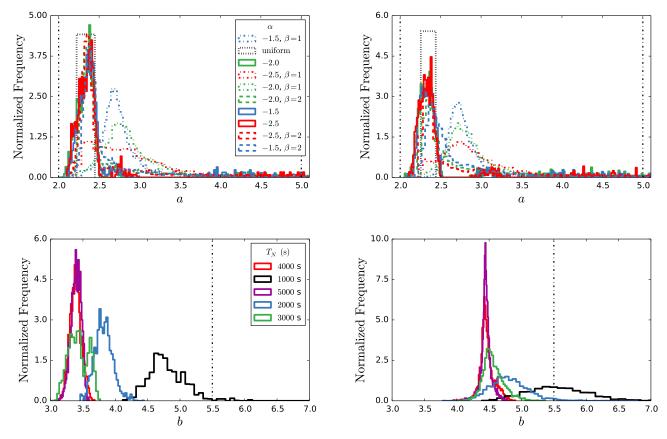


Fig. 7.— Histograms of emission measure slopes from the entire parameter space as described in Figure 1. Top left: cool slopes grouped by heating function for the electron heating case; **Top right:** cool slopes grouped by heating function for the ion heating case; **Bottom left:** hot slopes grouped by T_N for the electron heating case; **Bottom right:** hot slopes grouped by T_N value for the single-fluid case. In the cases where the slopes are grouped by T_N , only $T_N = 1000, 2000, 3000, 4000, 5000$ s are shown for aesthetic purposes.

lates cool emission measure slopes for $250 \le T_N \le 5000$ s while the solid blue $T_N = 2000$ s histogram in the 561 lower left panel includes emission measure slopes for all 562 10 types of heating functions (as listed in Figure 1 and 563 the legend in the upper left panel of Figure 7). All his-564 tograms are normalized such that for each distribution 565 P(x), $\int_{-\infty}^{\infty} \mathrm{d}x \; P(x) = 1$. Additionally, the bin widths 566 are calculated using the well-known Freedman-Diaconis 567 formula (Freedman & Diaconis 1981).

Concerning the distributions of cool slopes grouped by type of heating function (bottom row of Figure 7), we 569 note that there are no discernible differences between the cases of electron and ion heating. In both cases, all heating functions except for those where $\beta=1$ are peaked 571 sharply between 2 and 2.5. In the case where $\beta=1$ (for 572 all α), the distribution is peaked between 2.5 and 3, with 573 the width of the distribution increasing as α steepens. 574 This larger range of cool emission measure slopes for the 575 case of $\beta=1$ is consistent with Cargill (2014). 576

As stated in Subsection 3.1, we choose not to show the 577 hot emission measure slopes for the ion heating case as 578 they are not a good descriptor of the emission measure 579 distribution hotward of the peak as evidenced by the left 580 and bottom right panels of Figure 4. Instead, we compare 581 the hot emission measure slopes of the electron heating 582 and single-fluid cases, the bottom left and right panels 583 of Figure 7, respectively. In both cases, for $T_N < 3000$ 584 s, we see a strong dependence on T_N while for $T_N \geq$ 585

s, the slopes tend to be sharply peaked around a single value. In the electron heating case, distributions for $T_N < 3000$ s tend to be more narrow than their single-fluid counterparts and centered at lower values (i.e. more shallow hot slopes). Most notably, for $T_N \geq 4000$ s, the electron heating hot emission measure slopes are peaked between 3 and 3.5 while the single-fluid slopes are peaked at ~ 4.5 .

4. DISCUSSION

The main points we emphasize from the results presented in Section 3 are,

- 1. Cool emission measure slopes resulting from electron and ion heating are very similar and are well described by EM $\propto T^a$. As noted in Cargill (2014), using the relation $Q \propto T_N^\beta$ yields $2 \lesssim a \lesssim 5$, consistent with observations.
- 2. Hot emission from electron heating results in an enhanced hot shoulder while the equivalent ion heating cases show a relatively flat peak and a steep dropoff near 10^7 K. This effect is exacerbated as T_N increases.
- 3. Hot emission due to both electron and ion heating is poorly described by the scaling EM $\propto T^{-b}$. In the former, this is due to the flat hot shoulder between 10^7 and $10^{7.5}$ K. In the latter case, the relatively flat peak and steep drop off near 10^7 K

do not allow for a power-law description of the hot emission.

- 4. Using a linear fit to characterize the hot side of the EM distribution, Single-fluid models predict less hot-emission than two-fluid models in which only the electrons are heated. In particular, for $T_N \geq 4000$ s, our modified two-fluid EBTEL model predicts $3 \leq b \leq 3.5$ while the original single-fluid EBTEL model predicts $b \sim 4.5$.
- 5. Including NEI does not impact the cool emission measure slope. In the case of electron heating and the single-fluid case, NEI enhances the mid-range hot EM, but leads to a lower temperature cutoff. The emission measure distribution in the case of ion heating is unaffected.

We first focus on item 1. In the range $6.0 \le \log T \le 6.6$, the loop is undergoing both radiative and enthalpy-driven cooling. During this phase, the density is high and the temperature low relative to the heating and conductive cooling phase. Looking at the fourth term on the right-hand side of Equation A1 and Equation A6, the coupling term between the two species is roughly $\propto \bar{n}^2(\bar{T}_e - \bar{T}_i)/\bar{T}_e^{3/2}$; as density increases, so does the coupling strength. While the loop is also draining in this temperature range, the density has already increased such that $\bar{T}_e \approx \bar{T}_i$ and until the next heating event, there is nothing to drive the two species out of equilibrium. Thus, because the two-species are evolving together in this regime, we expect their emission measure distributions to be the same.

In item 2, we see quite the opposite situation. In the heating and conductive cooling phases, the density is relatively low and the electron (or ion) temperature relatively high. Because the heating pulses we have used are relatively short (100 s), the heated species quickly reaches high temperatures and cools significantly by thermal conduction before Coulomb collisions can bring the two species back into equilibrium. Since the emission measure depends on the electron temperature, this means that in the event that only the electrons are heated, the emission "sees" the full range of temperatures produced by heating and conductive cooling.

However, in the case of ion heating, in order for the emission measure to see the full range of temperatures for resulting from the heating and conductive cooling by the ions, $\bar{T}_e = \bar{T}_i$ would have to hold for this entire phase. Finstead, as the ions are impulsively heated, the electrons remain at a relatively low temperature, coupled only weakly to the ions because the loop has only just for begun to fill. As the coronal density increases, the electrons come into equilibrium with the ions, but because from the corona, the ions have now cooled far below for the temperature to which they were initially heated.

This scenario is clearly illustrated by Figure 8. In this $_{676}$ test case, we have impulsively heated the ions with a triangular pulse lasting 100 s with total energy $_{678}$ angular pulse lasting 100 s with total energy $_{678}$ In the top panel, we see that by the time the electrons $_{679}$ come into equilibrium with the ions, the ions have cooled $_{680}$ well below 10 MK and the loop has just begun to fill. $_{681}$ Additionally, the bottom panel shows that during the $_{682}$ period in which the ions are at their hottest tempera- $_{683}$ tures, $_{7C,i} \ll \tau_{ei}$, where $_{7C,i}$ is the ion thermal conduc-

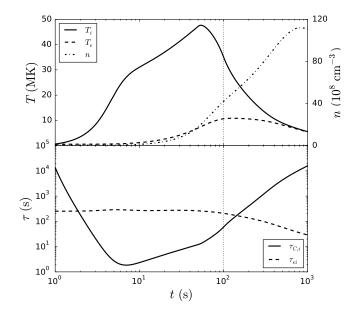


FIG. 8.— Single triangular heating pulse with duration $\tau_H=100$ s and total energy $Q=10^{25}$ erg injected into only the ions in a loop of half-length L=40 Mm. **Top:** Ion temperature, electron temperature, and coronal number density. **Bottom:** Ion thermal conduction $(\tau_{C,i})$ and Coulomb collision (τ_{ei}) timescales. The dotted black line at 100 s marks the end of the heating pulse.

tion timescale. Thus, while they are being heated, the ions are giving up nearly all of their energy to thermal conduction before they reach equilibrium with the electrons.

The result is a severely truncated hot emission measure distribution as seen in Figure 4. Additionally, this effect is exacerbated at long T_N . For short T_N , the heating is essentially steady, meaning that the loop has little to no time to drain or cool between heating events. This keeps the density at a roughly constant, near-equilibrium value which inhibits rapid heating to high temperatures and keeps the electrons and ions in equilibrium. However, for longer T_N , the loop is allowed to drain significantly between each pulse. Thus, at the start of each heating event, the density is low, allowing the species to very quickly evolve out of equilibrium.

Begin corrections: To address item 3 and item 4, we refer to our discussion in the introduction of Paper I. Using $\mathrm{EM} \sim n^2 \tau_{cool}$ and assuming constant pressure (such that $n \propto T^{-1}$), in the free-streaming regime, $\mathrm{EM} \propto T^{-5/2}$; in the regime described by classical Spitzer conduction, $\mathrm{EM} \propto T^{-11/2}$. Thus, at high temperatures where the free-streaming limit is imposed to prevent runaway cooling by thermal conduction, we expect a much more shallow emission measure slope than at slightly lower temperatures where Spitzer conduction dominates.

Significant emission in the free-streaming regime is produced in the case of electron heating as evidenced by the hot shoulder in the emission measure curves of Figure 3. The derivative in the lower-left panel also clearly shows the slope varying between roughly -5.5 and -2.5 as denoted by the two lower black dotted lines. Fitting a single slope to this entire range, we expect 2.5 < b < 5.5 which is indeed the case as evidenced by the bottom-left panel

686

687

688

689

690

691

692

693

694

695

696

697

698

699 700

701

702

703

704

705

706

707

708

709

710

711

712

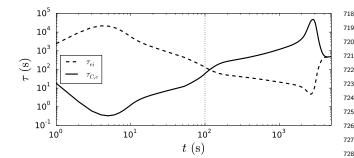
713

714

715

716

717



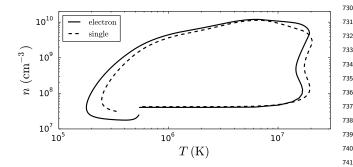


Fig. 9.— **Top:** Comparison between Coulomb collision timescale τ_{ei} and electron thermal conduction timescale $\tau_{C,e}$ for the single-pulse example shown in the top row of Figure 6. The vertical dotted line marks the end of the heating period. **Bottom:** n-T state space diagram for the single-pulse examples in the first (electron heating) and third (single-fluid) rows of Figure 6.

of Figure 7. When characterizing such hot emission in 748 the future, it may be more applicable to fit this emis- 749 sion with a double power-law in order to more properly 750 account for these two distinct cooling regimes. 751

In the single-fluid case, the hot shoulder is not pro- 752 duced because there is not a significant amount of emis- 753 sion at temperatures where thermal conduction enters 754 the free-streaming limit. This is likely for two reasons: 755 (1) the heating is essentially equally partitioned between 756 the electrons and ions, meaning less energy is directly injected into the electrons; (2) both species are helping to 758 "conduct away" the excess energy through thermal con- 759 duction. Even if the free-streaming limit is reached in the 760 single-fluid simulation, the density and amount of time 761 spent in this regime are not significant enough to pro- 762 duce a signature (i.e. the hot shoulder) in the emission 763 measure. In the case of ion heating, the emission measure never sees this temperature regime because the ions 765 have cooled significantly by thermal conduction before 766 they reach equilibrium with the electrons (as illustrated 767 by Figure 8). Thus, electron thermal conduction never 768 comes close to the free-streaming limit because the electrons remain relatively cool. End corrections

Finally, item 5 addresses the fact that NEI does not 771 affect cool emission or emission due to ion heating, while 772 it acts to enhance mid-range hot temperature emission 773 and creates a lower-temperature cutoff in the single-fluid 774 and electron heating cases as shown in Figure 6. As discussed in Paper I and Section 1, if the heating occurs 776 on a timescale faster than the ionization equilibration 777 timescale, high temperatures will not be detectable because the charge states indicative of such temperatures 779 will not have had time to form. Coolward emission is 780

due to radiative and enthalpy-driven cooling and during this phase, the density is relatively high and the temperature is changing relatively slowly, meaning that ionization equilibrium can be assumed. For hotward emission in the case of ion heating, we note that the effective heating timescale for the electrons is approximately τ_{ei} , the coupling timescale. As seen in Figure 8, for $Q \approx 10^{24}$, the electron temperature increases relatively slowly (compared to the heating timescale of the ions) and only gets above several MK once the density has increased significantly. Thus, ionization equilibrium can be assumed because the electrons undergo no direct impulsive heating. In the cases of electron heating and the single-fluid case, the electrons undergo direct impulsive heating when the density is relatively low. This is what leads to the lower-temperature cutoff in EM_{eff} : at these high temperatures and low densities, the ionization equilibration timescale is significantly longer than the heating timescale and so these very high temperatures are never seen. However, looking at the left panels in the first and third rows of Figure 6, we see that just after the heating ends at 100 s, $T_{eff} > T$ due to the fact that the thermal conduction timescale is shorter than the ionization equilibration timescale. This lag in the charge state due to the efficiency of thermal conduction leads to the midrange hot temperature emission enhancement seen in the right panels of the first and third rows of Figure 6.

729

5. CONCLUSIONS

In this paper, we have used a modified two-fluid version of the popular EBTEL model to study the effect of preferentially heating the electrons or ions on the hot and cool emission measure slopes over a parameter space that includes the power-law index describing the distribution of event energies, α , waiting time between successive heating events, T_N , and the scaling between the event energy and wait time, β . We have found that while there is little difference in the cool emission between the cases of electron and ion heating, when it comes to the hot emission, the emission measure curves of the electron-heated loops have an enhanced hot shoulder while the ion-heated loops show a truncated emission measure distribution on the hot side. This difference becomes more prominent as T_N increases. We note that given such a distinction in the EM distribution between the cases of electron and ion heating, the difference could be potentially observationally diagnosable by instruments such as MaGIXS, the Focusing Optics X-ray Solar Imager (FOXSI) (Krucker et al. 2011), or other future missions with adequate spectroscopic resolution in the hard X-rays.

Furthermore, by comparing these results with emission measure distributions obtained from the original single-fluid EBTEL model, we have found that heating only the electrons, because of the aforementioned hot shoulder due to flux limiting, leads to significantly more shallow hot emission measure slopes for equivalent values of T_N . Thus, using a single-fluid model to interpret observed hot emission measure distributions can potentially lead to a misdiagnosis of the heating frequency.

We note that in this study, we have constructed the most ideal emission measure curves by using the expression $EM = n^2(2L)$; that is, we have not taken into account the many complications involved when computing emission measure distributions from observed spectral

lines. For example, as we noted in Paper I, impulsive 794 heating leads to non-equilibrium ionization and a con-795 sequently lower effective temperature, meaning that the 796 emission does not see the hottest temperatures during the conductive cooling phase. By computing test cases 797 for electron heating, ion heating, and the single-fluid case, we have shown that NEI has the effect of steepening the hot emission measure distribution at very high temperatures and enhancing the mid-range hot temperature emission for the electron heating and single-fluid cases and has no impact on the emission measure distribution in the case of ion heating. We stress that when interpreting observed hot emission in the context of sim-

ulation, two-fluid and non-equilibrium ionization effects should be properly taken into account in order to extract meaningful properties of the heating.

ACKNOWLEDGMENT

All of the data analysis shown in this work was carried out using the IPython system for interactive scientific computing in Python as well as the NumPy and Scipy numerical and scientific Python libraries (Pérez & Granger 2007; van der Walt et al. 2011). All plots were produced using the Matplotlib graphics environment (Hunter 2007).

APPENDIX

The modified two-fluid EBTEL equations are,

$$\frac{d}{dt}\bar{p}_e = \frac{\gamma - 1}{L}[\psi_{TR} + \psi_C - (\mathcal{R}_{TR} + \mathcal{R}_C)] + k_B \bar{n}\nu_{ei}(\bar{T}_i - \bar{T}_e) + (\gamma - 1)\bar{E}_{H,e},\tag{A1}$$

$$\frac{d}{dt}\bar{p}_{i} = -\frac{\gamma - 1}{L}(\psi_{TR} + \psi_{C}) + k_{B}\bar{n}\nu_{ei}(\bar{T}_{e} - \bar{T}_{i}) + (\gamma - 1)\bar{E}_{H,i},\tag{A2}$$

$$\frac{d}{dt}\bar{n} = \frac{c_2(\gamma - 1)}{c_3\gamma L k_B \bar{T}_e} (\psi_{TR} - F_{0,e} - \mathcal{R}_{TR}),\tag{A3}$$

where

$$\psi_{TR} = \frac{1}{1+\xi} (F_{0,e} + \mathcal{R}_{TR} - \xi F_{0,i}), \tag{A4}$$

$$\psi_C = \bar{v}p_e^{(a)} - (p_e v)_0. \tag{A5}$$

Additionally, Equation A1, Equation A2, and Equation A3 are closed by the equations of state $p_e = k_B n T_e$ and $p_i = k_B n T_i$.

The volumetric heating rates, $E_{H,e}$ and $E_{H,i}$, are the primary degrees of freedom in our model. In the case of electron (ion) heating, $E_{H,i}(E_{H,e}) = 0$. \bar{p}_e, \bar{p}_i and \bar{T}_e, \bar{T}_i are the spatially-averaged coronal electron and ion pressures and temperatures, respectively and \bar{n} is the spatially-averaged coronal number density. $\mathcal{R}_C = \bar{n}^2 \Lambda(T)$ is the volumetric coronal radiative loss rate, where $\Lambda(\bar{T})$ is the radiative loss function, and $\mathcal{R}_{TR} = c_1 \mathcal{R}_C$ is the radiative loss rate in the transition region where the calculation of c_1 is described in Cargill et al. (2012a). Additionally, $F_{0,e}, F_{0,i}$ are the electron and ion conductive fluxes as computed at the base of the loop, respectively, and are calculated using the classical Spitzer formula with a free-streaming limit imposed to prevent runaway cooling at low densities. The Coulomb collision frequency, ν_{ei} , is given by,

$$\nu_{ei} = \frac{16\sqrt{\pi}}{3} \frac{e^4}{m_e m_i} \left(\frac{2k_B \bar{T}_e}{m_e}\right)^{-3/2} \bar{n} \ln \Lambda, \tag{A6}$$

where m_e , m_i are the electron and ion masses respectively and $\ln \Lambda$ is the Coulomb logarithm. Finally, $c_2 = \bar{T}/T_a = 0.6$, $c_3 = T_0/T_a = 0.9$, determined by static equilibrium, and $\xi = \bar{T}_e/\bar{T}_i$.

Note that in the limit that $\bar{T}_e = \bar{T}_i$ such that $\xi = 1$, Equation A3 reduces to the single-fluid density equation of Cargill et al. (2012a). Additionally, Equation A1 and Equation A2 can be added together to recover the single-fluid pressure equation. As with the original EBTEL model, the modified two-fluid version has been successfully benchmarked against the HYDRAD hydrodynamic code.

REFERENCES

```
      824
      Bradshaw, S. J. 2009, Astronomy and Astrophysics, 502, 409
      834
      Cargill, P. J. 19

      825
      Bradshaw, S. J., & Cargill, P. J. 2006, Astronomy and
      835
      —. 2014, The Astrophysics, 458, 987

      826
      Astrophysics, 458, 987
      836
      Cargill, P. J., E

      827
      —. 2013, The Astrophysical Journal, 770, 12
      837
      preparation

      828
      Bradshaw, S. J., & Klimchuk, J. A. 2011, The Astrophysical
      838
      Astrophysica

      830
      Bradshaw, S. J., Klimchuk, J. A., & Reep, J. W. 2012, The
      839
      Astrophysica

      831
      Astrophysical Journal, 758, 53
      841
      Cargill, P. J., &

      832
      Brosius, J. W., Daw, A. N., & Rabin, D. M. 2014, The
      842
      Journal, 605,

      833
      Astrophysical Journal, 759, 112
      842
      Journal, 605,
```

```
    Cargill, P. J. 1994, The Astrophysical Journal, 422, 381
    — 2014, The Astrophysical Journal, 784, 49
    Cargill, P. J., Bradshaw, S. J., & Barnes, W. T. 2016, in preparation
    Cargill, P. J., Bradshaw, S. J., & Klimchuk, J. A. 2012a, The Astrophysical Journal, 752, 161
    — 2012b, The Astrophysical Journal, 758, 5
    Cargill, P. J., & Klimchuk, J. A. 2004, The Astrophysical Journal, 605, 911
```

343	Cargill, P. J., Warren, H. P., & Bradshaw, S. J. 2015, Phil. Trans.	873
344	R. Soc. A, 373, 20140260	874
345	Cirtain, J. W., Golub, L., Winebarger, A. R., et al. 2013, Nature,	875
346	493, 501	876
347	Culhane, J. L., Harra, L. K., James, A. M., et al. 2007, Solar	877
348	Physics, 243, 19	878
349	De Pontieu, B., Title, A. M., Lemen, J. R., et al. 2014, Solar	879
350	Physics, 289, 2733	880
351	Drake, J. F., & Swisdak, M. 2014, Physics of Plasmas	881
352	(1994-present), 21, 072903	882
353	Freedman, D., & Diaconis, P. 1981, Zeitschrift für	883
354	Wahrscheinlichkeitstheorie und Verwandte Gebiete, 57, 453	884
355	Golub, L., Deluca, E., Austin, G., et al. 2007, Solar Physics, 243,	885
356	63	886
357	Hunter, J. D. 2007, Computing in Science & Engineering, 9, 90	887
358	Klimchuk, J. A. 2006, Solar Physics, 234, 41	888
359	Klimchuk, J. A., Patsourakos, S., & Cargill, P. J. 2008, The	889
360	Astrophysical Journal, 682, 1351	890
361	Kobayashi, K., Cirtain, J., Golub, L., et al. 2011, in Society of	891
362	Photo-Optical Instrumentation Engineers (SPIE) Conference	892
363	Series, Vol. 8147, 81471M	893
364	Kosugi, T., Matsuzaki, K., Sakao, T., et al. 2007, Solar Physics,	894
365	243, 3	895
366	Krucker, S., Christe, S., Glesener, L., et al. 2011, in Society of	896
367	Photo-Optical Instrumentation Engineers (SPIE) Conference	897
368	Series, Vol. 8147, 814705	898
369	Markovskii, S. A., & Hollweg, J. V. 2004, The Astrophysical	
370	Journal, 609, 1112	
371	Ono, Y., Yamada, M., Akao, T., Tajima, T., & Matsumoto, R.	
372	1996, Physical Review Letters, 76, 3328	

Parker, E. N. 1988, The Astrophysical Journal, 330, 474
Pérez, F., & Granger, B. E. 2007, Computing in Science & Engineering, 9, 21
Reale, F., & Orlando, S. 2008, The Astrophysical Journal, 684, 715 Reale, F., Testa, P., Klimchuk, J. A., & Parenti, S. 2009, The Astrophysical Journal, 698, 756
Reep, J. W., Bradshaw, S. J., & Klimchuk, J. A. 2013, The Astrophysical Journal, 764, 193
Schmelz, J. T., Saar, S. H., DeLuca, E. E., et al. 2009, The Astrophysical Journal Letters, 693, L131
Testa, P., De Pontieu, B., Martínez-Sykora, J., et al. 2013, The Astrophysical Journal Letters, 770, L1
Testa, P., De Pontieu, B., Allred, J., et al. 2014, Science, 346, 1255724 van der Walt, S., Colbert, S. C., & Varoquaux, G. 2011, Computing in Science & Engineering, 13, 22 Warren, H. P., Brooks, D. H., & Winebarger, A. R. 2011, The Astrophysical Journal, 734, 90 Warren, H. P., Winebarger, A. R., & Brooks, D. H. 2012, The Astrophysical Journal, 759, 141 Winebarger, A. R. 2014, AGU Fall Meeting Abstracts, 52, 03 Winebarger, A. R., Warren, H. P., Schmelz, J. T., et al. 2012, The Astrophysical Journal Letters, 746, L17 Yoo, J., Yamada, M., Ji, H., Jara-Almonte, J., & Myers, C. E. 2014, Physics of Plasmas (1994-present), 21, 055706