AP CSP Create Task

```
#include <string>
#include <stdio.h>
#include <string.h>
#include <vector>
#include <iostream>
#include <algorithm>
#include <fstream>
#include <stdlib.h>
#include <math.h>
#include <iomanip>
using namespace std;

ifstream fin("input.in");
ofstream fout("output.out");

struct expression
{
    bool type; // true for product, false for sum

    double power;

    double coefficient;

    vector <struct expression> inside;

    // returns if expression evaluates to 0
    bool is_zero() const
    {
        if(coefficient == 0)
        {
            return true;
        }
        return false;
    }

    // returns if function is a constant
    bool is_constant() const
    {
        if(coefficient != 0 and power == 0)
        {
            return true;
        }
        return false;
    }

    // used by the sort functions, it just needs to put identical things next to each other
    bool operator< (const struct expression other) const
    {
        if(inside.size() == other.inside.size()) // on this case, we want to separate expressions that are not equal from each other, but is_equal isn't defined...
        {
            return power < other.power;
        }

        return inside.size() < other.inside.size();
    }
};

// derivative functions
struct expression product_rule(struct expression in);
struct expression power_rule(struct expression in);
struct expression chain_rule(struct expression in);
struct expression derivative(struct expression in);
struct expression derivative_inside(struct expression in);

// input functions
int read_exp(void);
struct expression read_in_expression(void);

// comparison functions
bool is_equal(struct expression a, struct expression b);
bool by_power(struct expression a, struct expression b);

// output functions
void output_expression(struct expression in);
struct expression clean_up(struct expression in);

// because-I-needed-it function
int exp(int base, int power);
```

```
79
80  int main(void)
81  {
82      // =   <-- because some buttons on my keyboard don't work (for copying)
83
84      int n;
85      fin >> n; // takes in a number of expressions
86
87      for(int i = 0; i < n; i++)
88      {
89          struct expression test;
90
91          test = read_in_expression();
92
93          test = clean_up(test); // just to make sure final answer is in a simpler form, which starts by making sure the input is in simplest form
94
95          struct expression ans = derivative(test);
96
97          output_expression(ans);
98          fout << endl;
99      }
100 }
101
102 struct expression product_rule(struct expression in)
103 {
104     struct expression ans;
105
106     if(in.type != true)
107     {
108         cout << "product rule was given a sum" << endl;
109         exit(2);
110     }
111
112     ans.type = false; // sum of the products, it's a holder for the result
113     ans.coefficient = ans.power = 1; // just defaults
114
115     struct expression terms; // this is the stuff multiplied together
116     terms.inside = in.inside;
117     terms.coefficient = terms.power = 1;
118     terms.type = true;
119
120     for(int i = 0; i < terms.inside.size(); i++) // applying the generalized product rule
121     {
122         struct expression temp;
123         temp = terms.inside[i];
124
125         terms.inside[i] = derivative(temp);
126
127         ans.inside.push_back(terms);
128
129         terms.inside[i] = temp;
130     }
131
132     return ans;
133 }
134
135 struct expression power_rule(struct expression in)
136 {
137     struct expression ans;
138     if(in.power == 0) // it is a constant so just set everything to 0
139     {
140         ans.power = 0;
141         ans.coefficient = 0;
142         return ans;
143     }
144
145     ans.coefficient = in.coefficient * in.power; // apply the power rule
146     ans.power = in.power - 1;
147     ans.type = in.type;
148     ans.inside = in.inside;
149
150     return ans;
151 }
152
153 struct expression chain_rule(struct expression in)
154 {
155     struct expression ans;
156     ans.type = true; // product of f'(g(x)) and g'(x), so we need a new expression to contain them
157
158     ans.inside.push_back(derivative_inside(in));
159
160     in = power_rule(in); // only affects outer layer, f'(g(x))
161
162     ans.inside.push_back(in);
```

```
163
164     ans.coefficient = 1;
165     ans.power = 1;
166
167     return ans;
168 }
169
170 struct expression derivative(struct expression in)
171 {
172     if(in.inside.size() == 0)
173     {
174         return power_rule(in);
175     }
176     else
177     {
178         return chain_rule(in);
179     }
180 }
181
182 struct expression derivative_inside(struct expression in)
183 {
184     struct expression ans;
185     if(in.inside.size() == 0)
186     {
187         ans.power = 0;
188         ans.coefficient = 0;
189         ans.type = false;
190         return ans;
191     }
192     if(in.type == false) // added together
193     {
194         ans.type = false; // sum of the individual derivatives
195         ans.coefficient = 1;
196         ans.power = 1;
197         for(int i = 0; i < in.inside.size(); i++)
198         {
199             ans.inside.push_back(derivative(in.inside[i]));
200         }
201         return ans;
202     }
203     if(in.type == true) // multiplied together
204     {
205         // product rule...
206         return product_rule(in);
207     }
208 }
209
210 int read_exp(void) // just a simple helper function
211 {
212     int exponent;
213     fin >> exponent;
214     return exponent;
215 }
216
217 struct expression read_in_expression(void)
218 {
219     char in;
220     fin >> in;
221
222     int coefficient;
223
224     if((in >= '0' and in <= '9') or in == '-') // it's a number
225     {
226         fin.putback(in);
227         fin >> coefficient;
228     }
229     else
230     {
231         coefficient = 1;
232         fin.putback(in);
233     }
234
235     char x;
236     fin >> x;
237
238     int exponent;
239     struct expression ans;
240
241     if(x != 'x' and x != '(')
242     {
243         fin.putback(x);
244
245         exponent = 0; // it's a constant
246         ans.power = exponent;
```

```
247         ans.coefficient = coefficient;
248 
249         return ans;
250     }
251 
252     if(x == 'x')
253     {
254         // return the expression with an exponent, do nothing, the code after will do that
255     }
256     if(x == '(')
257     {
258         // recursively read more expressions
259 
260         struct expression temp;
261         temp = read_in_expression();
262 
263         ans.inside.push_back(temp);
264 
265         char next;
266 
267         do
268         {
269             fin >> next;
270 
271             if(next != '+' and next != '-' and next !=')' and next != '*')
272             {
273                 cout << "Expected *, +, - or )" << endl;
274                 exit(-1);
275             }
276 
277             if(next == '+')
278             {
279                 if(ans.type == true and ans.inside.size() > 1) // conflicts with previous operation
280                 {
281                     cout << "Expected * but got -" << endl;
282                 }
283                 temp = read_in_expression();
284 
285                 ans.type = false;
286 
287                 ans.inside.push_back(temp);
288             }
289             if(next == '-')
290             {
291                 if(ans.type == true and ans.inside.size() > 1) // conflicts with previous operation
292                 {
293                     cout << "Expected * but got -" << endl;
294                 }
295                 temp = read_in_expression();
296                 temp.coefficient *= -1;
297 
298                 ans.type = false;
299 
300                 ans.inside.push_back(temp);
301             }
302             if(next == '*')
303             {
304                 if(ans.type == false and ans.inside.size() > 1) // conflicts with previous operation
305                 {
306                     cout << "Expected +/- but got *" << endl;
307                 }
308 
309                 temp = read_in_expression();
310 
311                 ans.type = true;
312 
313                 ans.inside.push_back(temp);
314             }
315             if(next == ')')
316             {
317                 break;
318             }
319         }while(next != ')');
320     }
321 
322     char carat;
323     fin >> carat;
324 
325     if(carat != '^')
326     {
327         fin.putback(carat);
328 
329         exponent = 1;
330     }
```

```
    else
    {
        exponent = read_exp();
    }
    ans.power = exponent;
    ans.coefficient = coefficient;

    return ans;
}


bool is_equal(struct expression a, struct expression b) // only checks if stuff inside is equal
{
    if(a.inside.size() == 0 and b.inside.size() == 0)
    {
        return true;
    }
    if(a.inside.size() != b.inside.size())
    {
        return false;
    }

    sort(a.inside.begin(), a.inside.end(), by_power); // put stuff in order, puts equal stuff together
    sort(b.inside.begin(), b.inside.end(), by_power);

    for(int i = 0; i < a.inside.size(); i++)
    {
        if(a.inside[i].coefficient != b.inside[i].coefficient)
        {
            return false;
        }
        if(a.inside[i].power != b.inside[i].power)
        {
            return false;
        }
        if(is_equal(a.inside[i], b.inside[i]) == false)
        {
            return false;
        }
    }

    return true;
}

bool by_power(struct expression a, struct expression b)
{
    if(a.power == b.power)
    {
        return a.coefficient < b.coefficient;
    }
    return a.power > b.power;
}

void output_expression(struct expression in)
{
    in = clean_up(in);
    sort(in.inside.begin(), in.inside.end(), by_power);
    if(in.coefficient == 0) // should have been cleaned up already? but just in case
    {
        fout << "0";
        return;
    }
    if(in.power == 0)
    {
        fout << in.coefficient;
        return;
    }

    if(in.inside.size() == 0)
    {
        if(in.power == 0)
        {
            fout << in.coefficient;
        }
        else
        {
            if(in.coefficient != 1)
            {
                fout << in.coefficient;
            }
            fout << "x";
            if(in.power != 1)
            {
                fout << "^" << in.power;
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```
            }
        }
        return;
    }

    if(in.coefficient != 1)
    {
        fout << in.coefficient;
    }

    if(in.power == 0) // only care about coefficient
    {
        return;
    }

    if(in.inside.size() > 1)
        fout << "(";

    for(int i = 0; i < in.inside.size(); i++) // recursively print stuff inside
    {
        output_expression(in.inside[i]);
        if(i < in.inside.size() - 1)
        {
            if(in.type)
            {
                fout << " * ";
            }
            else
            {
                fout << " + ";
            }
        }
    }
    if(in.inside.size() > 1)
        fout << ")";

    if(in.power != 1)
    {
        fout << "^" << in.power;
    }
}

struct expression clean_up(struct expression in)
{
    for(int i = 0; i < in.inside.size(); i++)
    {
        clean_up(in.inside[i]); // clean up those first
    }

    if(in.inside.size() == 1) // bring everything up a level
    {
        in.coefficient *= exp(in.inside[0].coefficient, in.power);
        in.power *= in.inside[0].power;

        in.inside = in.inside[0].inside;

        return in;
    }

    if(in.type == true) // product
    {
        // clean constants
        for(int i = 0; i < in.inside.size(); i++)
        {
            if(in.inside[i].is_constant())
            {
                in.coefficient *= exp(in.inside[0].coefficient, in.power);

                in.inside.erase(in.inside.begin() + i);
                i--;
            }
        }

        // could also merge stuff that is the same base

        sort(in.inside.begin(), in.inside.end());

        for(int i = 1; i < in.inside.size(); i++)
        {
            if(is_equal(in.inside[i], in.inside[i - 1])) // they have the same base
            {
                in.inside[i].power += in.inside[i - 1].power;
                in.inside[i].coefficient *= in.inside[i - 1].coefficient;

```

```
                in.inside.erase(in.inside.begin() + i - 1);
                i--;
            }
        }

        return in;
    }

    else // sum
    {
        // clean zeroes
        for(int i = 0; i < in.inside.size(); i++)
        {
            if(in.inside[i].is_zero())
            {
                in.inside.erase(in.inside.begin() + i);
                i--;
            }
        }

        // could also merge stuff that is the same base and power

        sort(in.inside.begin(), in.inside.end());

        for(int i = 1; i < in.inside.size(); i++)
        {
            if(is_equal(in.inside[i], in.inside[i - 1]) and in.inside[i].power == in.inside[i - 1].power) // they have the same base and power
            {

                in.inside[i].coefficient += in.inside[i - 1].coefficient;

                in.inside.erase(in.inside.begin() + i - 1);
                i--;
            }
        }

        return in;
    }
}


int exp(int base, int power) // naive exponent function
{
    int ans = 1;
    for(int i = 0; i < power; i++)
    {
        ans *= base;
    }
    return ans;
}
```

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