

Homework 2

*Release Date: September 13, 2023**Due Date: September 20, 2023*

1 Written Questions

- **6.3** from the textbook.
- **6.12** from the textbook.
- **MGF/Chernoff.** Let X_1, \dots, X_N be i.i.d. random variables, with moment generating function $m_X(t) = \mathbb{E}[e^{tX}]$ and mean $\mu = \mathbb{E}[X]$. Consider the average of all N random variables: $Y = \frac{1}{N} \sum_{i=1}^N X_i$. Derive the form of $m_Y(t)$, the moment generating function for Y , and use the Chernoff method to derive a tail bound.
- **Bonus:** Use the Chernoff method to derive a tail bound for the χ^2 random variable. A χ^2 random variable is $X = Z^2$ where $Z \sim N(0, 1)$ is a standard normal.

Hint: consider the MGF when $t < 1/2$, and use the fact that $\frac{e^{-t}}{\sqrt{1-2t}} \leq e^{2t^2}$ for $|t| \leq 1/4$.