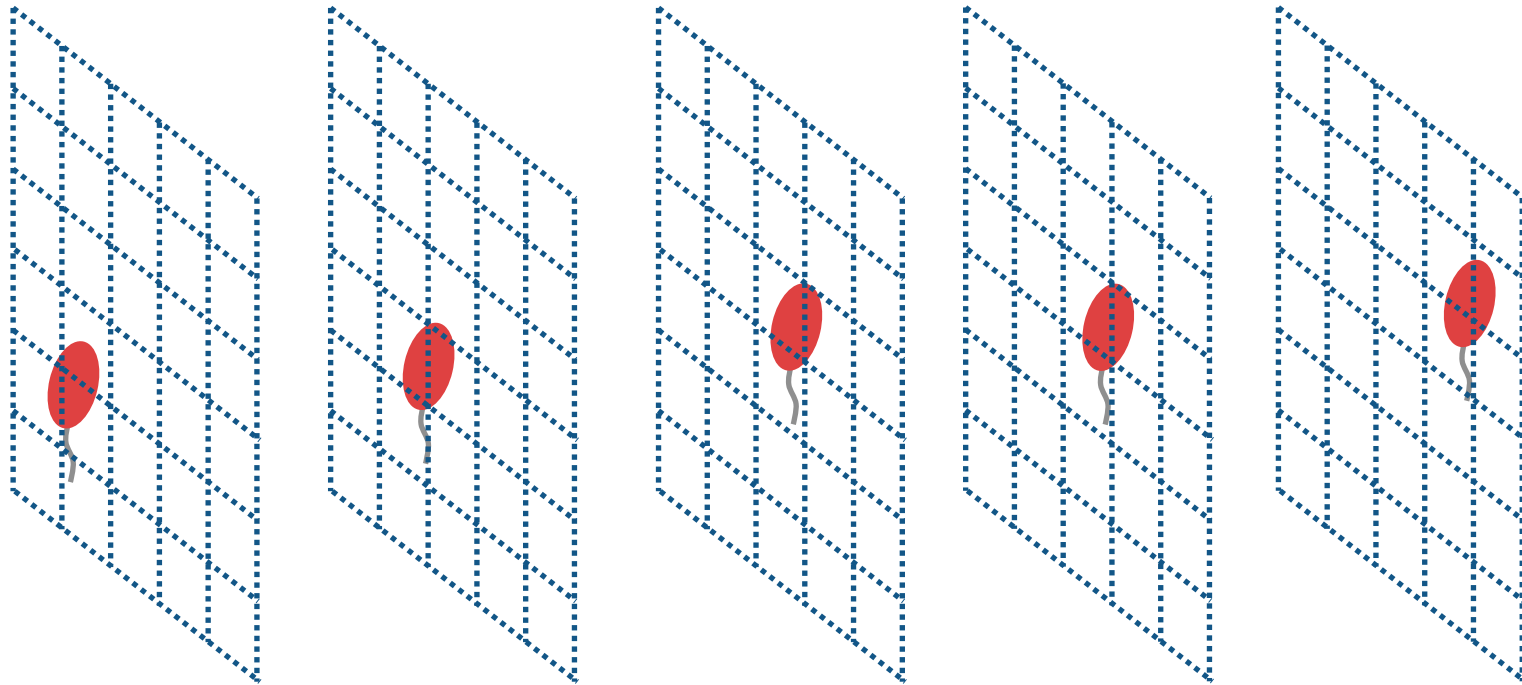


# Object Tracking



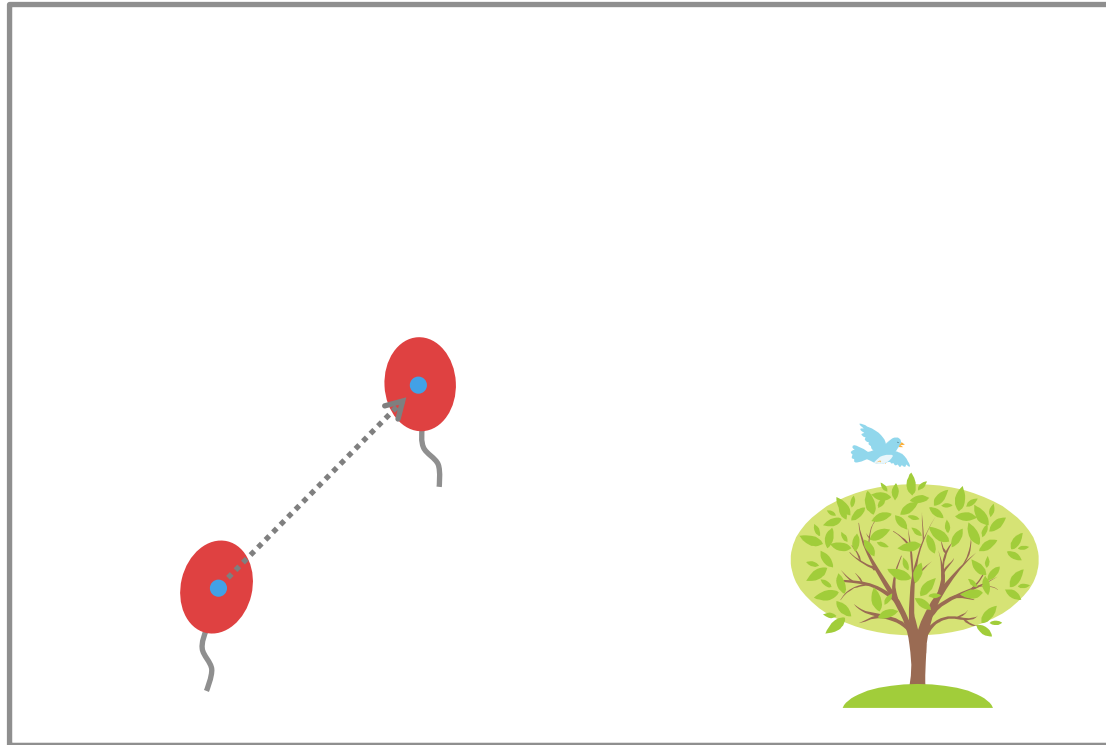
We are going to track a red object in a movie

# Searching red object in each frame might be an idea ... but



There might be more efficient way to do this work

# Object Tracking

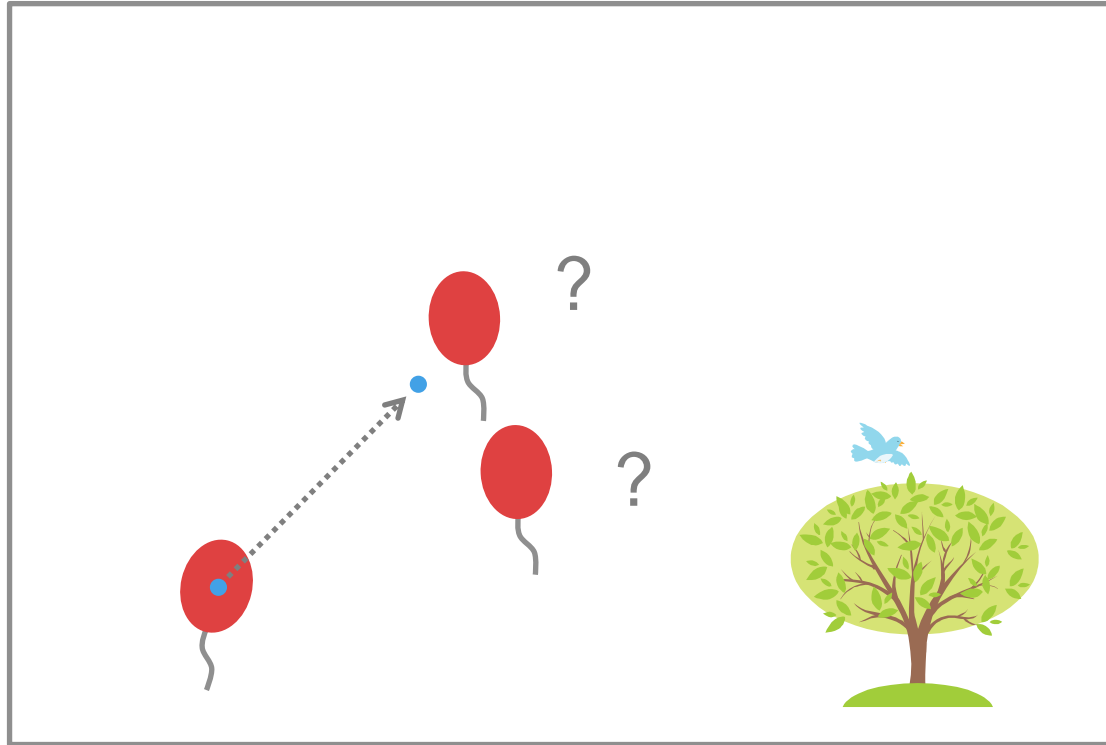


If you know the location and speed of this object ...



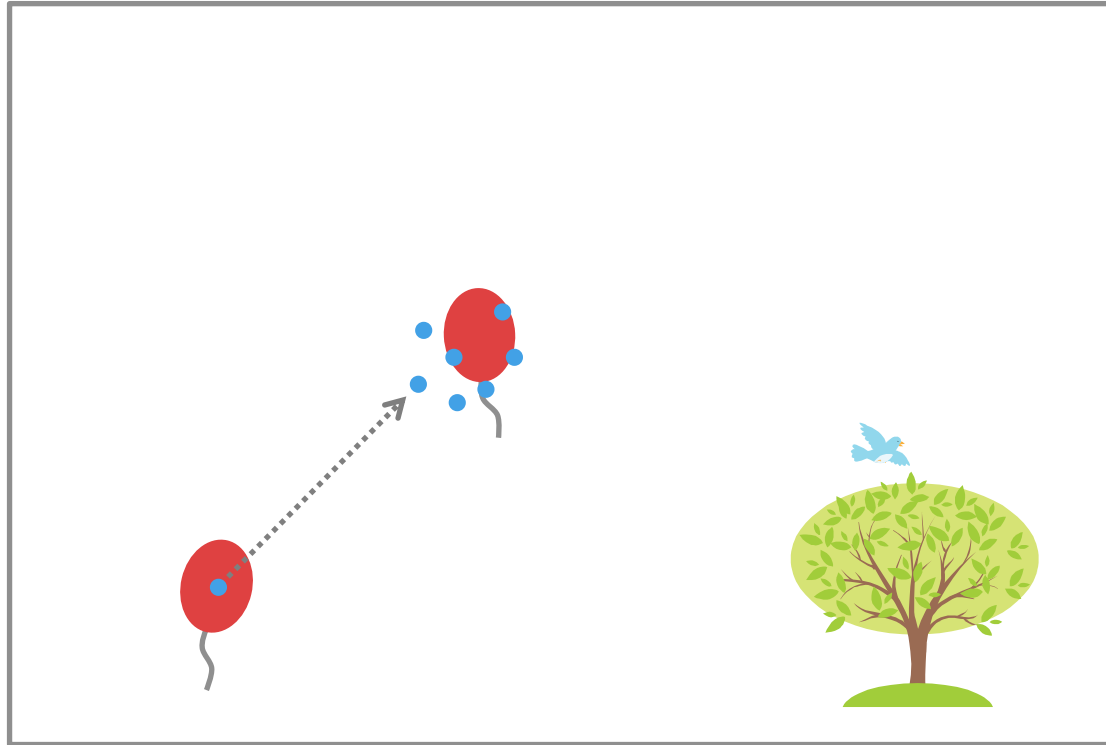
You can predict the future location assuming uniform linear motion for this object

# Object Tracking



But your prediction might fail sometimes ...

# Object Tracking

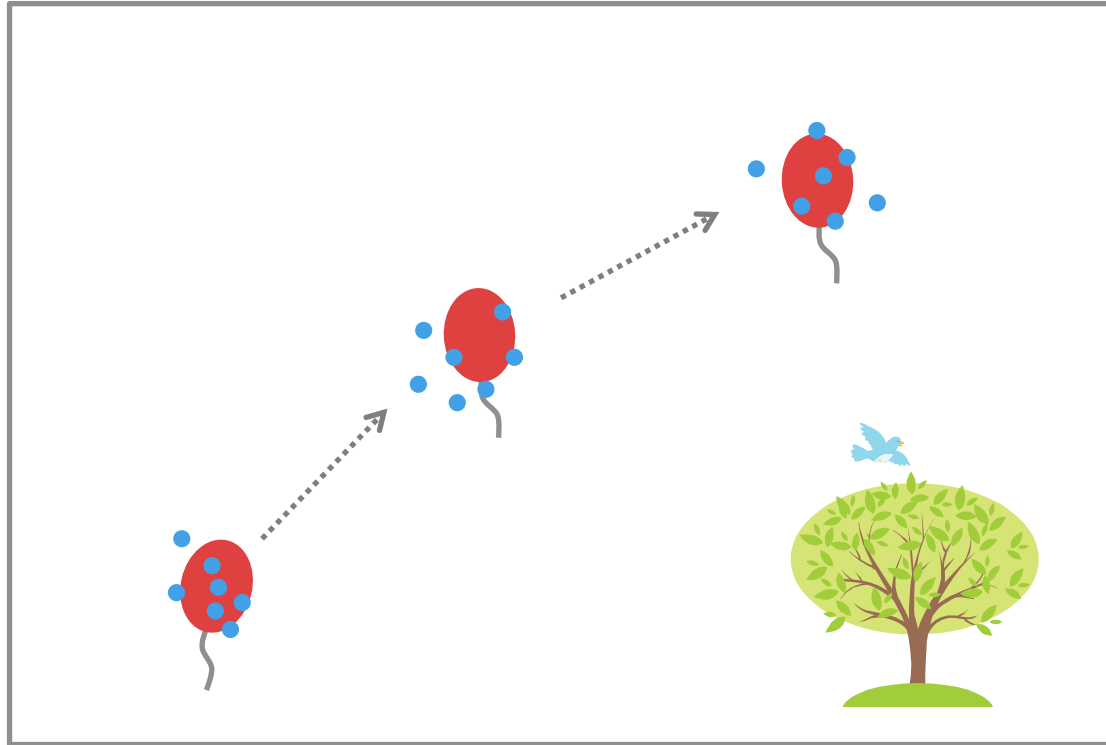


If you have many slightly different predictions ...



One of them might be near the right answer

# Object Tracking



Let's track this object by many particles which have slightly different location or speed

# Algorithm (Particle filter / Condensation)

## 1. Prediction

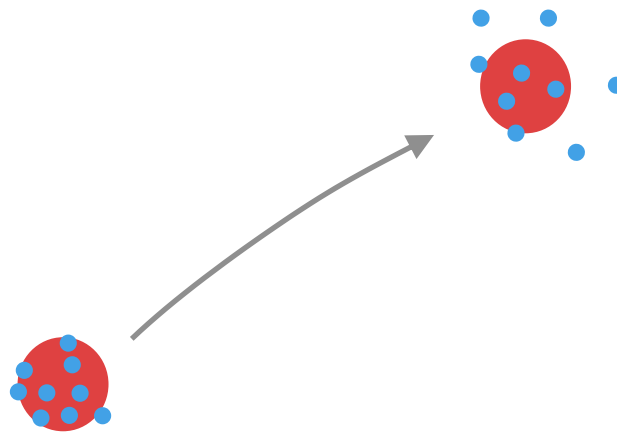
Time evolution of particles according to system model

## 2. Filtering

Reselection particles according to their likelihood



# Prediction (move particles)

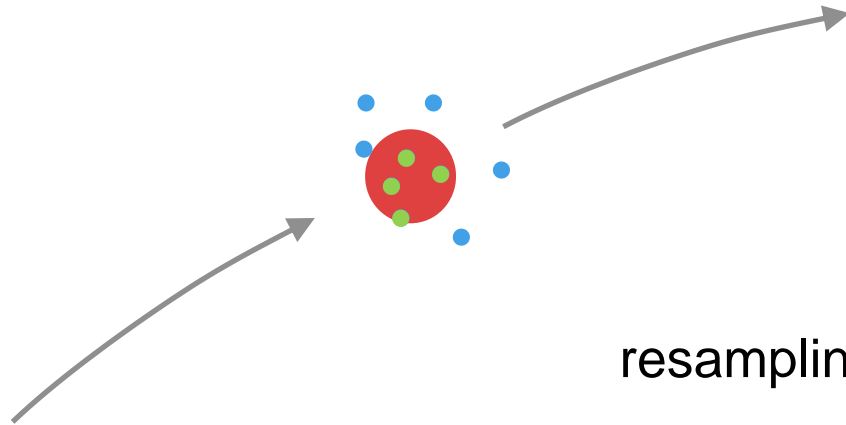


$$\begin{array}{c}
 \text{Location / Speed} \quad \text{Noise} \\
 \downarrow \qquad \qquad \downarrow \\
 \begin{pmatrix} x_n \\ y_n \\ \dot{x}_n \\ \dot{y}_n \end{pmatrix} = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_{n-1} \\ y_{n-1} \\ \dot{x}_{n-1} \\ \dot{y}_{n-1} \end{pmatrix} + \begin{pmatrix} v_x \\ v_y \\ v_{\dot{x}} \\ v_{\dot{y}} \end{pmatrix}
 \end{array}$$



# Filtering (resample particles)

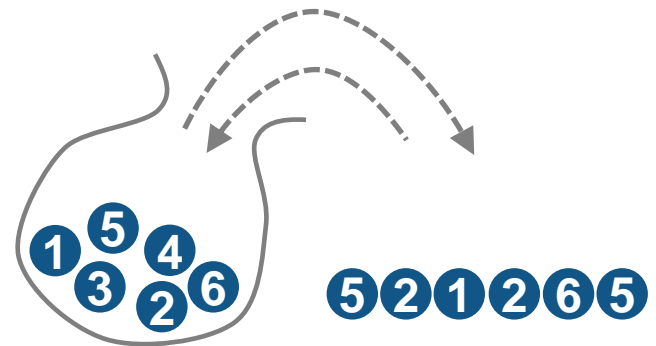
Multiple pick up of same particle is permitted



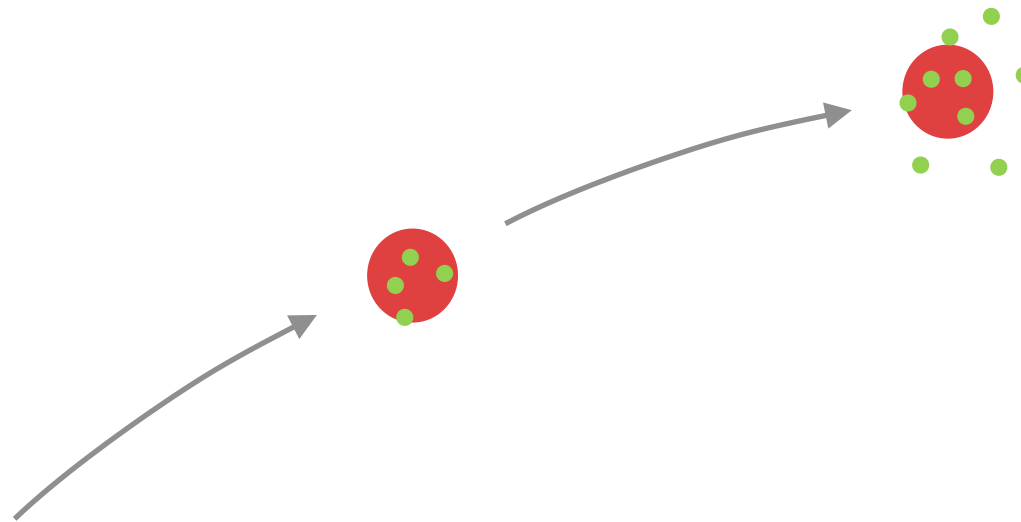
resampling with replacement

Picking up same number of particles

Particles which has large “likelihood” are more likely to be picked up



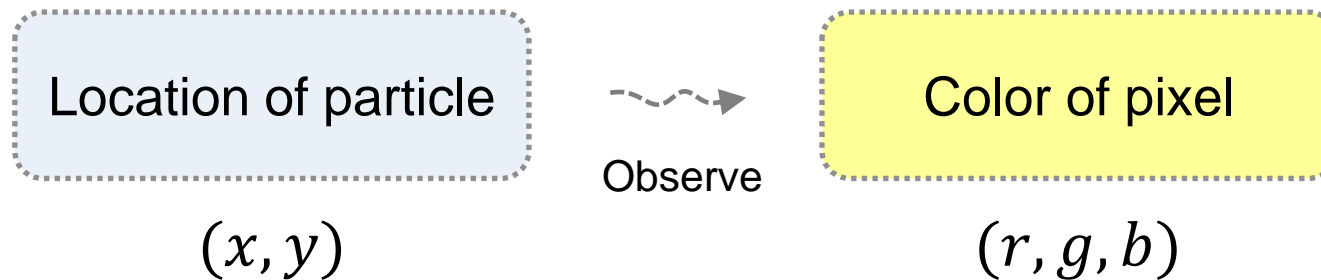
# Prediction (move particles)



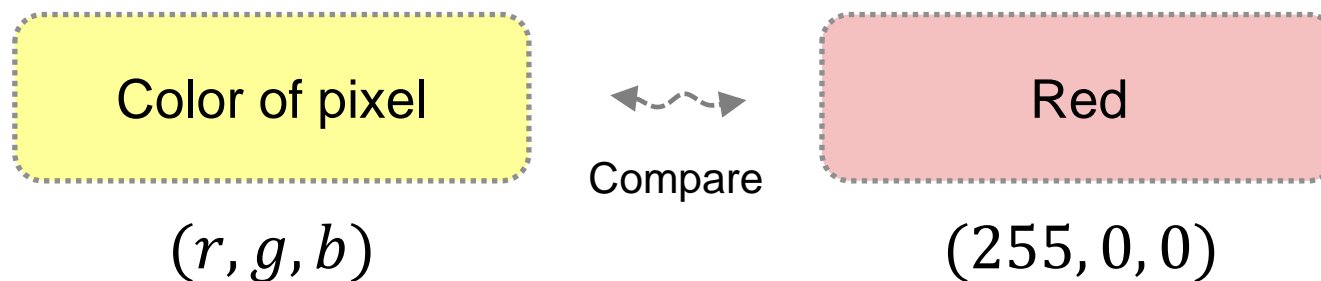
$$\begin{array}{c}
 \text{Location / Speed} \quad \text{Noise} \\
 \downarrow \qquad \qquad \downarrow \\
 \begin{pmatrix} x_{n+1} \\ y_{n+1} \\ \dot{x}_{n+1} \\ \dot{y}_{n+1} \end{pmatrix} = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} x_n \\ y_n \\ \dot{x}_n \\ \dot{y}_n \end{pmatrix} + \begin{pmatrix} v_x \\ v_y \\ v_{\dot{x}} \\ v_{\dot{y}} \end{pmatrix}
 \end{array}$$

# Calculation of “likelihood”

1) Get the color of pixel on which particle exists (observation)



2) Compare the RGB of pixel with red (255, 0, 0)



# Calculation of likelihood

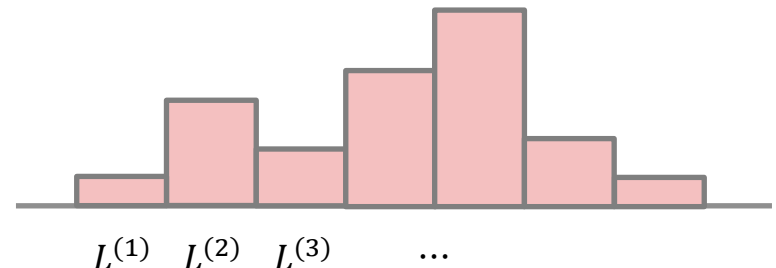
The closer the color we observe becomes red (255, 0, 0), the bigger the likelihood of particle becomes.

$$L = \frac{1}{\sqrt{2\pi\sigma}} \cdot \exp\left(-\frac{d^2}{2\sigma^2}\right) \quad \leftarrow \text{Likelihood}$$

$$d = \sqrt{(r - 255)^2 + g^2 + b^2}$$

Calculate likelihood for each particle

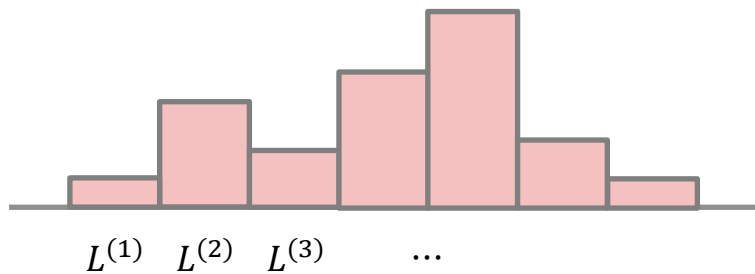
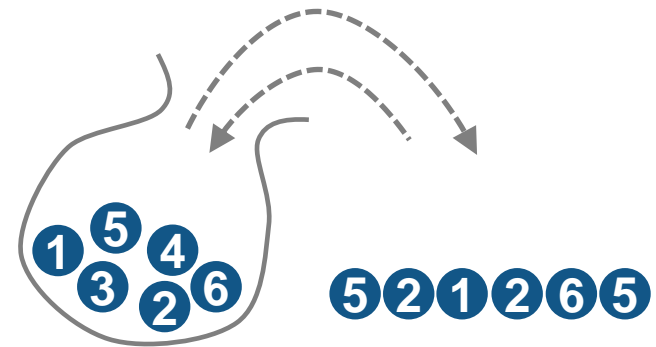
$$L^{(k)} \quad (k = 1, \dots, N)$$



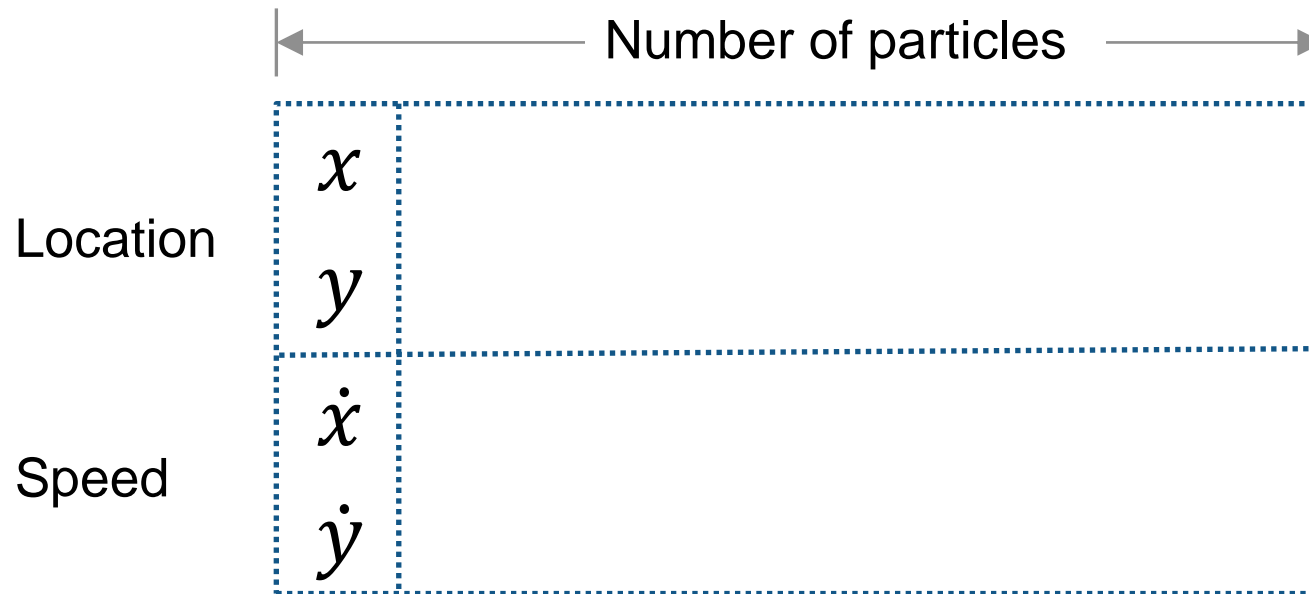
# Filtering

Execute “resampling with replacement” according to likelihood ratio

$$\frac{L^{(k)}}{\sum_{k=1}^N L^{(k)}} \quad (k = 1, \dots, N)$$

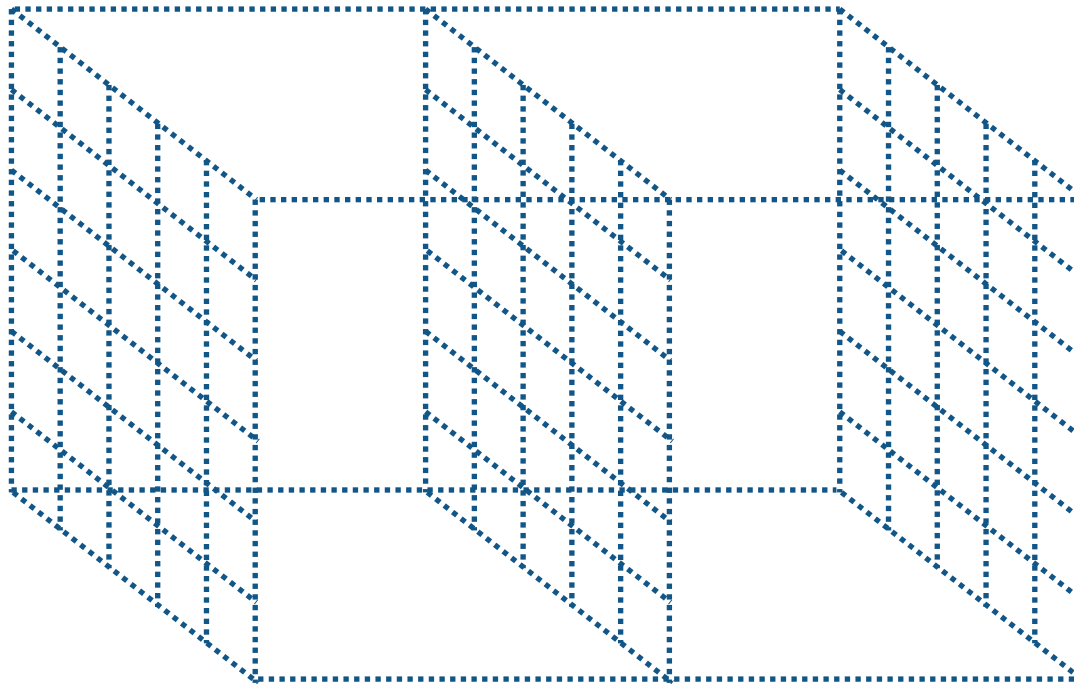


# Explanation of variable (particles)



When you multiple matrix  $F = \begin{pmatrix} 1 & 0 & 1 & 0 \\ 0 & 1 & 0 & 1 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$  from left, particles move

# Explanation of variable (color photo)

**R****G****B**

*480 X 640 X 3*