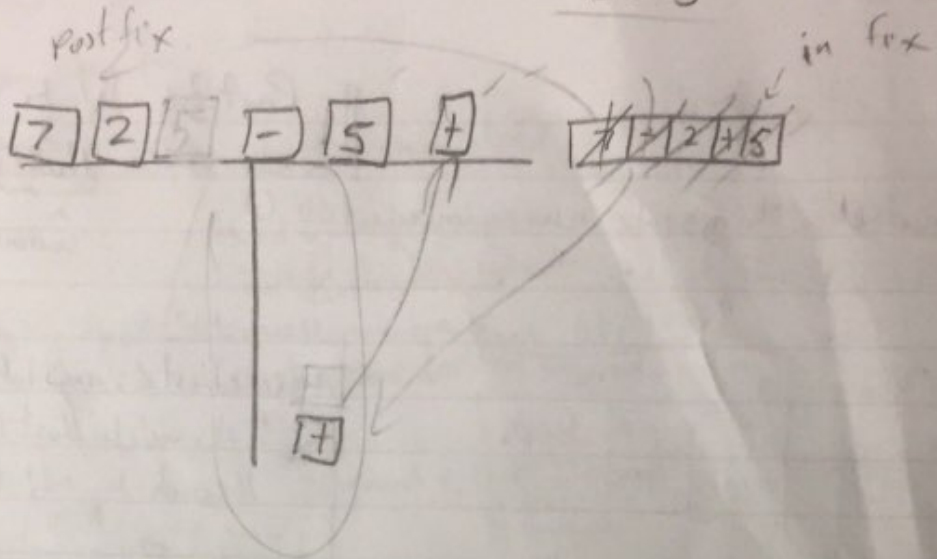
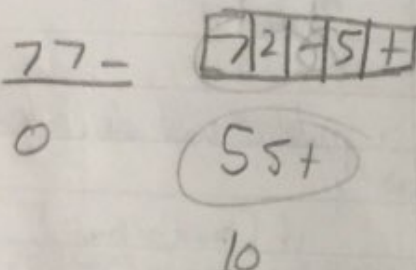


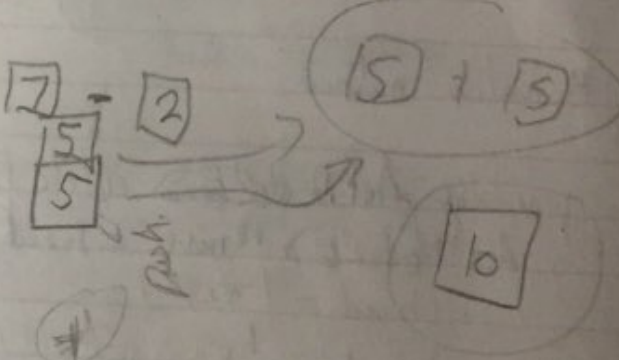
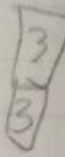
$$7-2+5$$



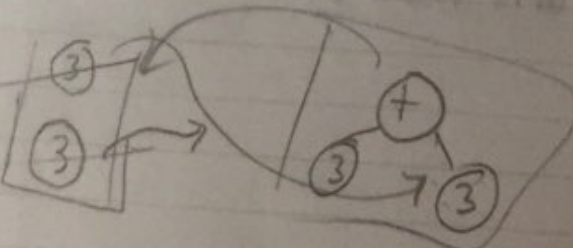
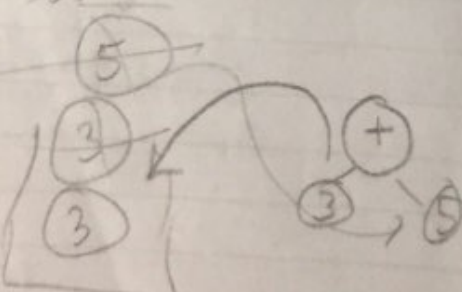
$$7-2+5$$



$$3-3+3+6-3+9$$



$$3-3+3+6-3+9$$



Youtube channel: myschool code
 Playlist: Data Structures
 Title: infix to Postfix

infix: $A + (B * C)$

Precedence of mul is higher so

$$\downarrow$$

$$A + (BC *)$$

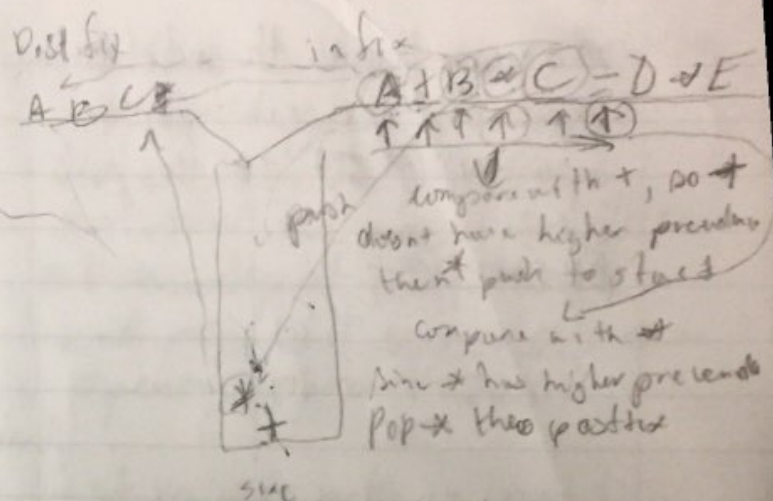
$$\downarrow$$

$$A(BC*) +$$

 Postfix: $ABC * +$

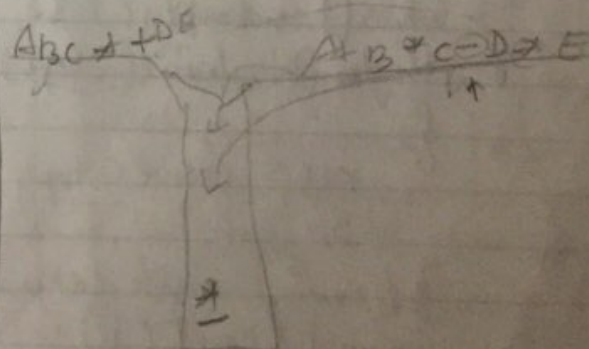
- In infix to postfix conversion, the position of operands and operators may change but the order in which operand occur from left to right will not change.
- ✓ the order of operator may change.

* In postfix form we will always have the operators in the same order in which they should be executed



- Any operator in the stack having higher precedence than the one we looking at can be popped and placed @ the postfix expression

- if an element in the stack has something on top of it then that something will always be of higher precedence when popping @ -



- There are 2 ways we can find the end of the right operand for an operator
 - a) if we get an operator of lesser precedence
 - b) if we reach the end of the expression (next)

• once we reach the end of the expression we can pop the operators (\rightarrow) to the post fix
 Ex
 ABC~~+~~DE~~-~~

Pseudo code *opens Queue*

InfixToPostfix(exp)

String result (empty) ← Queue postfix.
 create stack of String S.

for i = 0 to length(exp) - 1

if exp[i] is operand → char, token

res += exp[i], postfix.enqueue()

else if exp[i] is operator

& *Stack not empty*

while (!S.empty() && has change
 has Higher Precedence (s.top(), exp[i]))

{
 res += s.top(); ← postfix.enqueue(s.top())
 S.pop() ← remove the last element.

// end of while loop

So push (exp[i]);

// end of for loop, @ the end of it you may
 have operators in the stack

while (S.empty())

{ res += s.top(); ← postfix.enqueue(s.top());
 S.pop()

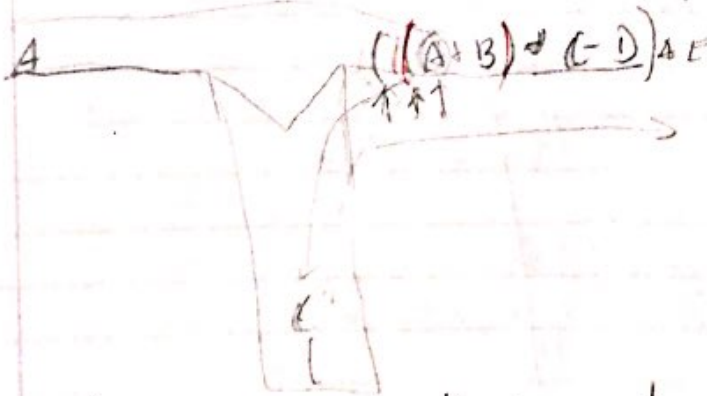
return result; // end of infix to postfix ← this does not take care of parentheses

Now with parentheses

$$((A+B) * (C-D)) \div E$$

its execution will be influenced by \div or $*$

- with parentheses any part of the expression within parentheses should be treated as independent, complete expression in itself, and no element outside the parentheses will influence its execution.
- If parentheses are nested, inner parentheses is sorted out or resolved first, and then only outer parentheses can be resolved.



- if opening parenthesis, push onto the stack.

similar when we looking @ operator we were looking at top of stack and popping as long as we were getting operator of higher precedence

earlier without parentheses we could go on popping and empty the stack. But now we need to look at the top of the stack and pop till we get an opening parenthesis.

• If we are getting an opening parenthesis, then it's the boundary of the last opened parentheses, and the operator does not influence any instance of it. That

Rules

- If you're seeing an operator look @ the top of stack
 - in order stack is higher precedence you can pop, look @ the next top
 - if higher precedence pop
 - stop when you see an open parenthesis

AB+

$((A+B) \times C - D) \div E$

(↑)

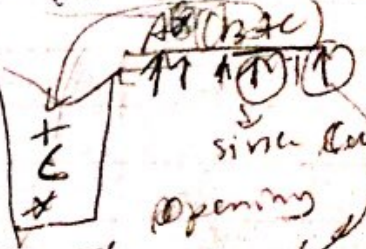
close parentheses similarly when we were reaching the end of expression, we were popping all the operators out and placing them

on postfix, so now we need to pop the operators out till we get an opening parenthesis, then pop the opening parenthesis without enqueueing it

- Rule for closing parentheses
 - pop operators till you find an opening parenthesis then

EX $A \div (B+C)$

ABC



parentheses Closing parenthesis pop till engine + delete open parenthesis.

ABC+÷



Pop removing stack

- only part of the code that need to be change is the

AB+CD÷

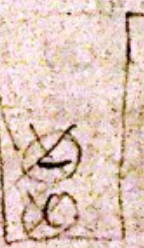
$((A+B) \times C - D) \div E$



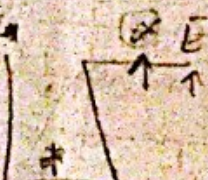
compares id pop since + higher precedence

AB+CD÷

$((A+B) \times C - D) \div E$



$A \div (B+C)$



Complete pseudo code

Infix to Postfix (exp)

string result \leftarrow ""
create a stack of string S

for $i = 0$ to $\text{length}(\text{exp}) - 1$ while $(\text{infix} \neq \text{empty}) /$

if $\text{exp}[i]$ is operand

result \leftarrow result + $\text{exp}[i]$ \leftarrow postfix. enqueue
else if $\text{exp}[i]$ is operator

while (!S.empty() && !isOpeningParentheses(S.top()))

if higher precedence (S.top(), $\text{exp}[i]$)

{ result \leftarrow result + S.top()

S.pop()

} end of while loop

push ($\text{exp}[i]$)

if $\text{exp}[i] == '('$

{ push ($\text{exp}[i]$)

else if $\text{exp}[i] == ')'$

{ while (!S.empty() && !isOpeningParentheses(S.top()))

{ result \leftarrow result + S.top()

S.pop()

} end of while loop

S.pop()

} end of if block

} end of for loop

while (!S.empty())

{ result \leftarrow result + S.top()

S.pop()

} end of while loop

return result

complete pseudo code

infix to postfix (exp)

string result ans = <string> postfix
create a stack of string S.

for $i = 0$ to $\text{length.exp} - 1$ while $(\text{infix.empty}()) /$

if $\text{exp}[i]$ is operand // need to be able to take a token and try to parse it and integer in a try catch b/c catch will return false
result = result + $\text{exp}[i]$ \leftarrow postfix.ans,
else if $\text{exp}[i]$ is operator

while ($! S.empty()$ && $! \text{isOpeningParentheses}(S.top())$
&& $\text{hasHigherPrecedence}(S.top(), \text{exp}[i])$)
{ result = result + $S.top()$ \rightarrow postfix.enqueue($S.pop()$)
S.pop()

end of while loop \leftarrow pop all higher precedence
then push ($\text{exp}[i]$) \leftarrow then push to top of given parentheses
// end of else if

new \rightarrow else if $\text{exp}[i] == '('$ // else if S opening parentheses ($\text{exp}[i]$) = more general
S.push($\text{exp}[i]$)

else if $\text{exp}[i] == ')'$ // else if S closing parentheses ($\text{exp}[i]$)
while ($! S.empty()$ && $! \text{isOpeningParentheses}(S.top())$)
{ result = result + $S.top()$ \rightarrow postfix.enqueue($S.pop()$)
S.pop()

S.pop() \leftarrow delete the open parentheses in stack.
// end of else state

// end of for loop

while ($! S.empty()$)
{ result = result + $S.top()$
S.pop()

return result.

• Title: Check for balanced parentheses using stack.

• Youtube channel: my school school!
Published date: Oct 28, 2013

Expression Balanced?

$(A+B)$ yes
 $\{(A+B) + (C+D)\}$ yes

$\{(A+B) + (C)\}$ No
 $[2+3] + (A)$ No

$\{A+B\}$ No

$\{ \}$ No
 $[()]$ yes
 $[(])$ No

So compare the closing & opening symbols using stack

- Every opening parenthesis must find a closing counterpart to its right
- every closing parenthesis must find an opening counterpart to its left.

- A parenthesis can close only when all the parentheses open after it are closed
last opened first closed

• As we scan the expression from left to right, any closure should be for the previous enclosed parenthesis

• any closure should be for the last unclosed

$[() ()]$

• scan the expression from left to right

• keep track of all the unclosed parentheses as we scan at any stage

— when you are across an opening symbol add it to a list. (push to stack)
— if closing symbol should be the closure of the last element in the list. if inconsistent like we

last opening symbol of the list is not of the same type as the closing symbol. or, if there is no last opening symbol at all (list is empty) stop the whole process

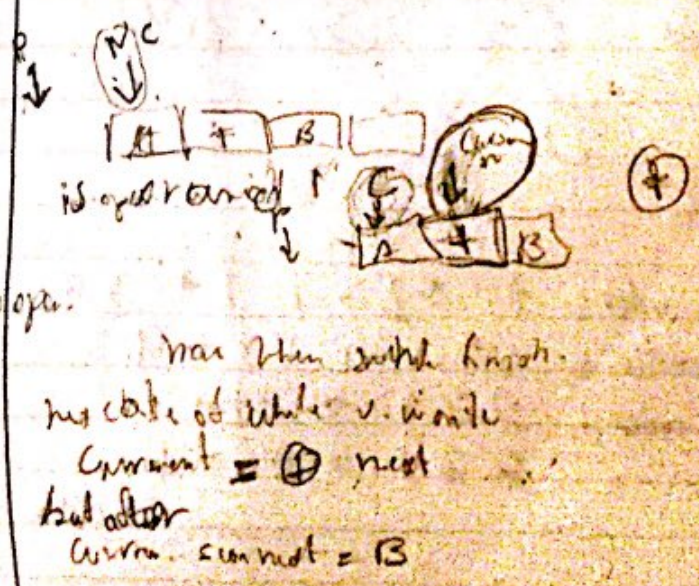
• else remove the last opening symbol in the list since matched & continue this whole process (pop)

[() ()]
 ↑ ↑ ↑
 list: empty
 list: [(] it's closing
 do look @ the last
 element in the list
 of same type & matching
 remove(it) & move up to
 the next.
 now list become
 list: [() ()]
 list: [(] remove
 list: [()] remove
 list: empty

• If every thing is a/b balance
 we will always end up with an
 empty list.

(A not valid.
 (4 - not valid ✓ taken
 care by is open.
 ((← valid
 if previous is not
)C would be invalid
) if 5 not valid
 - 1 open & 1 closed first

Pseudo Code
 check balanced parentheses (string exp)
 {
 n = length(exp)
 create stack S
 for i = 0 to n-1
 {
 if exp[i] is '(', or '{', or '['
 push(exp[i])
 else if exp[i] is ')', or '}', or ']'
 {
 if (S.isEmpty) ||
 (S.top does not pair with exp[i])
 {
 return false ← not balanced
 }
 }
 }
 }
 else // not a diff
 pop()
 }
 // end of for
 return S.isEmpty ? true : false

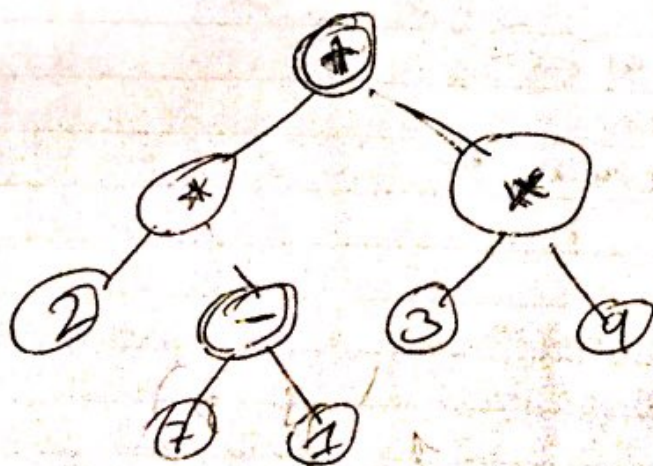


Now when switch from
 the state of while v. while
 current = ④ next
 but after
 current sum next = B

order of operation

- 1) Parentheses $() \{ \} \Sigma \gamma$ \rightarrow Right associative
 - 2) exponents (right to left) 2^3^2
 - 3) multiply & division (left to right) \rightarrow
 - 4) Addition & sub (left to right)
- $\Sigma \times \div$ $4-2+1$

$$((2 \times (7-1)) + (3 \times 9))$$



Traversals:

Preorder: $+ * 2 - 7 1 * 3 9$
 Inorder: $2 * 7 - 1 + 3 * 9$
 Post order: $2 7 1 - * 3 9 * +$
 Postfix: $2 7 1 - * 3 9 * +$