

VAMPIRE

Software for atomistic simulation of
magnetic materials

Sarah Jenkins

Workshop Programme

Monday	Spin Models and intro to VAMPIRE
Tuesday	Constrained Monte Carlo and dipole fields
Wednesday	Complex crystal structures: AFM's, skyrmions and magnetite
Thursday	Introduction to ARCHER and parallel VAMPIRE.
Friday	Project day.

VAMPIRE features covered

Methods	Spin dynamics, Monte Carlo, Constrained and Hybrid Constrained Monte Carlo, Dipole fields
Calculations	Curie/Néel Temperature, Hysteresis loops, Temperature dependent anisotropy, Domain Wall width, ground state spin structures
Systems	Multilayers, multiple sublattices, nanoparticles, Skyrmions, antiferromagnets, complex crystal structures
Technical	Parallel and GPU acceleration, visualization and data analysis

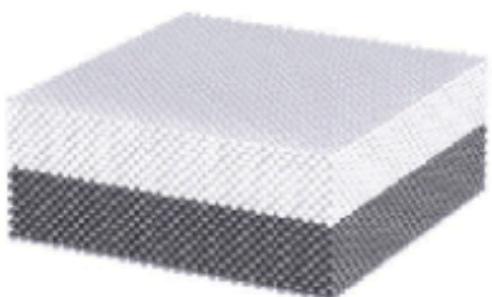
Day 1 Overview



Brief review of atomistic spin models

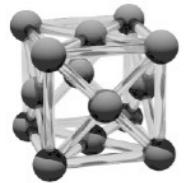


VAMPIRE code overview



Practicals

Past, present and future of atomistic spin models



Introduction



Atomistic spin models

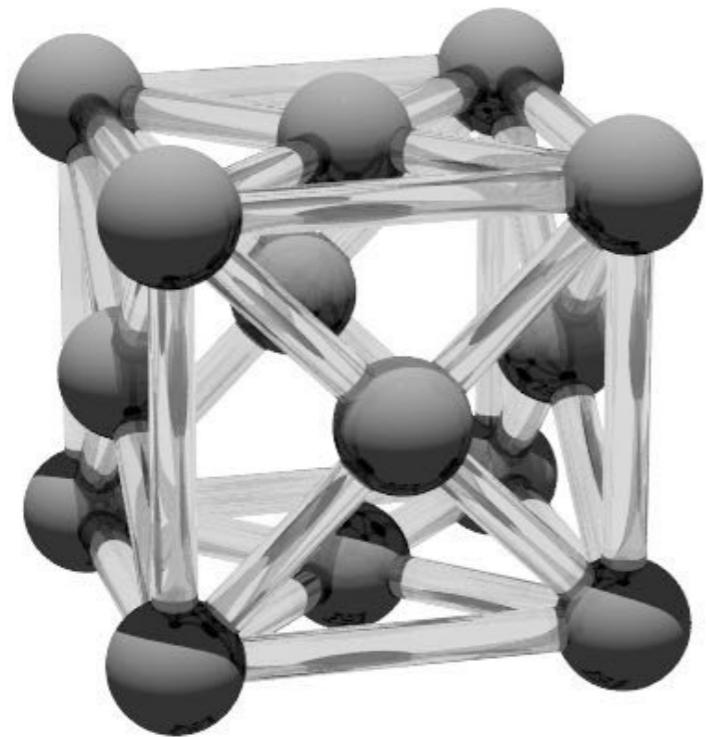


VAMPIRE and what it can do



Future plans and challenges

Bulk magnetic properties intrinsically tied to electronic structure

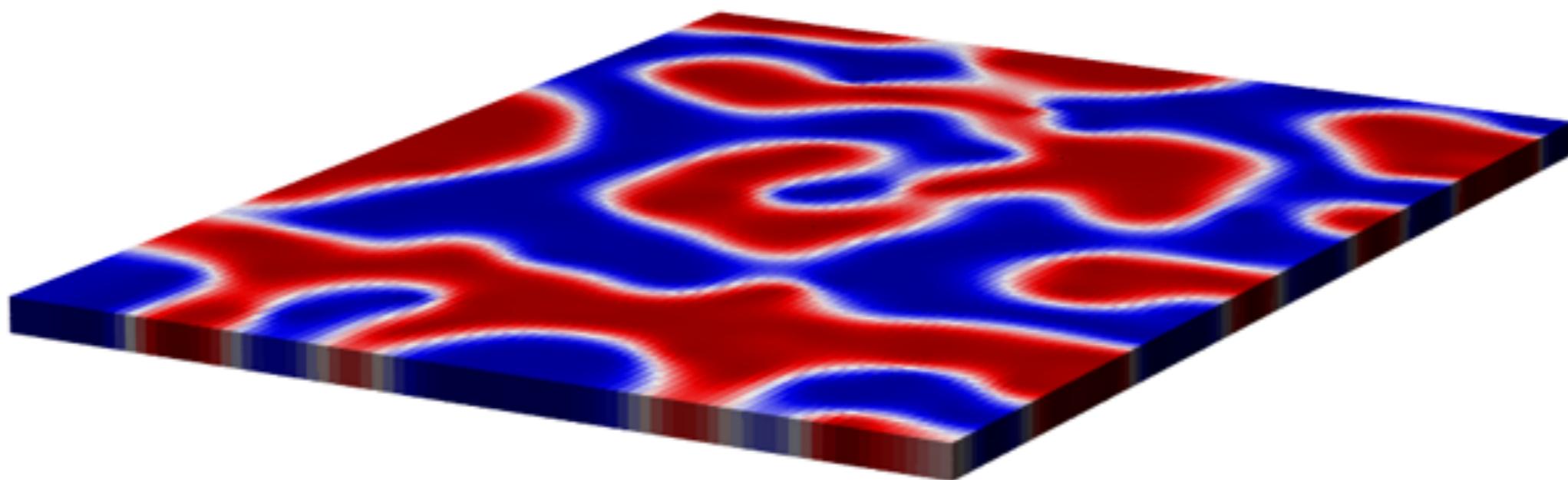


Magnetic moments

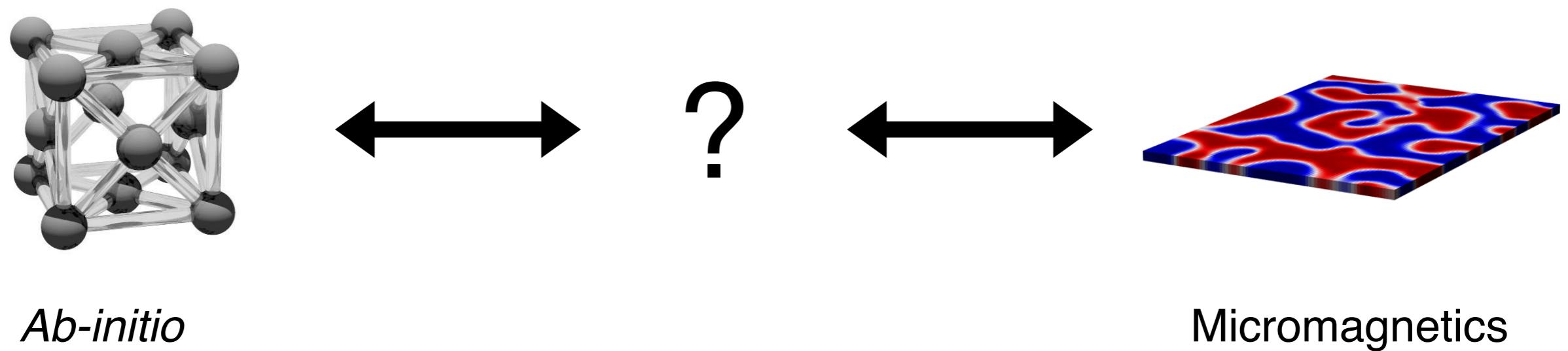
Exchange interactions

Anisotropy

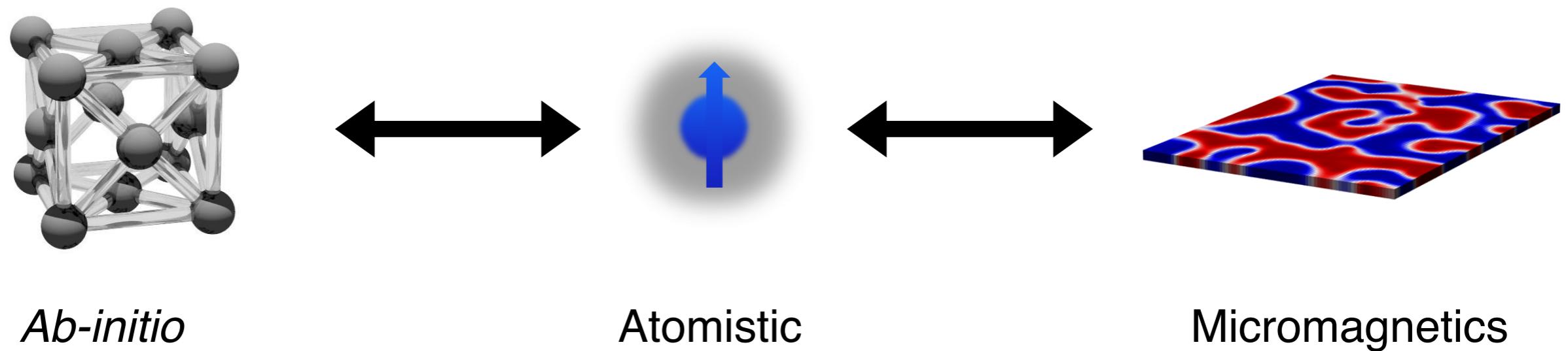
Numerical micromagnetics enables us to really understand how magnetic materials behave



But... no direct link between electronic
structure and micromagnetics



Atomistic modes provide a
natural link between these length scales



Often we need to consider problems where continuum micromagnetics is a poor approximation

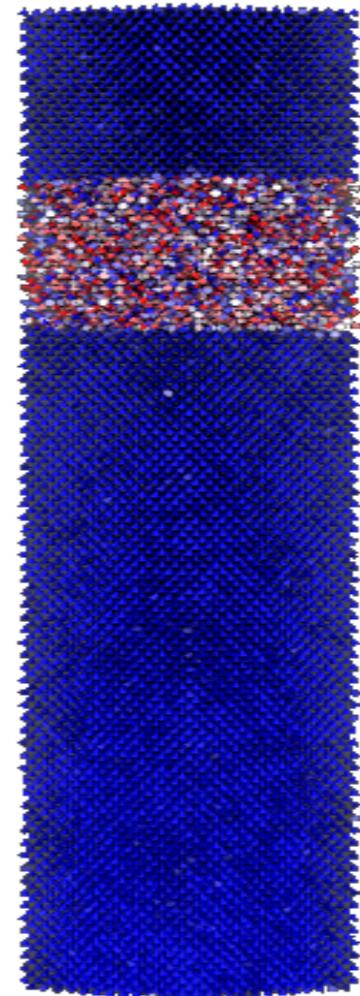
Multi-sublattice ferro, ferri and antiferromagnets

Realistic particles with surface effects

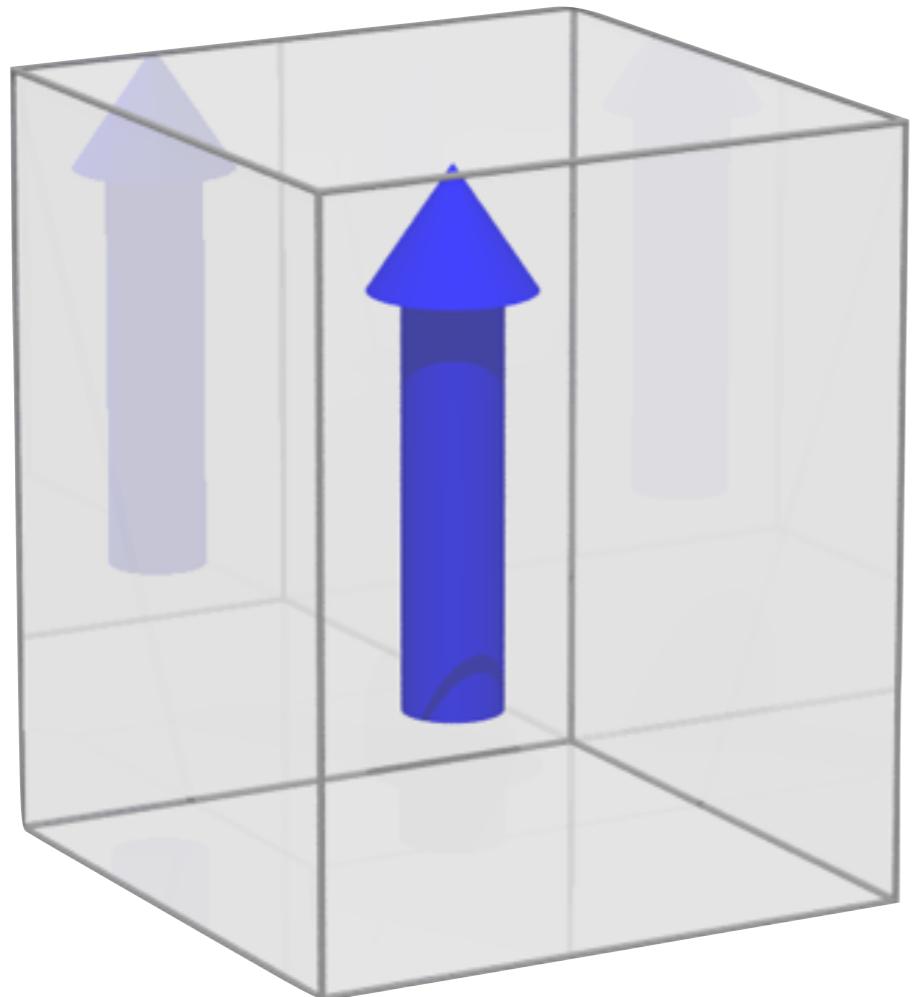
Elevated temperatures near T_c

Magnetic interfaces

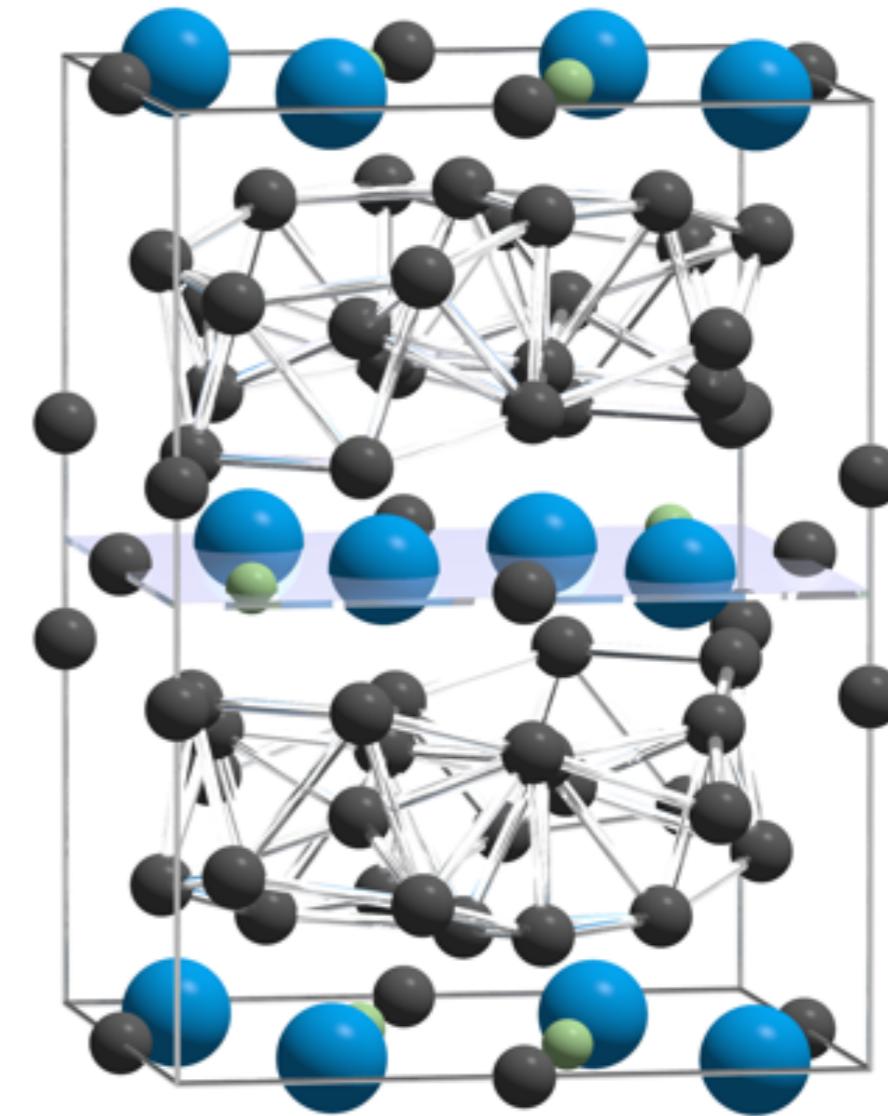
Crystal defects and disorder



Example: Nd₂Fe₁₄B permanent magnets



Micromagnetics



Atomistic

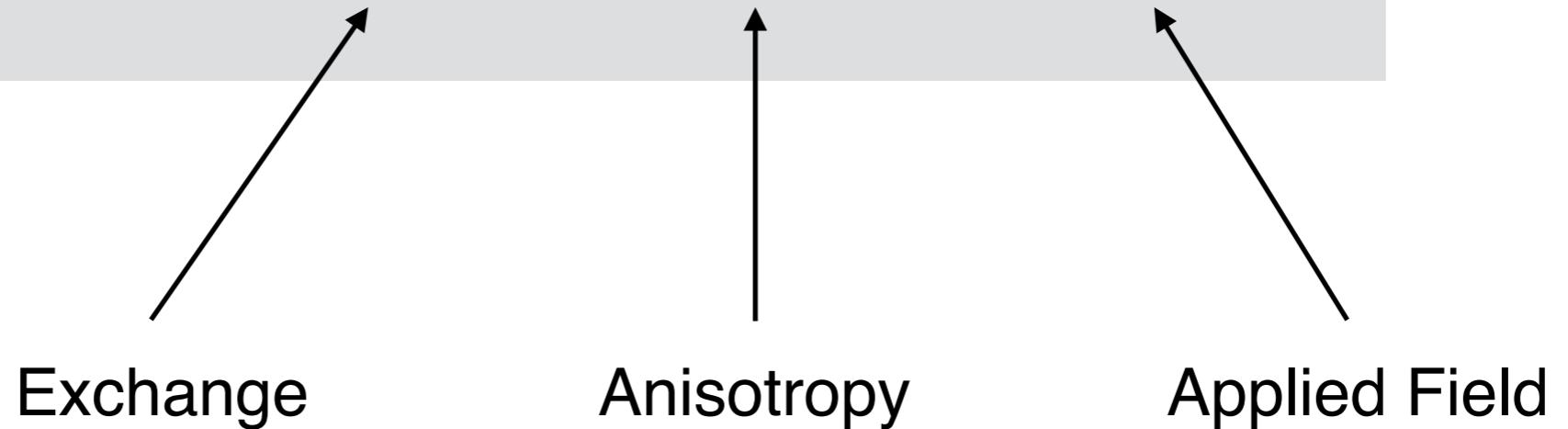
Atomistic spin models

The atomistic model treats each atom as possessing a localized magnetic ‘spin’

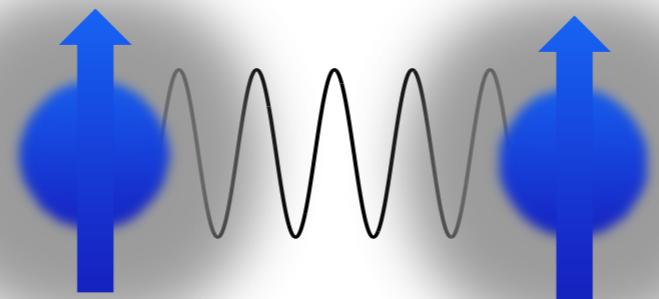


The ‘spin’ Hamiltonian

$$\mathcal{H} = \mathcal{H}_{\text{exc}} + \mathcal{H}_{\text{ani}} + \mathcal{H}_{\text{app}}$$



Foundation of the atomistic model is Heisenberg exchange



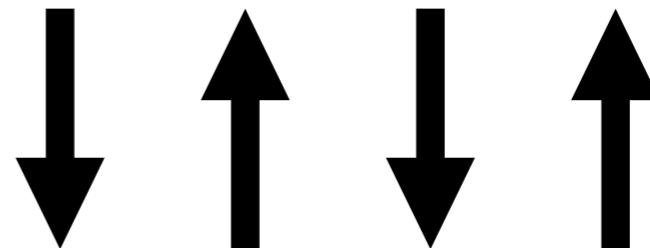
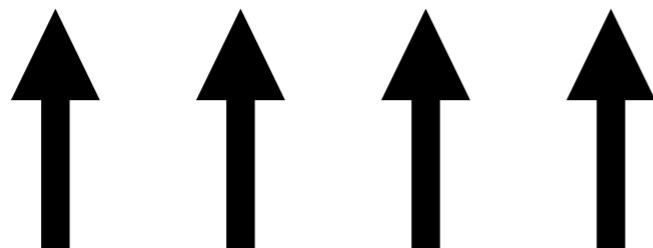
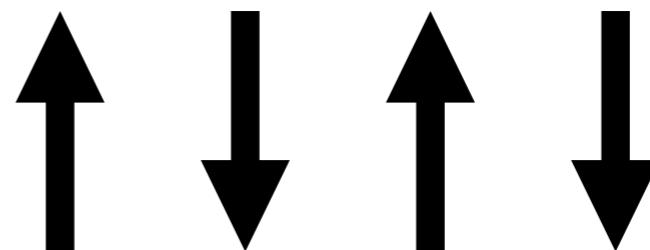
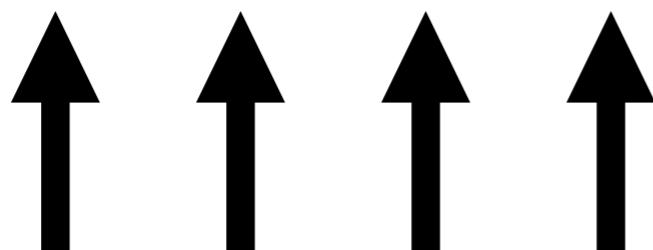
\mathbf{S}_i

\mathbf{S}_j

$$\mathcal{H}_{\text{exc}} = - \sum_{i \neq j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

Natural discrete limit of magnetization

Exchange interaction determines type of magnetic ordering



$$J_{ij} > 0$$

Ferromagnet

$$J_{ij} < 0$$

Anti-ferromagnet

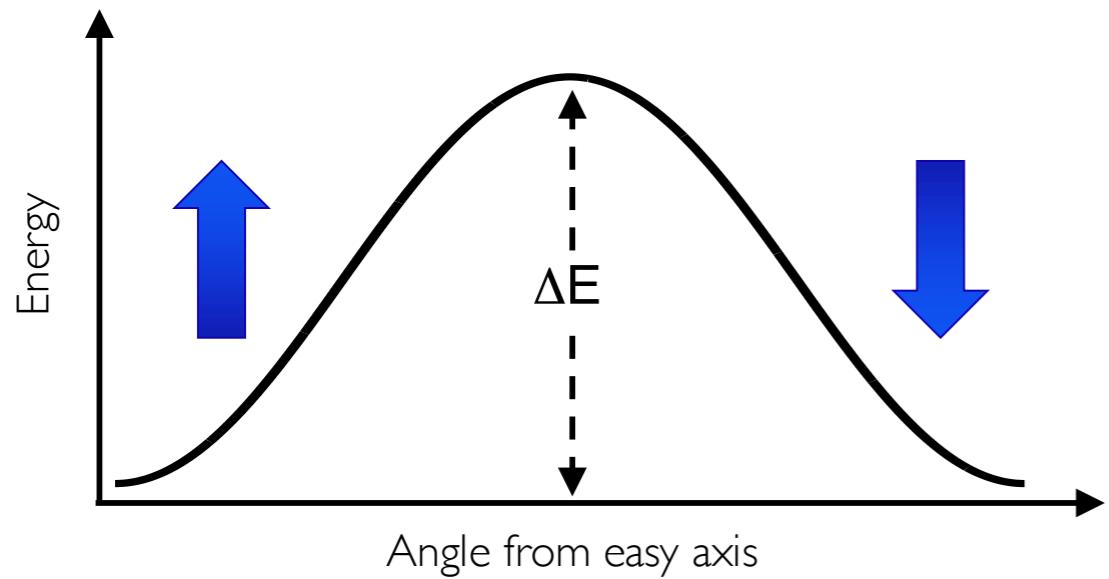
Exchange energy defines the Curie / Néel temperature of the material

$$J_{ij} = \frac{3k_B T_c}{\epsilon z}$$

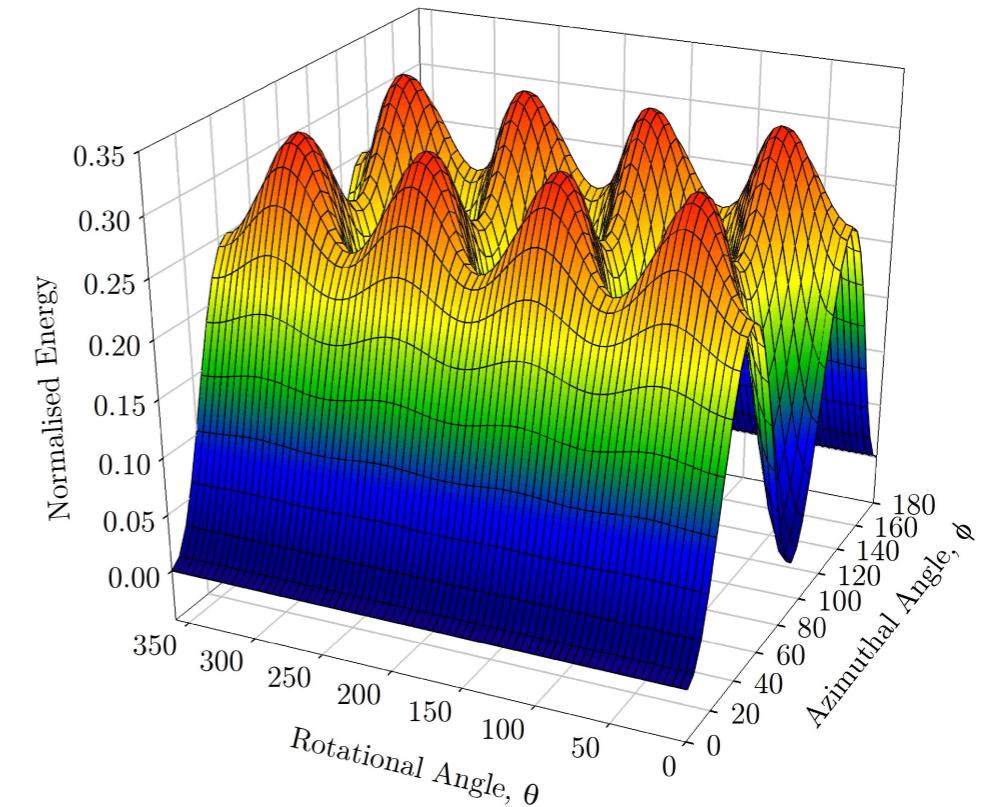
Mean field approximation with correction factor for spin waves

Magnetic anisotropy energy

Uniaxial



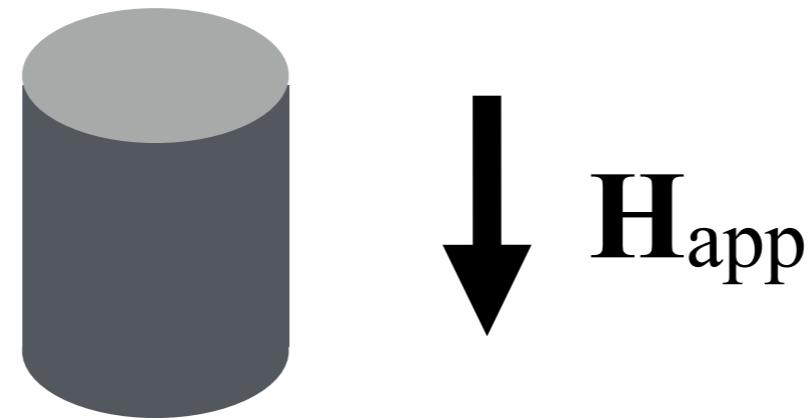
Cubic



$$\mathcal{H}_{\text{ani}}^{\text{uni}} = -k_{\text{u}} \sum_i (\mathbf{S}_i \cdot \mathbf{e})^2$$

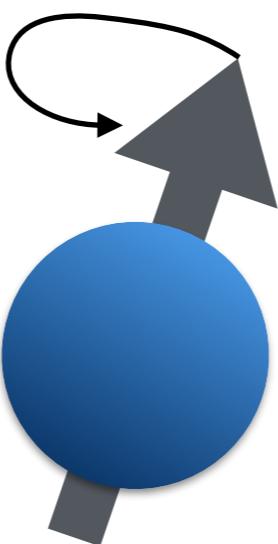
$$\mathcal{H}_{\text{ani}}^{\text{cub}} = \frac{k_{\text{c}}}{2} \sum_i (S_x^4 + S_y^4 + S_z^4)$$

Externally applied fields



$$\mathcal{H}_{app} = - \sum_i \mu_s S_i \cdot H_{app}$$

Integration methods



Ising model

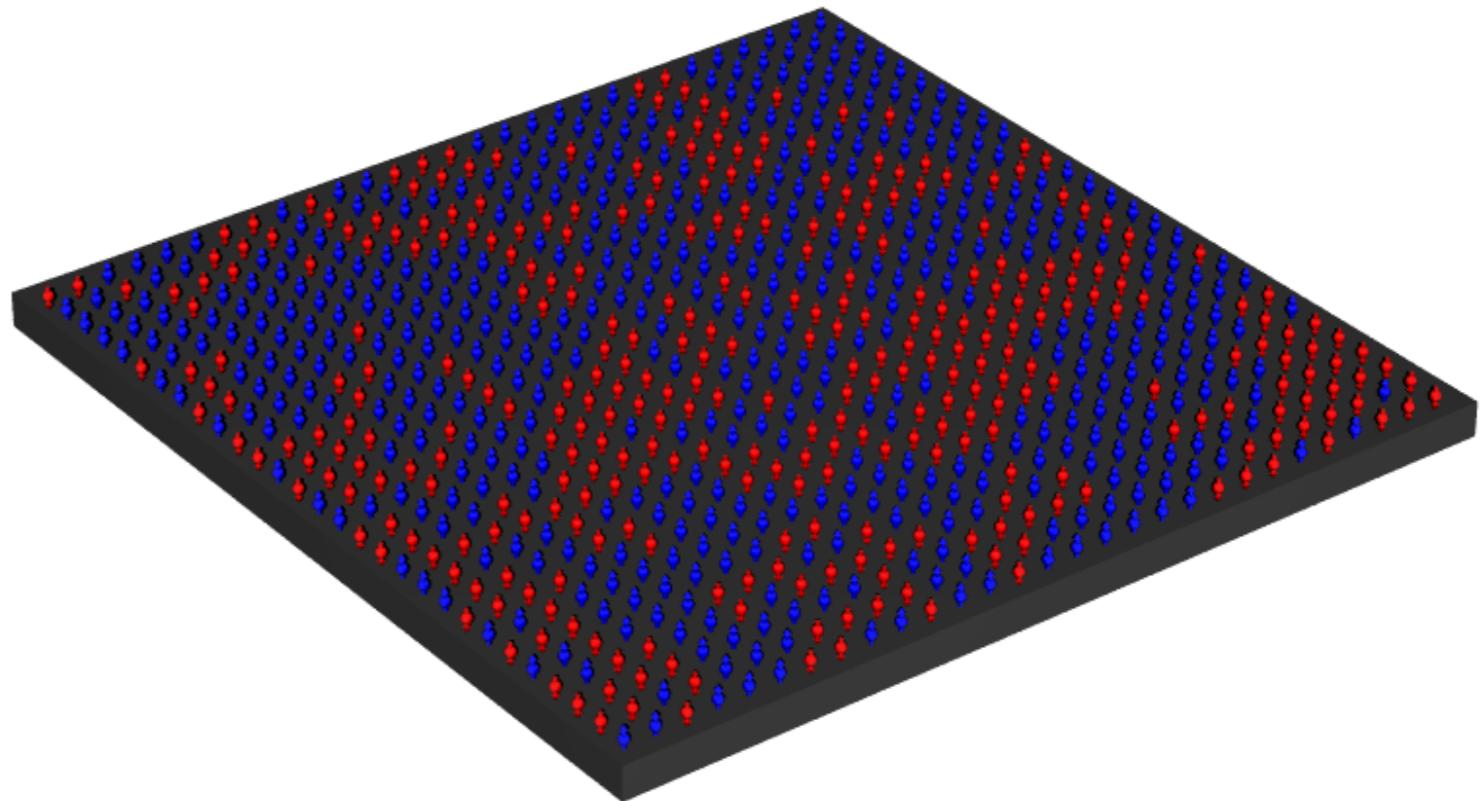
Beitrag zur Theorie des Ferromagnetismus¹⁾.

Von Ernst Ising in Hamburg.

(Eingegangen am 9. Dezember 1924.)

Es wird im wesentlichen das thermische Verhalten eines linearen, aus Elementarmagneten bestehenden Körpers untersucht, wobei im Gegensatz zur Weissschen Theorie des Ferromagnetismus kein molekulares Feld, sondern nur eine (nicht magnetische) Wechselwirkung benachbarter Elementarmagnete angenommen wird. Es wird gezeigt, daß ein solches Modell noch keine ferromagnetischen Eigenschaften besitzt und diese Aussage auch auf das dreidimensionale Modell ausgedehnt.

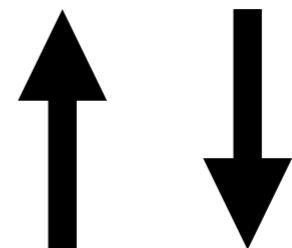
1. Annahmen. Die Erklärung, die P. Weiss²⁾ für den Ferromagnetismus gegeben hat, ist zwar formal befriedigend, doch läßt sie besonders die Frage nach einer physikalischen Erklärung der Hypothese des molekularen Feldes offen. Nach dieser Theorie wirkt auf jeden



Simplest model of spin-1/2 ferromagnet phase transition
“Toy model”

Ising model

Two allowable states, up, down

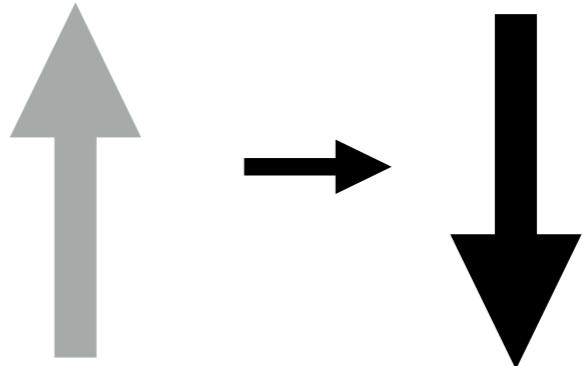


Energy barrier between states
defined by exchange energy

$$\mathcal{H}_{\text{exc}} = - \sum_{i \neq j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

Monte Carlo algorithm

1. Pick a new trial state (or move)



2. Evaluate energy before (E_1) and after (E_2) spin flip

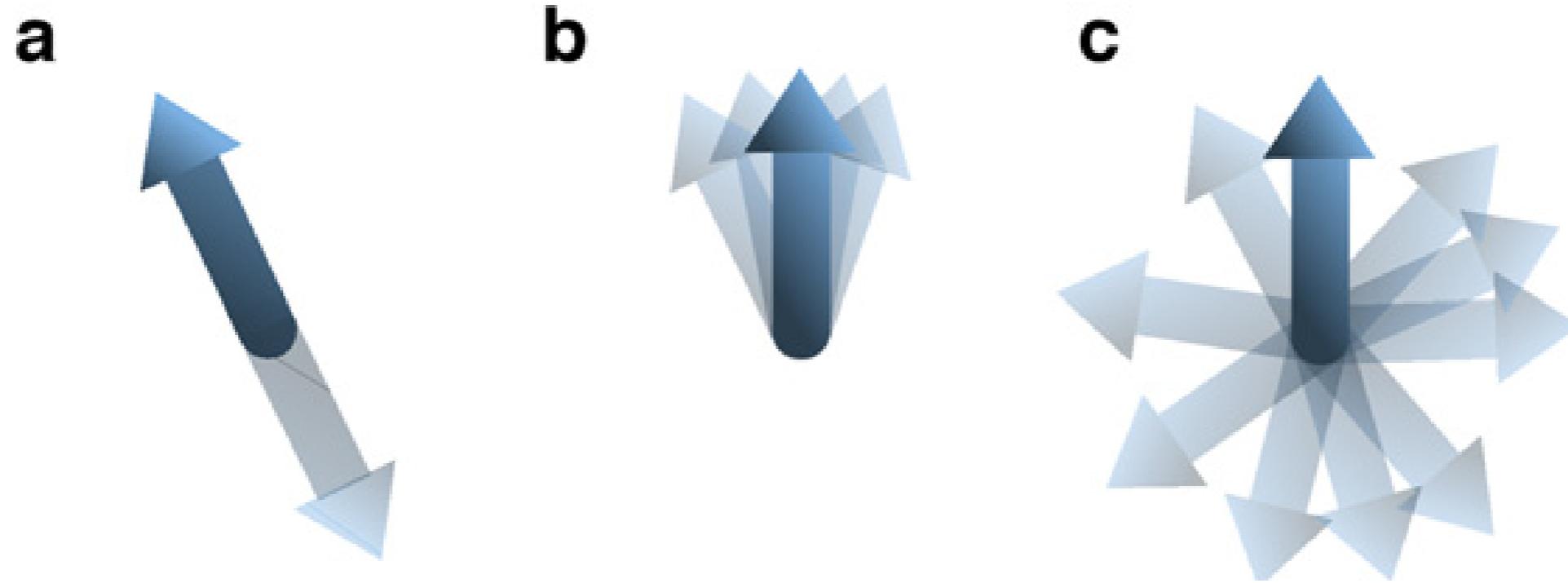
3. Evaluate energy difference between states

$$\Delta E = (E_2 - E_1)$$

4. Accept move with probability

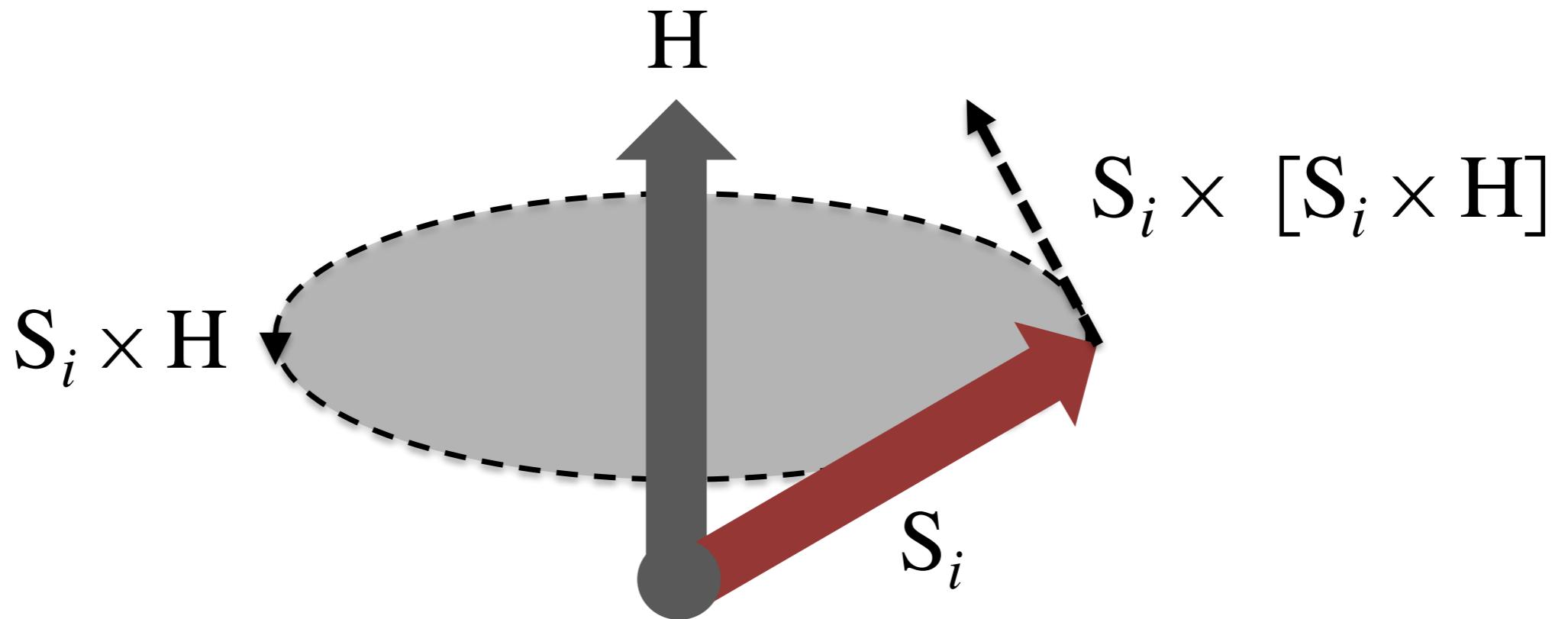
$$\exp(-\Delta E/k_B T)$$

Extension to 3D Heisenberg model straightforward



Use a combination of different trial moves

Spin dynamics

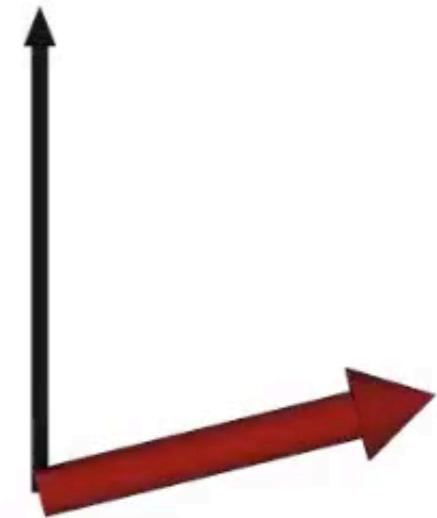


$$\frac{\partial \mathbf{S}_i}{\partial t} = -\frac{\gamma}{(1 + \lambda^2)} [\mathbf{S}_i \times \mathbf{H}_{\text{eff}}^i + \lambda \mathbf{S}_i \times (\mathbf{S}_i \times \mathbf{H}_{\text{eff}}^i)]$$

Stochastic Landau-Lifshitz-Gilbert equation

$$\mathbf{H}_{\text{eff}}^i = -\frac{1}{\mu_s} \frac{\partial \mathcal{H}}{\partial \mathbf{S}_i} + \mathbf{H}_{\text{th}}^{i,\delta}.$$

$$\mathbf{H}_{\text{th}}^i = \Gamma(t) \sqrt{\frac{2\lambda k_{\text{B}} T}{\gamma \mu_s \Delta t}}$$



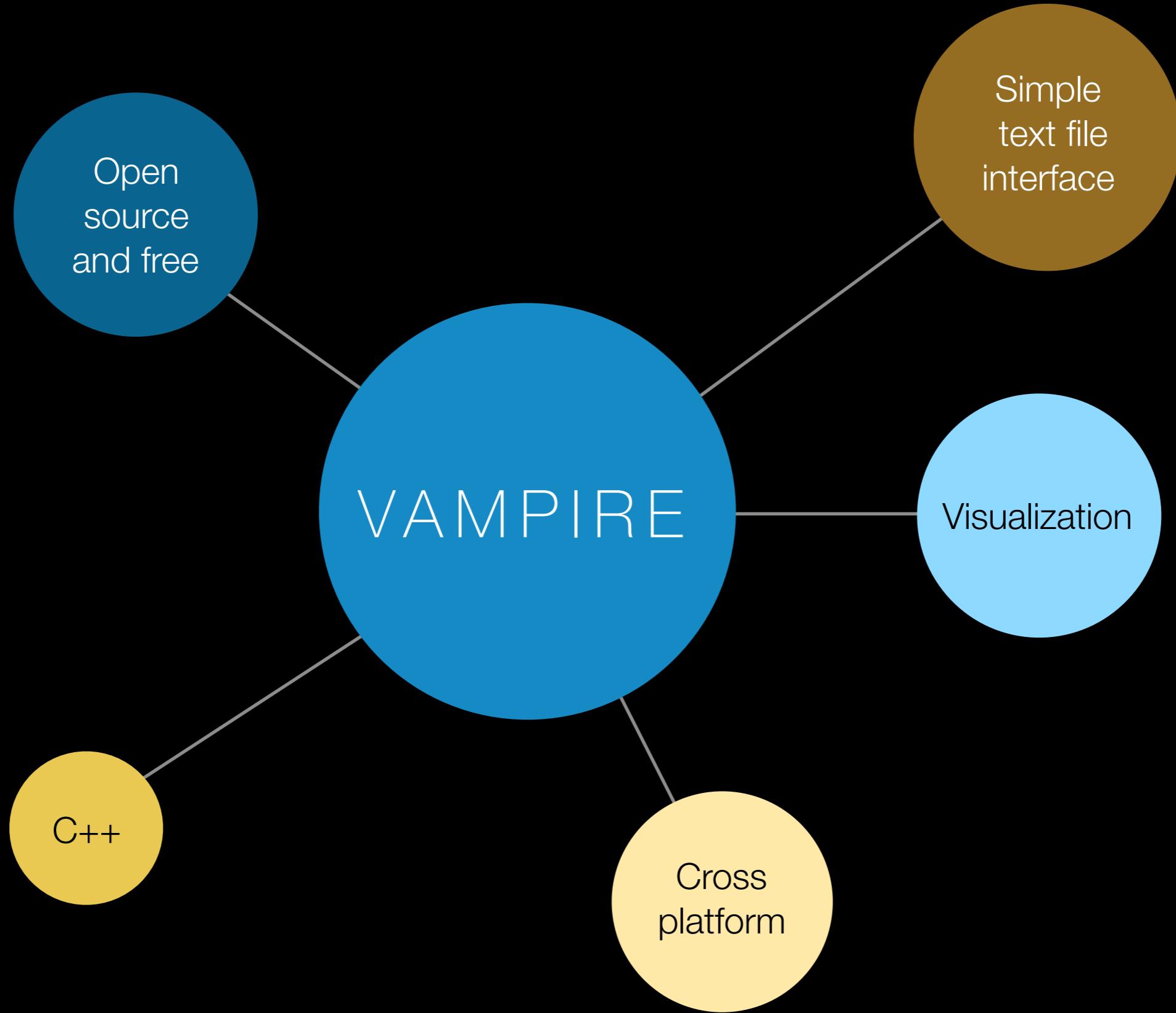
**Spin dynamics is the magnetic
analogue of molecular dynamics**



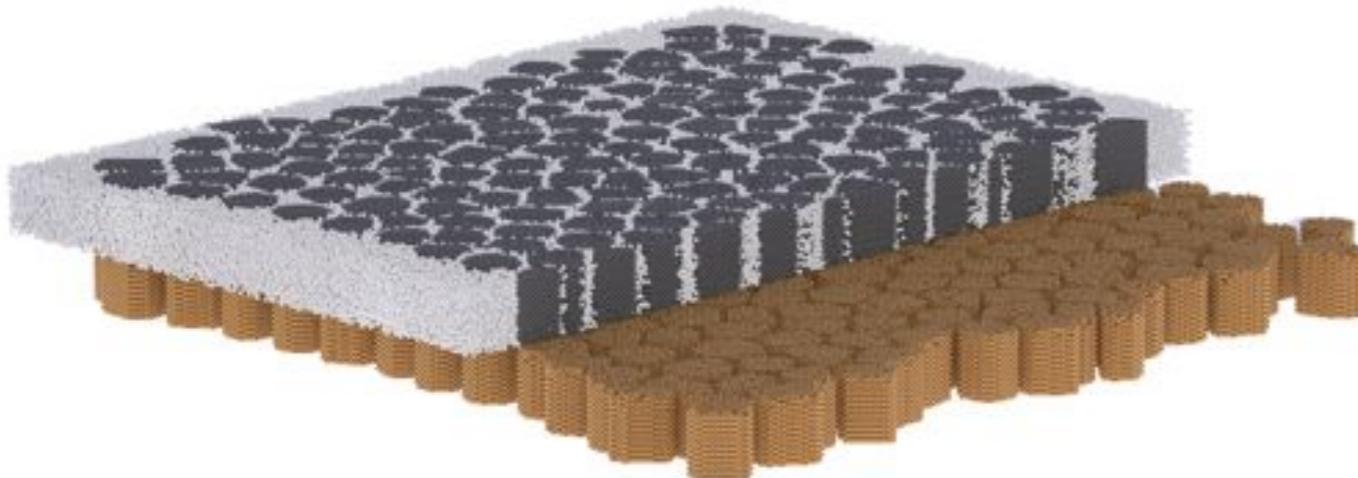
But typically more complicated set of interactions

VAMPIRE

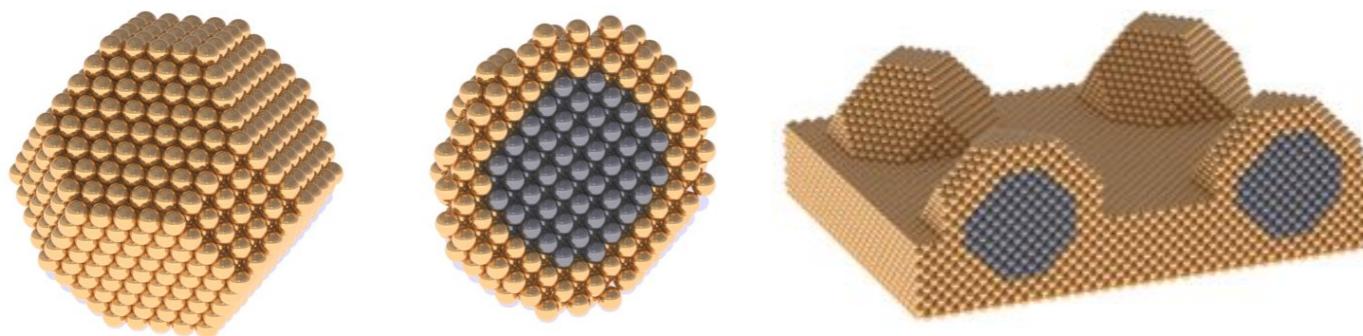
vampire.york.ac.uk



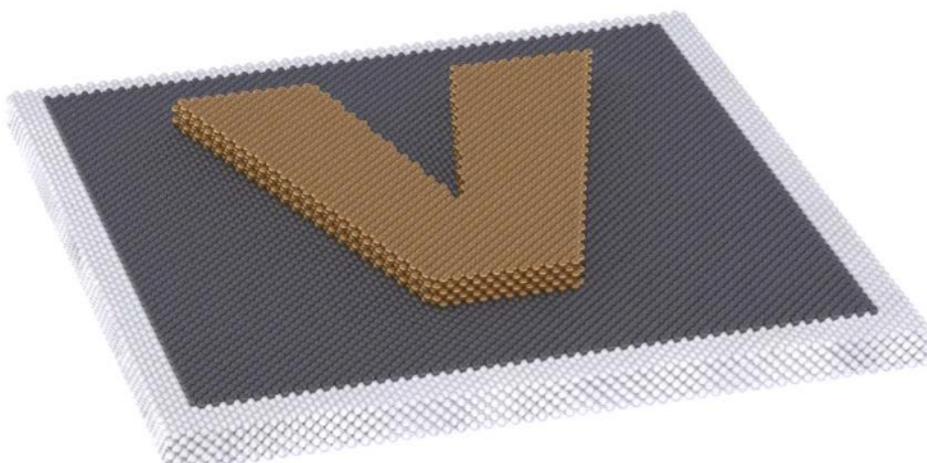
Wide range of system generation capabilities



Multilayer granular recording media

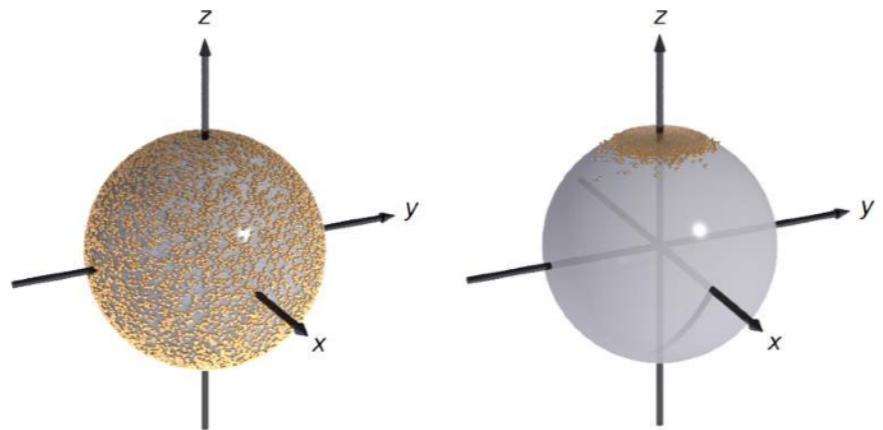


Nanoparticles, core-shell systems, particle arrays



Lithography

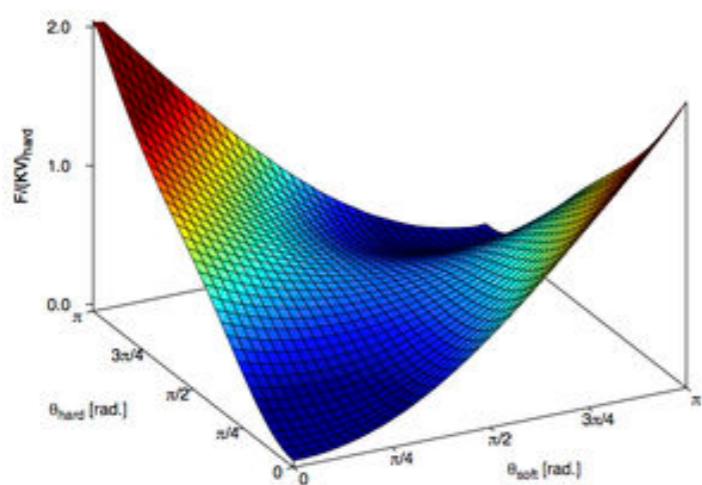
Different integration methods



Monte Carlo solver

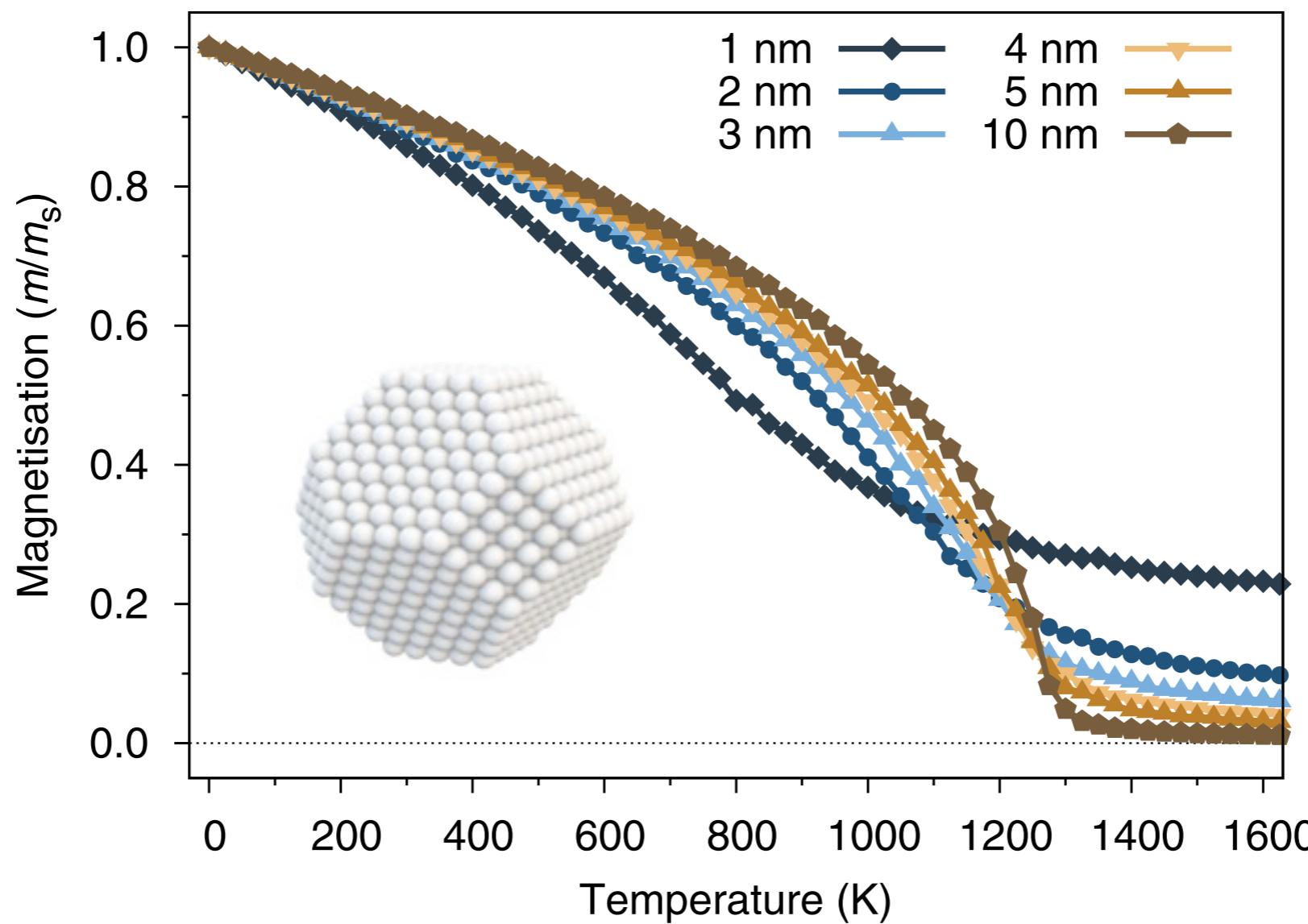
Stochastic
Landau-Lifshitz-Gilbert
Spin Dynamics

$$\frac{\partial \mathbf{S}}{\partial t} = -\frac{\gamma}{1+\alpha^2} (\mathbf{S} \times \mathbf{H} + \alpha \mathbf{S} [\mathbf{S} \times \mathbf{H}])$$
$$\frac{d\mathbf{f}}{dt} = -\frac{J+\sigma_3}{1+\alpha^2} (\mathbf{f} \times \mathbf{H} + \alpha \mathbf{f} [\mathbf{f} \times \mathbf{H}])$$

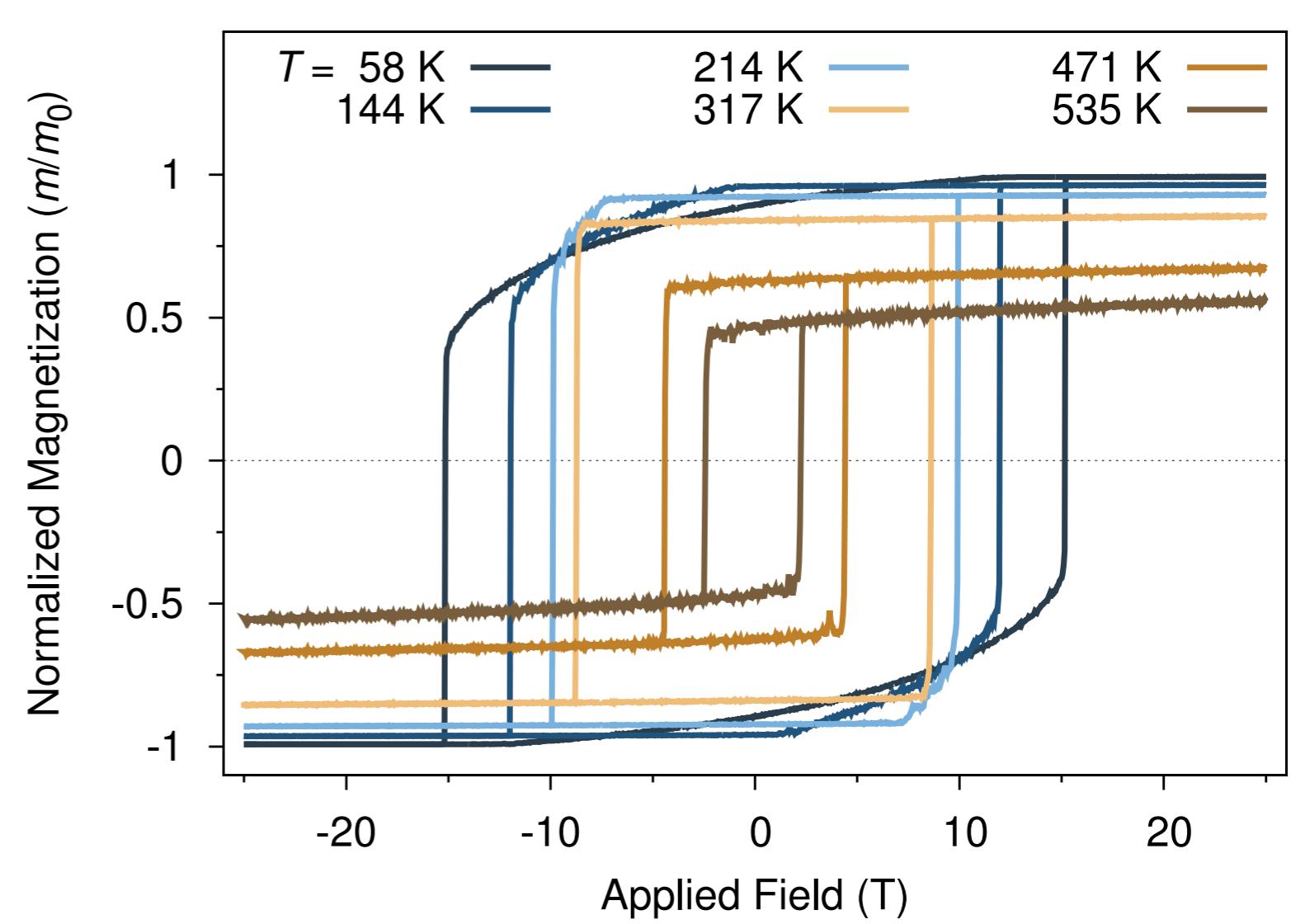
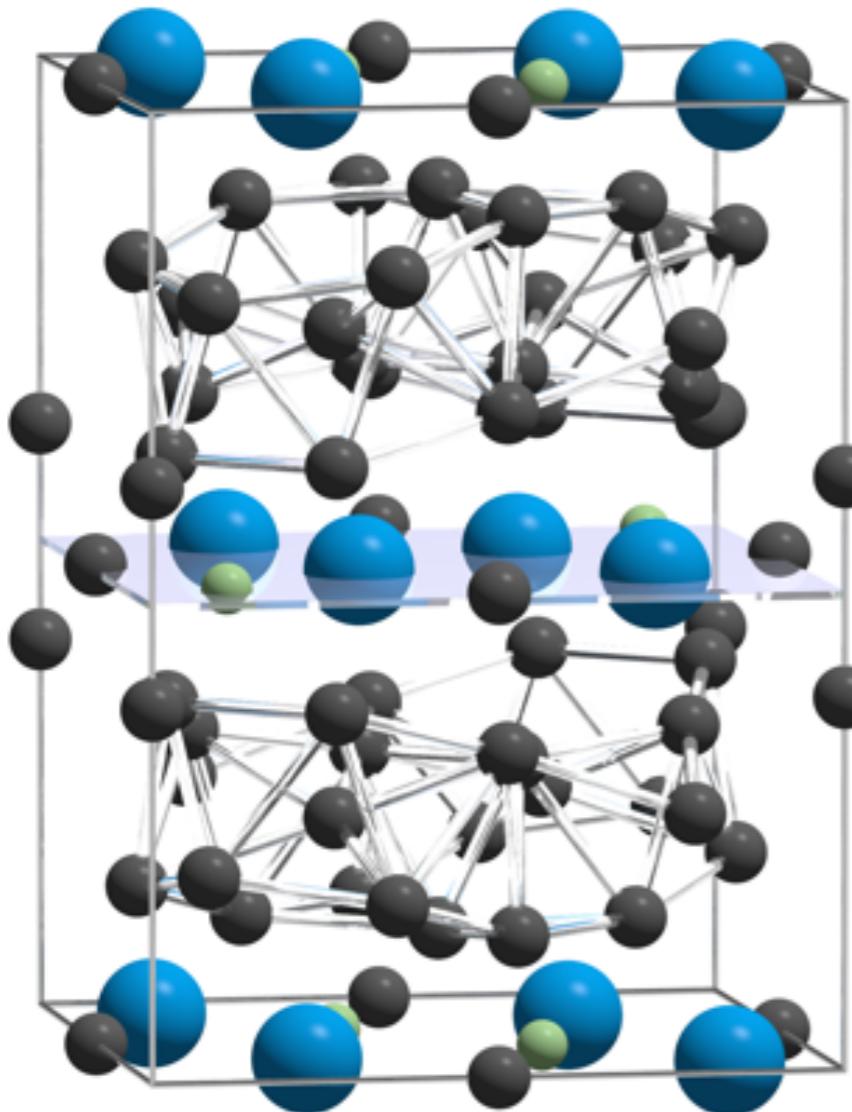


Constrained Monte Carlo

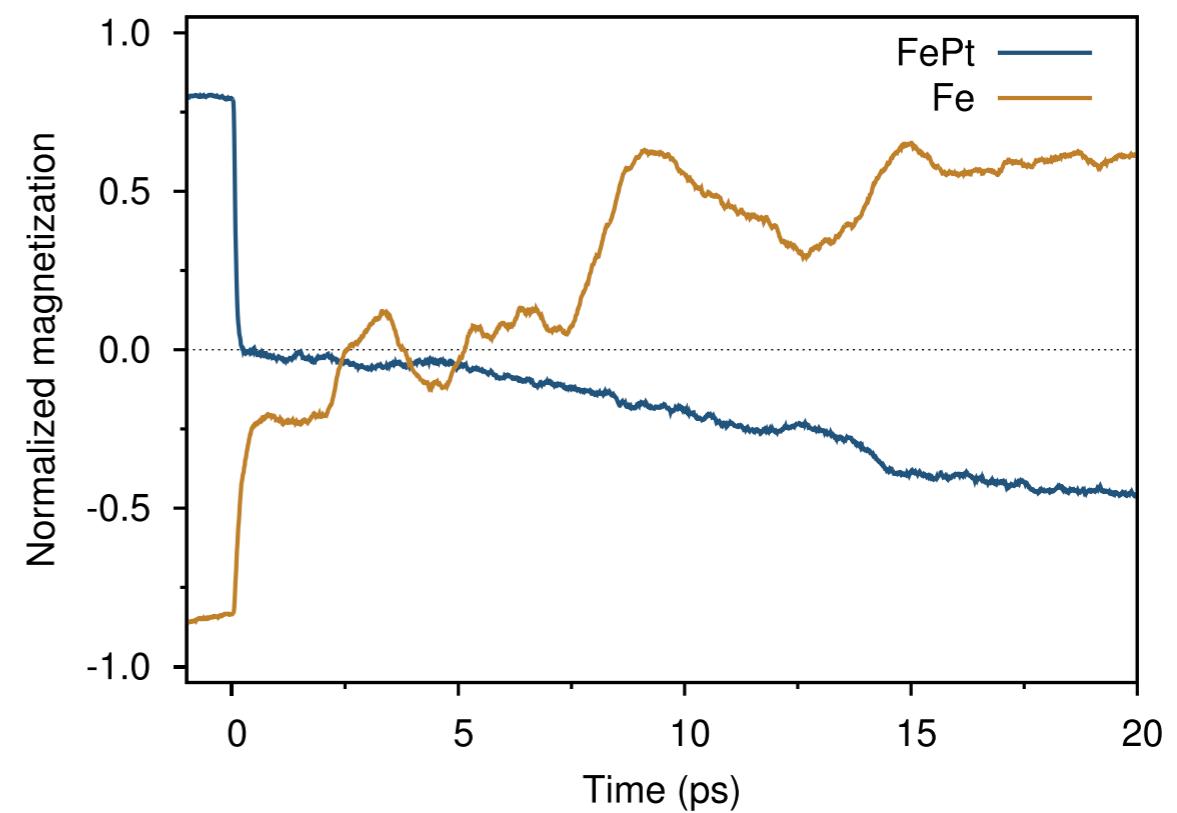
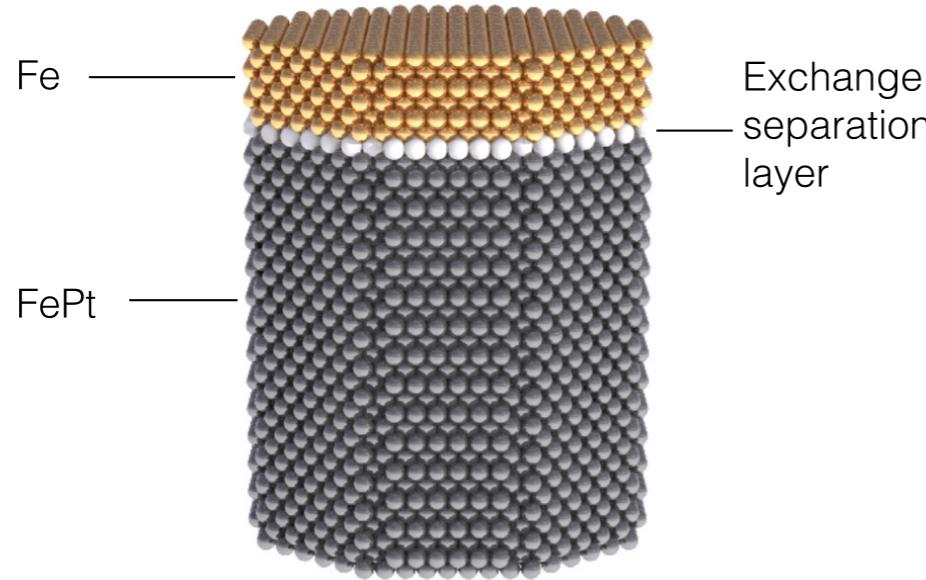
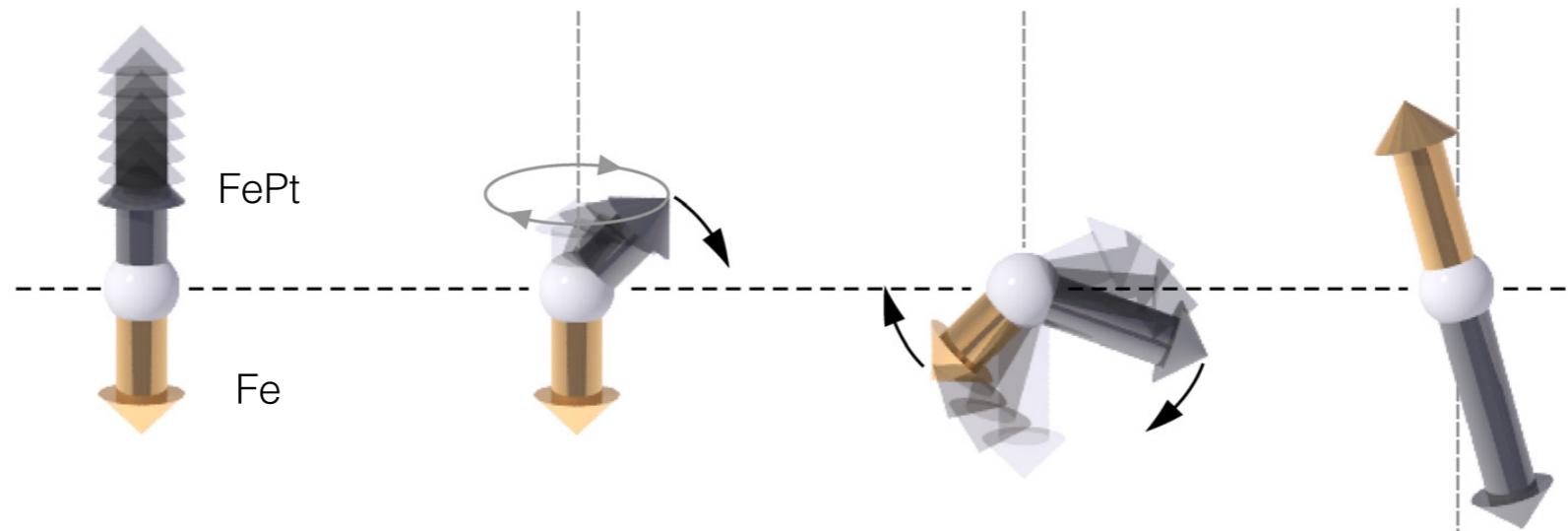
Temperature dependent magnetization for different particle sizes



Hysteresis properties in multicomponent systems

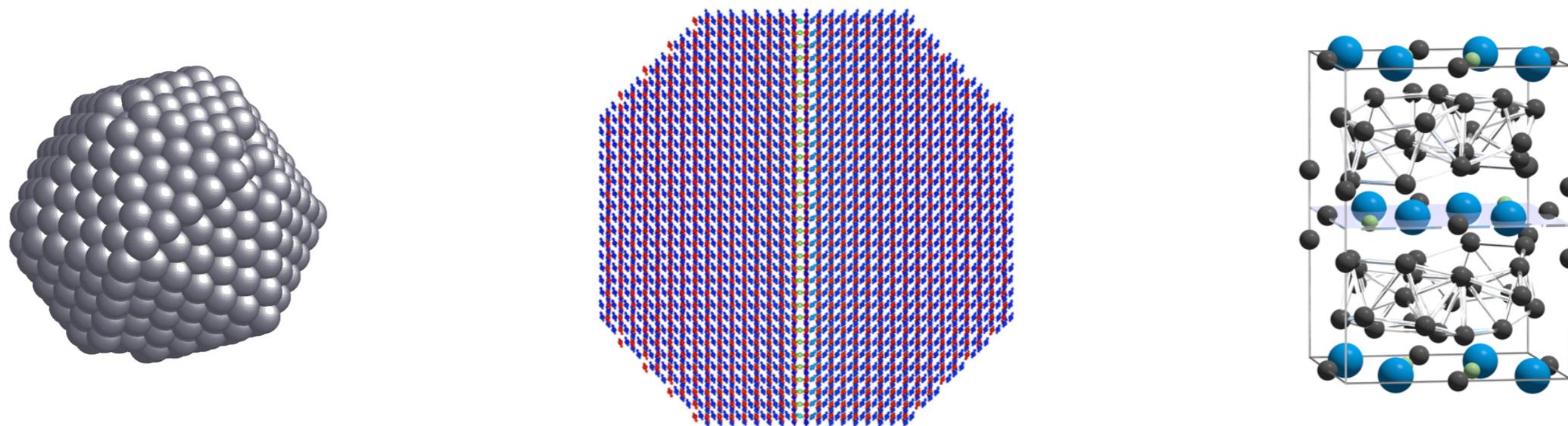


Ultrafast spin dynamics



Multiscale simulations with *ab-initio* parameters

$$\mathcal{H}_{\text{exc}}^{\text{M}} = - \sum_{i \neq j} [S_x^i S_y^i S_z^i] \begin{bmatrix} J_{xx} & J_{xy} & J_{xz} \\ J_{yx} & J_{yy} & J_{yz} \\ J_{zx} & J_{zy} & J_{zz} \end{bmatrix} \begin{bmatrix} S_x^j \\ S_y^j \\ S_z^j \end{bmatrix}$$



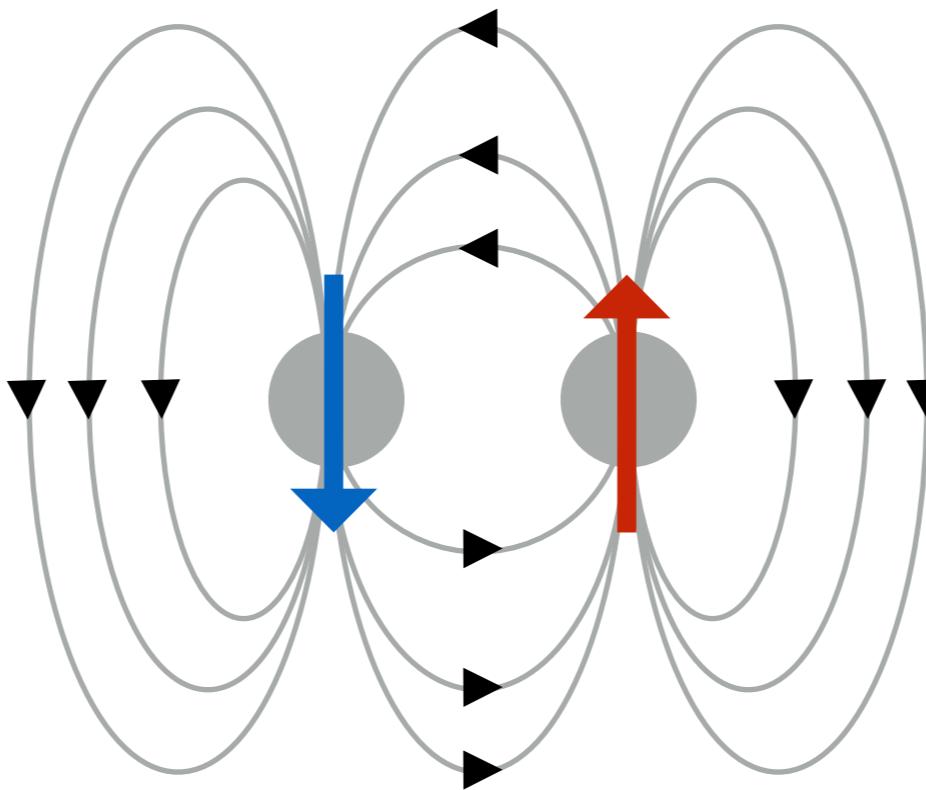
VAMPIRE includes a file specification capable of representing any structure and most interactions

Unit Cell File specification (.ucf)

```
# Unit cell size:  
3.854 3.854 3.715  
# Unit cell vectors:  
1.0 0.0 0.0 0.0  
0.0 1.0 0.0 0.0  
0.0 0.0 0.1 0.0  
# Atoms num, id cx cy cz mat lc hc  
2  
0 0.0 0.0 0 0 0 0  
1 0.5 0.5 0 0 1 0  
# Interactions n exctype, id i j dx dy dz Jij  
2718 1  
0 0 0 -1 -4 -5 2.22436e-27 2.22436e-27 2.35828e-27  
1 0 0 0 -4 -5 4.44872e-27 4.44872e-27 4.71655e-27  
2 0 0 1 -4 -5 2.22436e-27 2.22436e-27 2.35828e-27  
...
```

Contains atomic structure and interactions

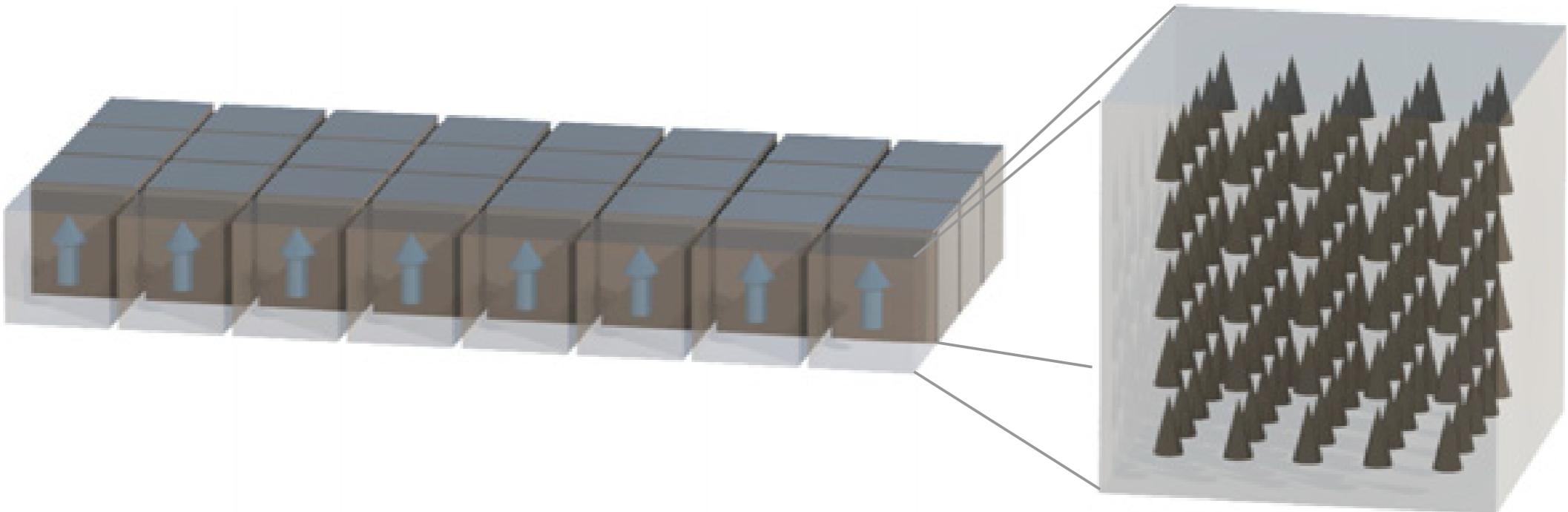
Demagnetising fields



Dipole-Dipole
approximation
- n^2 problem!

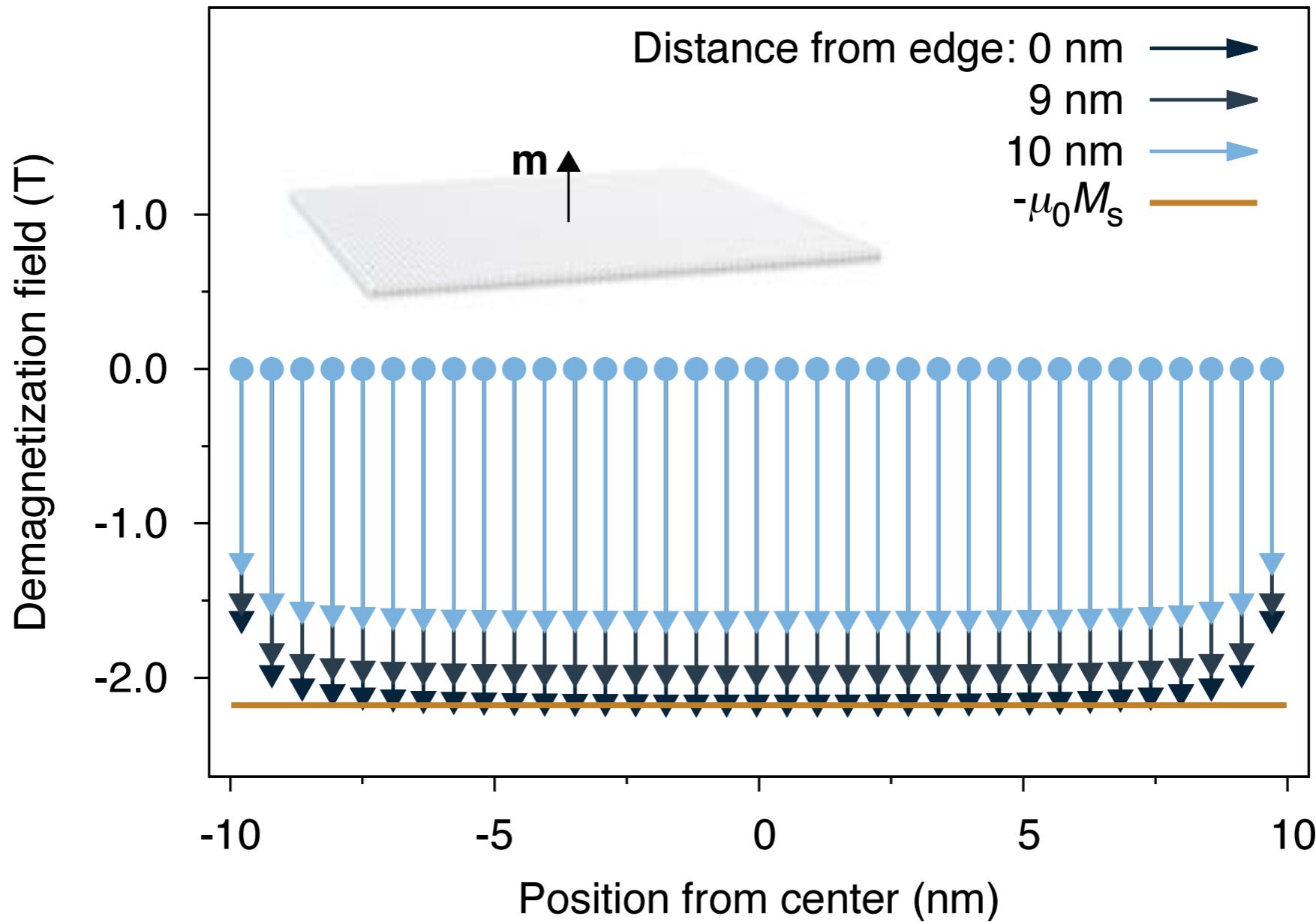
$$\mathbf{H}_{\text{dp}}^i = \frac{\mu_0}{4\pi} \left(\sum_{i \neq j} \frac{3(\boldsymbol{\mu}_j \cdot \hat{\mathbf{r}}_{ij})\hat{\mathbf{r}}_{ij} - \boldsymbol{\mu}_j}{r_{ij}^3} \right)$$

Macrocell approximation

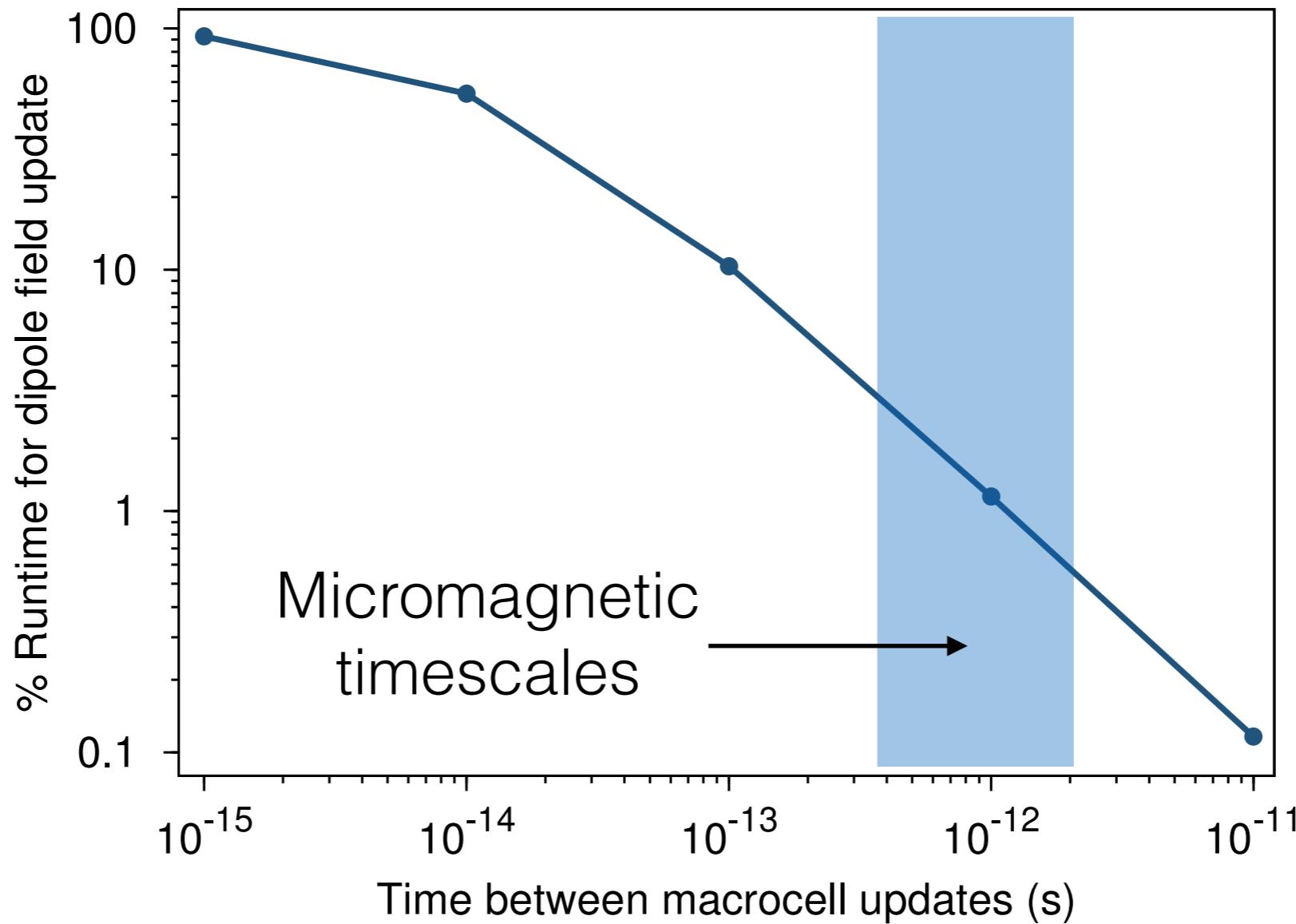


$$\mathbf{H}_{\text{demag}}^{\text{mc}, p} = \frac{\mu_0}{4\pi} \left(\sum_{p \neq q} \frac{3(\mathbf{m}_{\text{mc}}^q \cdot \hat{\mathbf{r}}) \hat{\mathbf{r}} - \mathbf{m}_{\text{mc}}^q}{r^3} \right) - \frac{\mu_0}{3} \frac{\mathbf{m}_{\text{mc}}^p}{V_{\text{mc}}^p}$$

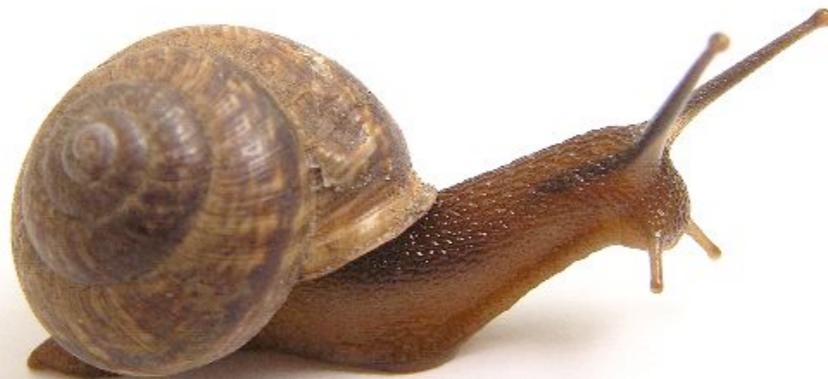
Demagnetising field for a platelet



Performance for different update rates

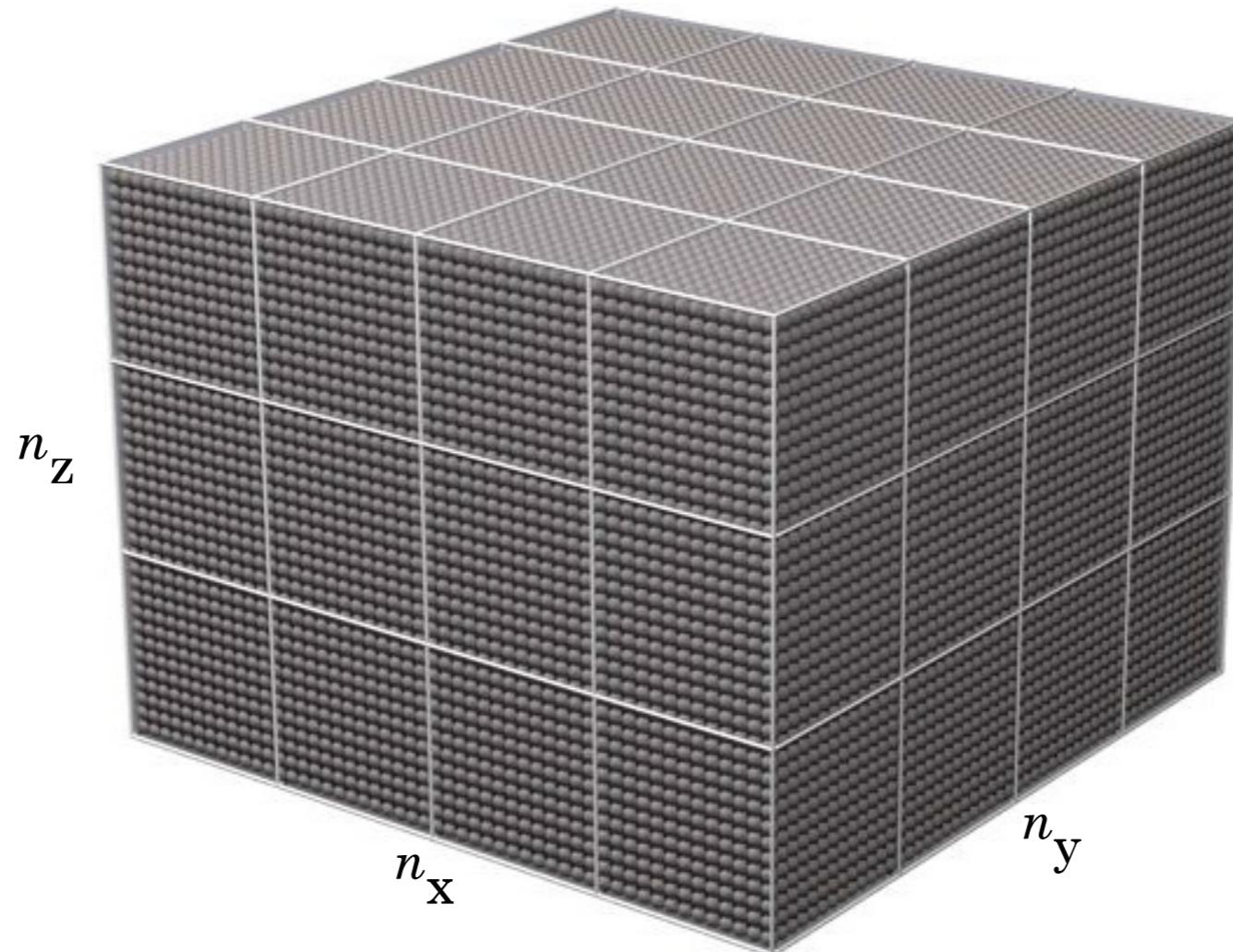


Atomistic simulations are very useful, but...



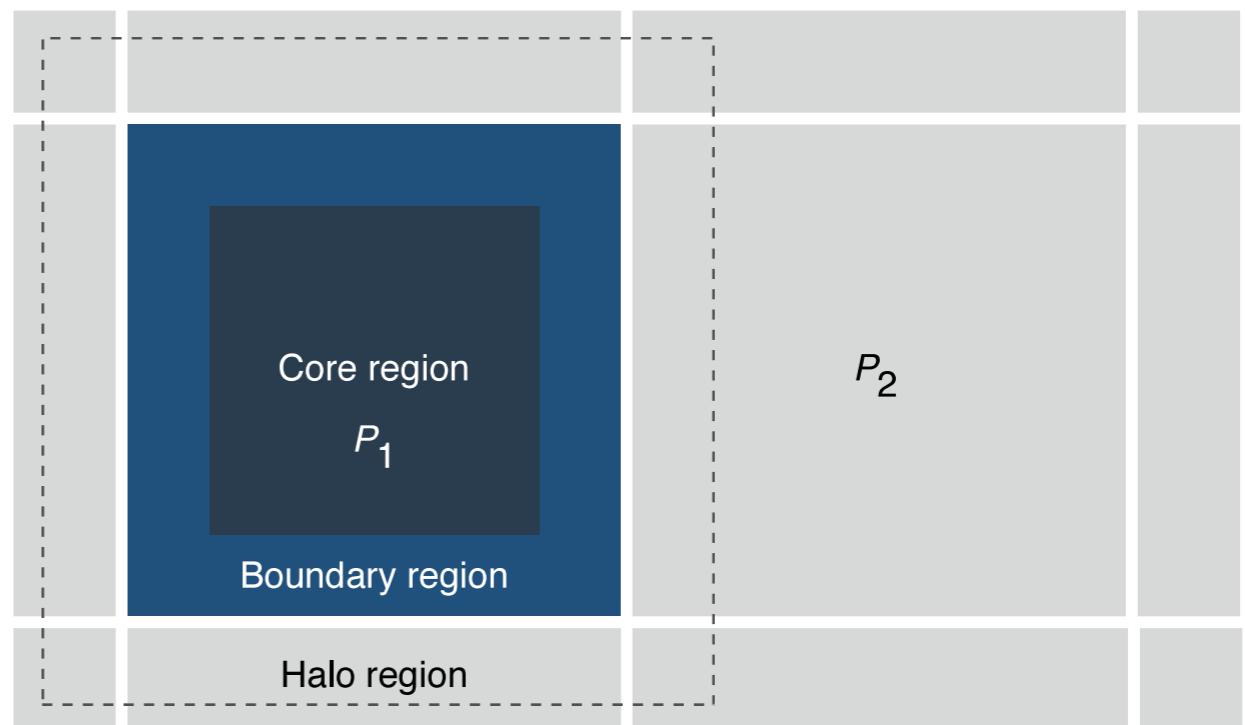
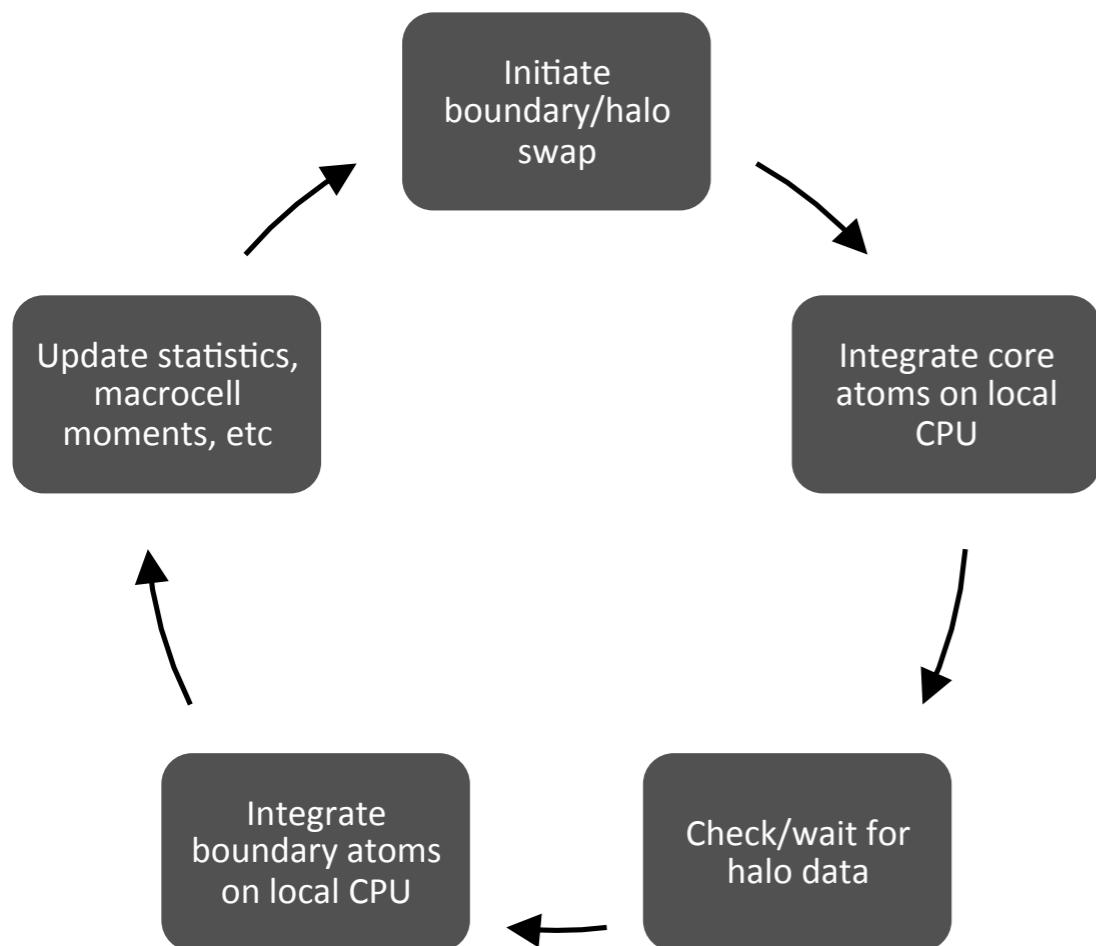
typically 1000 times slower than micromagnetics

Need to use fast computers to simulate reasonable system sizes



Use parallelization to divide big problem into smaller parts

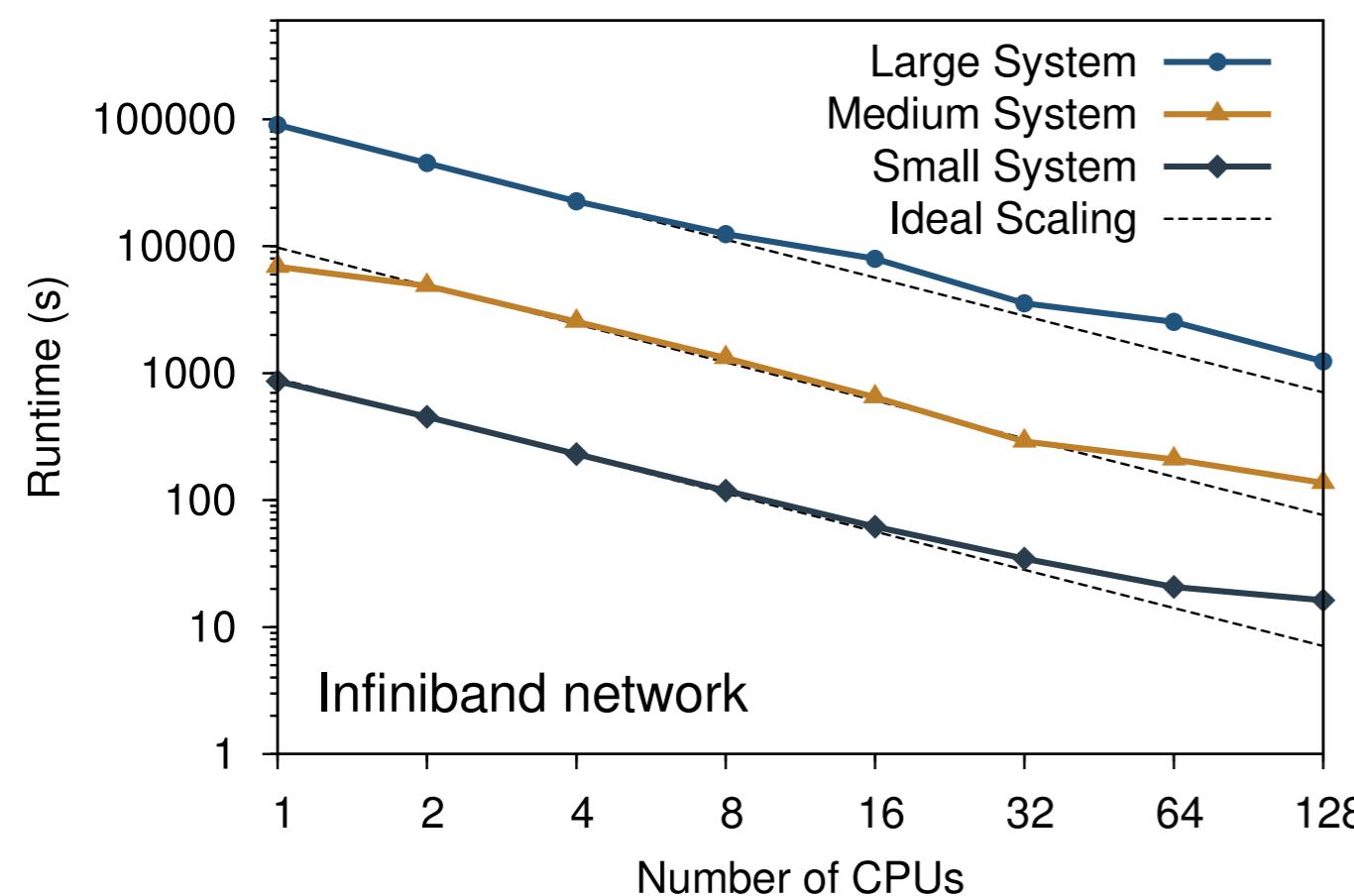
Domain decomposition places separate parts of the problem on different processors





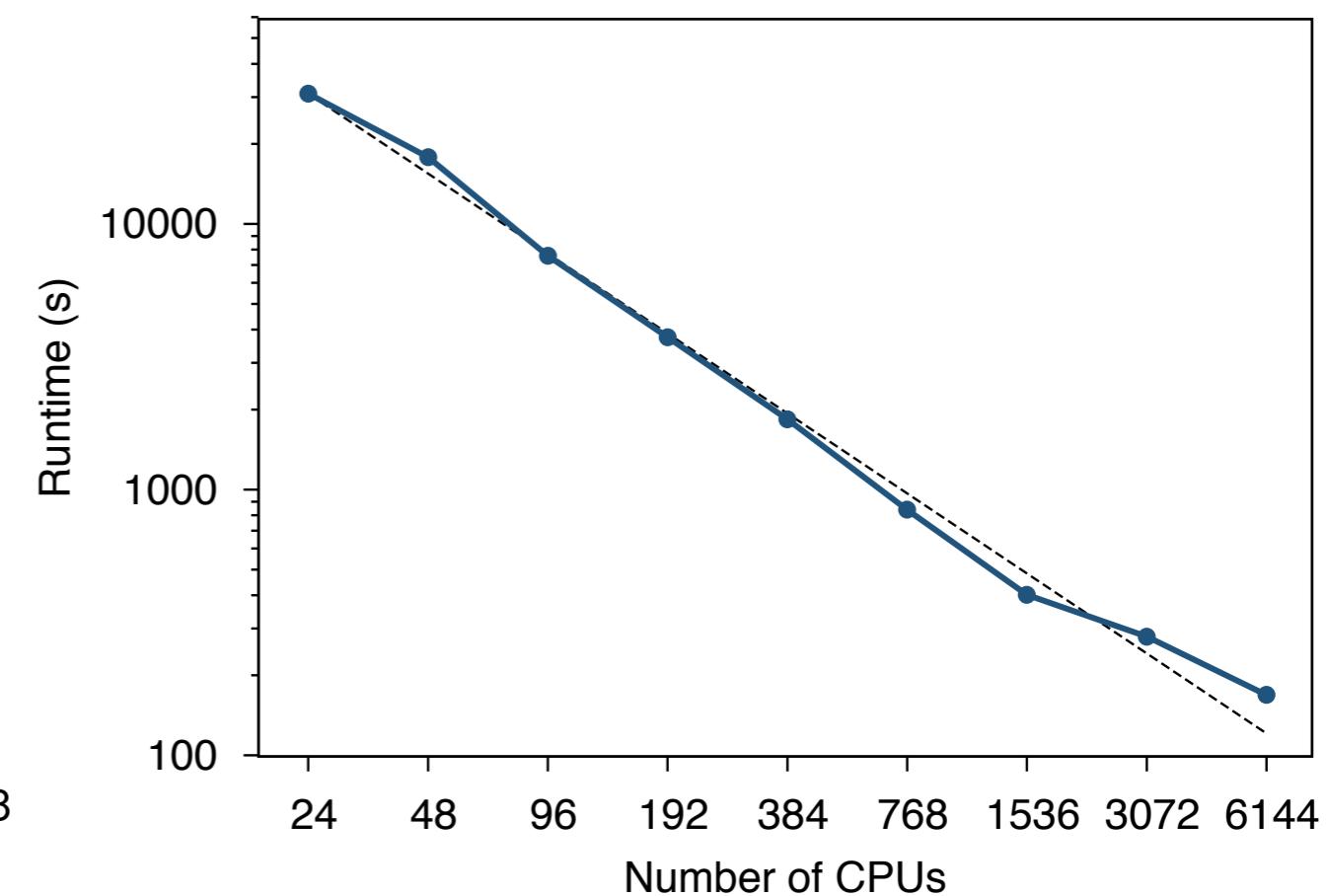
VAMPIRE is a parallel code

Group Cluster



10K, 100K and 1M spins

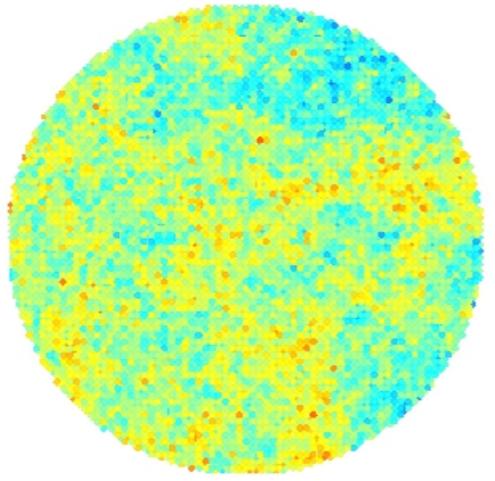
ARCHER
(National Supercomputer)



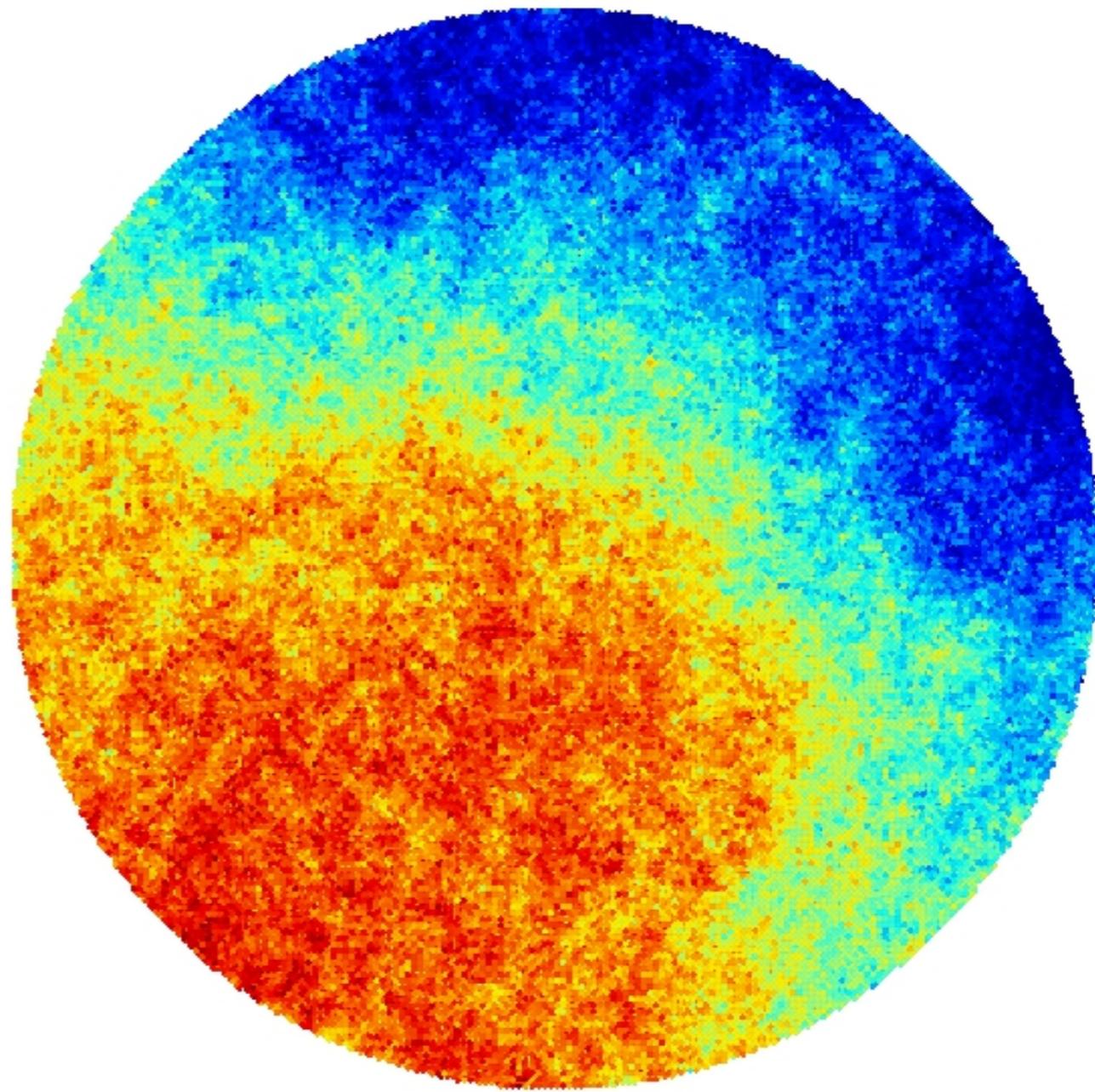
100 nm x 100 nm x 20 nm
(18M spins)

eCSE proposal to make VAMPIRE available on ARCHER

Magnetic reversal mechanisms in CoFeB/MgO nanodots

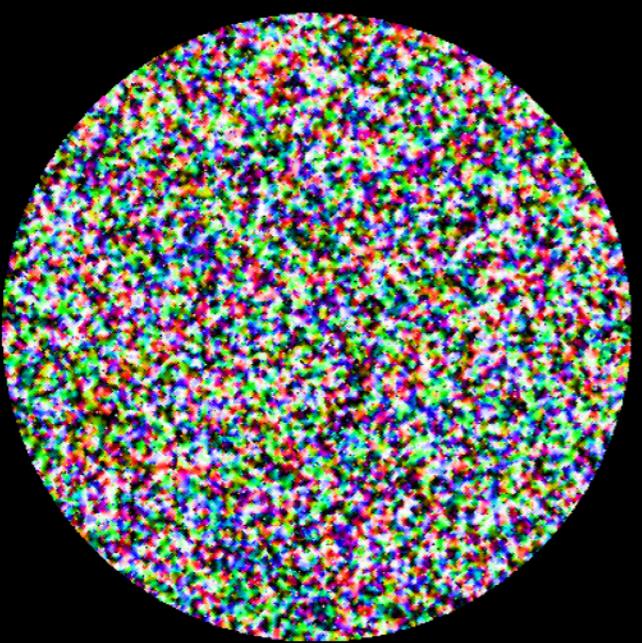


20 nm



50 nm

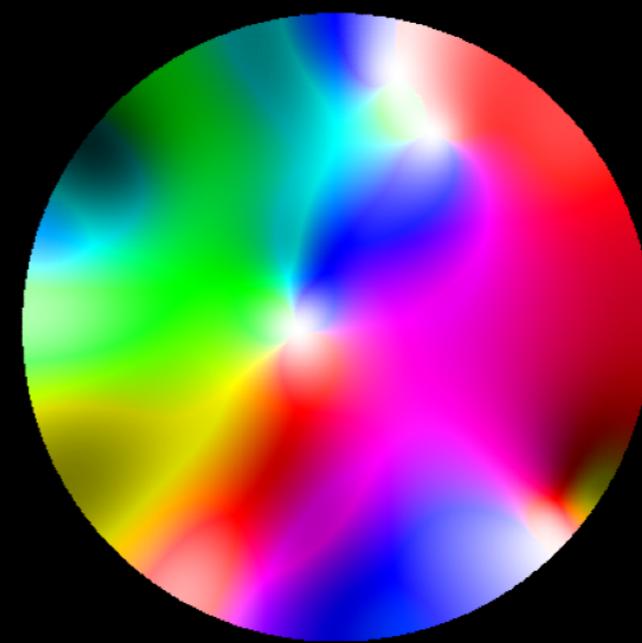
Vortex core simulation in Permalloy



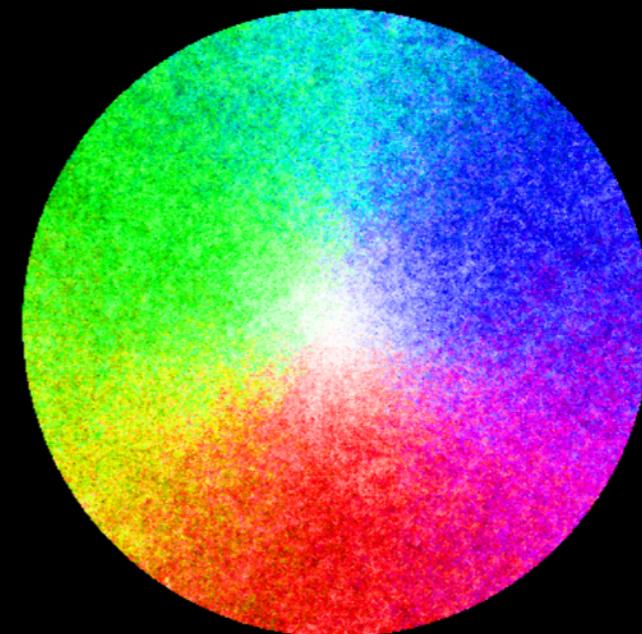
↔

70 nm

$T = 0K$



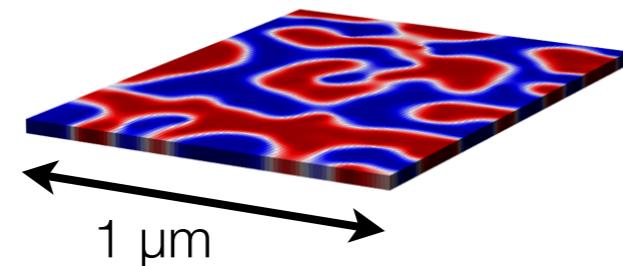
$T = 300K$



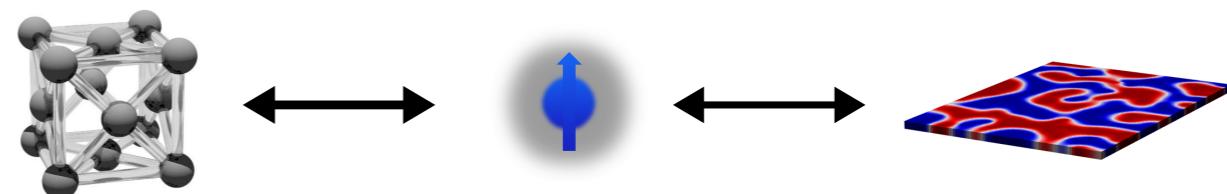
Computational efficiency and scale
Towards billion-atom simulations



GPGPU

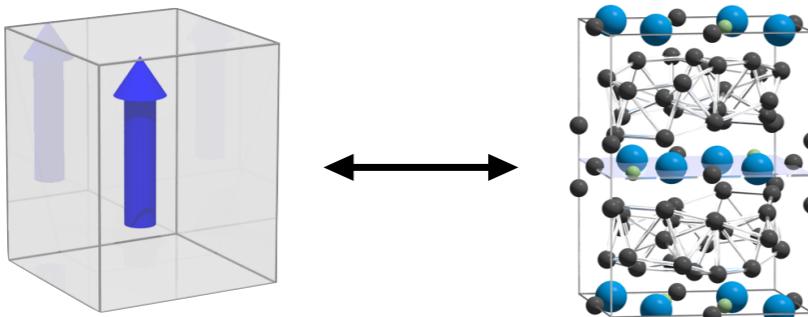


Beyond Heisenberg
Some materials require more complex interactions, e.g. 4-spin exchange, delocalized moments, spin electronics

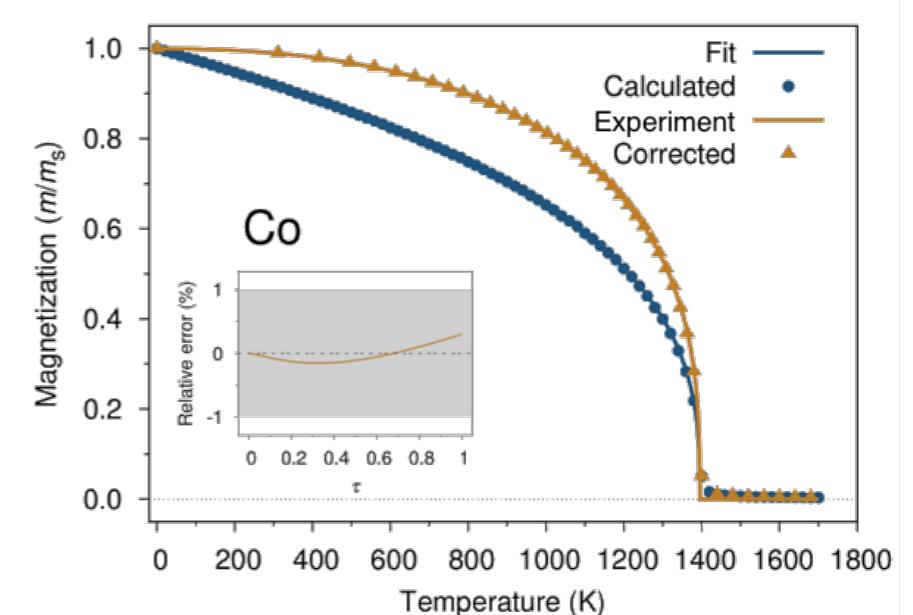


Future challenges

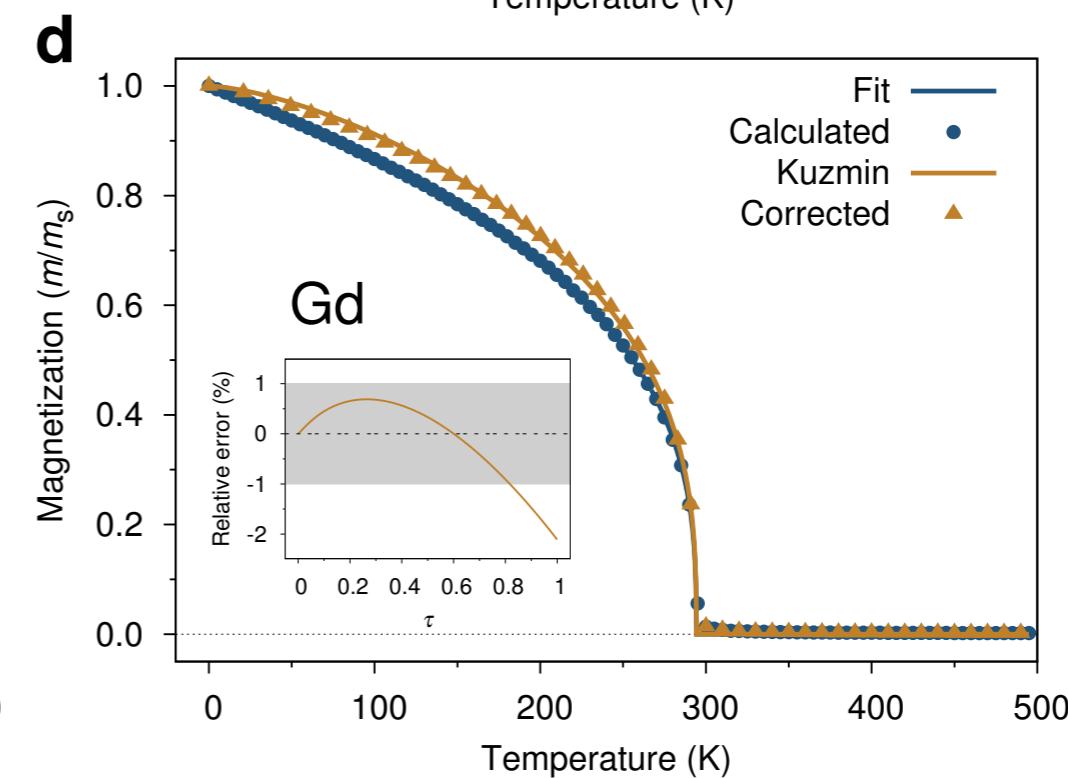
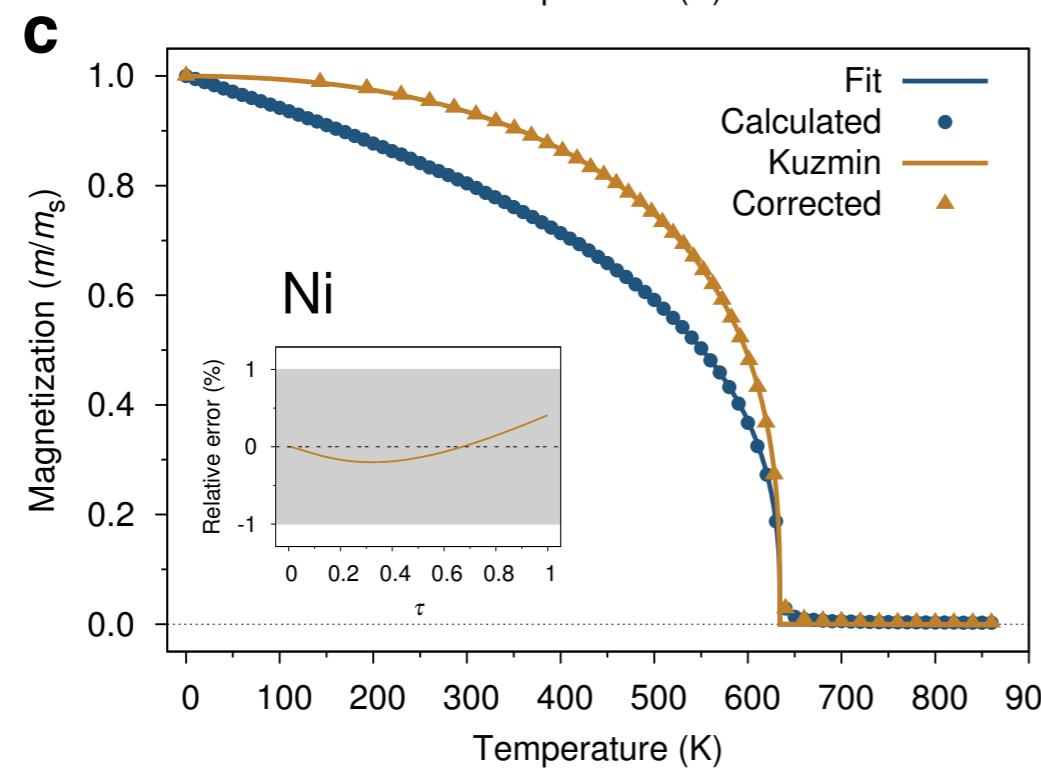
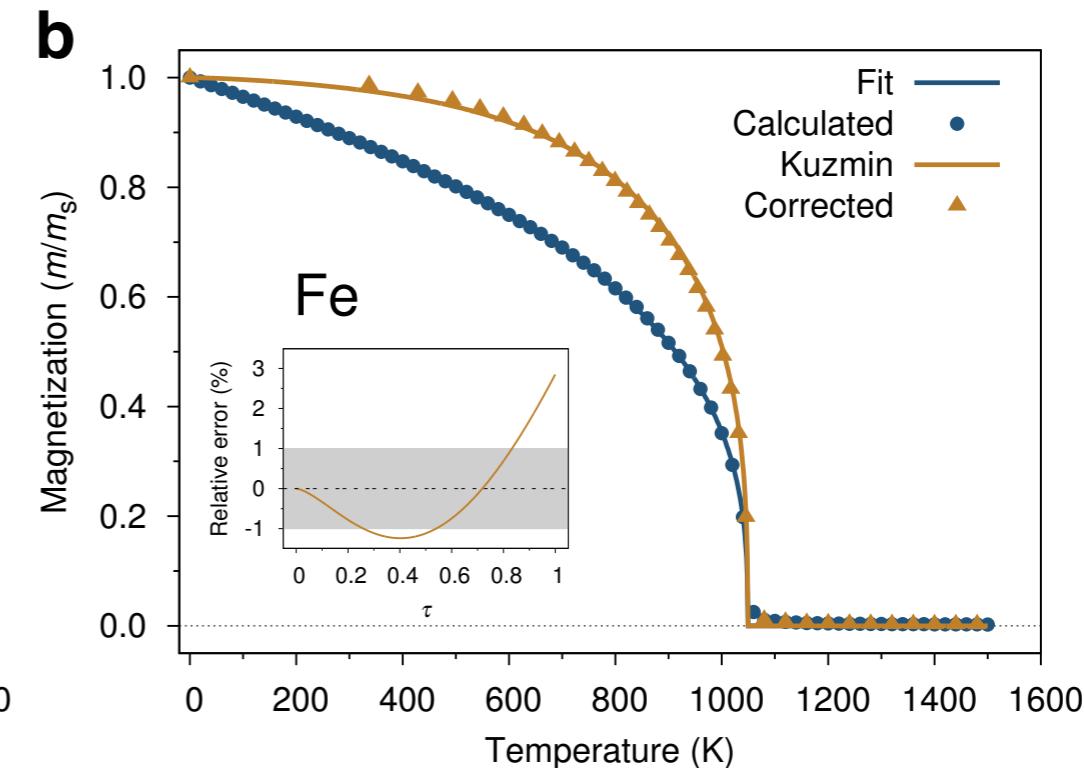
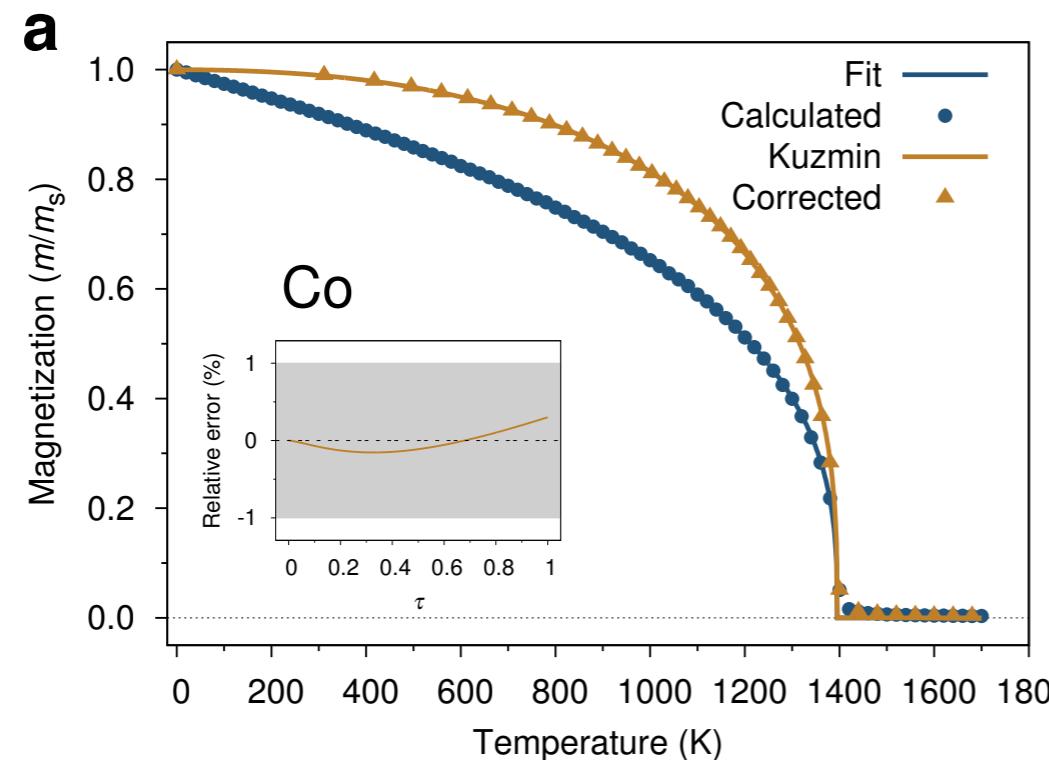
Multiscale stochastic simulations



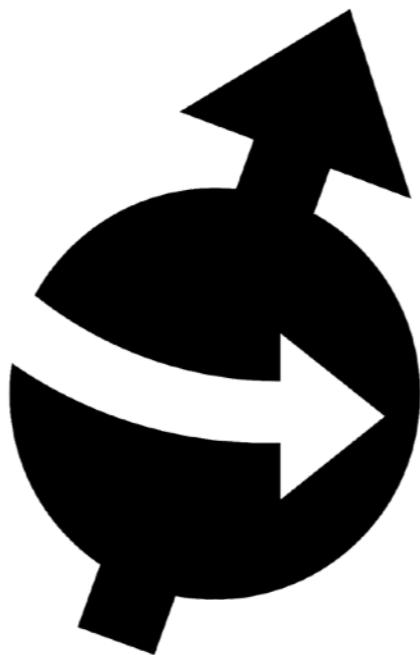
Advanced materials by design
Quantitative prediction of macroscopic behaviour



VAMPIRE magnetic materials library (VMM)



VAMPIRE



Code Overview

Programming language and approach

Written in C++ (2011 standard)

A mixture of object oriented (creation routines) and functional (high performance) programming styles

Supports Message Passing Interface (MPI)
parallelization, CUDA and OpenCL in alpha test.

Increasingly modular code base, work in progress

Version control

Managed with git version control system and hosted at Github

Open source with mixture of GPL and BSD licenses

Branches maintain different parallel versions of the code

- master branch - official releases (very old)
- develop - current up to date version (a bug or two)
- cuda - testing branch for CUDA version

New module structure for new additions

src/module/data.cpp	variables and arrays in module
src/module/interface.cpp	user interface to module
src/module initialise.cpp	function to initialize module data and variables
src/module/internal.h	header file for sharing variables within a module
hdr/module.h	interface to main VAMPIRE code

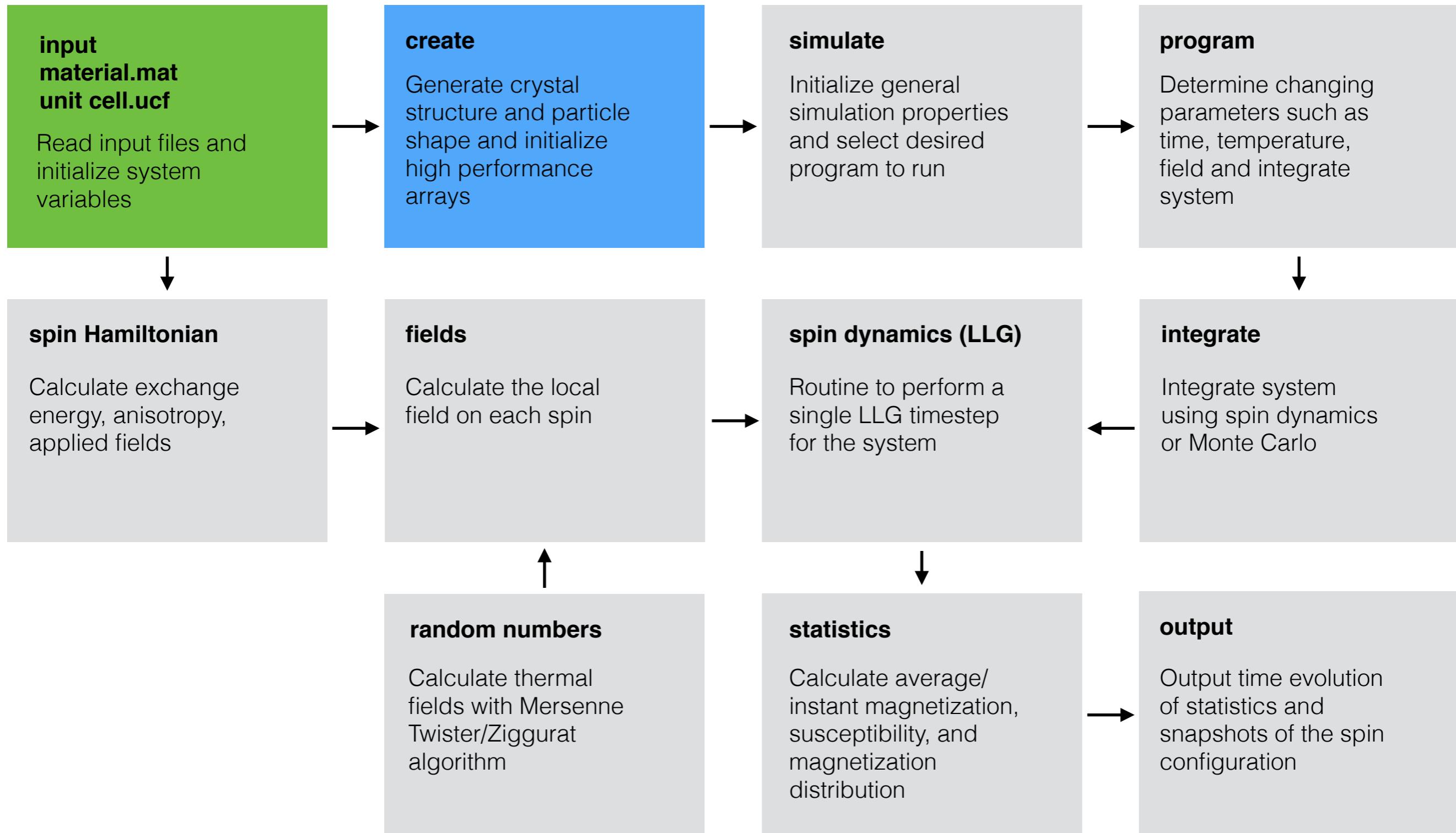
Modules

Each module is self contained and only interacts with the main vampire code with a defined interface in the module header file

Each module has its own namespace to separate it from the main code

Not all code is in modules - but work is underway

VAMPIRE execution flowchart



VAMPIRE Input files

Control of the code is through plain text files

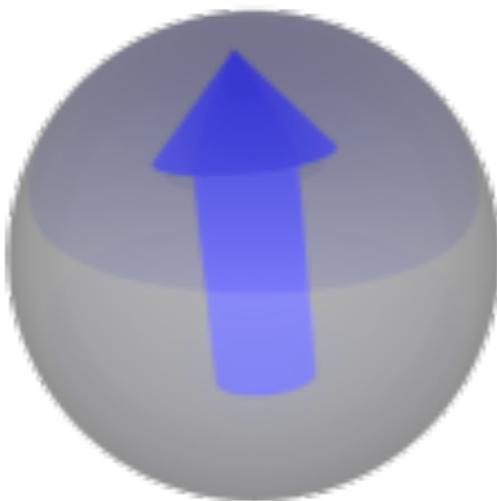
input

Main control file specifying system parameters, program, time steps, integrators, global fields, data output

material file

Lists magnetic parameters for different atom types in the simulation and provides a way to identify different magnetic states, interactions, etc

Practical 1: compiling the code



Getting the source code

Download the code from github

```
git clone https://github.com/richard-evans/vampire/
```

Checkout the develop branch

```
git checkout develop
```

Compiling the code

Different make targets for different compilers:

- g++ (default)
- intel (icc)
- llvm (macOS)
- cray/archer

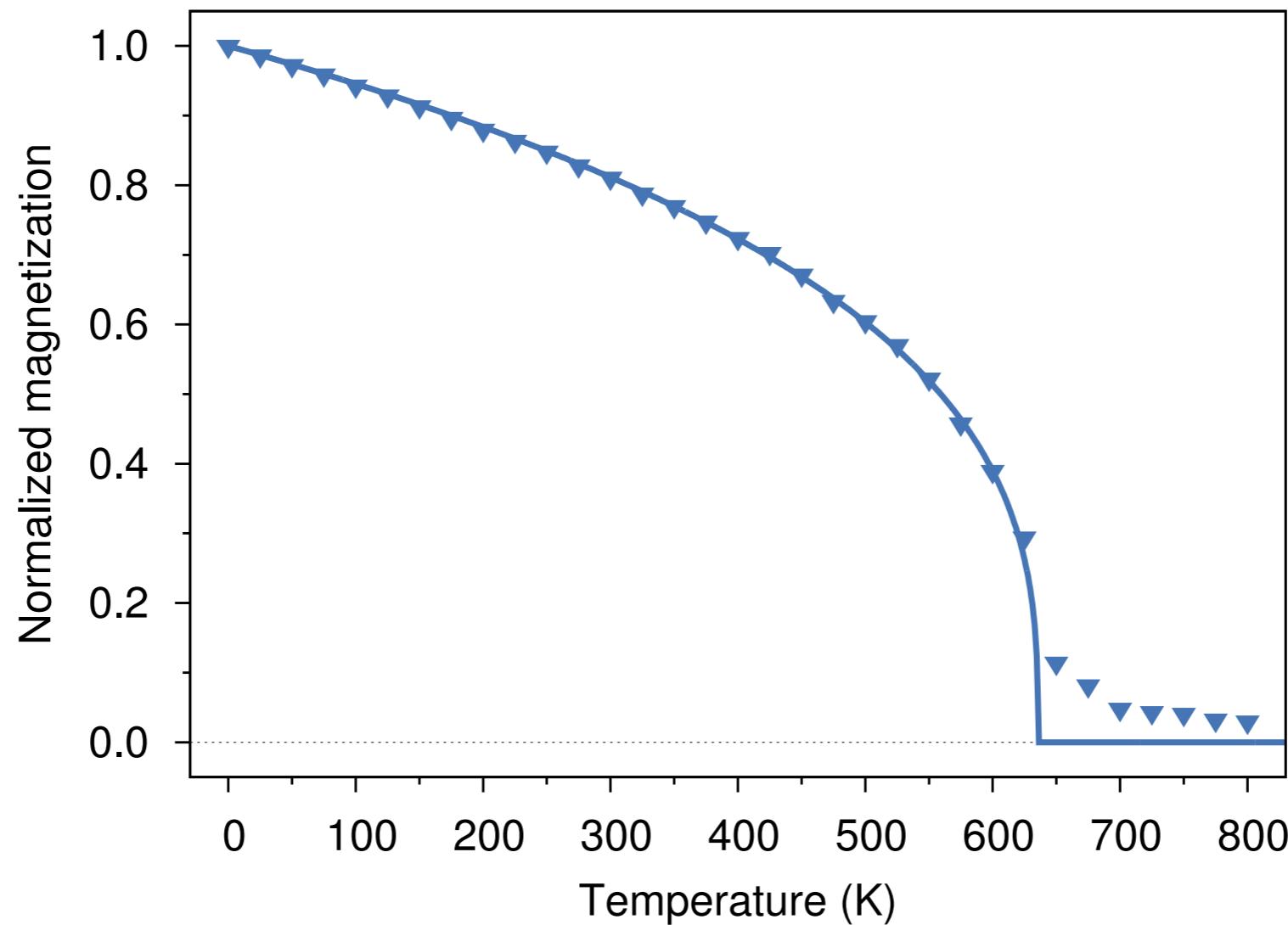
Different targets for different functionality

- serial
- parallel
- gcc-cuda

Combine compiler and version to compile code

- make serial
- make serial-llvm

Practical 2: Curie temperature



Create an input file

Step 1: choose your system type.

```
create:crystal-structure= sc  
                                bcc  
                                fcc
```

Step 2: choose your system size.

```
create:system-dimensions-x= X !nm  
create:system-dimensions-y= Y !nm  
create:system-dimensions-z= Z !nm
```

```
dimensions:unit-cell-size = 3.524 !A
```

Step 3: choose your simulation program.

curie-temperature

sim:program= field-cool
hysteresis

Step 4: choose your system size.

monte-carlo

sim:integrator= llg-heun
Constrained-monte-Carlo

Step 5: choose your simulation parameters.

temperature
sim: time-steps
List in manual

For a curie-temperature simulation

sim:maximum-temperature = X
sim:minimum-temperature = X
sim:temperature-increment = X
sim:loop-time-steps = X

Step 6: set outputs.

output: temperature
 magnetisation
 Real-time
 List in manual

Step 7: set material file

material:"material.mat"

```
#-----
# Creation attributes:
#-----
create:crystal-structure=sc

#-----
# System Dimensions:
#-----
dimensions:unit-cell-size = 3.54 !A
dimensions:system-size-x = 4 !nm
dimensions:system-size-y = 4 !nm
dimensions:system-size-z = 4 !nm

#-----
# Material Files:
#-----
material:file=Ni.mat

#-----
# Simulation attributes:
#-----

sim:minimum-temperature=0.0
sim:maximum-temperature=500.0
sim:temperature-increment=10
sim:loop-time-steps=30000

#-----
```

```
# Program and integrator details
#-----
sim:program=curie-temperature
sim:integrator=monte-carlo

#-----
# data output
#-----
output:real-time
output:temperature
output:magnetisation
```

Create a material file

Step 1: Choose your number of materials

```
material:num-materials= N
```

Step 2: Set material parameters for each N materials:

```
material[N]:exchange-matrix[N] = J
```

```
material[N]:damping-constant = d
```

```
material[N]:atomic-spin-moment = mu
```

```
material[N]:uniaxial-anisotropy-constant = ku
```

```
material[N]:material-element=N
```

```
material[N]:material-name = Name
```

Spin Hamiltonian for Ni

$$\mathcal{H} = - \sum_{i < j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j - \sum_i k_u S_{i,z}^2$$

```
#-----
# Number of Materials
#-----
material:num-materials=1
#-----
# Material 1 Nickel Generic
#-----
material[1]:material-name=Ni
material[1]:damping-constant=0.01
material[1]:exchange-matrix[1]=2.757e-21
material[1]:atomic-spin-moment=0.606 !muB
material[1]:uniaxial-anisotropy-constant=5.47e-26
material[1]:material-element=Ni
```

Running Vampire

```
rfle500@MacPro:~$ vampire
```



Version 3.0.3 Aug 4 2014 21:00:13

Licensed under the GNU Public License(v2). See licence file for details.

Lead Developer: Richard F L Evans <richard.evans@york.ac.uk>

Contributors: Weijia Fan, Phanwadee Chureemart, Joe Barker,
Thomas Ostler, Andreas Biernas, Roy W Chantrell

Compiled with: GNU C++ Compiler
Compiler Flags:

```
=====
```

Mon Aug 4 21:56:21 2014

```
=====
```

Initialising system variables
Creating system

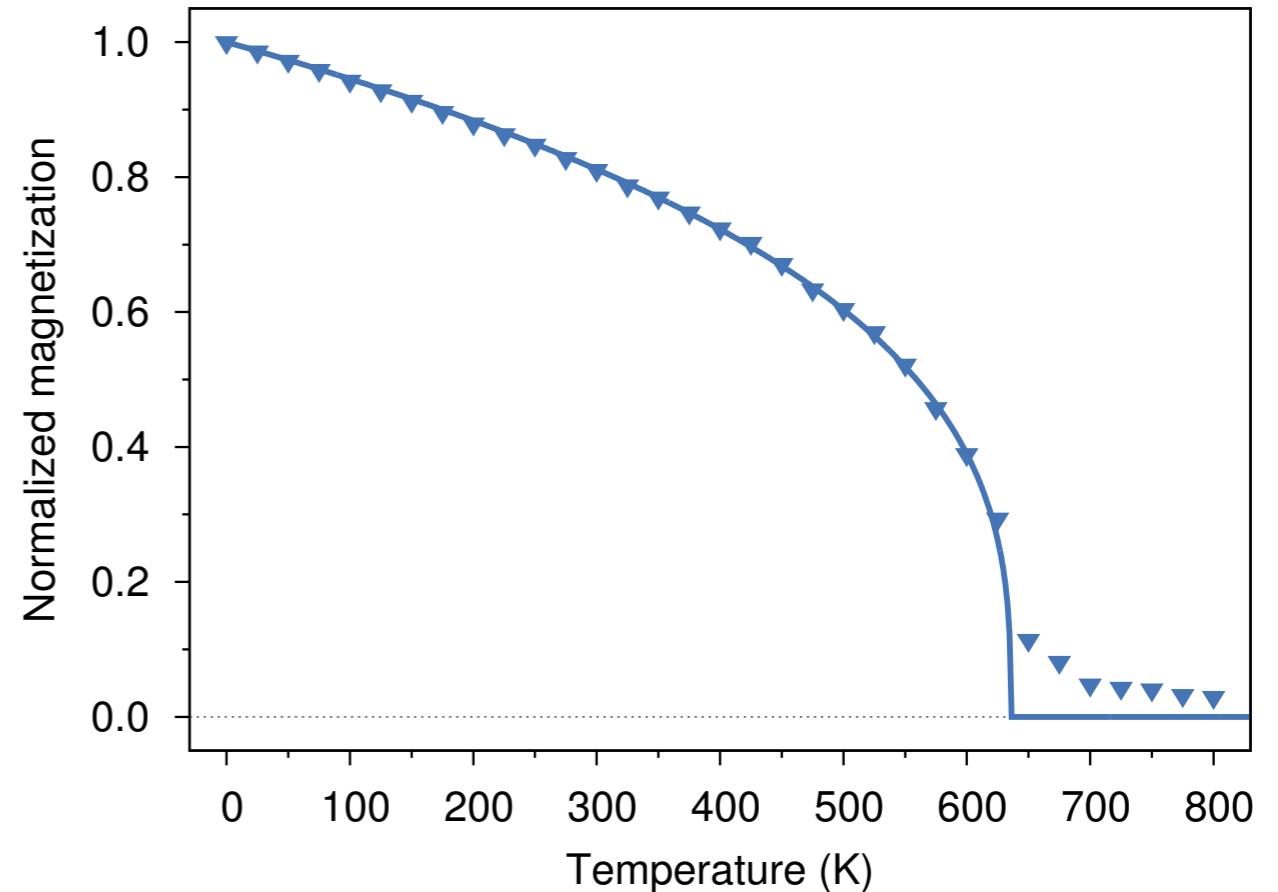
Curie temperature calculation

Calculate phase transition in Ni

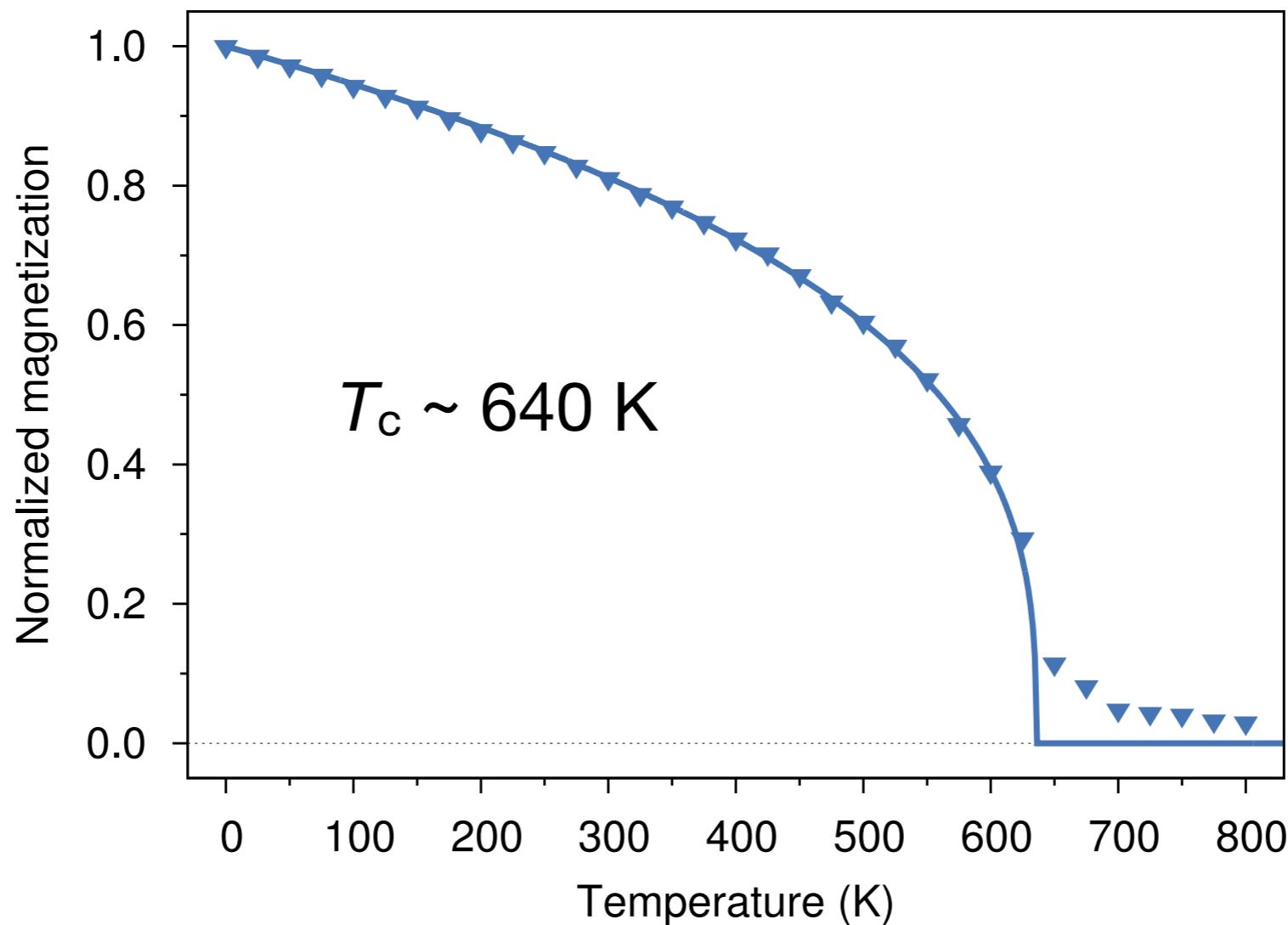
Essential temperature dependent property of a magnetic material

$$\mathcal{H} = - \sum_{i < j} J_{ij} \mathbf{S}_i \cdot \mathbf{S}_j$$

$$J_{ij} = \frac{3k_B T_c}{\gamma z}$$



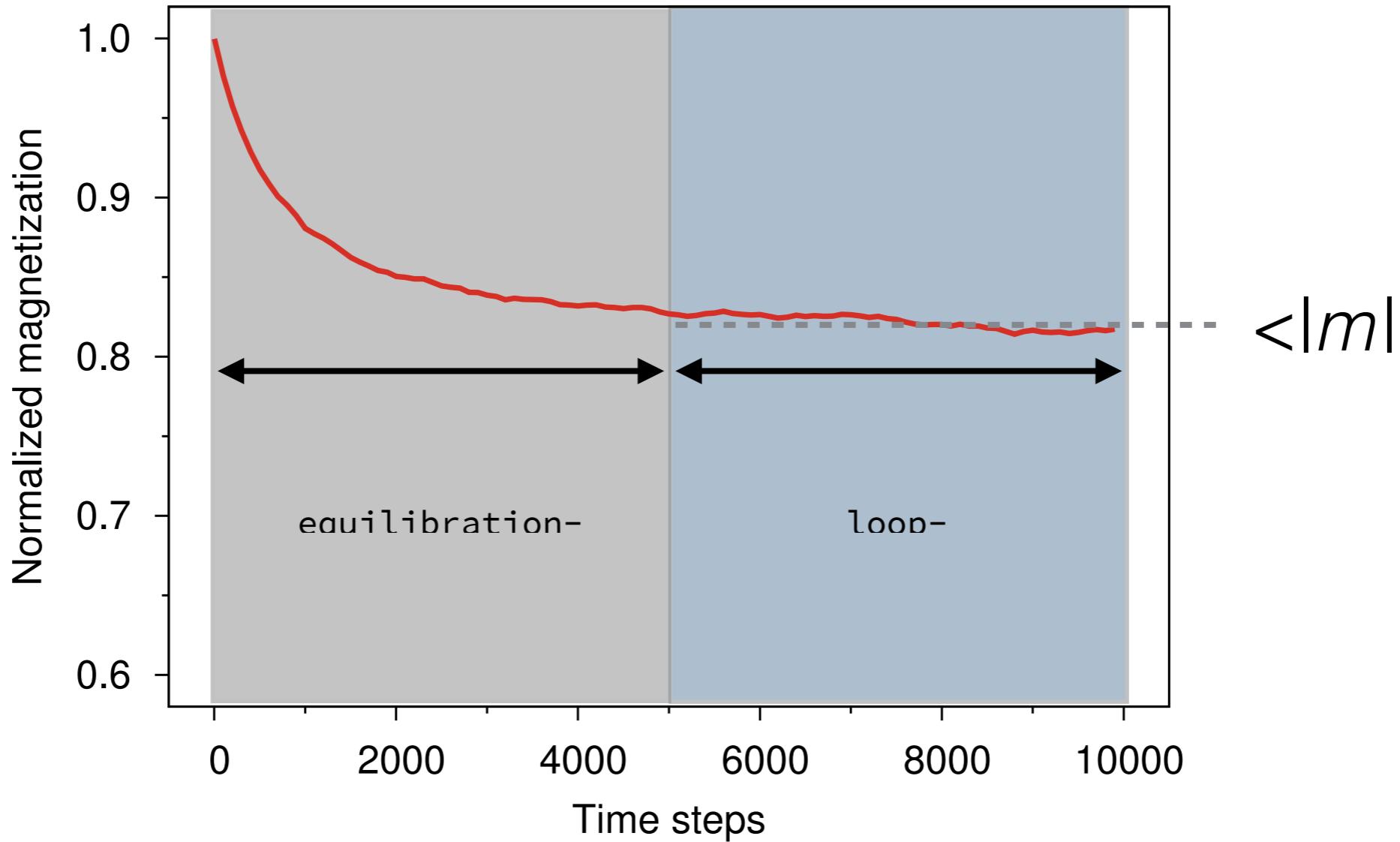
Curie temperature calculation



$$m(T) = \left[1 - \left(\frac{T}{T_c} \right) \right]^\beta$$

Challenge: reproduce and $M_s(T)$ curve for Nickel

Equilibrating the system

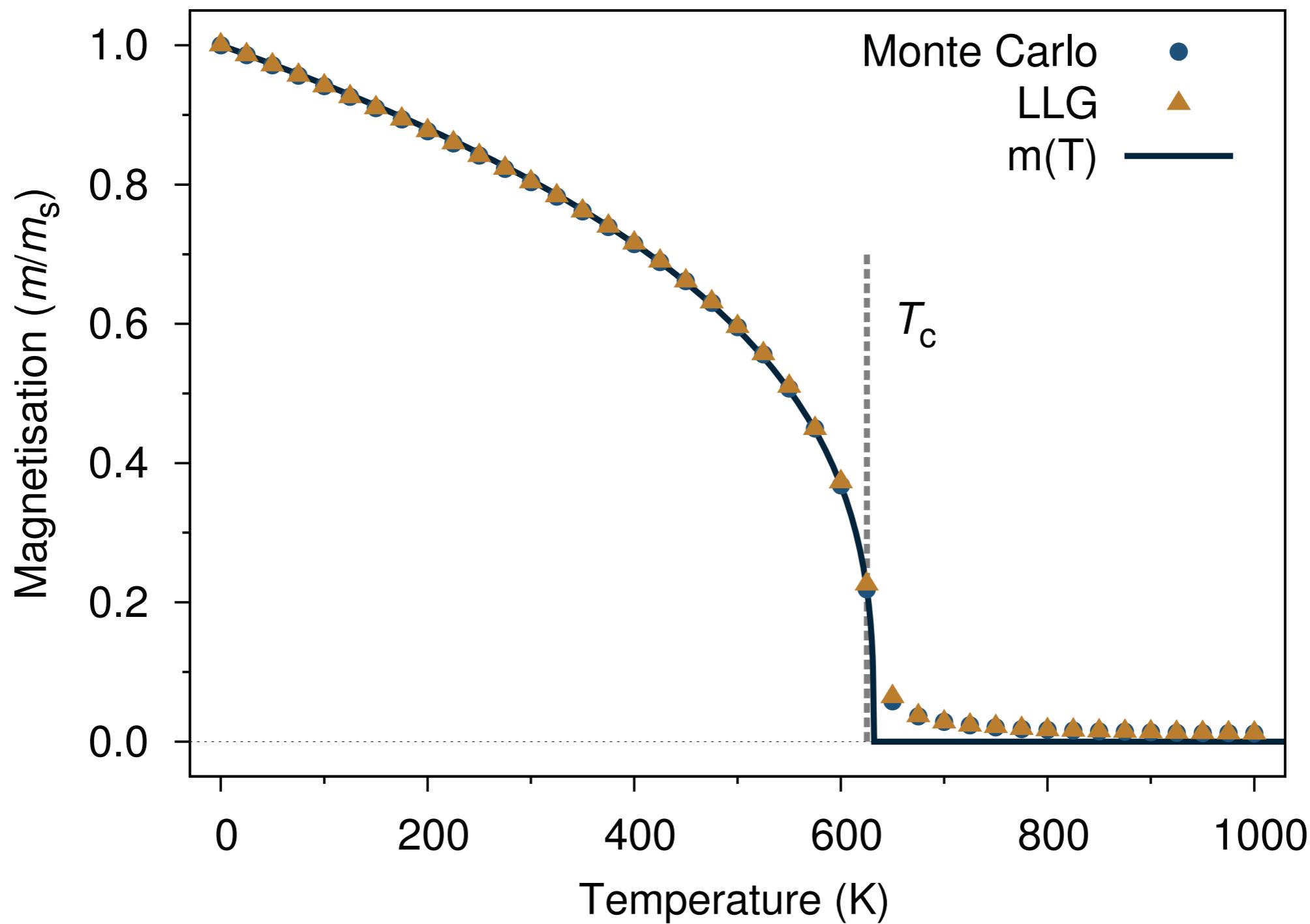


Sim:equilibration-time-steps
sim:equilibration-temperature

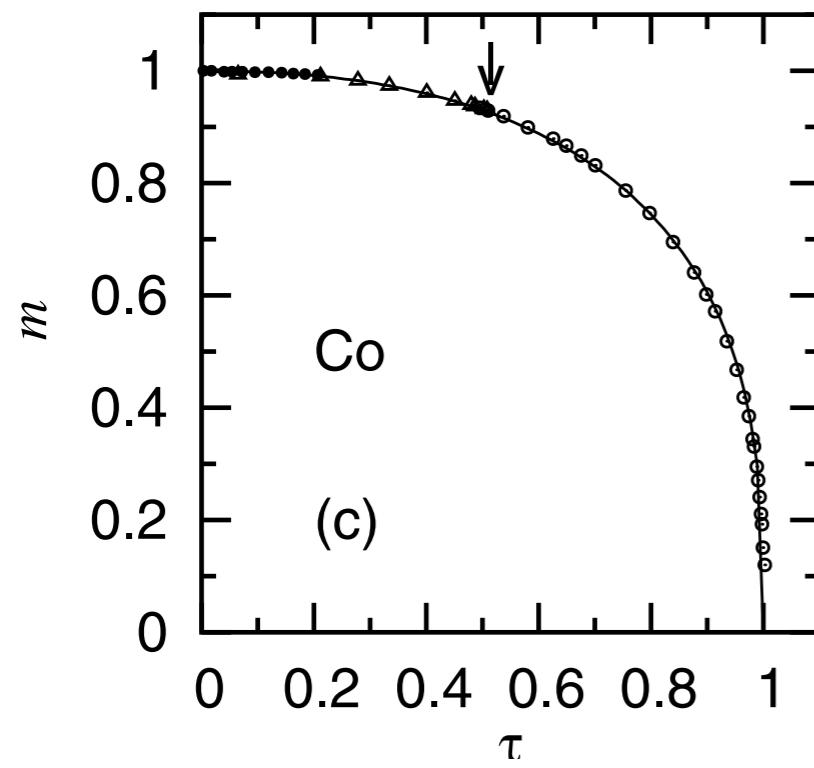
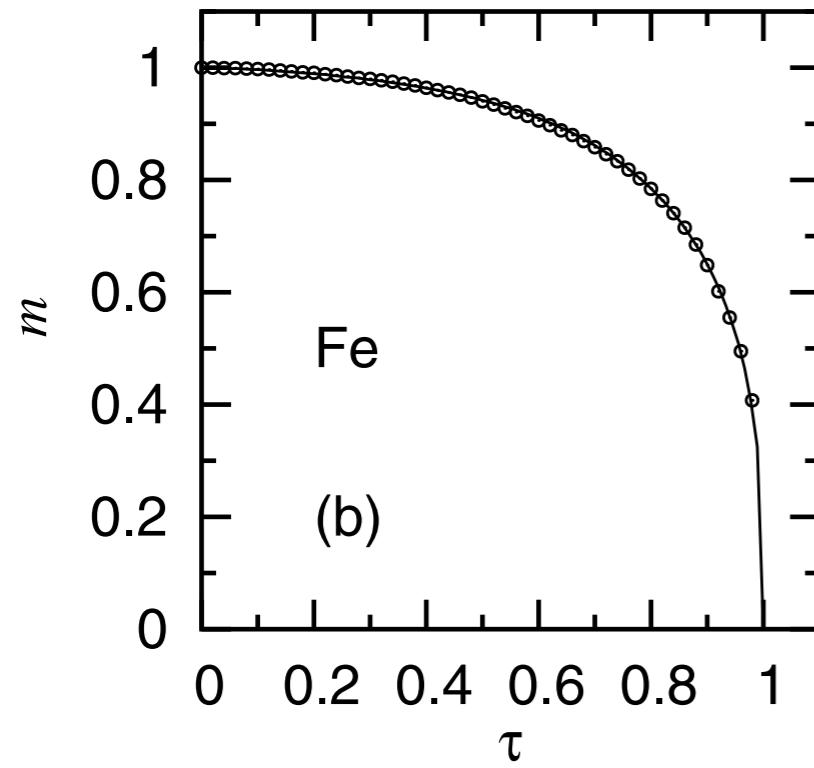
**Challenge: reproduce and $M_s(T)$ curve for Nickel
With an equilibration**

Spin temperature rescaling

Classical spin model $m(T)$ simulation



Real ferromagnets: Kuz'min equation



$$m(\tau) = [1 - s\tau^{3/2} - (1 - s)\tau^p]^{1/3}$$

Real ferromagnets very
different from classical model
→ problem!

Phenomenological temperature rescaling

Classical model

$$m(T) = (1 - T/T_c)^\beta$$

Assume $m(T)$ well fitted by Curie-Bloch equation

$$m(\tau) = (1 - \tau^\alpha)^\beta$$

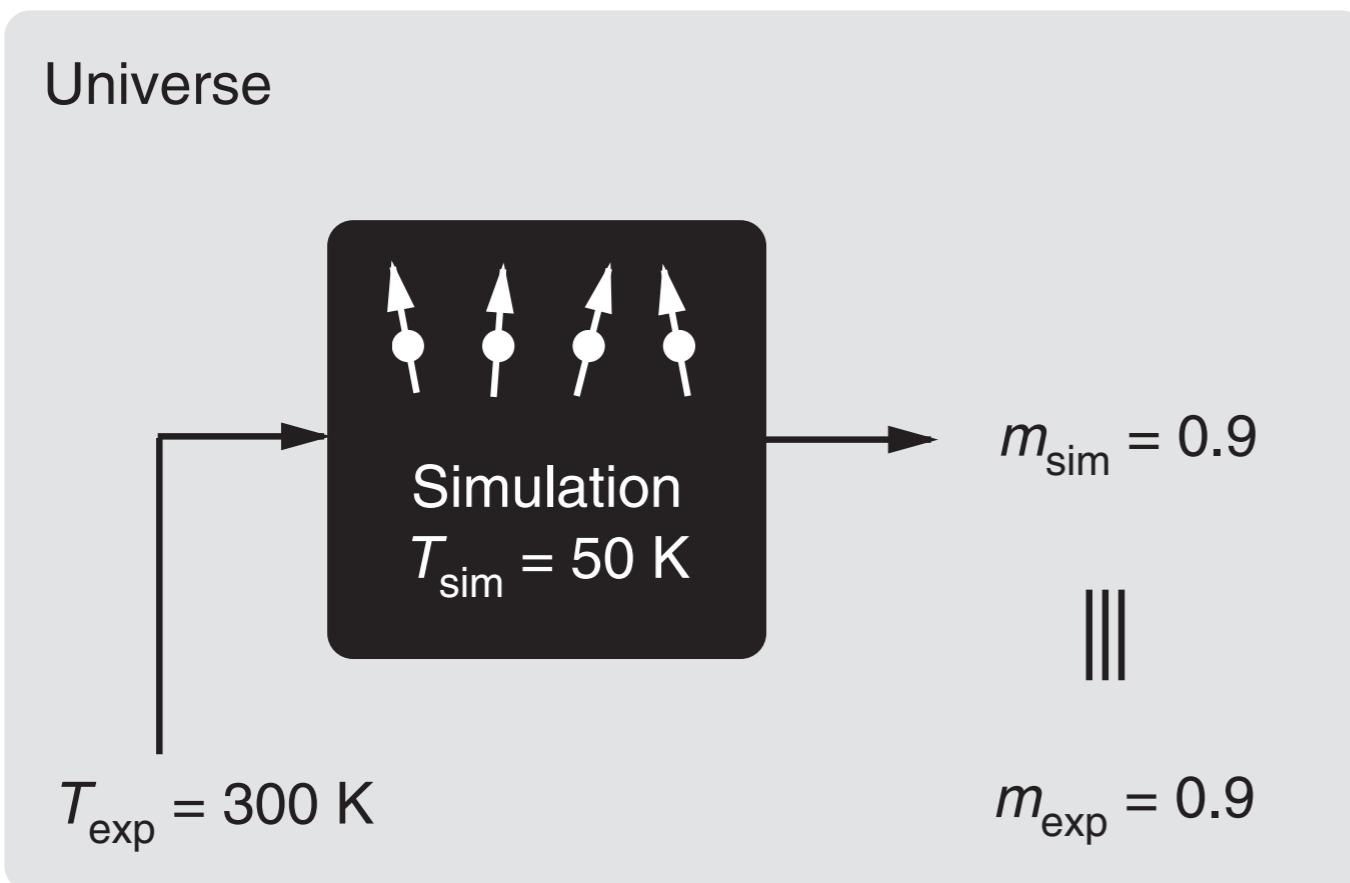
Classical model: $\alpha = 1$

Real ferromagnets: $\alpha \neq 1$

Simplest rescaling:

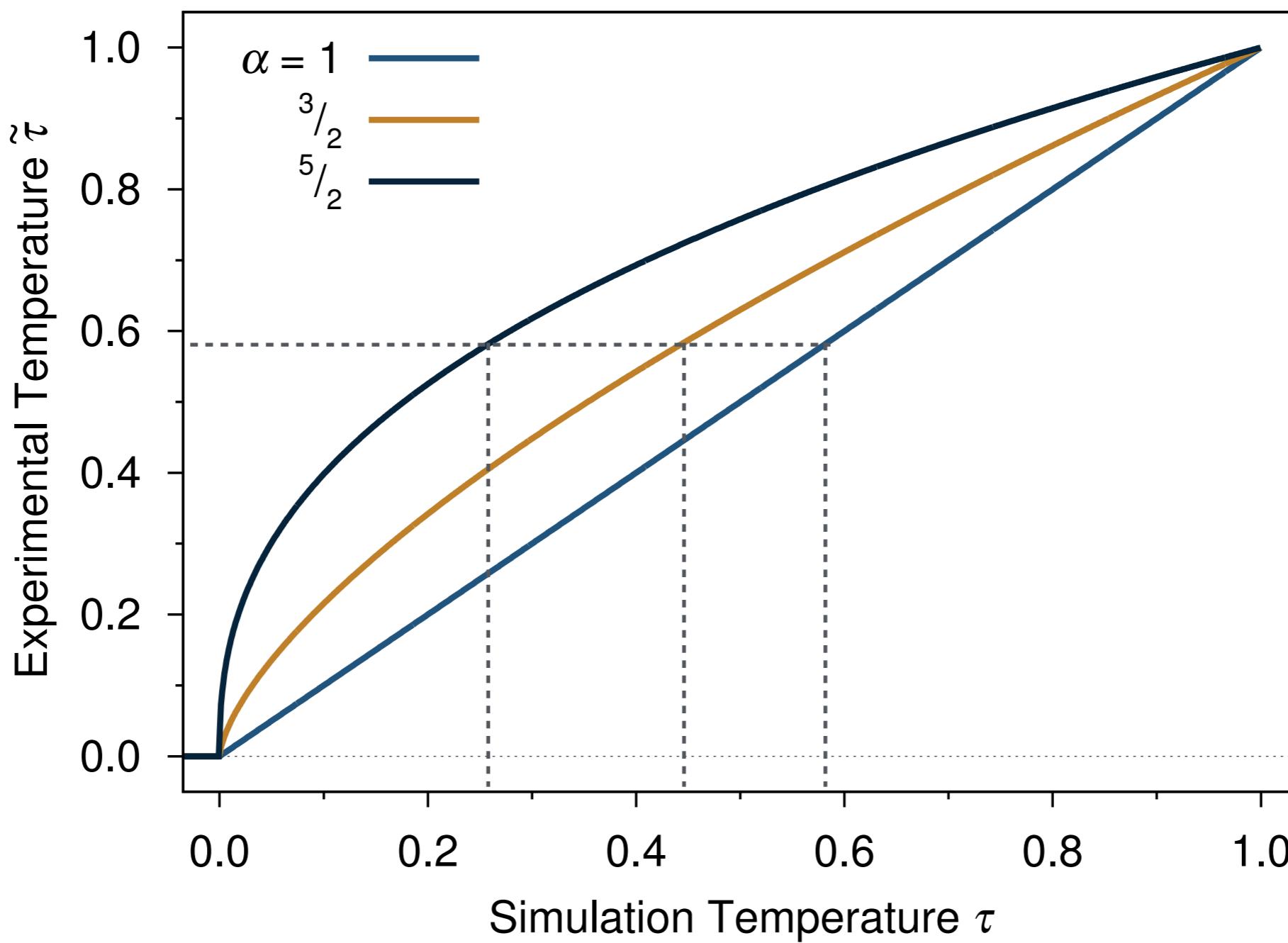
$$\tilde{\tau} = \tau^{\frac{1}{\alpha}}$$

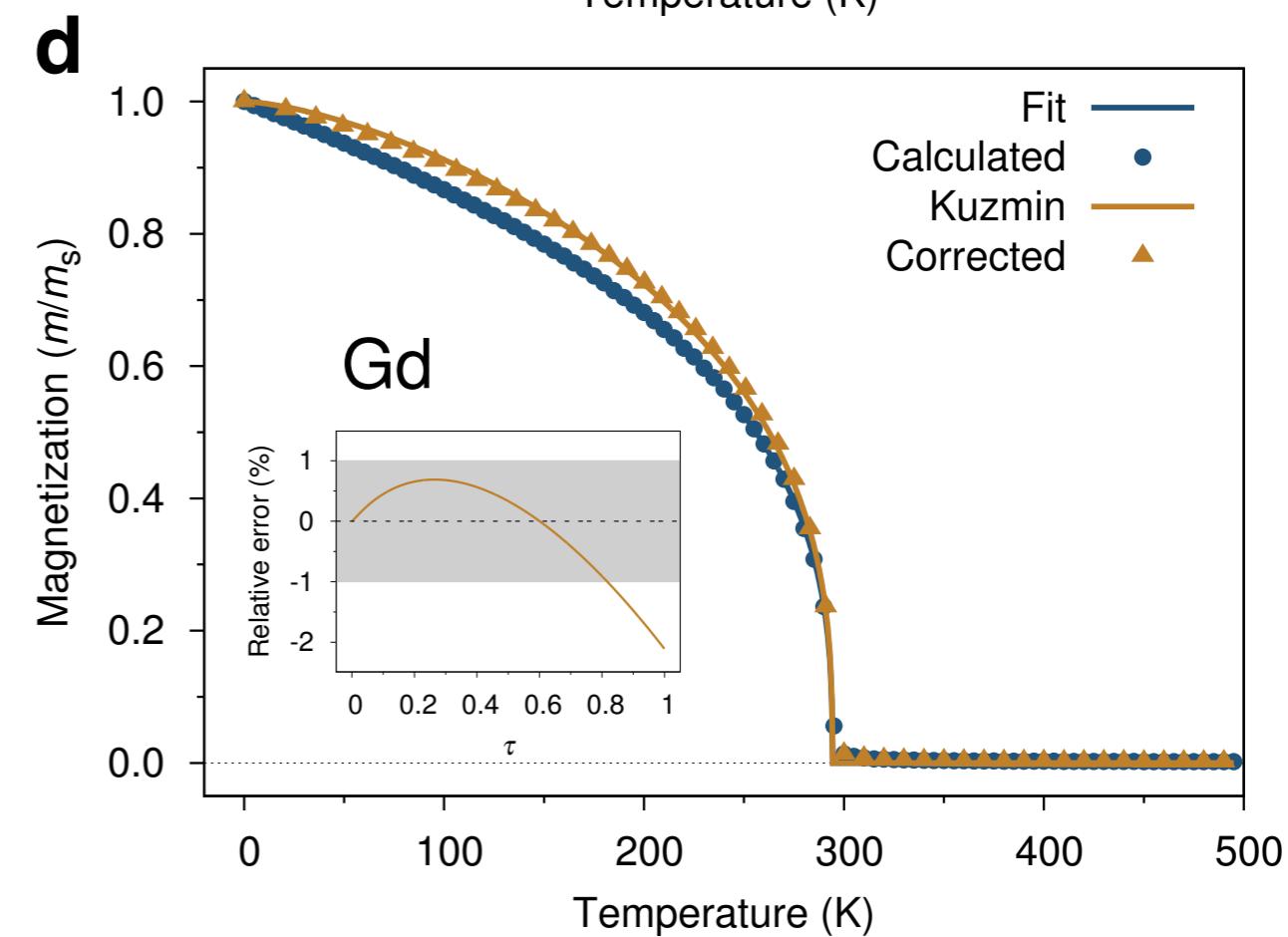
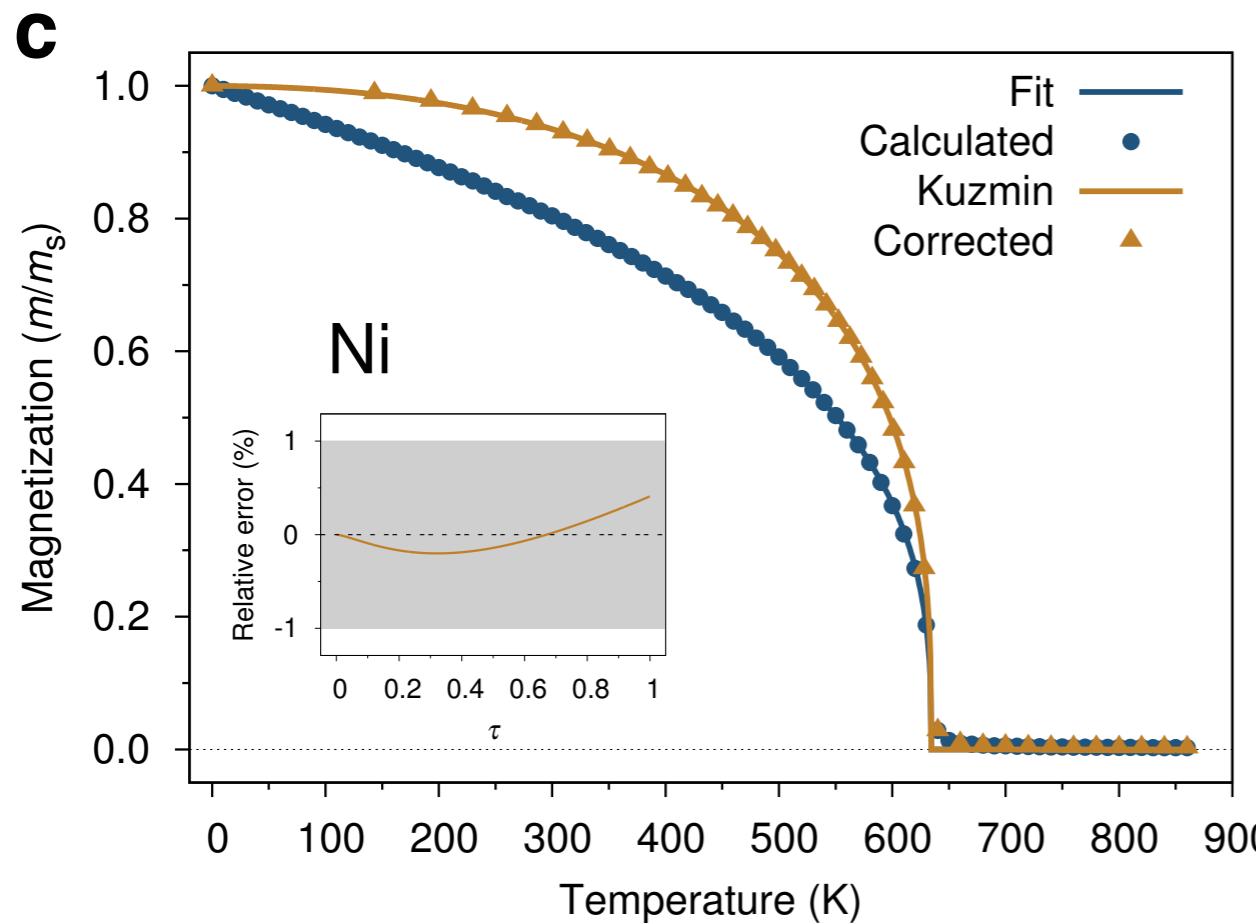
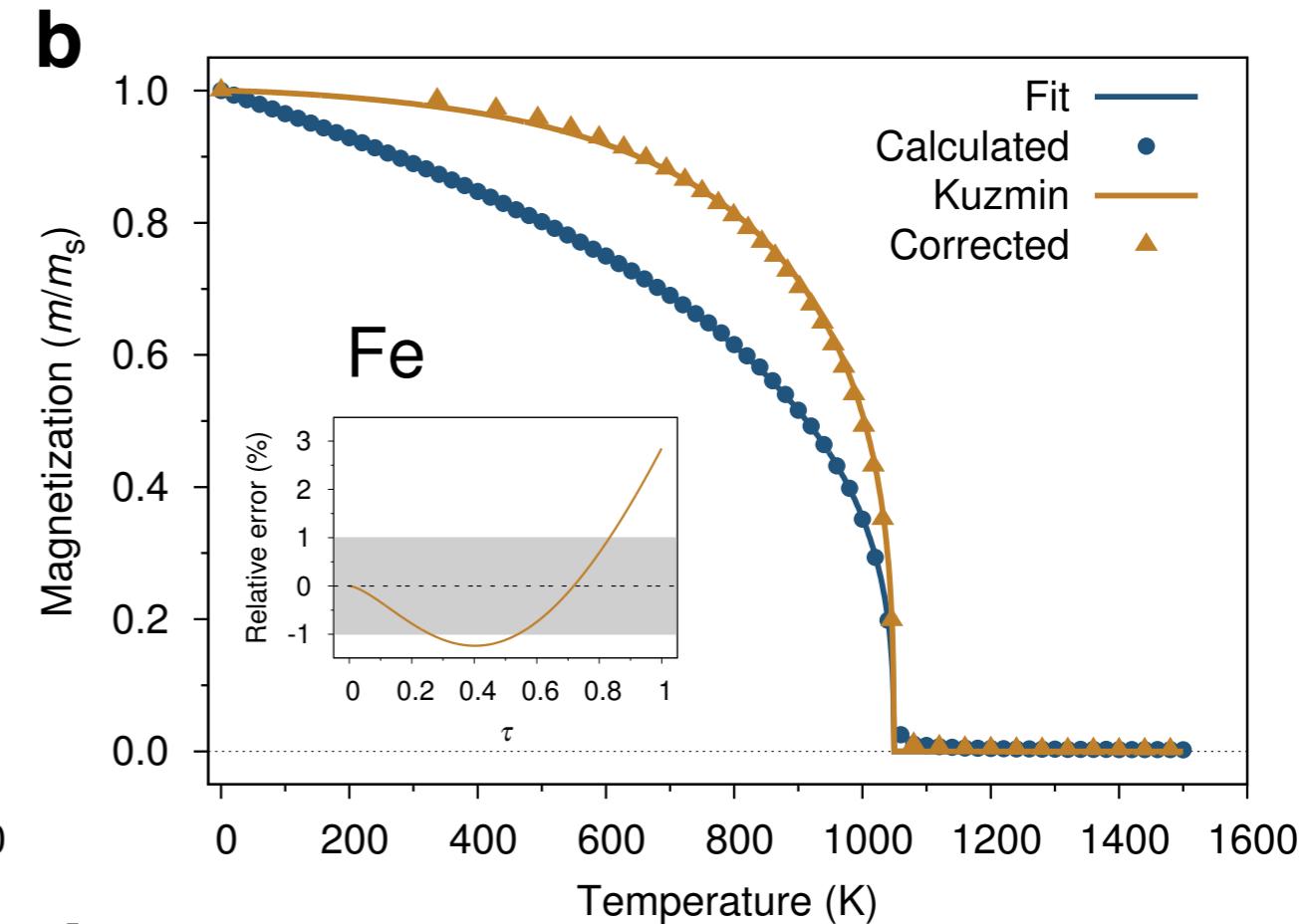
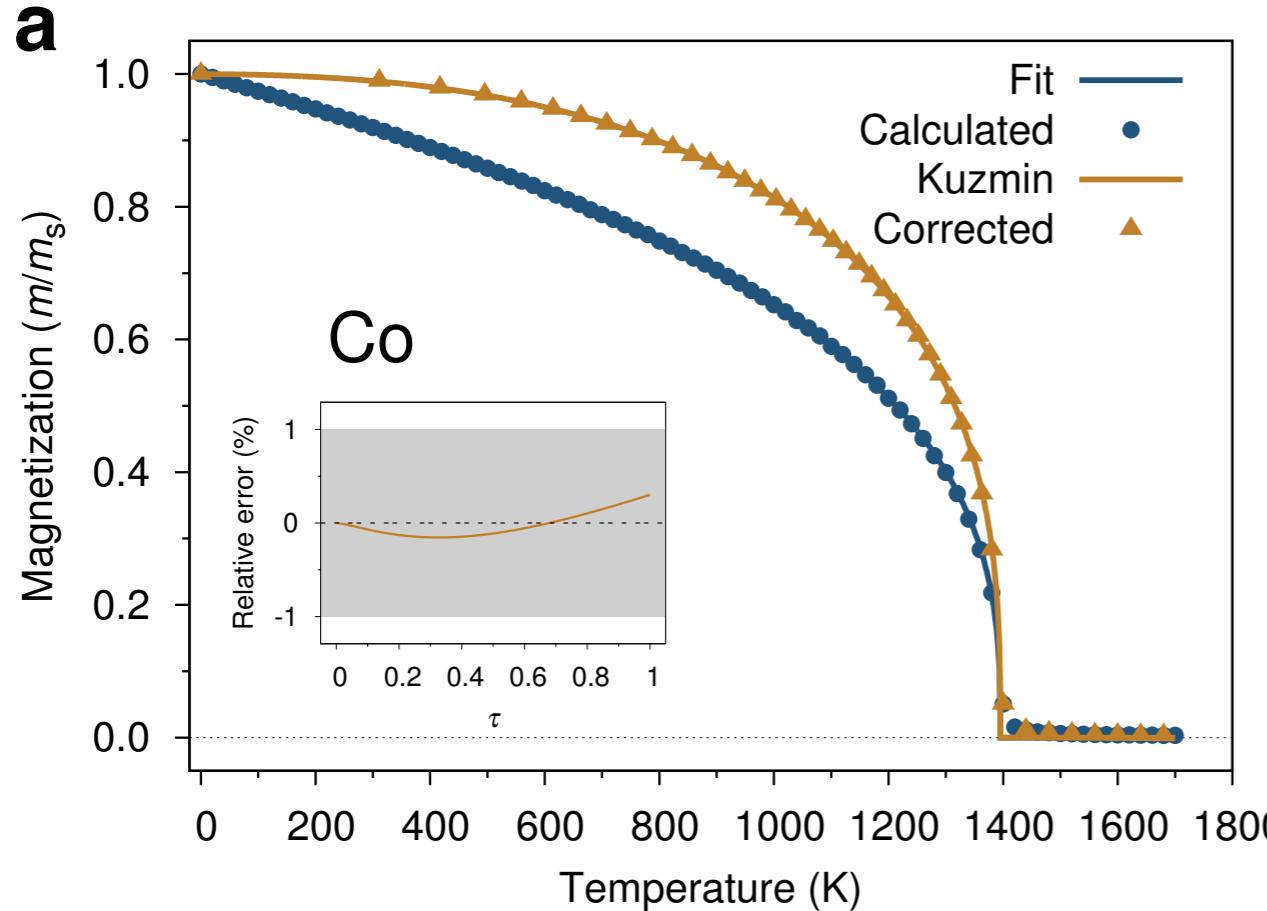
Spin temperature rescaling (STR) method



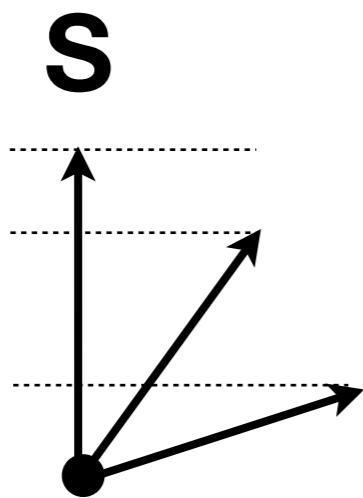
$$\frac{T_{\text{sim}}}{T_{\text{c}}} = \left(\frac{T_{\text{exp}}}{T_{\text{c}}} \right)^{\alpha}$$

Spin temperature rescaling (STR) method

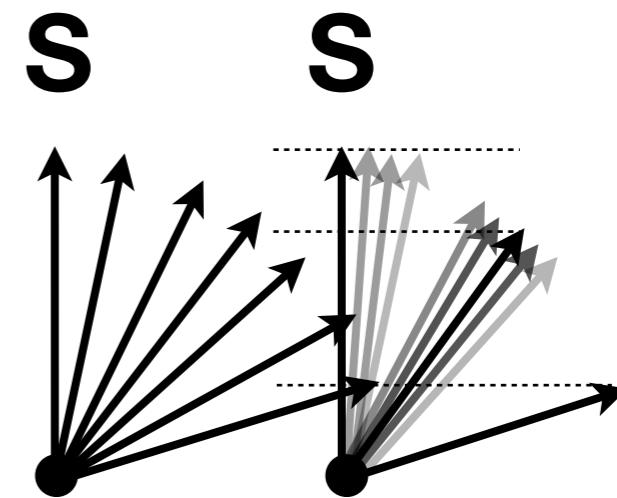




Physical picture of temperature rescaling



Quantum



Classical Rescaled

Stochastic spin dynamics with rescaled temperature

$$\mathbf{H}_{\text{eff}}^i = - \frac{1}{\mu_s} \frac{\partial \mathcal{H}}{\partial \mathbf{S}_i} + \mathbf{H}_{\text{th}}^i$$

$$\mathbf{H}_{\text{th}}^i = \boldsymbol{\Gamma}(t) \sqrt{\frac{2\lambda k_{\text{B}} T_{\text{sim}}}{\gamma_e \mu_s \Delta t}}$$

Applying spin temperature rescaling in VAMPIRE

```
material[1]:temperature-rescaling-exponent=2.322  
material[1]:temperature-rescaling-curie-temperature=635.0
```

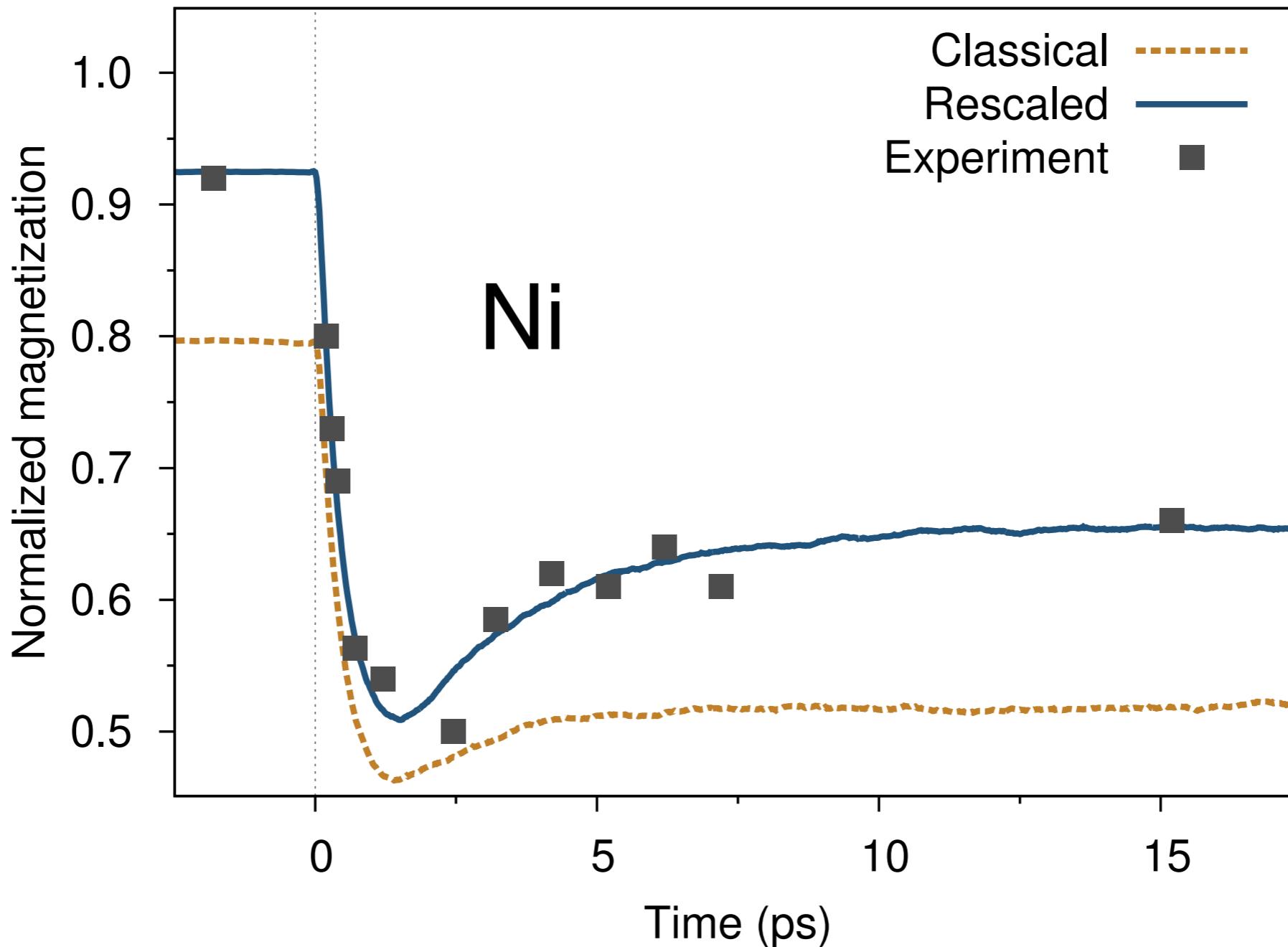
Downsides:

Need to know Cure temperature in advance

Very tricky for more than one sublattice since Tc depends on rescaling -> iterative process

Quantum statistics for a heat bath is the natural solution but has its own complexities...

Ultrafast demagnetization in Ni

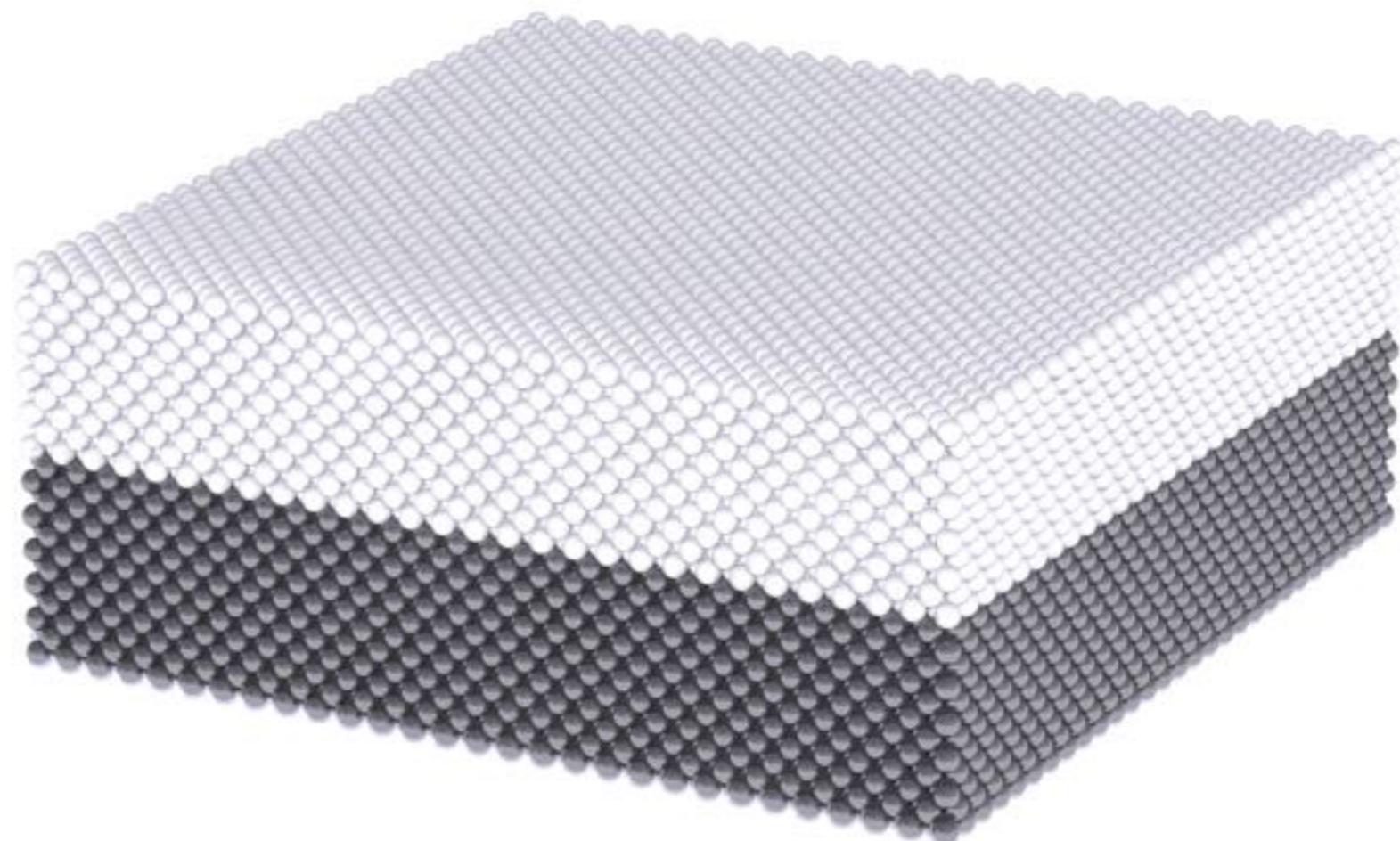


E. Beaurepaire *et al*, Phys. Rev. Lett. **76**, 4250 (1996)

R. F. L. Evans *et al*, Phys. Rev. B **91**, 144425 (2015)

Challenge: reproduce and $M_s(T)$ curve for Nickel including temperature rescaling

Practical 3: System Generation

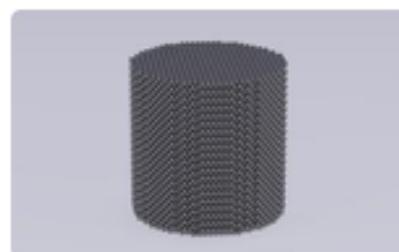


<http://vampire.york.ac.uk/tutorials/>

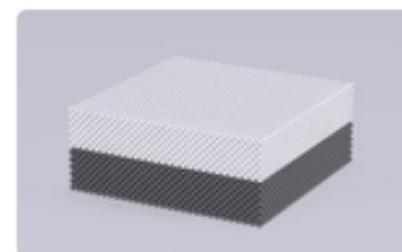
Tutorials

Vampire is a large software package with a lot of options, and so the following tutorials give a brief introduction to using Vampire. As time allows more tutorials will be added here.

Introductory



System generation

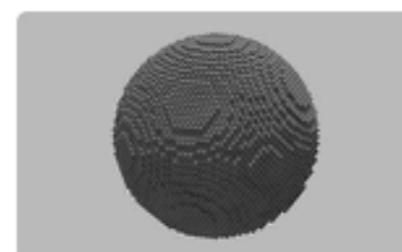


Bilayer

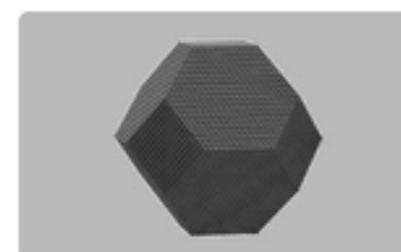
System generation



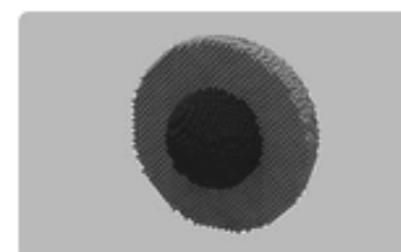
Crystal structures



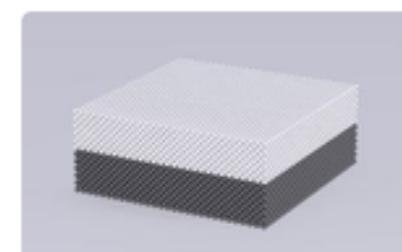
Sphere



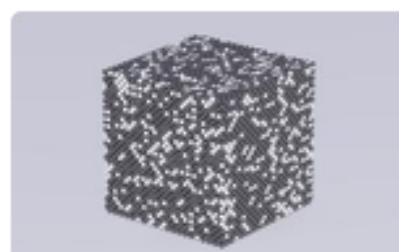
Truncated octahedron



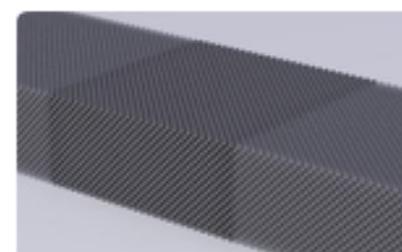
Core-shell



Multilayers



Random alloys



Periodic boundaries

View your structures with rasmol

Compile vdc (VAMPIRE data convertor) utility

```
make vdc
```

Run the vdc utility

```
/path/to/vdc/vdc
```

View the generated structure with rasmol

```
rasmol -xyz crystal.xyz
```

Enable configuration output

Enable output with default parameters

```
config:atoms
```

Change output rate (as multiple of main data output rate)

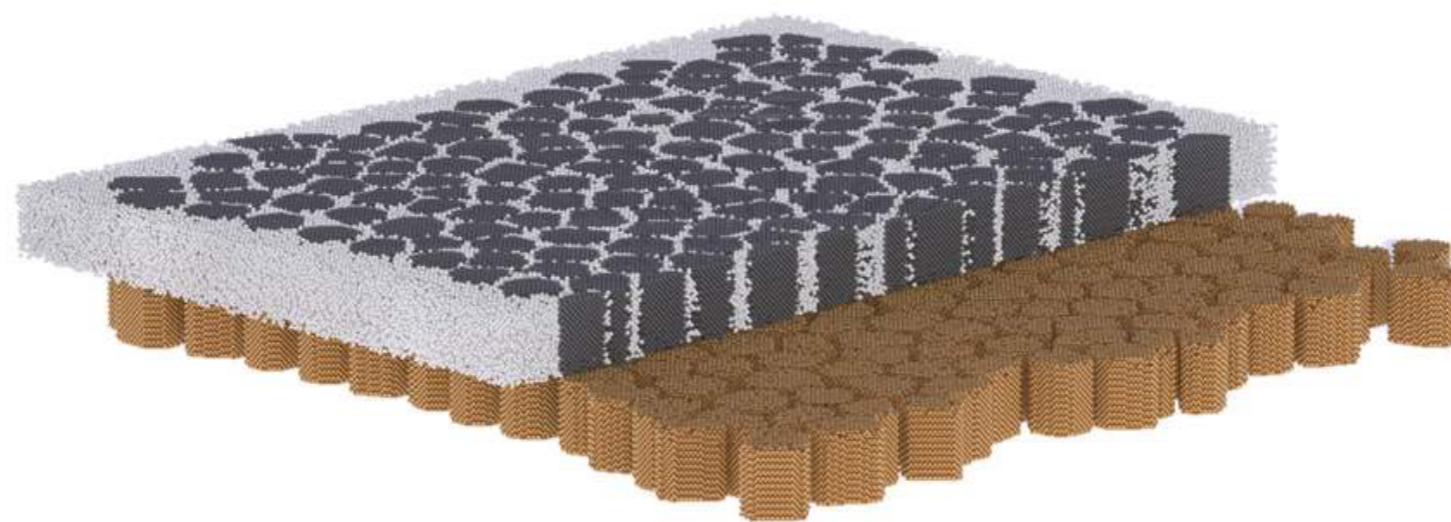
```
config:atoms-output-rate = 100
```

Select slices of the data

```
config-atoms
```

Challenge: generate a single material structure, a bilayer and core-shell structure

Challenge: generate a voronoi grain structure



create:voronoi-film

create:voronoi-rounded-grains

dimensions:particle-size = 6.0 !nm

dimensions:particle-spacing = 1.0 !nm

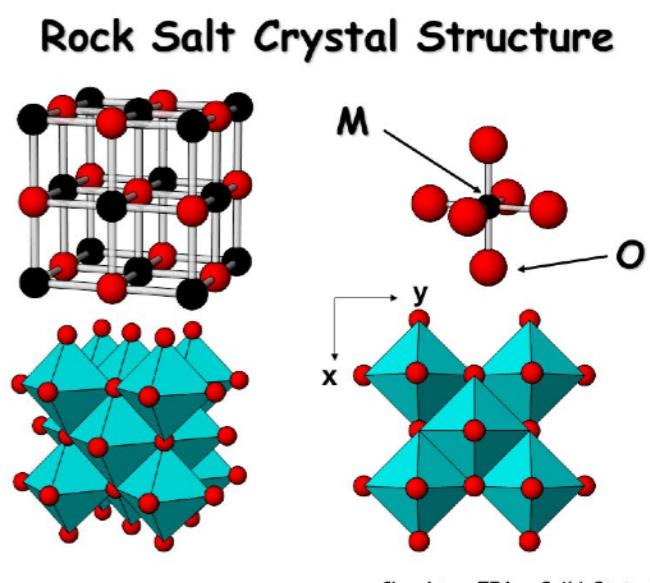
(Also compatible with multilayers/core shell structures)

Unit cells with more than one material

Develop branch has new feature better supporting unit cells (and unit cell files) with more than one material

Example Rocksalt (CsCl) structure now built-in

```
create:crystal-structure = rocksalt
```



Associate different materials in unit cell with different materials in VAMPIRE

```
material[1]:unit-cell-category = 1  
material[2]:unit-cell-category = 2
```

Non-magnetic materials

Develop branch now has support for non-magnetic atoms for improved visualisation and also effects such as SO coupling

Can identify a material as non-magnetic (removed from simulation)

```
material[1]:non-magnetic = remove
```

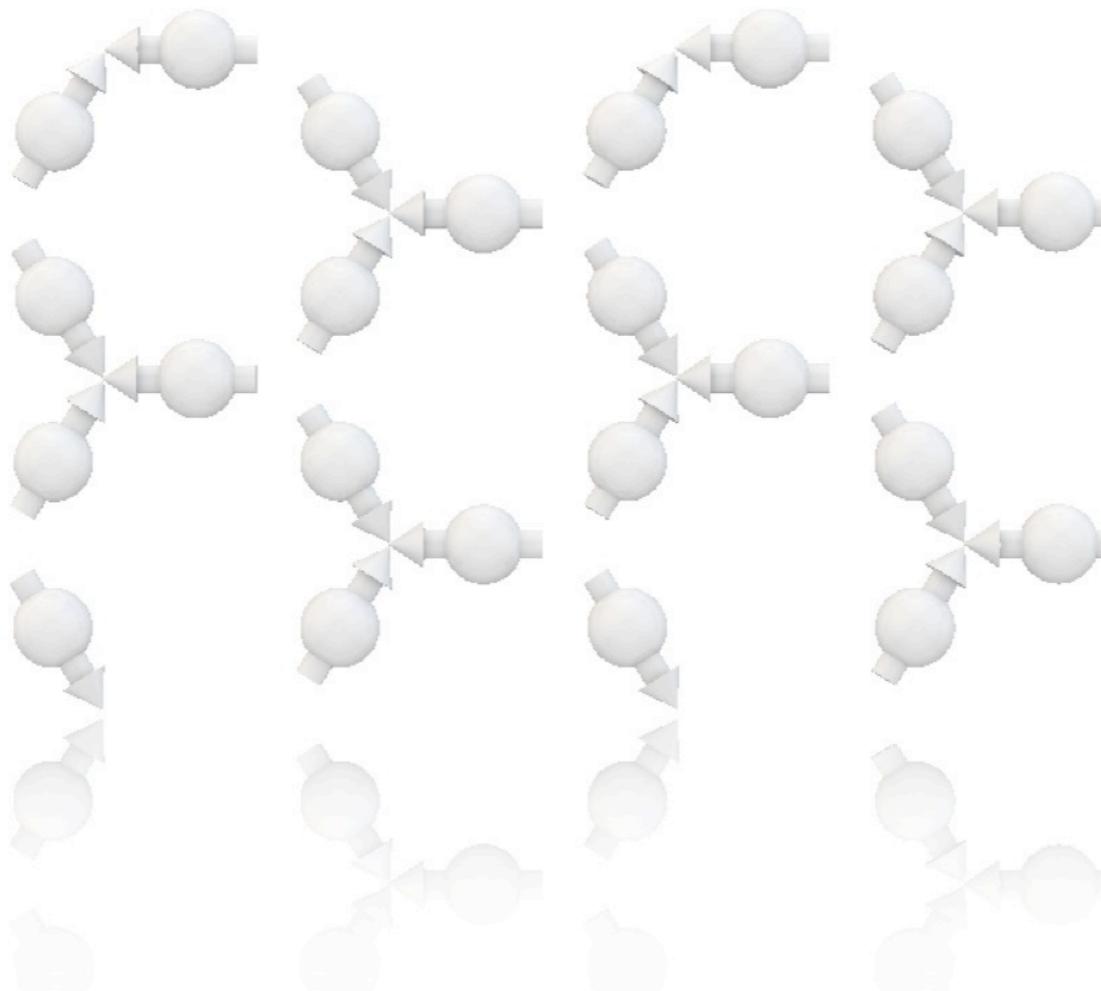
Or non-magnetic (keep in simulation but not in statistics/dipole)

```
material[1]:non-magnetic = keep
```

Using vdc utility removed atoms are retained for visualisation

**Challenge: generate a core-shell nanoparticle
with a multiple material unit cell**

Practical 4: Statistics



Magnetization statistics

VAMPIRE contains a range of methods for calculating statistical properties

Can output total magnetization specified in input file

output:magnetisation

Data output is in 4 columns (unit vector and length)

$\hat{m_x}$ $\hat{m_y}$ $\hat{m_z}$ | m |

Can control rate of output as a multiple of increment

output:output-rate = 10

Average statistics

Average (mean) data can also be selected (seen earlier)

output:mean-magnetisation-length

Generally want a time step increment of 1-5 (rate at which statistics are calculated)

Time series calculations produce a running average (useful for convergence)

Loop calculations produce average at end of loop increment (temperature, field etc)

Material/height statistics

Can slice magnetization data by material and/or height

output:magnetisation

output:material-magnetisation

output:height-magnetisation

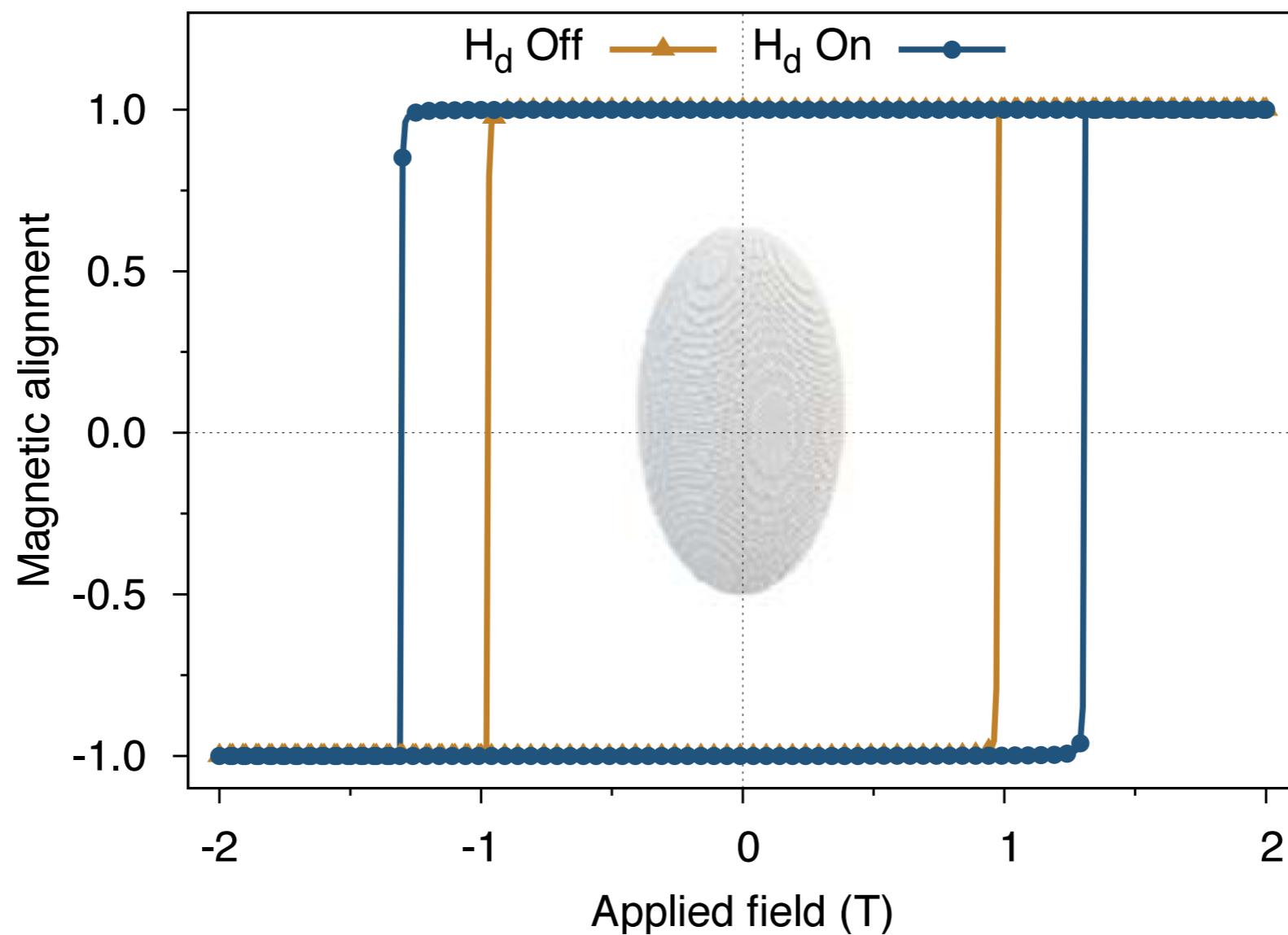
output:height-material-magnetisation

Very useful for analysing sublattice magnetization in the case of multiple materials or domain wall processes

Challenge:

Calculate sublattice $M(T)$ curves for rock salt structure with two materials and different exchange constants

Practical 5: Hysteresis simulations



Hysteresis calculations

Generally a ‘slow’ process - typically 10s of nanoseconds

For comparison with experiment, use high damping limit, $\lambda = 1$

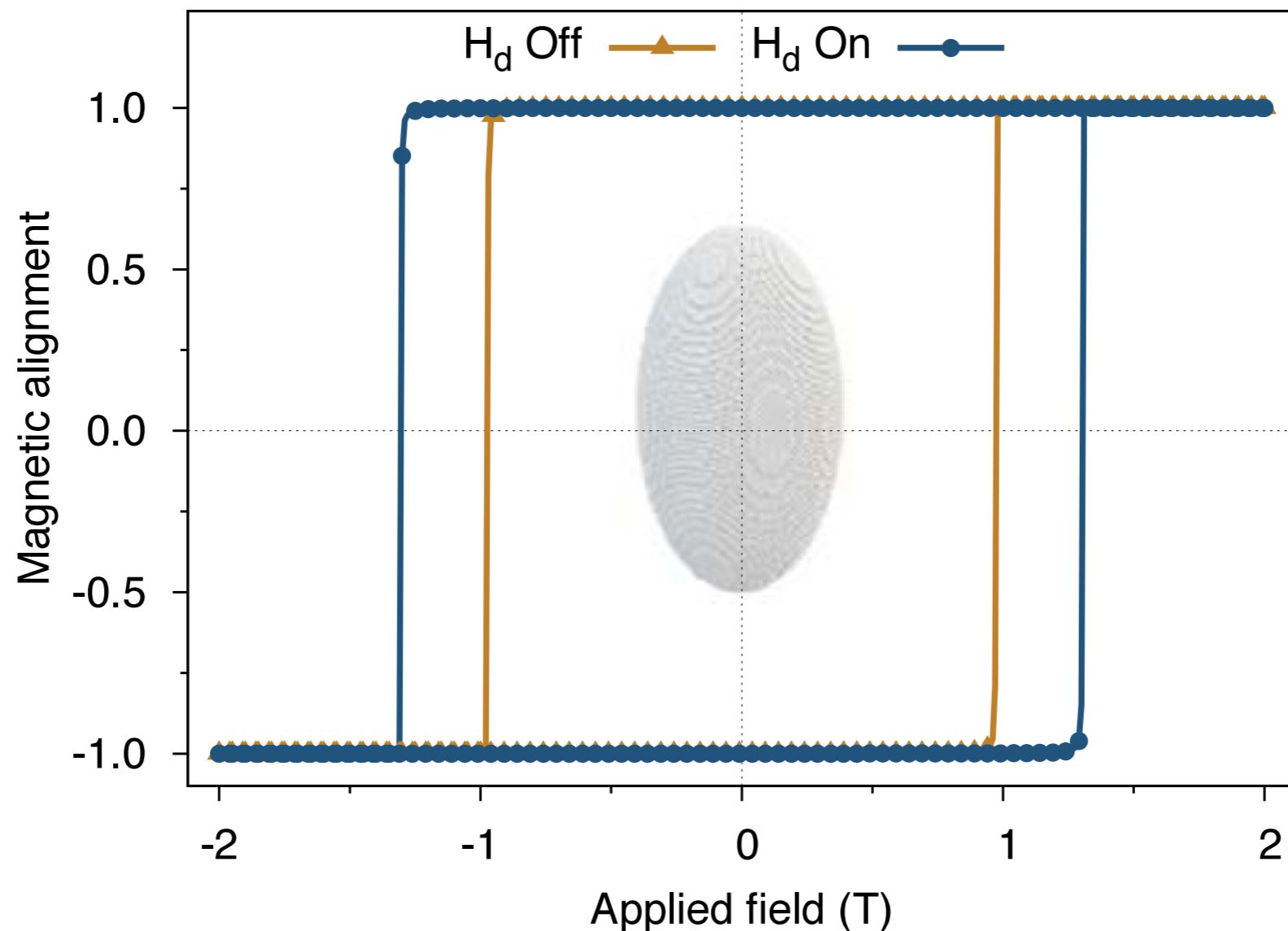
Coercivity **strongly** field rate dependent - slower is better!

input file

```
sim:loop-time-steps=100000
sim:program=hysteresis-loop
sim:integrator=llg-heun
sim:time-step=1.0e-15
sim:temperature = 0
sim:equilibration-applied-field-strength = 2.0 !T
sim:maximum-applied-field-strength = 2.0 !T
sim:applied-field-strength-increment = 0.01 !T
Sim:applied-field-unit-vector = 0,1,0
```

```
output:real-time
output:applied-field-strength
output:applied-field-alignment
output:magnetisation
```

hysteresis-loop program



Cycles field from $+H_{\max}$ to $-H_{\max}$ in a user defined increment

Calculates dynamic response of the magnetisation to the field

Challenge:

**Generate $M(H)$ curves for a $(1 \text{ nm})^3$ sample at 0K
for different field rates, anisotropy and damping**

Questions

What happens to the hysteresis loop if you change loop-time?

How many steps (field rate) do you need to reach the limit $H_c = 2k_u/\mu_s$

What effect does changing the field angle have?

What effect does the damping have?