

7  
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a and b) For the sorting algorithm, I implemented merge sort. I used arrays in my implementation, so I had to create the initial array from the linked list and then convert the sorted array into a linked list.

Merge sort is  $O(n \log n)$  for the worst, average, and best cases. Converting from a linked list to array would be  $O(n)$  since we would need to iterate through the linked list to add the nodes to the array. To transfer from array to linked list again would be  $O(n)$  since we would need to iterate through the array to add the nodes back to the linked list, which luckily the `addLast` method is  $O(1)$ . But for a big enough  $n$ , only the run time for merge sort matter, so it will be  $O(n \log n)$ .

Pseudocode:

```
arr = []
while list.hasNext():
    arr.push(list.next)

sorted_arr = merge_sort(arr)

while sorted_arr:
    list.add(sorted_arr)

def merge_sort(arr):
    if arr.len <= 1:
        return arr

    for i = 0; i < arr.len/2; i++:
        left[] = arr[i]

    mid = arr.len / 2
    for i = 0; i < arr.len - mid; i++:
        right[] = arr[mid + i]

    left = merge_sort(left)
    right = merge_sort(right)

    return merge(left, right)

def merge(left, right):
    result = []

    while !left.empty and !right.empty:
        if left.current >= right.current:
            result.push(left.pop_current())
        else:
            result.push(right.pop_current())

    while !left.empty:
        result.push(left.pop_current())

    while !right.empty:
        result.push(right.pop_current())

    return result
```

c)

I tried to use the `Java System.nanoTime()` method to do benchmarks, but it gave me inconsistent results. I think this is due to the JVM.

```
Run 0
Count: 1000    Time: 8316000 ns
Count: 10000   Time: 98831000 ns
Count: 100000  Time: 358395000 ns
```

```
Run 1
Count: 1000    Time: 284000 ns
Count: 10000   Time: 9781000 ns
Count: 100000  Time: 56893000 ns
```

```
Run 2
Count: 1000    Time: 316000 ns
Count: 10000   Time: 3099000 ns
Count: 100000  Time: 104849000 ns
```

8  
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a and b) The best case scenario for the `add` method is adding nodes to the head of the list. The node should be added to the head in  $O(1)$  time. The average and worse cases would be  $O(n)$  since the iterator would have to search in order to find the position of the  $n$ th node.

Pseudocode:

```
def add(pos, object):
```

```

if(pos == 0){
    if(!isEmpty()){
        head.prev = new Node(object, null, head);
        head = head.prev;
    } else {
        head = tail = new Node(object);
    }
} else if(!isEmpty()){
    InternalIter iter = nodeIterator();
    int curPos = 0;
    Node prev = null;
    Node current = null;
    while(iter.hasNext()){
        prev = current;
        current = iter.next();
        if(curPos == pos){
            Node newNode = new Node(object, prev, current);
            prev.next = newNode;
            current.prev = newNode;
            return this;
        }
        ++curPos;
    }
}

```

c)

Best Case Run 0

```

Count: 1000    Time: 7321000 ns
Count: 10000   Time: 42821000 ns
Count: 100000  Time: 132195000 ns

```

Best Case Run 1

```

Count: 1000    Time: 103000 ns
Count: 10000   Time: 1004000 ns
Count: 100000  Time: 60357000 ns

```

Best Case Run 2

```

Count: 1000    Time: 91000 ns
Count: 10000   Time: 755000 ns
Count: 100000  Time: 64137000 ns

```

Worst Case Run 0

```

Count: 1000    Time: 12102000 ns
Count: 10000   Time: 275556000 ns
Count: 100000  Time: 99095511000 ns

```

Worst Case Run 1

```

Count: 1000    Time: 1295000 ns
Count: 10000   Time: 306585000 ns
Count: 100000  Time: 77112483000 ns

```

Worst Case Run 2

```

Count: 1000    Time: 1205000 ns
Count: 10000   Time: 260828000 ns
Count: 100000  Time: 71324190000 ns

```