

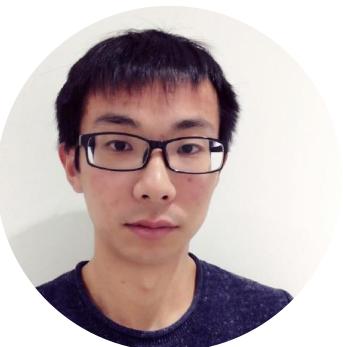
Unbiased Offline Recommender Evaluation for Missing-Not-At-Random Implicit Feedback



Longqi Yang



Yin Cui



Yuan Xuan



Chenyang Wang



Serge Belongie



Deborah Estrin



**CORNELL
TECH**



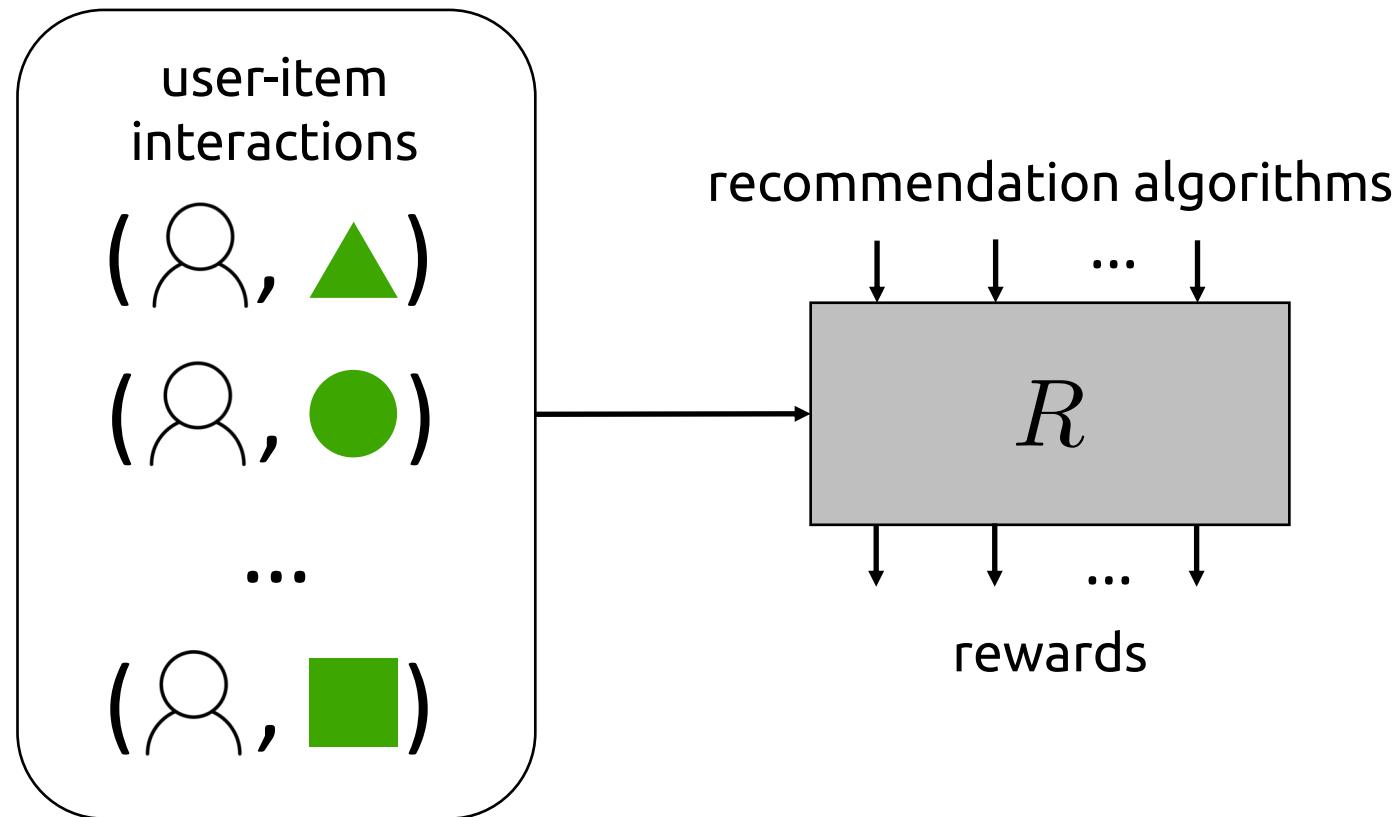
Cornell CIS
Computer Science

Funders:

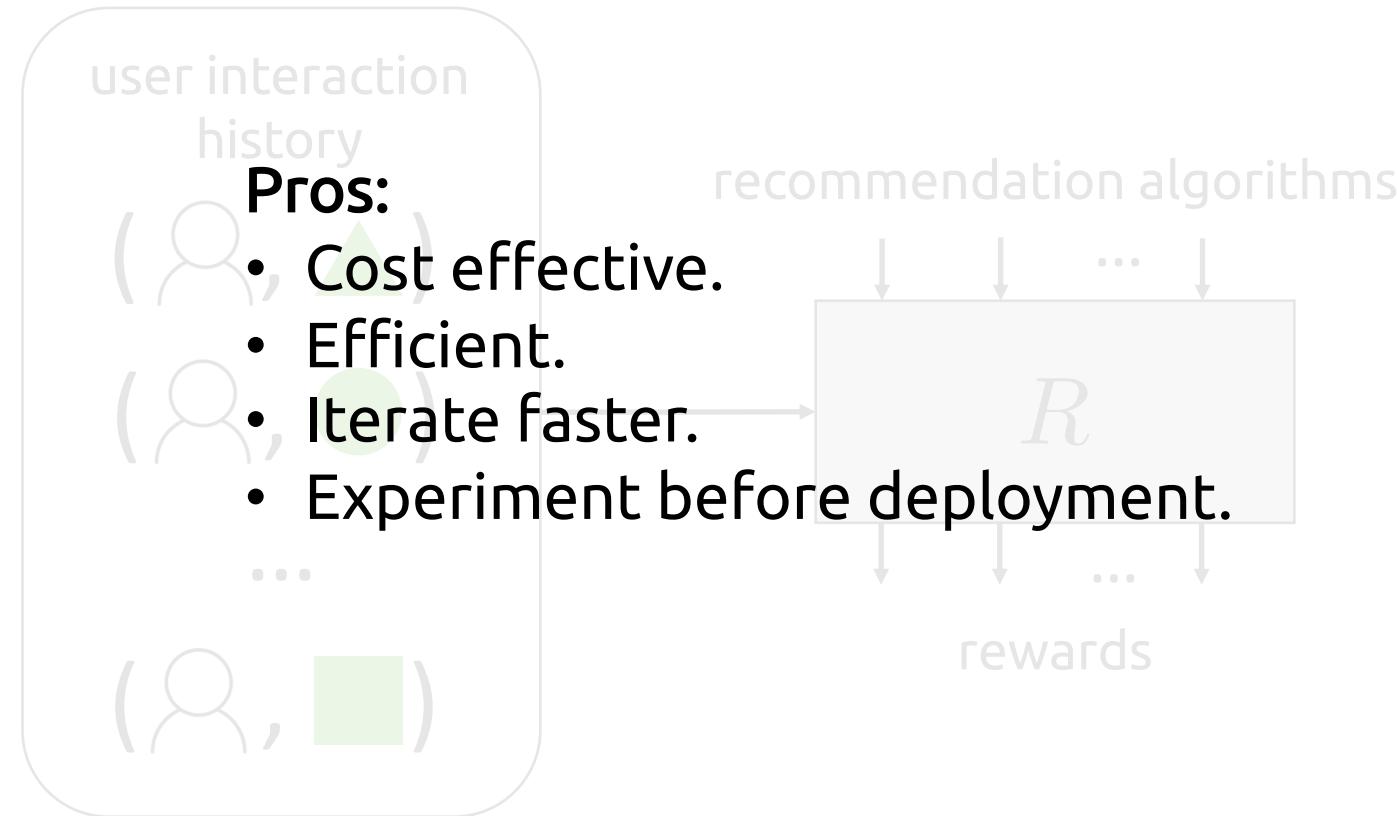


Oath:
A Verizon company

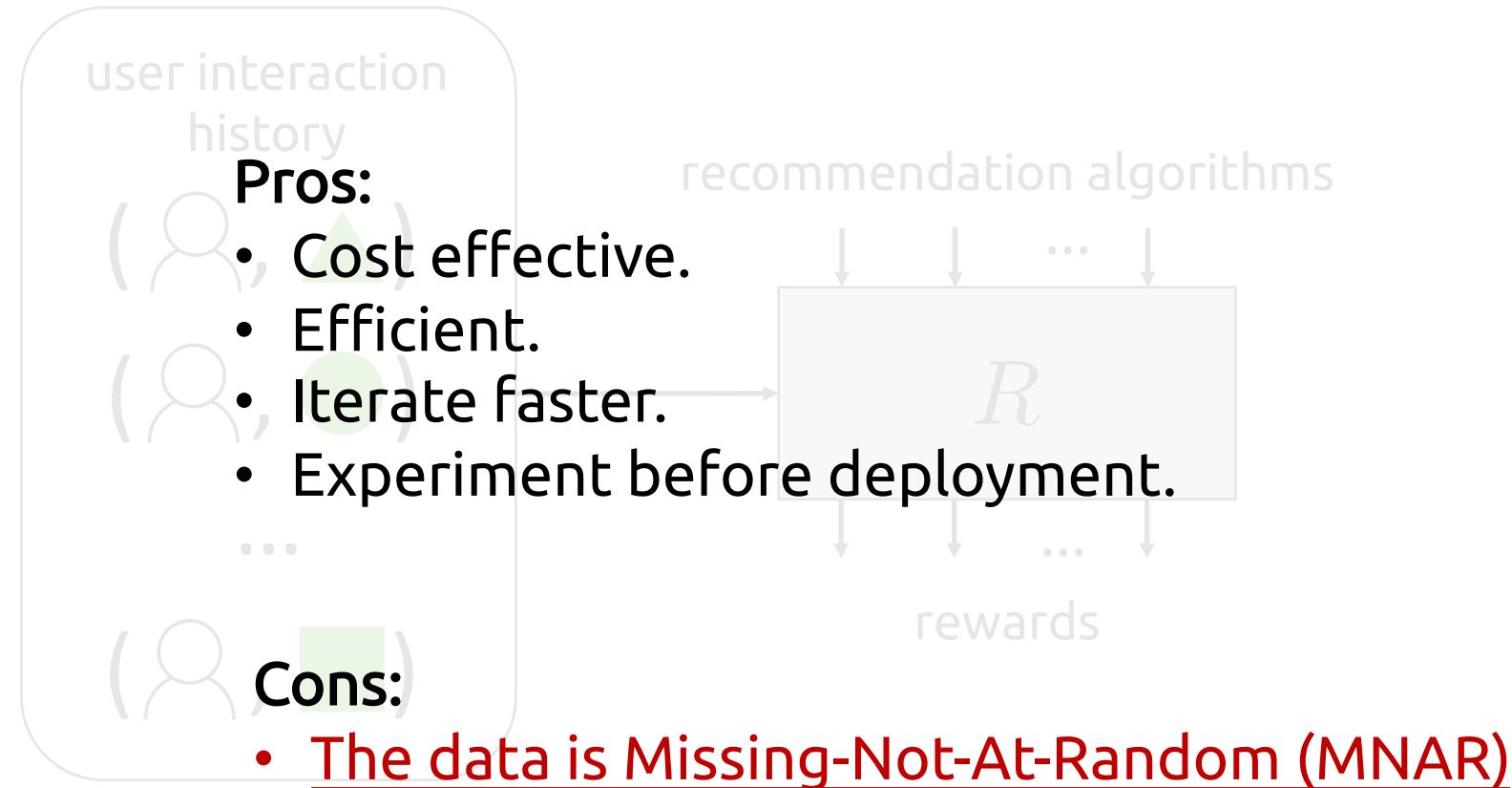
Offline Evaluation of Recommendation Algorithm



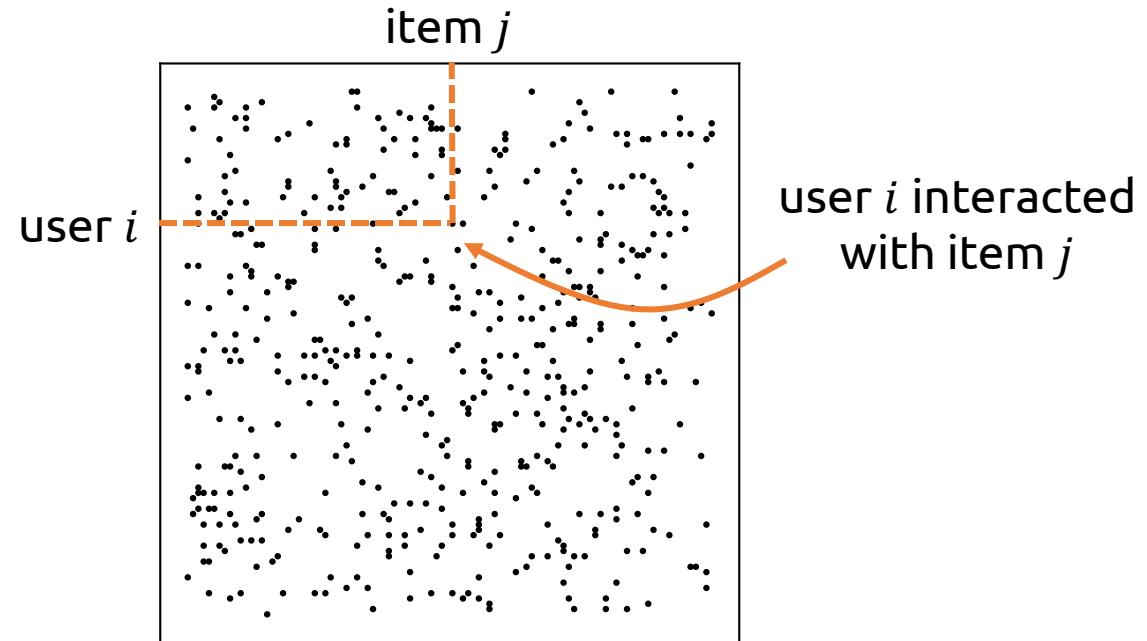
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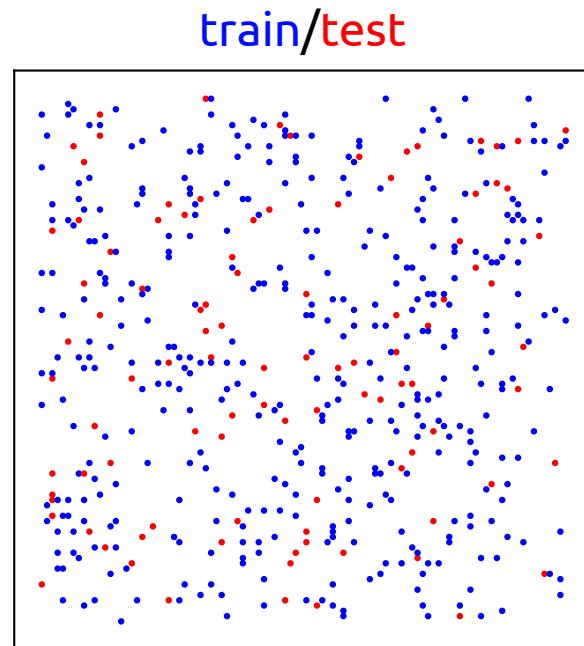
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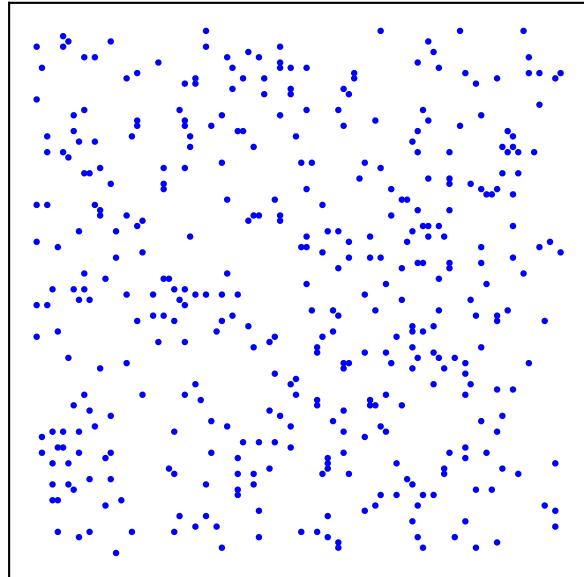
Offline Evaluation procedure



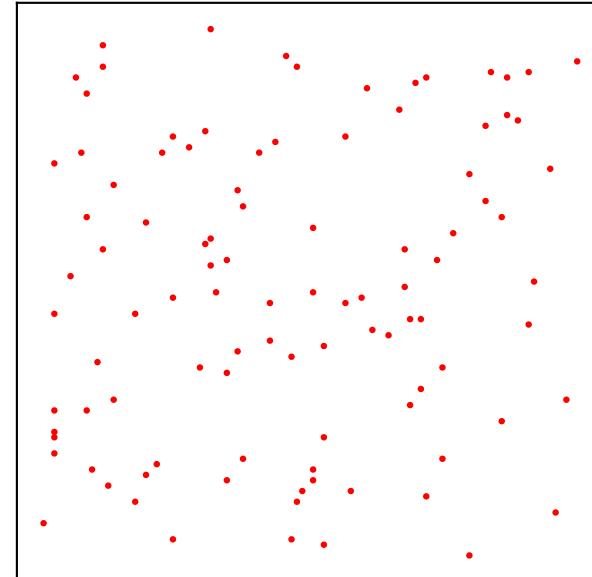
Offline Evaluation procedure



Offline Evaluation procedure

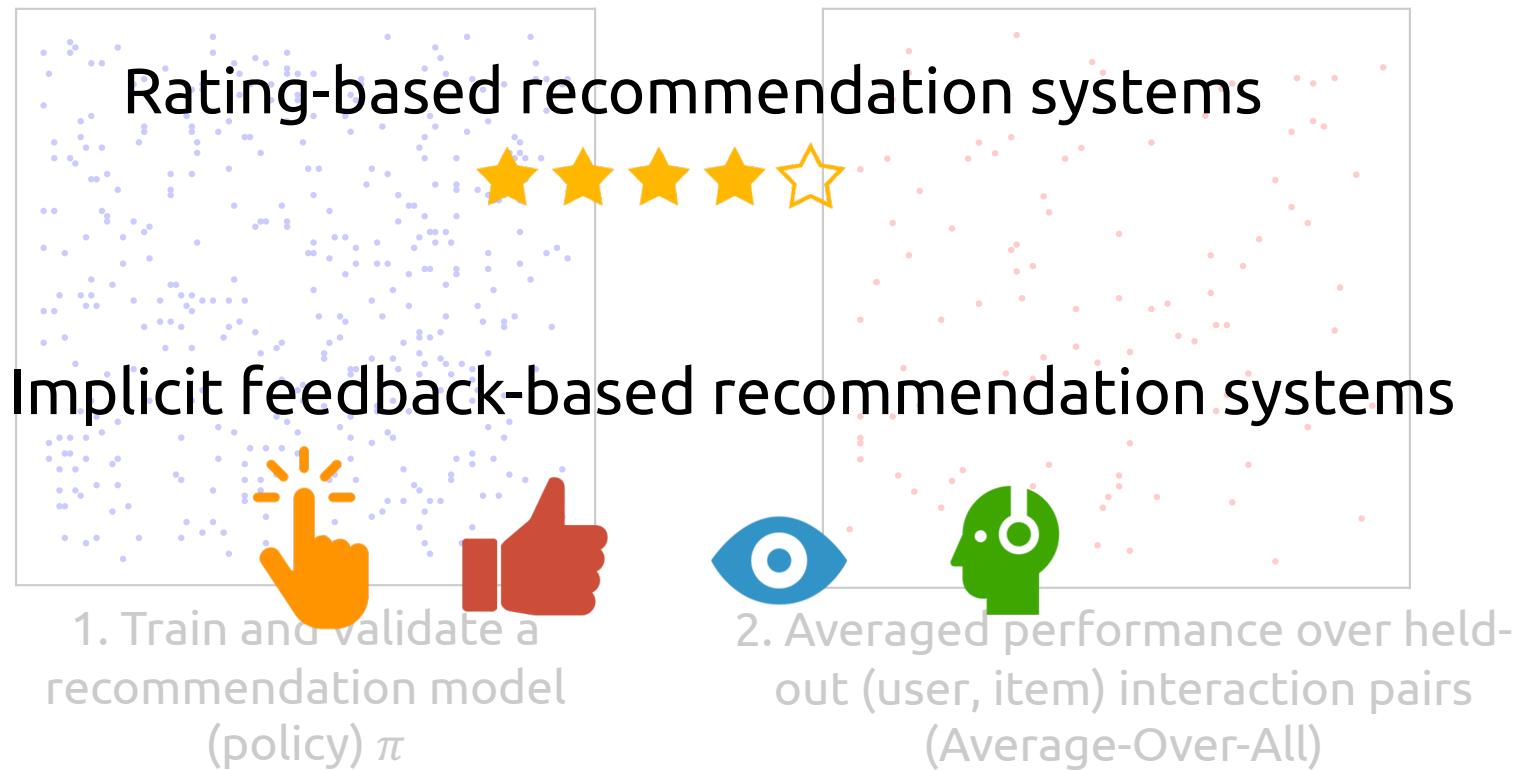


1. Train and validate a recommendation model



2. Averaged performance over held-out (user, item) interaction pairs
(Average-Over-All)

Offline Evaluation procedure



Previous work: Average-Over-All is **biased** for rating-based recommendation systems, because ratings are **MNAR**
[Marlin et al. 09], [Schnabel et al. 16], [Steck 10], [Steck 11], and [Steck 13]

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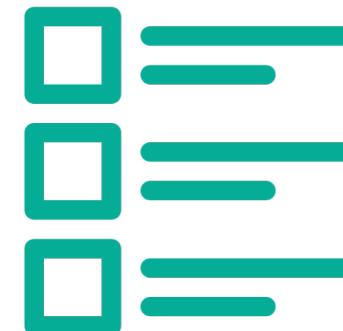
Previous work: Average-Over-All is **unbiased** for implicit feedback-based recommendation systems, because implicit feedback is **missing uniformly at random**.
[Lim 15]

This work: Average-Over-All is **biased** for implicit feedback-based recommendation systems, because implicit feedback is **NOT missing uniformly at random.**

This work: Average-Over-All is **biased** for implicit feedback-based recommendation systems, because implicit feedback is **NOT missing uniformly at random.**



trending



recommendation

Popularity bias (Users are more likely to be exposed to popular items)

A Hypothetical Example

	Popular Items	Long-tail Items	
# of liked items (over all items)	1	:	10
# of liked items (over observations)	10	:	1
Algorithm 1 Performance	0.8	0	
Algorithm 2 Performance	0.75	0.75	

A Hypothetical Example

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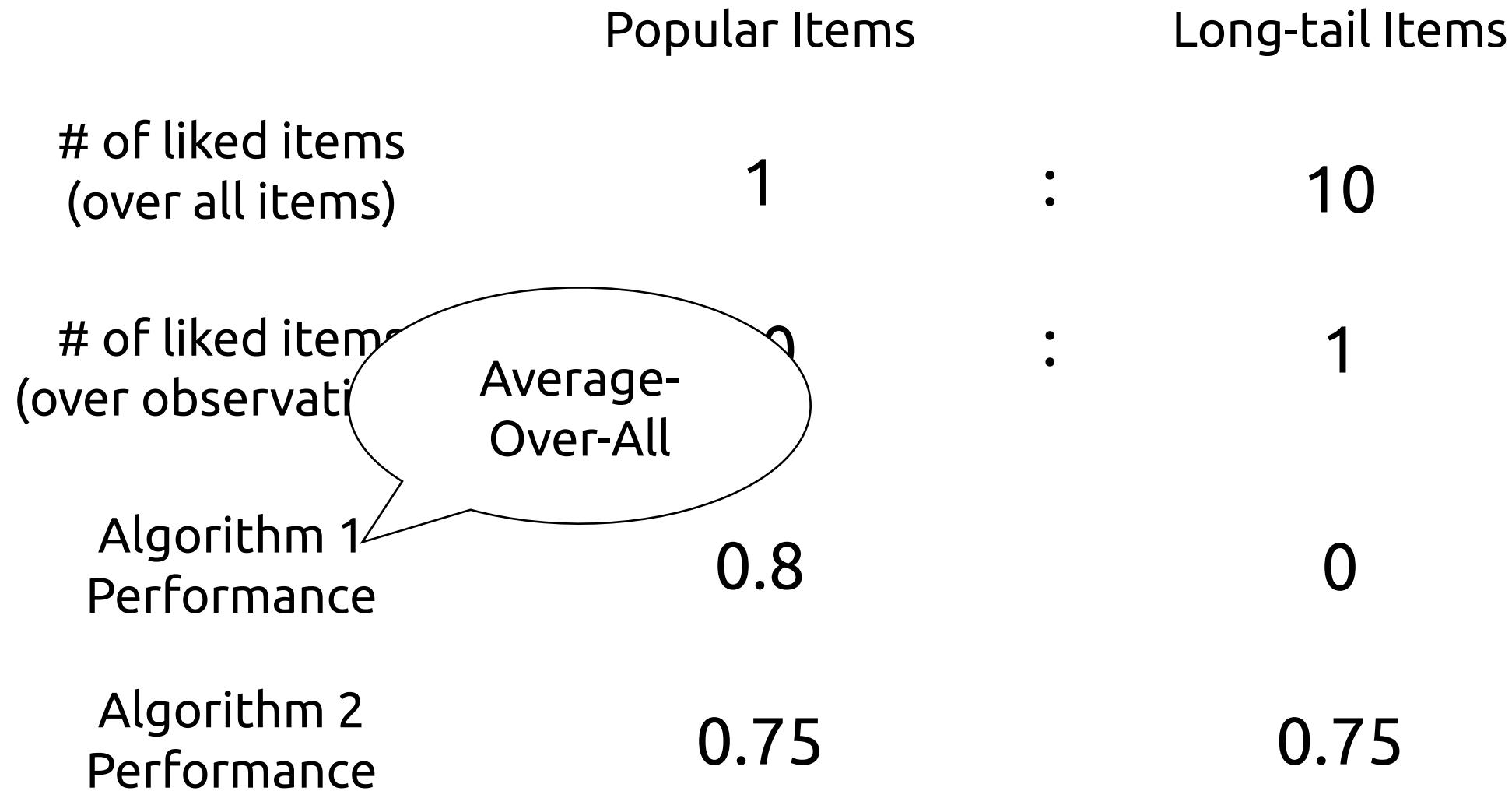
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A Hypothetical Example

	Popular Items	:	Long-tail Items
# of liked items (over all items)	1	:	10
# of liked items (over observations)	10	:	1
Algorithm 1 Performance	Any sensible evaluation		
Algorithm 2 Performance	0.75		0.75

A Hypothetical Example



Formalize Reward R

Item rankings predicted by an algorithm

Ideal evaluation: $R(\hat{Z}) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \frac{1}{|\mathcal{S}_u|} \sum_{i \in \mathcal{S}_u} c(\hat{Z}_{u,i})$

An orange curved arrow points from the text "Item rankings predicted by an algorithm" up towards the symbol \hat{Z} in the equation $R(\hat{Z})$.

Formalize Reward R

Item rankings predicted by an algorithm

Ideal evaluation: $R(\hat{Z}) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \frac{1}{|\mathcal{S}_u|} \sum_{i \in \mathcal{S}_u} c(\hat{Z}_{u,i})$

Items liked by user u among the entire item set

Predicted ranking of item i for user u

scoring metric

Reward for (u, i) pair

Items liked by user u among the entire item set

Formalize Reward R

Item rankings predicted by an algorithm Predicted ranking of item i for user u

Ideal evaluation: $R(\hat{Z}) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \frac{1}{|\mathcal{S}_u|} \sum_{i \in \mathcal{S}_u} c(\hat{Z}_{u,i})$

Items liked by user u among the entire item set

scoring metric

Reward for user u

Formalize Reward R

Item rankings predicted by an algorithm Predicted ranking of item i for user u

Ideal evaluation: $R(\hat{Z}) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \frac{1}{|\mathcal{S}_u|} \sum_{i \in \mathcal{S}_u} c(\hat{Z}_{u,i})$

Items liked by user u among the entire item set scoring metric

Reward for the algorithm

Formalize Reward R

Average-Over-All: $\hat{R}_{AOA}(\hat{Z}) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \frac{1}{|\mathcal{S}_u^*|} \sum_{i \in \mathcal{S}_u^*} c(\hat{Z}_{u,i})$



Items liked by user u (observed)

Formalize Bias

$$\mathbb{E}_O \left[\hat{R}_{\text{AOA}}(\hat{Z}) \right] \neq R(\hat{Z})$$



$O_{u,i} = 1$ if (u, i) is observed, and $O_{u,i} = 0$ otherwise

$$O_{u,i} \sim \mathcal{B}(1, P_{u,i})$$

Inverse-Propensity-Scoring (IPS)

$$\hat{R}_{\text{AOA}}(\hat{Z}) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \left[\frac{1}{|\mathcal{S}_u^*|} \sum_{i \in \mathcal{S}_u^*} c(\hat{Z}_{u,i}) \right]$$

$$\hat{R}_{\text{IPS}}(\hat{Z}|P) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \left[\frac{1}{|\mathcal{S}_u|} \sum_{i \in \mathcal{S}_u^*} \frac{c(\hat{Z}_{u,i})}{P_{u,i}} \right]$$

Inverse-Propensity-Scoring (IPS)

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$$\boxed{\mathbb{E}_O \left[\hat{R}_{\text{IPS}}(\hat{Z}|P) \right] = R(\hat{Z})}$$

Self-Normalized Inverse-Propensity-Scoring (SNIPS)

[Swaminathan et al.15]

$$\hat{R}_{\text{IPS}}(\hat{Z}|P) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \left[\frac{1}{|\mathcal{S}_u|} \right] \sum_{i \in \mathcal{S}_u^*} \frac{c(\hat{Z}_{u,i})}{P_{u,i}}$$



$$\hat{R}_{\text{SNIPS}}(\hat{Z}|P) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \left[\frac{1}{\sum_{i \in \mathcal{S}_u^*} \frac{1}{P_{u,i}}} \right] \sum_{i \in \mathcal{S}_u^*} \frac{c(\hat{Z}_{u,i})}{P_{u,i}}$$

Estimating Propensity Scores

Factor: Popularity bias (Users are more likely to be exposed to popular items)

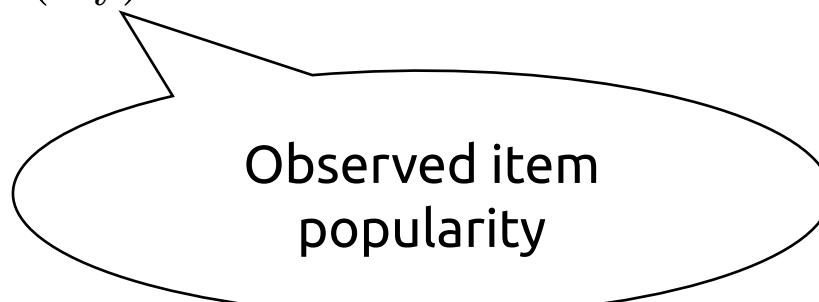
Assumptions:

- User-independence assumption $P_{u,i} = P(O_{u,i} = 1) = P(O_{*,i} = 1) = P_{*,i}$
- Two-steps assumption $P_{*,i} = P_{*,i}^{\text{select}} \cdot P_{*,i}^{\text{interact|select}}$
- User preference is not affected by item presentation

$$P_{*,i}^{\text{interact|select}} = P_{*,i}^{\text{interact}}$$

Estimating Propensity Scores

Popularity bias model [Steck 11]:

$$\hat{P}_{*,i}^{\text{select}} \propto (n_i^*)^\gamma$$


Observed item popularity

Estimating Propensity Scores

Popularity bias model [Steck 11]:

$$\hat{P}_{*,i}^{\text{select}} \propto (n_i^*)^\gamma$$

Estimated from
known online content
serving policy

$$\hat{P}_{*,i} \propto (n_i^*)^{\left(\frac{\gamma+1}{2}\right)}$$

Measuring bias in recommender evaluation (Yahoo! music rating dataset)

Mean Absolute Error (MAE), Recall

Model	Average-Over-All	R_{SNIPS} ($\gamma = 1.5$)	R_{SNIPS} ($\gamma = 2.0$)	R_{SNIPS} ($\gamma = 2.5$)	R_{SNIPS} ($\gamma = 3.0$)
U-CML	0.401	0.270	0.260	0.253	0.248
A-CML	0.399	0.274	0.264	0.258	0.253
BPR	0.380	0.275	0.264	0.258	0.258
PMF	0.386	0.267	0.264	0.258	0.258

R_{SNIPS} produces significantly lower MAE

Measuring bias in recommender evaluation (Yahoo! music rating dataset)

Mean Absolute Error (MAE), Recall

Model	Average- Recall	R_{SNIPS}	R_{SNIPS}	R_{SNIPS}	R_{SNIPS}
U-CML	0.391	0.270	0.263	0.258	0.248
A-CML	0.399	0.274	0.266	0.258	0.253
BPR	0.380	0.275	0.264	0.258	0.258
PMF	0.386	0.267	0.261	0.258	0.258

The accuracy of recommending popular items is a significant **overestimation** of the true recommendation performance

R_{SNIPS} produces significantly lower MAE

Please come to our poster or refer to our paper for:

- Proofs
- Experimental details.
- More experiments.
- Deeper analysis of the unbiased evaluator.

Conclusions and Future Work

$$\mathbb{E}_O \left[\hat{R}_{\text{IPS}}(\hat{Z}|P) \right] = R(\hat{Z})$$

$$\hat{R}_{\text{SNIPS}}(\hat{Z}|P) = \frac{1}{|\mathcal{U}|} \sum_{u \in \mathcal{U}} \frac{1}{\sum_{i \in \mathcal{S}_u^*} \frac{1}{P_{u,i}}} \sum_{i \in \mathcal{S}_u^*} \frac{c(\hat{Z}_{u,i})}{P_{u,i}}$$

- Understanding variance of evaluators.
- Propensity estimation (e.g., incorporate auxiliary user and item information).
- Debias training of recommendation systems (e.g., [Liang et al. 16]).



<http://www.openrec.ai>

Github link, documents, and tutorials

Longqi Yang

Ph.D. candidate

Computer Science, Cornell Tech, Cornell University

Email: ylongqi@cs.cornell.edu

Web: bit.ly/longqi

Twitter: [@ylongqi](https://twitter.com/ylongqi)

Connected Experiences Lab

<http://cx.jacobs.cornell.edu/>

Small Data Lab

<http://smalldata.io/>



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