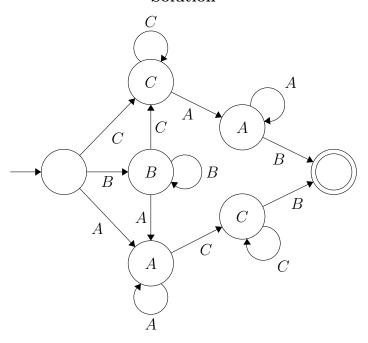
CPSC 3400 - Homework 6 DFAs, Regular Expressions and Turing machines

Minh-Hieu Nguyen May 28, 2022

Part I. DFAs

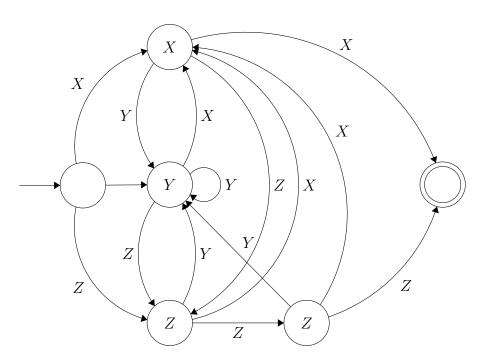
Draw DFAs for the following language specifications.

1. All strings on $\Sigma = \{A, B, C\}$ that contain each letter (A, B, A) and (A, B) at least once.

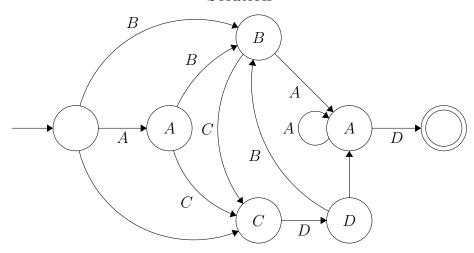


2. All strings on $\Sigma = \{X, Y, Z\}$ that contain two secutive Xs or three consecutive Zs (or both).

Solution



3. All strings on $\Sigma = \{A, B, C, D\}$ that match the Python regular expression ^ (A?(B|CD)*A+D)\$



Part II. Regular Expressions

For each item, write a *single* regular expression that mathces that item. Note that in ALL cases, the entire string must match without additional characters.

1. A string of digits that contains only digits and contains exactly two fives. Examples of acceptable strings include: "15445", "55", "05563"

The string should be rejected if it contains anything other than a digits.

Solution

- Answer: ^[0-4,6-9]*5[0-4,6-9]*5[0-4,6-9]*\$
- Explanation:
 - [0,4,6-9]*: Accept all strings that contain digits in range from 0 to 9 except 5. It also accept empty strings. (1)
 - $-5{1}$: Accept only a digit-5 string. (2)
- 2. A regular expression that matches a time expressed in the form "1:45 PM".

The hours part must be a number from 1 to 12, the minutes range from 00 to 59, and the time must indicate either AM or PM (uppercase only and preceded by exactly one space).

- Answer: ^((1[0-2]|[1-9]))(:)([0-5][0-9]) ([AP]M)\$
- Explanation:
 - (1[0-2] | [1-9]): Accept all digit strings that are either in range from 10 to 12 or in range from 0 to 9 without leading zeroes.
 - (:): Accept the separator, ":", between hours and minutes.
 - ([0-5][0-9]): Accept all digit strings from 00 to 59 (with leading zeroes).
 - ([AP]M): Accept "AM" or "PM" with one preceding space to indicate the time meridiem.
- 3. A regular expression that matches a string representing a comma separated list of variable names such as: hello, get_max, sum3

- A variable name consists of letters, digits, and underscores but cannot start with a digit.
- There is exactly one space after every comma. No other spaces are allowed.
- Commas and spaces are not allowed before the first name and after the last name.
- An empty string is considered a match.

- Answer: $^{\frac{1}{([a-zA-Z_{-}]\setminus w*)(,))*([a-zA-Z_{-}]\setminus w*)}}$
- Explanation:
 - ^\$: Accept empty string.
 - ([a-zA-Z_]\w*): Accept variable names that match with the requirements. \w is equivalent to [a-zA-Z0-9_].
 - (([a-zA-Z_]\w*)(,))*: As the previous one, but additionally accept previous variable names followed by exactly one comma and one space, if there are more than one variable name.

Part III. Turing Machines

Design a Turing machine on the input alphabet $\{x,y,z\}$ that removes all z characters from the input such there are no gaps. If the input string is xzzyxzy, the output should be xyxy.

• Hint: The final string does not need to reside on the same part of the tape where it started.

