# **EECS 2011 Notes**

### Richard Robinson

## December 31, 2018

## Contents

1	Fundamental Data Structures	2
2	Algorithmic Analysis	4
3	Stacks, Queues, & Deques	5
4	Lists & Iterators	7

#### 1 Fundamental Data Structures

### 1.1 Insertion-Sort Algorithm $\mathcal{O}(n^2)$

The insertion-sort algorithm is used to sort an array of elements. Analytically, the non-recursive version of algorithm operates by:

- 1. Iterate through each element *e* in the array
- 2. For each element, compare to each element left of e.
- 3. If *e* is less than such element, swap the indices of those elements

because the algorithm fully iterates through 2 nested loops, the complexity is described by  $\mathcal{O}(n^2)$ . Expressed algorithmically, it is represented as:

```
insertionSort(arr, arr.size() - 1);
public static void insertionSort(List<T> arr, int n) {
    if (n > 0) {
        insertionSort(arr, n - 1);
        int j;
        T elem = arr.get(n);

    for (j = n - 1; j >= 0 && arr.get(j) > elem; j--) {
            arr.set(j + 1, arr.get(j));
        }
        arr.set(j + 1, elem)
    }
}
```

The recursive version shown above improves upon this by

- turning the outer loop into a recursive call of size n-1, and
- separating the swapping algorithm from the innermost loop

## **1.2** Singly Linked Lists $\mathcal{O}(n)$

A linked list is a collection of nodes that form a linear sequence. Each node stores a reference to an element of the sequence, as well as a reference to the next node and alternatively a reference to the previous node (doubly-linked list).

A linked list must keep a reference to the first element (the head) and the last element (the tail), which has null as its reference. An element may be added to the head and tail of a linked list, respectively, via:

```
public void addFirst(T e) {
   Node newest =
        new Node(e, this.head);
   this.head = newest;
   size++;
}
```

```
public void addLast(T e) {
   Node newest = new Node(e, null);
   this.tail.setNext(newest);
   this.tail = newest;
   size++;
}
```

To remove an element from the head of the list, this.head is simply dereferenced and assigned to this.head.getNext()

### 1.3 Other Linked Lists $\mathcal{O}(n)$

In a *circularly linked list* (CCL), the reference of the tail node is linked to the head node instead of null. This requires an additional rotate() method, which assigns tail to the next element. A CCL has the following methods:

```
public void addFirst(T e) {
    if (this.isEmpty()) {
        this.tail = new Node(e, null);
        this.tail.setNext(this.tail);
    } else {
        Node newest =
            new Node(e, tail.getNext);
        tail.setNext(newest);
    }
    size++
}
```

```
public void removeFirst(T e) {
   if (this.isEmpty()) return null;
   Node head = tail.getNext();

   if (head == tail) this.tail = null
   else tail.setNext(head.getNext());
   size--;
}
```

```
public void addLast(T e) {
    this.addFirst(e);
    this.rotate();
}
```

The primary use of circularly linked lists is in implementations of *round-robin scheduling*, which for a list *C*, gives a time slice to C.first(), then executes C.rotate().

### 2 Algorithmic Analysis

#### 2.1 Notation and Definitions

The set of *primitive operations* consists of the following operations:

- Assigning a value to a variable or reference
- Performing an arithmetic operation or boolean comparison
- Accessing a single element of an array
- Calling or returning from a method

The main functions by which complexities are measured with reference to include:

in order of increasing time complexity. The *Big-Oh* notation is defined as follows:

$$f(n) \in \mathcal{O}(g(n)) \iff \exists (c > 0) \exists (n_0 > 1) \forall (n \ge n_0) (f(n) \le c \cdot g(n)) \tag{1}$$

### **2.2 Binary Search** $\mathcal{O}(\log n)$

Binary search is a recursive search algorithm for sorted arrays to see if it contains an element e. In this algorithm, a target value  $v = \lfloor (\min + \max)/2 \rfloor$  is selected. If e > v, the procedure is continued with  $\min \mapsto v + 1$  and similarly for e < v, and continues until e is found or  $\min \ge \max$ .

Algorithmically, binary search is given by:

```
bSearch(List<T> data, data.size() / 2, 0, data.size() - 1);
static boolean bSearch(List<T> data, T target, T lo, T hi) {
   if (lo > hi) return false;
   T mid = (lo + hi) / 2;

   if (target == data.get(mid)) return true;
   return (target < data.get(mid))
    ? bSearch(data, target, lo, mid - 1);
    : bSearch(data, target, mid + 1, hi);
}</pre>
```

In general, a binary-based recursive algorithm tests base cases, and otherwise returns itself with one or more of two sets of parameters, based on a boolean comparison.

### 3 Stacks, Queues, & Deques

## **3.1** Stacks **§** *O*(1)

A stack is an *abstract data type* (ADT) whose elements operate according to the *last-in, first-out* (LIFO) principle. A general stack API has the following methods:

void push(T e) Adds the element e to the top of the stack

T pop() Removes and returns the top element

T peek() Returns the top element of the stack, or null if empty.

Most commonly, stacks are used when a history or matching of elements in a list is required. In general, the following algorithm can be used to check if a string has matched delimiters:

```
static boolean isMatched(String str, String start, String end) {
   Stack<String> st = new Stack<>();
   for (char c : str.toCharArray()) {
      if (start.contains(c)) st.push(c);
      else if (end.contains(c)) {
        if (buf.isEmpty()) return false;

        char p = buf.pop();
        if (end.indexOf(c) != start.indexOf(p)) return false;
      }
   }
}
return buf.isEmpty();
}
```

### 3.2 Queues $\mathcal{O}(1)$

The queue ADT operates on a FIFO principle such that the oldest element is retrieved first, with the following API methods:

**void enqueue**(T **e**) Adds the element *e* to the back of queue

T dequeue() Removes and returns the first element

Since there is no reference to the back of the queue, the formula

$$i_b = (i_f + n) \mod \ell_{\text{arr}}$$
 (2)

in which  $i_f$  is the index of the first element, n is the number of elements, and  $\ell$  is the array length.

## 3.3 Deques $\mathcal{O}(1)$

A double-ended queue is an ADT of a generalization between queues and stacks, in that an element may be added to the front of the queue and/or removed from the back. A deque has these API methods:

void addFirst(T e) Adds the element e to the front of the deque (similarly, addLast())

T removeFirst() Removes and returns the first element (similarly, removeLast())

Typically, deques are implemented via doubly-linked lists.

#### 4 Lists & Iterators

### **4.1 Positional Lists** $\mathcal{O}(1)$

Positional list ADTs use a *cursor* to define a particular position within a list without indices via a getElement() method. A positional list may implement a traversal method via:

Note, all positional list methods except set(p,e) and remove(p) return the position of the element.

#### 4.2 Iterators

An iterator is a pattern for the abstraction of sequences, which is generally an interface with methods E next() and boolean hasNext().

As well, there exists an Iterator iterator() for use in data structures, which returns an iterator of the elements in the collection, which is used as a substitute for the for each loop when remove() is used, as for example to filer a list:

```
public void filter(List<E> list, double threshold) {
   Iterator<E> iter = list.iterator();
   while (iter.hasNext()) if (iter.next() > threshold) {
      iter.remove();
   }
}
```