

RICHARD ROBINSON

CHEMISTRY &
MATERIALS
SCIENCE



Introduction

Stoichiometry

ALL STOICHIOMETRIC equations for quantities may be derived from

$$n_1/v_1 = n_2/v_2 \quad (1)$$

The **percentage yield** is defined as

$$\% \text{ yield} = \frac{\text{actual yield}}{\text{theo. yield}} \times 100\% \quad (2)$$

A crucial aspect in confirming stoichiometric results is using **dimensional analysis**; that is, using the dimensions of each unit in the equation(s) and confirming the final unit has the proper dimensions.

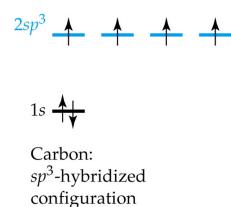
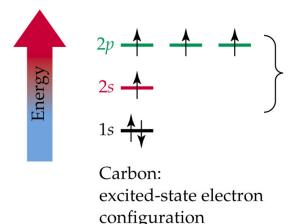
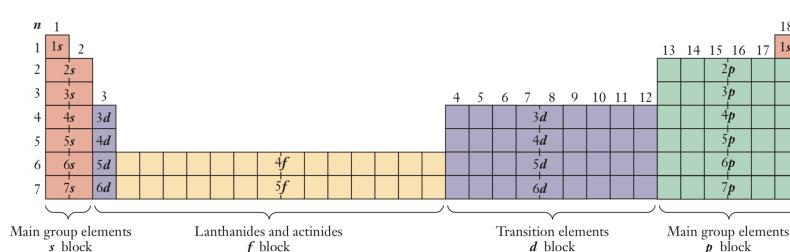
moles	$n = m/M = CV$
atoms	$n_{\text{atoms}} = \rho V N_a / M$
molarity	$C = mn/MV$
dilution	$n_1 = n_2$

Bonding

The total number of **orbitals** is equal to n^2 , where n is the principle quantum number, wherein each orbital has a maximum of two electrons. The orbitals are filled in the order of

$$1s^2 2s^2 2p^6 3s^2 3p^6 4s^2 3d^{10} 4p^6 5s^2 \dots \quad (3)$$

This maximum occurs only if all subshells contain one electron originally, known as Hund's rule.



The **formal charge** is given by $q_f = n_v - n_l - \frac{1}{2}n_s$ in which $\sum q_f = 0$, where n_v is the total number of valence electrons; n_l is the number of lone pairs; and n_s is the number of electrons shared in bonds.

Hybrid orbitals are dependent on molecular geometry, and filled by sp^3d^2 . The number of orbitals is equal to the number of electron pairs. The number of **sigma and pi bonds** is equal to

$$n_\sigma = \sum n_{\text{all}} \quad \text{and} \quad n_\pi = \sum n_{\text{dbl}} + 2 \sum n_{\text{tri}} \quad (4)$$

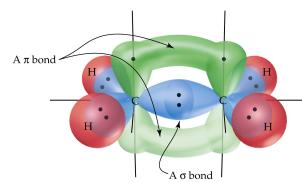
Other properties of the periodic table include

- Atomic size increases toward the bottom left;
- Ionization energy and electronegativity increase towards the top right;

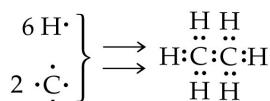
Atoms & Molecules

Lewis dot structures are created via the following algorithm:

1. Count the total number of valence electrons in the molecule
2. Place single bonds between all connected atoms;
3. Place the remaining valence electrons not accounted for in (2) on individual atoms, specifically as lone pairs whenever possible;
4. Create multiple bonds as needed for any atoms that do not have a full octet



Sigma and pi bonds overlapping for hybridization.



Constructing a lewis dot structure.

Chemical Equilibrium

Equilibrium Constants

A system is said to be at **dynamic equilibrium** if the rates of both reactions are equal but do not approach zero. For a general chemical reaction, the reaction quotient and equilibrium constant are

$$Q = \frac{[C]^c[D]^d}{[A]^a[B]^b} \quad \text{and} \quad K_c = \frac{[C]_{eq}^c[D]_{eq}^d}{[A]_{eq}^a[B]_{eq}^b} \quad (5)$$

respectively. For reactions which take place in the gas phase,

$$K_p = K_c RT^{\Delta n_g} \iff [X] \equiv P_X = [X]RT \quad (6)$$

where $\Delta n_g = c + d - (a + b)$. Reactions are **homogeneous** iff all constituents are either exclusively gaseous or aqueous. Incidentally, in a heterogeneous reaction, K only includes the compounds in the reaction which are not solid nor liquid. For a series of reactions,

$$K_n = \prod K_i \quad (7)$$

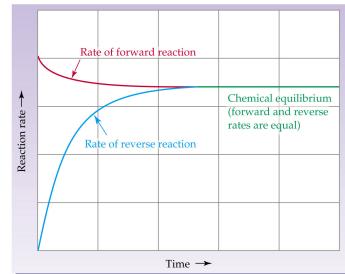
The procedure to calculate **final concentrations** of specific compounds in a reaction $A \rightleftharpoons B$ is as follows:

1. For reactants and products, $[A_i]_{eq} = [A_i] \mp ax$, respectively.
2. Using these concentrations in K , solve for x .
3. Substitute x into the original equilibrium concentrations.

R	A	A'	B
I	$[A_i]$	$[A'_i]$	$[B_i]$
C	$-ax$	$-a'x$	$+bx$
E	$[A]_{eq}$	$[A']_{eq}$	$[B]_{eq}$

LeChatelier's Principle

LeChatelier's principle states that when a system at equilibrium is stressed, it reestablishes itself to avoid such stress; that is,



Dynamic equilibrium.

- If the concentration of products is increased or reactants decreased, $Q > K$ and more reactants are formed;
- If vice versa, $Q < K$ and more products are formed.

Pressure is inversely proportional to the amount of moles the side to which equilibrium moves to has. Note that catalysts have no effect upon the properties of equilibrium systems, unlike temperature.

Exothermic reactions produce heat and endothermic reactions absorb heat. If a reaction is exothermic and temperature increases or vice versa, more reactants are formed. Otherwise, more products are formed.

Solubility Equilibria

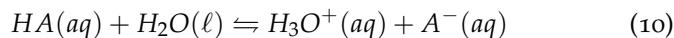
For a reaction $A(s) \rightleftharpoons cC(aq) + dD(aq)$, the solubility constant is defined as

$$K_{sp} = [C]^c[D]^d \quad (8)$$

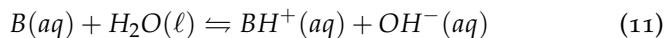
and the molar solubility is

$$x = (K_{sp}/c^c d^d)^{1/(c+d)} \quad (9)$$

A Brønsted-Lowry acid is a proton H^+ donor, and a base a proton acceptor. The equation for the **dissociation** of a weak acid HA is

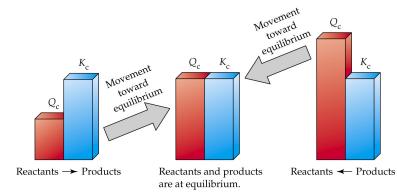


and for a weak base B ,

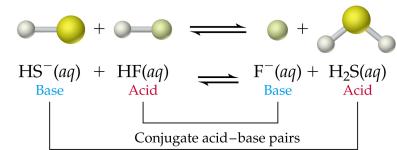


The acid and base ionization constants are $K_a, K_b = K_s$ respectively such that $[X]_{eq} = [X]_i$ for $X = HA, B$. The **Gibbs free energy** is related to K by

$$\Delta G^\ominus = -RT \ln K = H - TS \quad (12)$$



Predicting the direction of reaction. The direction of reaction depends on the relative values of Q and K_c .



Conjugate acid-base pairs for the reaction between HS^- and HF .

Thermodynamics

The Second Law

A SPONTANEOUS REACTION occurs without the need for continuous intervention. When heating a system, its **entropy** S increases. The second law states that for a spontaneous reaction,

$$\Delta S_u = \Delta S + \Delta S_{sur} > 0 \quad (13)$$

where $\Delta S_{sur} = -\Delta H/T$. If $\Delta \sum v > 0$, then $\Delta S > 0$. The change in standard entropy is

$$\Delta S^\ominus = \Delta \sum v_i S_i^\ominus \quad (14)$$

The change in Gibbs free energy is thus also equal to

$$\Delta G = \Delta H - T\Delta S = -T\Delta S_u \quad (15)$$

If $\Delta G < 0$, a reaction is spontaneous and vice versa. The change in standard free energy is

$$\Delta G^\ominus = \Delta \sum v_i G_i^\ominus \quad (16)$$

Entropy is proportional to T, r, V, n and inversely proportional to P .

Enthalpy

Heat is expressed as $\Delta E - w$. The specific & molar **heat capacities** are defined as

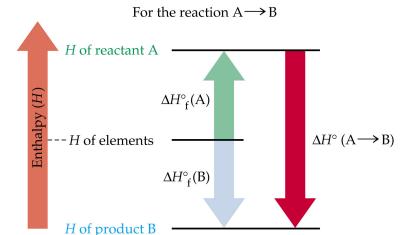
$$q_s = mc\Delta T \quad \text{and} \quad q_m = nC_p\Delta T \quad (17)$$

For **calorimetry**, heat is given by

$$q_c = -(q/\Delta T_i)\Delta T_f \quad (18)$$

Enthalpy is defined as

$$\Delta H = \Delta E + \Delta(PV) = q_p - n\Delta H_{\Delta\text{phase}} \quad (19)$$



The enthalpy ΔH^\ominus for the reaction $A \rightarrow B$ is the difference between the standard heats of formation of products and reactants.

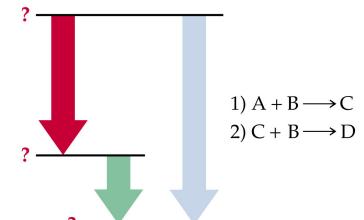


Diagram of Hess' Law.

A reaction is exothermic for $\Delta H < 0$ and vice versa. A **formation reaction** is one in which one mole of a compound is formed from its elements such that

$$aA + bB = 1AB \quad \Delta H_f^\ominus = \Delta H_f^\ominus[AB] \quad (20)$$

Hess's Law states the enthalpy change of a process is independent of path; that is, $\Delta H = \sum \Delta H_i$ meaning that sub-reactions and their enthalpies may be summed together to yield the desired reaction and its enthalpy. The change in standard enthalpy is

$$\Delta H^\ominus = \Delta \sum v \Delta H_f^\ominus \quad (21)$$

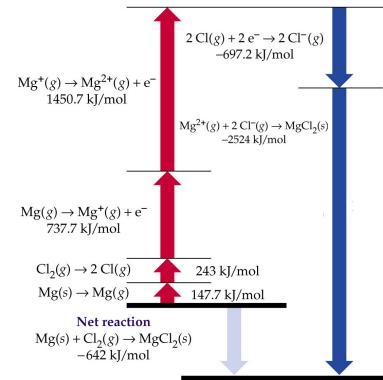
In thermodynamical equations, always convert to moles from mass or molarity using

$$q = \pm n \Delta H / N_a \quad (22)$$

The **Born-Haber cycle** is used to find the H_f of an ionic compound MX , given by

$$\Delta H_f = H_{\text{sub}} + \frac{1}{2}B_X + IE_M - EA_X + LE \quad (23)$$

where B is the bond energy of X_2 from $M + \frac{1}{2}X_2 \rightarrow MX$, and LE is defined as exothermic.



Using the Born-Haber cycle to calculate the enthalpy of formation.

Materials Science

Crystal Structures

MAXIMUM PACKING density is achieved with ccp and hcp configurations. The cubic unit cell may be one of sc, bcc, or fcc. The number of atoms per unit cell is equal to $\frac{1}{2}$ number of face-centered atoms + $\frac{1}{8}$ number of atoms.

	n	cn	a_0
sc	1	6	$2r$
bcc	2	8	$4r/\sqrt{3}$
fcc	4	12	$2\sqrt{2}r$

The density of a cell is given by

$$\rho = \frac{m}{a^3} \quad \text{for} \quad m = \frac{nM}{N_a} \quad (24)$$

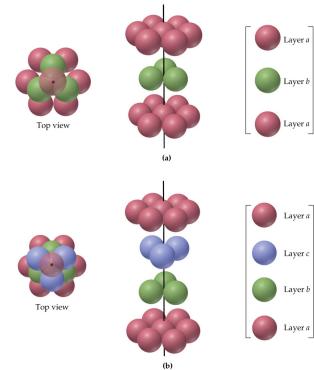
The **packing efficiency** of a lattice is defined as nV_{sph}/a^3 .

Types of Bonding

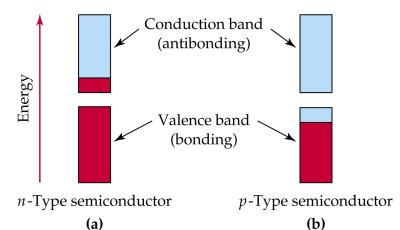
The concept of **band theory** describes metallic bonding in **semiconductors**. In metals / conductors, semiconductors, and insulators, the gap between the lower valence and upper conduction bands is negligible, moderate, and large, respectively.

In an **n-type semiconductor**, donor electrons are promoted easily into the conduction band, and the dopant has more valence electrons than the semiconductor. Likewise, in a **p-type**, vice versa. In semiconductors, temperature is proportional to conductivity, and opposite for conductors.

Hydrogen bonding is the strongest intermolecular force, and occurs between a hydrogen atom and a highly electronegative atom. **Dipole force** occur for non-symmetrical compounds, and **dispersion forces** occur in the absence of the former three.



(a) hexagonal close packing and (b) cubic close packing.



The band theory for semiconductors.

Condensed Phases

In the liquid state, the force is proportional to boiling point, viscosity, number of OH^- ions, H , and inversely proportional to vapor pressure and T .

An **addition polymerization** begins with a molecule breaking down into two free radicals. A radical then attaches to a monomer molecule breaking the double bond, forming a new radical. This recursive procedure when the remaining original radical combines with the new polymer.

A **condensation reaction** is one in which two monomers with functional groups combine to form a monomer and H_2O .

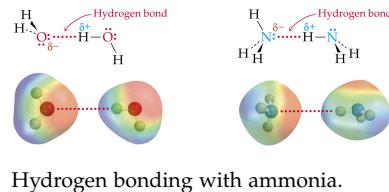
Polymers

A **block copolymer** has repeated segments of each monomer, and a **graft copolymer** has segments of one monomer branching off the main chain. Additionally, **thermoplastic** polymers melt and deform upon heating, conversely of thermosetting ones.

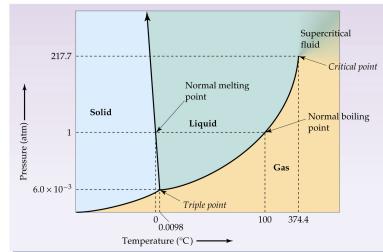
The **degree of polymerization** is $\overline{M}/M_{\text{mon}}$ and the average molecular weight of such chains is

$$\overline{M}_n = \frac{\sum MN}{\sum N} \quad \text{and} \quad \frac{\sum M^2 N}{\sum MN} \quad \text{for} \quad n_{\text{chains}} = \frac{m N_a}{\overline{M}} \quad (25)$$

The primary polymer structures are **linear, branched, and crosslinked**. The former two are connected by non-bonded interactions and can be easily recycled, and the latter by covalent bonds. Linear polymers form crystal more easily and thus become liquid when heated.



Hydrogen bonding with ammonia.



The phase diagram of water.

Miscellaneous

Organic Chemistry

SOME COMMON functional groups include

Alcohol	-OH	Amides	-C(=O)N-
Ethers	-O-	Aldehydes	-C(=O)H
Amines	-N-	Ketones	-C(=O)-
Carboxylic	-C(=O)OH	Esters	-C(=O)O-

LDPE and HDPE are linear and branched versions of polyethylene.

Energetics

The **ionization energy** is the energy required for the reaction $A \rightarrow A^+ + e^-$. Conversely, **electron affinity** is the energy required for $B + e^- \rightarrow B^-$.

The **lattice energy** is defined as $U_{lat} = |\Delta H_{lat}^\ominus|$, and is proportional to q and inversely proportional to r . This energy occurs in formation reactions $A^+ + B^- \rightarrow AB$ when $\Delta H_\ell < 0$.

Gases

The **partial pressure** of one gas is

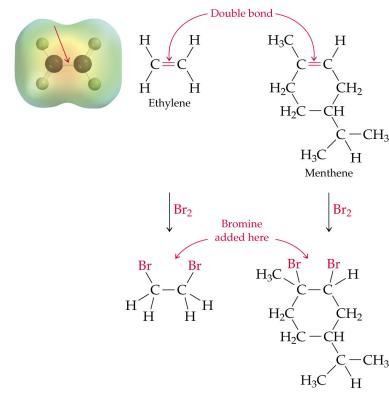
$$P_i = X_i P \quad \text{for } X_i = n_i / \sum n \quad \text{and} \quad P = \sum P_i \quad (26)$$

Consequently, or a reactant A dissociated $\delta\%$, then

$$P_A = (1 - \delta)x \quad \text{and} \quad P_B = (v_B \delta / v_A)x \quad (27)$$

where x_i is the mole fraction,

$$x_i = \frac{m_i}{m} \frac{M}{M_i} = \frac{n_i}{n} \quad (28)$$



Breaking a double bond when adding a molecule. Similar to an addition reaction.

Cheatsheet

For stoichiometric problems, use

$$n_1/v_1 = n_2/v_2 \quad (1)$$

where $n = m/M = CV$. Lewis dot structures are created by:

1. Find the sum of valence electrons
2. Connect the atoms with single bonds
3. Create multiple bonds and lone pairs for an octet

For an equilibrium reaction, the constant is

$$K_c = \prod[B]_{eq}^b / \prod[A]_{eq}^a = \prod K_i \quad (2)$$

and only includes gaseous or aqueous compounds.
For gaseous reactions, then the constant is

$$K_p = K_c RT^{\Delta v_g} \iff P_x \equiv [X] \quad (3)$$

Reactions are homogeneous iff all constituents are the same phase.

To calculate the equilibrium concentrations, construct an ICE table such that

$$[X_i]_{eq} = [A_i] \mp ax \quad (4)$$

As well, more reactants are formed if

$$[A] \uparrow \iff [B] \downarrow \iff Q > K \quad (5)$$

and $P^{-1} \propto n$ where n is the moles the side to which equilibrium moves to has.

Exothermic reactions produce heat such that if temperature increases as well, more reactants are formed.

For a reaction $A(s) \rightleftharpoons bB(aq)$, the constant

$$K_{sp} = [B]^b \iff x = (K_{sp}/\Pi b^b)^{1/\Sigma b} \quad (6)$$

Gibbs free energy is defined as

$$\Delta G^\ominus = -RT \ln K = H - TS = -T\Delta S_u \quad (7)$$

When heating a system S increases such that

$$\Delta S_u = \Delta S + \Delta S_s > 0 \quad (8)$$

where $\Delta S_s = -\Delta H/T$ for a spontaneous reaction.
If $\Delta \sum v > 0 \iff \Delta S > 0$.

The change in $\{S, G, \Delta H_f\}$ is

$$\Delta X^\ominus = \Delta \sum v X^\ominus \quad (9)$$

If $G < 0$ the reaction is spontaneous. Entropy is proportional to T, r, V, n, P^{-1} .