



# Time Series Forecasting

Programming for Data Science

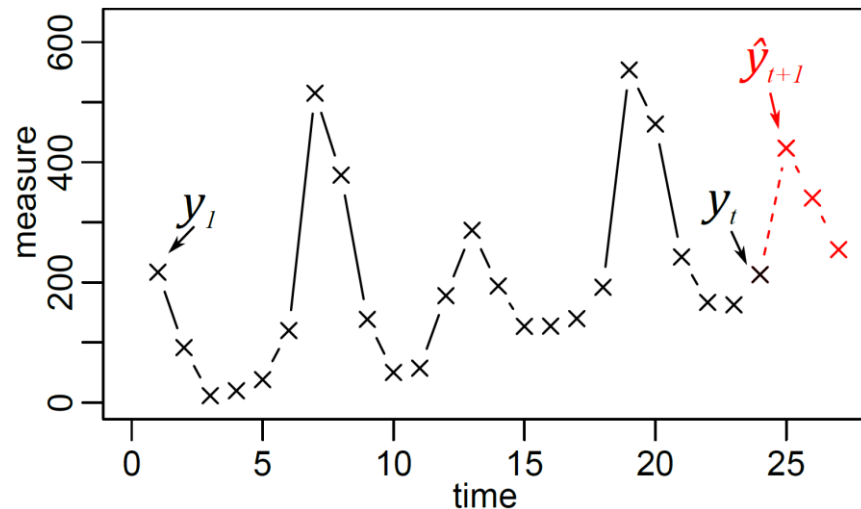
# Classical Time Series Forecasting

## Time Series

- Sequence of measure values
- Equidistant
- Complete

## Forecast Models

- One model represents one time series
  - Trend (long-term changes)
  - Season (regular reoccurring changes)
- Accuracy is the only requirement

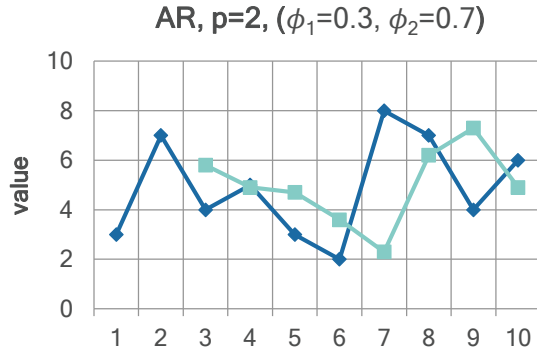


## Box and Jenkins Methodology

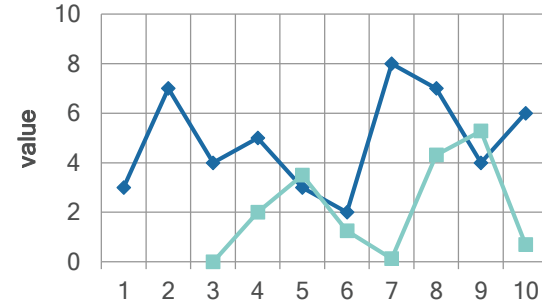
- Modeling time series with AutoRegression

## Classification and Model Hierarchy

- AR(p):  $\hat{x}_t = c + \sum_{i=1}^p \phi_i \cdot x_{t-i}$   
AutoRegression



- MA(q):  $\hat{x}_t = \sum_{i=1}^q \theta_i \cdot \varepsilon_{t-i}$   
Moving Average
- $\varepsilon_0, \dots, \varepsilon_q = 0, \varepsilon_i = x_{t-i} - \hat{x}_{t-i}$   
MA, q=2, ( $\theta_1=0.5$ ,  $\theta_2=0.5$ )



- Combine AR and MA by addition:  $\hat{x}_t = \sum_{i=1}^p \phi_i \cdot x_{t-i} + \sum_{i=1}^q \theta_i \cdot \varepsilon_{t-i} + c$

# Model Estimation (Math Part)

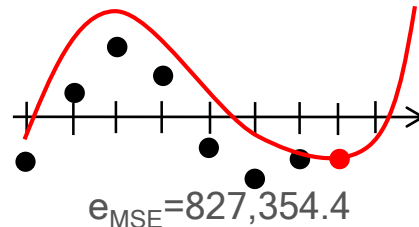
## Problem

- Find the model parameters that minimize the error on the training data

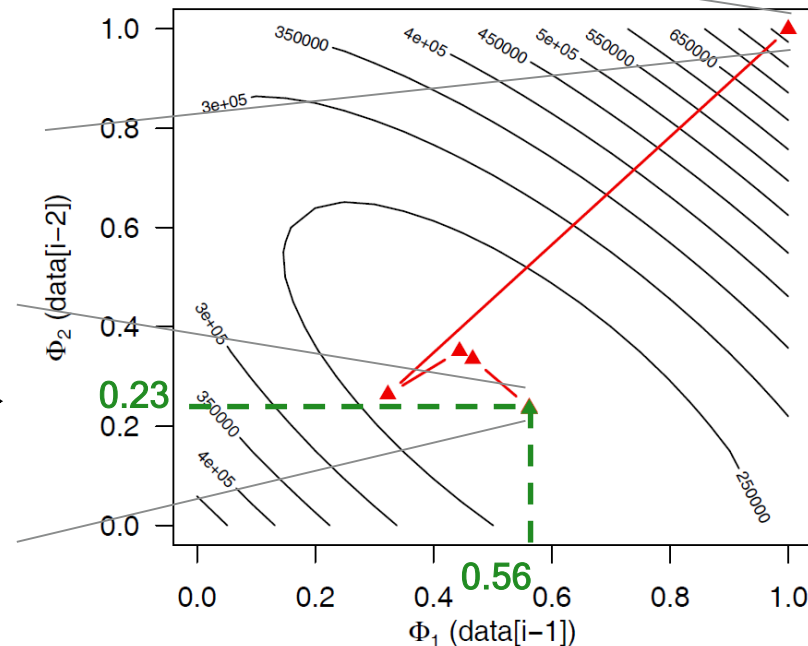
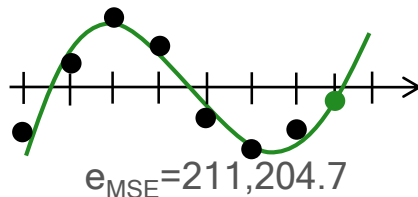
## Example

- Forecast Model Type AR(2):
  - $\hat{x}_t = \phi_1 \cdot x_{t-1} + \phi_2 \cdot x_{t-2}$
- Error Metric: MSE
  - $-\frac{1}{n} \sum_{i=1}^n (x_i - \hat{x}_i)^2$

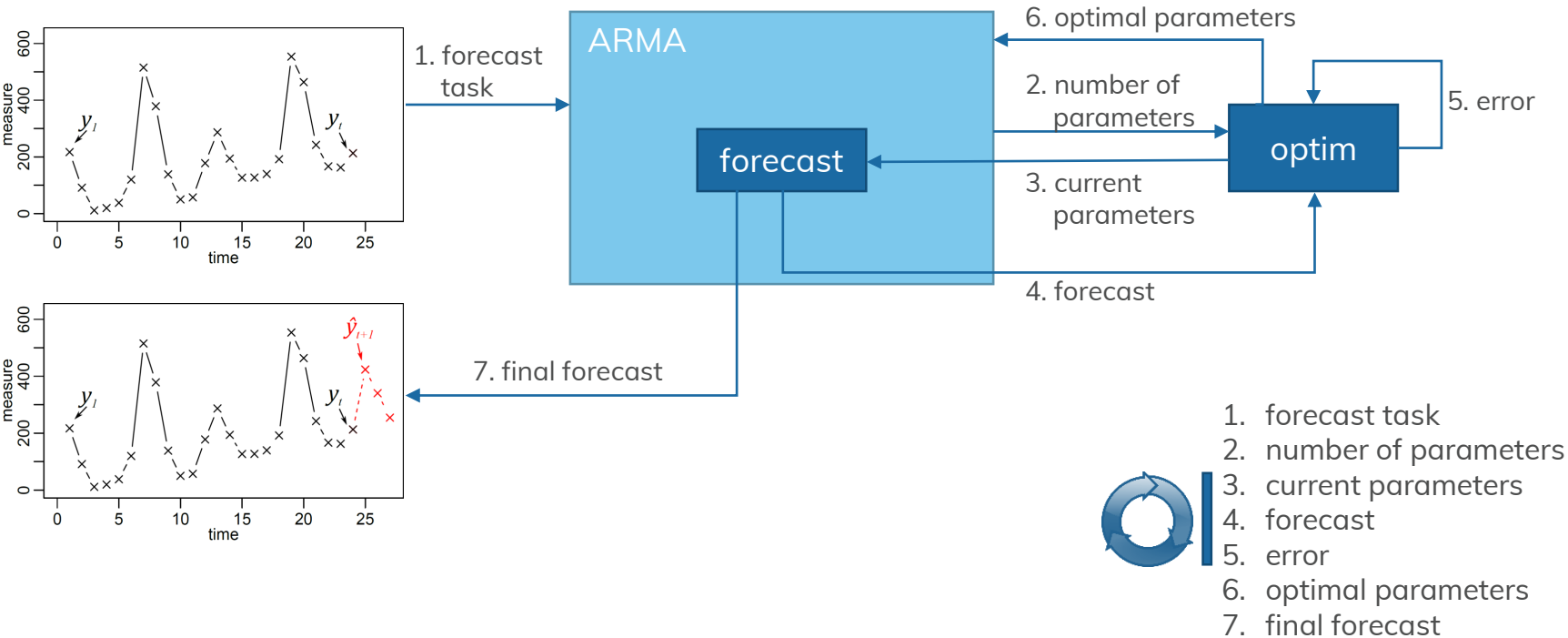
Start of Optimization



End of Optimization

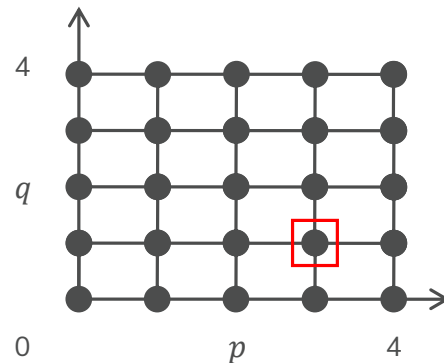


# Model Estimation (Technical Part)



## Grid Search (Derivation Free)

- Simple but robust method: no local suboptimal
- First define a step width to sample the parameter space (Grid)
- Exponential number of combinations  $X^D$  (granularity  $X$  and dimensionality  $D$ )
- Model evaluation for every combination



# Task

## Step 0

- Load the given csv file in your language/environment.
- Explore the data and its structure.

## Step 1

- Implement the AR and MA parts of the ARMA model\*.

## Step 2

- Use a general purpose optimizer (Nelder-Mead) to fit the model parameters to a given time series.

## Step 3

- Search for the optimal combination of AR ( $p$ ) and MA ( $q$ ) components of the model for each given time series\*. Perform a grid search\* for  $p \in [0,3]$  and  $q \in [0,3]$ .
- Report the forecast error.

\*use your own implementation

# Package suggestions

## R

- (data.table)
- stats

## python3

- pandas
- numpy
- scipy.optimize
- (matplotlib)



# Modeling Results

## Result

- Mean Squared Error of all time series using the best combination of  $p$  and  $q$  and a constant  $c$

## Comparison

- The values for  $p$  and  $q$  can vary based on your implementation and parameter initialization
- Only compare if your MSE correlate with our solution and are in a similar range

shop_id	Mean Squared Error
145	210
260	345
315	303
375	265
548	403
560	1272
750	539
897	9458
1332	3476
1750	377

# Exercise Appointment

## *We compare and discuss the results*

- Tuesday, 17.12.2019,
- Consultation: 12.12.2019,
- Please prepare your solutions! Send us your code!

*If you have questions, please mail us:*

[claudio.hartmann@tu-dresden.de](mailto:claudio.hartmann@tu-dresden.de) Orga + Code

[lucas.woltmann@tu-dresden.de](mailto:lucas.woltmann@tu-dresden.de) Tasks + Python

[lars.kegel@tu-dresden.de](mailto:lars.kegel@tu-dresden.de) Tasks + R

