

Conference Slides

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Lambda: Beyond The Basics

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Function

Function

Cbn

```
// Cbn<Z> zName = ...;  
// Z zValue = zName._();  
  
// in what follows we name cbn parameters like cbv ones  
  
public interface Cbn<Z> {  
    Z _();  
}
```

Block

```
// Block block = ...;  
// block._();  
  
public interface Block {  
    void _();  
}
```

Function

```
// Z z = ...;  
// Function<Z, Y> z2y = ...;  
// Y y = z2y._(z);  
  
public interface Function<Z, Y> {  
    Y _(Z z);  
}
```

FunctionStatics

```
public class FunctionStatics {  
    public static <Z>  
    Z identity(Z z) {  
        return z;  
    }  
}
```

BiFunction

```
// Z z = ...;  
// Y y = ...;  
// BiFunction<Z, Y, X> zny2x = ...;  
// X x = zny2x._(z, y);  
  
public interface BiFunction<Z, Y, X> {  
    X _(Z z, Y y);  
}
```

Ref

```
public class Ref<Z> {  
    private Z value;  
  
    public Z deref() {  
        return value;  
    }  
  
    public void assign(Z value) {  
        this.value = value;  
    }  
}
```


while (CbnApp)

```
private static Function<Block, Block> _while(  
    Cbn<Boolean> cond  
) {  
    return  
        block ->  
            () -> {  
                if (cond._()) {  
                    block._();  
                    _while(cond)._ (block)._ ();  
                }  
                ;  
            };  
}
```

example (CbnApp)

```
// before 0
// after 10

public static void main(String[] args) {
    Ref<Integer> integerRef = new Ref<>();
    integerRef.assign(0);
    System.out.println("before " + integerRef.deref());
    _while(() ->
        (integerRef.deref() < 10))._(() -> {
            integerRef.assign(integerRef.deref() + 1);
        })._();
    System.out.println("after " + integerRef.deref());
}
```

Option

Option

Option

```
public interface Option<Z> {
```

Some

```
final public class Some<Z>  
    implements Option<Z> {  
  
    final Z value;
```

None

```
final public class None<Z>  
    implements Option<Z> {
```

fold (Option)

```
// abstract method
// follows the structure of Option

public <Y>
Y fold(
    final Function<Z, Y> z2y,
    final Cbn<Y> y
);
```

fold (Some)

```
// uses z2y

@Override
public <Y>
Y fold(
    final Function<Z, Y> z2y,
    final Cbn<Y> y
) {
    return
        z2y._(value);
}
```


fold (None)

```
// uses y

@Override
public <Y>
Y fold(
    final Function<Z, Y> z2y,
    final Cbn<Y> y
) {
    return
        y._();
}
```

some (OptionStatics)

```
// specific factory method  
// not part of generic DSL
```

```
public static <Z>  
Option<Z> some(  
    final Z value  
) {  
    return  
        new Some<>(value);  
}
```

none (OptionStatics)

```
// specific factory method  
// not part of generic DSL
```

```
public static <Z>  
Option<Z> none(  
    ) {  
    return  
        new None<Z>();  
}
```

identity (Option)

```
default public Option<Z> identity() {  
  return  
    fold(  
      OptionStatics::some,  
      OptionStatics::none  
    );  
}
```

length (Option)

```
default public int length() {  
  return  
    fold(  
      z -> 1,  
      () -> 0  
    );  
}
```

bindM (Option)

```
// binding is a fundamental
// (functional) programming concept

default public <Y>
Option<Y> bindM(
    final Function<Z, Option<Y>> z2oy
) {
    return
        fold(
            z2oy,
            OptionStatics::none
        );
}
```

one (OptionStatics)

```
// multiplicative method

public static <Z>
Option<Z> one(
    final Z z
) {
    return
        some(z);
}
```

bindF (Option)

// typically used at the end of a binding chain

```
default public <Y>
Option<Y> bindF(
  final Function<Z, Y> z2y
) {
  return
    bindM(z ->
      one(z2y._(z))
    );
}
```


bindA (Option)

```
// multiplicative method
// note: z is only used within the scope of bindF

default public <Y>
Option<Y> bindA(
  final Option<Function<Z, Y>> o_z2y
) {
  return
    bindM(z ->
      o_z2y.bindF(z2y ->
        z2y._(z)
      )
    );
}
```

join (OptionStatics)

```
public static <Z>  
Function<Option<Option<Z>>, Option<Z>> join(  
) {  
    return  
        ooz ->  
            ooz.bindM(oz ->  
                oz  
            );  
}
```

choice (Option)

```
default public Option<Z> choice(  
    final Function<Z, Boolean> z2b,  
    final Function<Z, Option<Z>> t_z2oz,  
    final Function<Z, Option<Z>> f_z2oz  
) {  
    return  
        bindM(z ->  
            z2b._(z)  
            ? t_z2oz._(z)  
            : f_z2oz._(z)  
        );  
}
```

example01 (OptionApp)

```
// example01 = one(abc)

Option<String> example01 =
  one("a").bindM(a ->
    one("b").bindM(b ->
      one("c").bindM(c ->
        one(a + b + c)
      )
    )
  );
```

example02 (OptionApp)

```
// example02 = one(abc)

Option<String> example02 =
  one("a").bindM(a ->
    one("b").bindM(b ->
      one("c").bindF(c ->
        a + b + c
      )
    )
  );
```

example03 (OptionApp)

```
// example03 = one(abc)

Option<String> example03 =
  one("a").bindA(
    one("b").bindA(
      one("c").bindF(c -> b -> a ->
        a + b + c
      )
    )
  );
```

example06 (OptionApp)

```
// example06 = one(c)

Option<String> example06 =
  one("a").choice(a ->
    a.equals("b"),
    a -> one("b"),
    a -> one("c")
  );
```

zero (OptionStatics)

```
// additive method
```

```
public static <Z>  
Option<Z> zero(  
) {  
    return  
        none();  
}
```


example04 (OptionApp)

```
// example04 = zero  
  
Option<String> example04 =  
  one("a").bindM(a ->  
    zero().bindM(z ->  
      one("c").bindF(c ->  
        a + z + c  
      )  
    )  
  );
```

example05 (OptionApp)

```
// example05 = zero

Option<String> example05 =
  one("a").bindA(
    zero().bindA(
      one("c").bindF(c -> z -> a ->
        a + z + c
      )
    )
  );
```

filter (Option)

```
default public Option<Z> filter(  
    final Function<Z, Boolean> z2b  
) {  
    return  
        choice(  
            z2b,  
            z -> one(z),  
            z -> zero()  
        );  
}
```

example07 (OptionApp)

```
// example07 = zero  
  
Option<String> example07 =  
  one("a").filter(a ->  
    a.equals("b")  
  );
```

plus (Option)

```
// additive method

default public Option<Z> plus(
    final Cbn<Option<Z>> _2oz
) {
    return
        fold(
            OptionStatics::some,
            _2oz
        );
}
```

plus (OptionStatics)

```
// static version of plus
```

```
public static <Z>  
Option<Z> plus(  
    final Option<Z> oz1,  
    final Cbn<Option<Z>> oz2  
) {  
    return  
        oz1.plus(oz2);  
}
```

someOptions (OptionApp)

```
private static final
Option<String> oneA_plus_oneB =
    one("a").plus(() -> one("b"));
private static final
Option<String> oneC_plus_oneD =
    one("c").plus(() -> one("d"));
```

someOptionsUsingZero (OptionApp)

```
private static final
Option<String> oneA_plus_zero =
    one("a").plus(() -> zero());
// note: sometimes we have to help the type inferencer
private static final
Option<String> zero_plus_oneA =
    OptionStatics.<String>zero().plus(() -> one("a"));
```


example08 (OptionApp)

```
// example08 = one(a)  
  
Option<String> example08 =  
  oneA_plus_oneB;
```

example09 (OptionApp)

```
// example09 = one(a)  
  
Option<String> example09 =  
  oneA_plus_zero;
```

example10 (OptionApp)

```
// example10 = one(a)  
  
Option<String> example10 =  
  zero_plus_oneA;
```

example11 (OptionApp)

```
// example11 = one(ac)

Option<String> example11 =
  oneA_plus_oneB.bindM(apb ->
    oneC_plus_oneD.bindF(cpd ->
      apb + cpd
    )
  );
```

example12 (OptionApp)

```
// example12 = one(a)  
  
Option<String> example12 =  
  oneA_plus_oneB.identity();
```

example13 (OptionApp)

```
// example13 = 1  
  
int example13 =  
    oneA_plus_oneB.length();
```

Stream

Stream

Stream

```
public interface Stream<Z> {
```


More

```
final public class More<Z>  
    implements Stream<Z> {  
  
    final Z current;  
    final Cbn<Stream<Z>> next;
```

Done

```
final public class Done<Z>  
    implements Stream<Z> {
```

fold (Stream)

```
// abstract method
// follows the recursive structure of Stream

public <Y>
Y fold(
    final BiFunction<Z, Cbn<Y>, Y> zny2y,
    final Cbn<Y> y
);
```

fold (More)

```
@Override
public <Y>
Y fold(
    final BiFunction<Z, Cbn<Y>, Y> zny2y,
    final Cbn<Y> y
) {
    return
        zny2y._(
            current,
            () -> next._().fold(zny2y, y)
        );
}
```

fold (Done)

```
@Override
public <Y>
Y fold(
    final BiFunction<Z, Cbn<Y>, Y> zny2y,
    final Cbn<Y> y
) {
    return
        y._();
}
```

more (StreamStatics)

```
public static <Z>  
Stream<Z> more(  
    final Z current,  
    final Cbn<Stream<Z>> next  
) {  
    return  
        new More<>(current, next);  
}
```

done (StreamStatics)

```
public static <Z>  
Stream<Z> done(  
) {  
    return  
        new Done<>();  
}
```

identity (Stream)

```
default public Stream<Z> identity() {  
    return  
        fold(  
            StreamStatics::more,  
            StreamStatics::done  
        );  
}
```


length (Stream)

```
default public Integer length() {  
    return  
        fold(  
            (z, l) -> 1 + l._(),  
            () -> 0  
        );  
}
```

zero (StreamStatics)

```
public static <Z>  
Stream<Z> zero(  
    ) {  
    return  
        done();  
}
```

plus (Stream)

```
default public Stream<Z> plus(  
    final Cbn<Stream<Z>> sz  
) {  
    return  
        fold(  
            StreamStatics::more,  
            sz  
        );  
}
```

bindM (Stream)

```
default public <Y>
Stream<Y> bindM(
  final Function<Z, Stream<Y>> z2sy
) {
  return
    fold(
      (z, sy) -> z2sy._(z).plus(sy),
      StreamStatics::zero
    );
}
```

one (StreamStatics)

```
public static <Z>  
Stream<Z> one(  
    final Z z  
) {  
    return  
        more(z, StreamStatics::done);  
}
```

example01 (StreamApp)

```
// example01 = one(abc) : zero
```

```
Stream<String> example01 =  
  one("a").bindM(a ->  
    one("b").bindM(b ->  
      one("c").bindM(c ->  
        one(a + b + c)  
      )  
    )  
  );
```

example02 (StreamApp)

```
// example02 = one(abc) : zero
```

```
Stream<String> example02 =  
  one("a").bindM(a ->  
    one("b").bindM(b ->  
      one("c").bindF(c ->  
        a + b + c  
      )  
    )  
  );
```

example03 (StreamApp)

```
// example03 = one(abc) : zero

Stream<String> example03 =
  one("a").bindA(
    one("b").bindA(
      one("c").bindF(c -> b -> a ->
        a + b + c
      )
    )
  );
```


example06 (StreamApp)

```
// example06 = one(c) : zero
```

```
Stream<String> example06 =  
  one("a").choice(a ->  
    a.equals("b"),  
    a -> one("b"),  
    a -> one("c")  
  );
```

example04 (StreamApp)

```
// example04 = zero  
  
Stream<String> example04 =  
  one("a").bindM(a ->  
    zero().bindM(z ->  
      one("c").bindF(c ->  
        a + z + c  
      )  
    )  
  );
```

example05 (StreamApp)

```
// example05 = zero  
  
Stream<String> example05 =  
  one("a").bindA(  
    zero().bindA(  
      one("c").bindF(c -> z -> a ->  
        a + z + c  
      )  
    )  
  );
```

example07 (StreamApp)

```
// example07 = zero  
  
Stream<String> example07 =  
    one("a").filter(a ->  
        a.equals("b")  
    );
```

example08 (StreamApp)

```
// example08 = one(a) : one(b) : zero
```

```
Stream<String> example08 =  
    oneA_plus_oneB;
```

example09 (StreamApp)

```
// example09 = one(a) : zero
```

```
Stream<String> example09 =  
  oneA_plus_zero;
```

example10 (StreamApp)

```
// example10 = one(a) : zero
```

```
Stream<String> example10 =  
  zero_plus_oneA;
```

example11 (StreamApp)

```
// example11 = one(ac) : one(ad) : one(bc) : one(bd) : zero
```

```
Stream<String> example11 =  
  oneA_plus_oneB.bindM(apb ->  
    oneC_plus_oneD.bindF(cpd ->  
      apb + cpd  
    )  
  );
```


example12 (StreamApp)

```
// example12 = example12 = one(a) : one(b) : zero
```

```
Stream<String> example12 =  
    oneA_plus_oneB.identity();
```

example13 (StreamApp)

```
// example13 = 2  
  
int example13 =  
    oneA_plus_oneB.length();
```

take (Stream)

```
// note: a stream can be infinite
```

```
public Stream<Z> take(  
    int n  
);
```

take (More)

```
@Override
public Stream<Z> take(
    int n
) {
    return
        (n > 0)
        ? more(
            current,
            () -> next._().take(n - 1)
        )
        : done();
}
```

take (Done)

```
@Override  
public Stream<Z> take(  
    int n  
) {  
    return  
        done();  
}
```

infinitelyMany (StreamApp)

```
private static <Z>  
Stream<Z> infinitelyMany(  
    Z z  
) {  
    return  
        one(z).plus(  
            () -> infinitelyMany(z)  
        );  
}
```

example14 (StreamApp)

```
// example14 = one(a) : one(a) : one(a) : one(a) : zero
```

```
Stream<String> example14 =  
  infinitelyMany("a").take(4);
```

fibonacciNumbersFrom (StreamApp)

```
private static Stream<Integer> fibonacciNumbersFrom(  
    Integer fib0,  
    Integer fib1  
) {  
    return  
        one(fib0).plus(  
            () -> fibonacciNumbersFrom(fib1, fib0 + fib1)  
        );  
}
```


example15 (StreamApp)

```
// example15 = one(1) : one(2) : one(3) : one(5) : zero
```

```
Stream<Integer> example15 =  
    fibonacciNumbersFrom(1, 2).take(4);
```

lift (StreamStatics)

```
// cbn version of one

public static <Z>
Cbn<Stream<Z>> lift(
    final Cbn<Z> z
) {
    return
        () -> one(z._());
}
```

liftF (StreamStatics)

```
// static version of bindF

public static <Z, Y>
Function<Stream<Z>, Stream<Y>> liftF(
    final Function<Z, Y> z2y
) {
    return
        sz ->
            sz.bindF(z2y);
}
```

liftA (StreamStatics)

```
// static version of bindA

public static <Z, Y>
Function<Stream<Z>, Stream<Y>> liftA(
    final Stream<Function<Z, Y>> s_z2y
) {
    return
        sz -> sz.bindA(s_z2y);
}
```

liftBF (StreamStatics)

```
public static <Z, Y, X>  
BiFunction<Stream<Z>, Cbn<Stream<Y>>, Stream<X>> liftBF(  
    final BiFunction<Z, Cbn<Y>, X> zny2x  
) {  
    return  
        (sz, sy) ->  
            sz.bindA(  
                sy._().bindF(y -> z ->  
                    zny2x._(z, () -> y)  
                )  
            );  
}
```

foreachDeclaration (Stream)

```
default public <Y, X, MY, MX>  
Function<Function<Z, MY>, MX> foreach(  
    final Cbn<X> x,  
    final BiFunction<Y, Cbn<X>, X> ynx2x,  
    final Function<Cbn<X>, Cbn<MX>> lift,  
    final Function<  
        BiFunction<Y, Cbn<X>, X>,  
        BiFunction<MY, Cbn<MX>, MX>  
        > liftBF  
)
```

foreachDefinition (Stream)

```
{  
  return  
    z2my ->  
      fold(  
        (z, mx) ->  
          liftBF._(ynx2x)._ (z2my._(z), mx),  
          lift._(x)  
      );  
}
```

sequenceOpDeclaration (OptionStatics)

```
public static <Z>  
Function<Stream<Option<Z>>, Option<Stream<Z>>> sequenceOp(  
    final Cbn<Stream<Z>> sz,  
    final BiFunction<  
        Stream<Z>, Cbn<Stream<Z>>,  
        Stream<Z>  
        > sznsz2sz  
)
```


sequenceOpDefinition (OptionStatics)

```
{  
  return  
    soz ->  
      soz.foreach(  
        sz,  
        sznsz2sz,  
        OptionStatics::lift,  
        OptionStatics::liftBF  
      )._(  
        liftF(StreamStatics::one)  
      );  
}
```

sequenceAccDeclaration (OptionStatics)

```
public static <Z>  
Function<Stream<Option<Z>>, Option<Stream<Z>>> sequenceAcc(  
    final Cbn<Stream<Z>> sz,  
    final BiFunction<Z, Cbn<Stream<Z>>, Stream<Z>> znsz2sz  
)
```

sequenceAccDefinition (OptionStatics)

```
{  
  return  
    soz ->  
      soz.foreach(  
        sz,  
        znsz2sz,  
        OptionStatics::lift,  
        OptionStatics::liftBF  
      )._(  
        liftF(FunctionStatics::identity)  
      );  
}
```

someStreamsOfOptions (OptionApp)

```
private static final
Stream<Option<String>> oneOA_plus_oneOB =
    StreamStatics.one(one("a")).plus(() ->
        StreamStatics.one(one("b")))
    );
private static final
Stream<Option<String>> oneZ_plus_oneOB =
    StreamStatics.<Option<String>>one(zero()).plus(() ->
        StreamStatics.one(one("b")))
    );
private static final
Stream<Option<String>> oneOA_plus_oneZ =
    StreamStatics.one(one("a")).plus(() ->
        StreamStatics.one(zero()))
    );
```

example14 (OptionApp)

```
// example14 = one(one(a) : one(b) : zero)

Option<Stream<String>> example14 =
  OptionStatics.<String>sequenceOp(
    StreamStatics::zero,
    StreamStatics::plus
  )._(
    one0A_plus_one0B
  );
```

example15 (OptionApp)

```
// example15 = zero

Option<Stream<String>> example15 =
  OptionStatics.<String>sequenceAcc(
    StreamStatics::done,
    StreamStatics::more
  )._(
    oneZ_plus_one0B
  );
```

example16 (OptionApp)

```
// example16 = zero

Option<Stream<String>> example16 =
  OptionStatics.<String>sequenceAcc(
    StreamStatics::done,
    StreamStatics::more
  )._(
    one0A_plus_oneZ
  );
```

example17 (OptionApp)

```
// example17 = one(one(A)) : zero
Stream<Option<String>> example17 =
  oneA_plus_oneB.<
    Option<String>, Option<String>,
    Stream<Option<String>>, Stream<Option<String>>
  >foreach(
    OptionStatics::zero, FunctionStatics::identity,
    StreamStatics::lift, StreamStatics::liftF
  )._(s ->
    StreamStatics.one(
      one(s.toUpperCase())
    )
  );
```


foreachDeclaration (Option)

```
default public <Y, X, MY, MX>  
Function<Function<Z, MY>, MX> foreach(  
    final Cbn<X> x,  
    final Function<Y, X> y2x,  
    final Function<Cbn<X>, Cbn<MX>> lift,  
    final Function<Function<Y, X>, Function<MY, MX>> liftF  
)
```

foreachDefinition (Option)

```
{  
  return  
    z2my ->  
      fold(  
        z -> liftF._(y2x)._ (z2my._(z)),  
        lift._(x)  
      );  
}
```

sequenceFunDeclaration (StreamStatics)

```
public static <Z>  
Function<Option<Stream<Z>>, Stream<Option<Z>>> sequenceFun(  
    final Cbn<Option<Z>> oz,  
    final Function<Option<Z>, Option<Z>> oz2oz  
)
```

sequenceFunDefinition (StreamStatics)

```
{  
  return  
    osz ->  
      osz.foreach(  
        oz,  
        oz2oz,  
        StreamStatics::lift,  
        StreamStatics::liftF  
      )._(  
        liftF(OptionStatics::one)  
      );  
}
```

example16 (StreamApp)

```
// example16 = one(one(a)) : zero

Stream<Option<String>> example16 =
  StreamStatics.<String>sequenceFun(
    OptionStatics::zero,
    FunctionStatics::identity
  )._(
    oneSA_plus_oneSB
  );
```

example17 (StreamApp)

```
// example17 = zero

Stream<Option<String>> example17 =
  StreamStatics.<String>sequenceFun(
    OptionStatics::zero,
    FunctionStatics::identity
  )._(
    oneZ_plus_oneSB
  );
```

example18 (StreamApp)

```
// example18 = one(one(a)) : zero

Stream<Option<String>> example18 =
  StreamStatics.<String>sequenceFun(
    OptionStatics::zero,
    FunctionStatics::identity
  )._(
    oneSA_plus_oneZ
  );
```

example19 (StreamApp)

```
// example19 = one(one(A) : one(B) : zero)
Option<Stream<String>> example19 =
  oneA_plus_oneB.<
    Stream<String>, Stream<String>,
    Option<Stream<String>>, Option<Stream<String>>
  >foreach(
    StreamStatics::zero, StreamStatics::plus,
    OptionStatics::lift, OptionStatics::liftBF
  )._(s ->
    OptionStatics.one(
      one(s.toUpperCase())
    )
  );
```


Tuple

Tuple

Tuple

```
// Tuple<Z, Y> zny = ...;  
// Z z = zny._1;  
// Y y = zny._2  
  
public final class Tuple<Z, Y> {  
    public final  
    Z _1;  
    public final  
    Y _2;  
}
```

TupleStatics

```
public final class TupleStatics {  
    public static <Z, Y>  
    Tuple<Z, Y> tuple(  
        final Z z,  
        final Y y  
    ) {  
        return  
            new Tuple<>(z, y);  
    }  
}
```

Unit

Unit

Unit

```
public final class Unit {  
    @Override  
    public String toString() {  
        return "unit";  
    }  
}
```

UnitStatics

```
public final class UnitStatics {  
    public final static  
        Unit unit =  
            new Unit();  
}
```

State

State

State

```
// note: functional interface  
  
public interface State<S, Z> {  
  
    public Function<S, Tuple<Z, S>> open();  
  
}
```


bindM (State)

```
// note: function literal

default public <Y>
State<S, Y> bindM(
  final Function<Z, State<S, Y>> z2sy
) {
  return
    () ->
      s -> {
        Tuple<Z, S> zns = open()._(s);
        return
          z2sy._(zns._1).open()._(zns._2);
      };
}
```

one (StateStatics)

```
public static <S, Z>  
State<S, Z> one(  
    final Z z  
) {  
    return  
        () ->  
        s ->  
            tuple(z, s);  
}
```

get (StateStatics)

```
public static <S>  
State<S, S> get(  
) {  
    return  
        () ->  
        s ->  
        tuple(s, s);  
}
```

set (StateStatics)

```
static <S>
State<S, Unit> set(
  final S newS
) {
  return
    () ->
      oldS ->
        tuple(unit, newS);
}
```

exec (StateStatics)

```
public static <S>
State<S, Unit> exec(
    final Function<S, S> s2s
) {
    return
        StateStatics.<S>get().bindM(s ->
            set(s2s._(s))
        );
}
```

Status (StateApp)

```
public enum Status {  
    FREE, BUSY  
}
```

Action (StateApp)

```
public enum Action {  
    COIN, CANDY  
}
```

Machine (StateApp)

```
public class Machine {  
    Status status;  
    int candies;  
    int coins;
```


actions (StateApp)

```
private static final Stream<Action> coin =  
    one(COIN);  
private static final Stream<Action> candy =  
    one(CANDY);  
private static final Stream<Action> actions =  
    coin.plus(  
        () -> candy  
    ).plus(  
        () -> coin  
    ).plus(  
        () -> candy  
    );
```

stateMachinePartOne (StateApp)

```
private static State<Machine, Unit> stateMachine(  
  final Stream<Action> actions  
) {  
  return  
    actions.<  
      Unit, Unit,  
      State<Machine, Unit>, State<Machine, Unit>  
    >foreach(  
      () -> unit, (u, v) -> unit,  
      StateStatics::lift, StateStatics::liftBF  
    )  
}
```

stateMachinePartTwo (StateApp)

```
._(a ->
  exec(
    m ->
      m.candies == 0 ||
        a == COIN && m.status == BUSY ||
        a == CANDY && m.status == FREE
      ? m
      : a == COIN && m.status == FREE
      ? new Machine(BUSY, m.candies, m.coins + 1)
      : a == CANDY && m.status == BUSY
      ? new Machine(FREE, m.candies - 1, m.coins)
      : null // this should never happen
    )
  );
}
```

stateMachineTest (StateApp)

```
System.out.println(  
    stateMachine(actions).open()._(  
        new Machine(FREE, 10, 0)  
    )._2  
);
```

Concurrent

Concurrent

SimpleFuture

```
public interface SimpleFuture<Z>
    extends Future<Z> {
    public Z compute(long total);

    default public Z get() {
        return
            compute(Long.MAX_VALUE);
    }

    default public Z get(long total, TimeUnit timeUnit) {
        return
            compute(MILLISECONDS.convert(total, timeUnit));
    }
}
```

notImplemented

```
default public boolean isDone() {  
    throw  
        new IllegalStateException("not implemented");  
}
```

```
default public boolean isCancelled() {  
    throw  
        new IllegalStateException("not implemented");  
}
```

```
default public boolean cancel(boolean interruptable) {  
    throw  
        new IllegalStateException("not implemented");  
}
```

Future

```
public interface Future<Z> {  
  
    public Function<ExecutorService, SimpleFuture<Z>> open();  
}
```


bindMDeclaration (Future)

```
default public <Y>  
Future<Y> bindM(  
    final Function<Z, Future<Y>> z2fy  
)
```

bindMDefinition (Future)

```
{  
  return  
    () -> es -> totalTime -> {  
      try {  
        final long start = currentTimeMillis();  
        final Z z = open()._(es).get(totalTime, MILLISECONDS);  
        final long stop = currentTimeMillis();  
        final long remainingTime = totalTime - (stop - start);  
        final Future<Y> fy = z2fy._(z);  
        return  
          fy.open()._(es).get(remainingTime, MILLISECONDS);  
      } catch (Exception e) {  
        throw new IllegalStateException("not implemented");  
      }  
    };  
}
```

one (FutureStatics)

```
public static <Z>  
Future<Z> one(  
    final Z z  
) {  
    return  
        () ->  
            es ->  
                timeout ->  
                    z;  
}
```

bindADeclaration (Future)

```
// note: has other default definition
```

```
default public <Y>
```

```
Future<Y> bindA(
```

```
    final Future<Function<Z, Y>> f_z2y
```

```
)
```

bindADefinitionPartOne (Future)

```
{  
  return  
    () -> es -> {  
      final SimpleFuture<Z> sfz =  
        open()._(es);  
      final SimpleFuture<Function<Z, Y>> sf_z2y =  
        f_z2y.open()._(es);
```

bindADefinitionPartTwo (Future)

```
return
totalTime -> {
  try {
    final long start = currentTimeMillis();
    final Z z = sfz.get(totalTime, MILLISECONDS);
    final long stop = currentTimeMillis();
    final long remainingTime = totalTime - (stop - start);
    final Function<Z, Y> z2y =
      sf_z2y.get(remainingTime, MILLISECONDS);
    return z2y._(z);
  } catch (Exception e) {
    throw new IllegalStateException("not implemented");
  }
};
```

bindF (Future)

// note: has other default definition

```
default public <Y>
Future<Y> bindF(
    final Function<Z, Y> z2y
) {
    return
        bindA(
            one(z2y)
        );
}
```

forkDeclaration (FutureStatics)

```
public static <Z>  
Future<Z> fork(  
    final Cbn<Future<Z>> fz  
)
```


forkDefinitionPartOne (FutureStatics)

```
{  
  return  
    () -> es -> {  
      final CountdownLatch latch = new CountdownLatch(1);  
      final Ref<Z> rz = new Ref<Z>();  
      es.submit(  
        () -> {  
          try {  
            rz.assign(fz._().open()._().get());  
            latch.countDown();  
          } catch (Exception e) {  
            throw new IllegalStateException("not implemented");  
          }  
        }  
      );  
    }  
}
```

forkDefinitionPartTwo (FutureStatics)

```
return
  timeout -> {
    try {
      latch.await(timeout, MILLISECONDS);
      return rz.deref();
    } catch (Exception e) {
      throw new IllegalStateException("not implemented");
    }
  };
};
```

async (FutureStatics)

```
public static <Z>
Future<Z> async(
    final Cbn<Z> z
) {
    return
        fork(
            () -> one(z._())
        );
}
```

sleep (FutureApp)

```
private static void sleep(long time) {  
    try {  
        Thread.sleep(time);  
    } catch (Exception e) {  
        throw new IllegalStateException("not implemented");  
    }  
}
```

mkExecutorService (FutureApp)

```
private static final ExecutorService executorService =  
    Executors.newScheduledThreadPool(10);
```

fourTimesZero (FutureApp)

```
private final static
Stream<Integer> fourTimesZero =
    one(0).plus(
        () -> one(0)
    ).plus(
        () -> one(0)
    ).plus(
        () -> one(0)
    );
```

future (FutureApp)

```
private static Future<Integer> future(int i) {  
    return  
        async(() -> {  
            sleep(5000);  
            return 10;  
        });  
}
```

foreachTest (FutureApp)

```
// one(10) : one(10) : one(10) : one(10) : zero

System.out.println(
  fourTimesZero.<
    Integer, Stream<Integer>,
    Future<Integer>, Future<Stream<Integer>>
  >foreach(
    StreamStatics::done, StreamStatics::more,
    FutureStatics::lift, FutureStatics::liftBF
  )._(
    i -> future(10)
  ).open()._(executorService).get()
);
```


fourTimesFuture (FutureApp)

```
private static final
Stream<Future<Integer>> fourTimesFutureTen =
    one(future(10)).plus(
        () -> one(future(10))
    ).plus(
        () -> one(future(10))
    ).plus(
        () -> one(future(10))
    );
```

sequenceTest (FutureApp)

```
// one(10) : one(10) : one(10) : one(10) : zero

System.out.println(
  FutureStatics.<Integer>sequenceAcc(
    StreamStatics::done, StreamStatics::more
  )._(
    fourTimesFutureTen
  ).open()._(executorService).get()
);
```