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Lambda: Beyond The Basics

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Function

Function



Cbn

```
// Cbn<Z> zName = ...;
// Z zValue = zName._();

// in what follows we name cbn parameters like cbv ones
public interface Cbn<Z> {
    Z _();
}
```

Block

```
// Block block = ...;
// block._();
public interface Block {
  void _();
}
```

Function

```
// Z z = ...;
// Function<Z, Y> z2y = ...;
// Y y = z2y._(z);

public interface Function<Z, Y> {
   Y _(Z z);
}
```

FunctionStatics

```
public class FunctionStatics {
  public static <Z>
  Z identity(Z z) {
   return z;
  }
}
```

BiFunction

```
// Z z = ...;
// Y y = ...;
// BiFunction<Z, Y, X> zny2x = ...;
// X x = zny2x._(z, y);
public interface BiFunction<Z, Y, X> {
    X _(Z z, Y y);
}
```

Ref

```
public class Ref<Z> {
  private Z value;

public Z deref() {
  return value;
 }

public void assign(Z value) {
  this.value = value;
 }
}
```

while (CbnApp)

```
private static Function<Block, Block> _while(
 Cbn<Boolean> cond
 return
 block ->
   () -> {
    if (cond._()) {
     block._();
     _while(cond)._(block)._();
  };
```

example (CbnApp)

```
// before 0
// after 10
public static void main(String[] args) {
 Ref<Integer> integerRef = new Ref<>();
 integerRef.assign(0);
 System.out.println("before " + integerRef.deref());
 while(() ->
  (integerRef.deref() < 10))._(() -> {
  integerRef.assign(integerRef.deref() + 1);
 }). ():
 System.out.println("after " + integerRef.deref());
```

Option

Option



Option

```
{\tt public\ interface\ Option< Z>\ \{}
```



Some

```
final public class Some<Z>
  implements Option<Z> {
  final Z value;
```



None

```
final public class None<Z>
  implements Option<Z> {
```



fold (Option)

```
// abstract method
// follows the structure of Option
public <Y>
Y fold(
  final Function<Z, Y> z2y,
  final Cbn<Y> y
);
```

fold (Some)

```
// uses z2y

@Override
public <Y>
Y fold(
  final Function<Z, Y> z2y,
  final Cbn<Y> y
) {
  return
    z2y._(value);
}
```

fold (None)

```
// uses y
@Override
public <Y>
Y fold(
  final Function<Z, Y> z2y,
  final Cbn<Y> y
) {
  return
  y._();
}
```

some (OptionStatics)

```
// specific factory method
// not part of generic DSL
public static <Z>
Option<Z> some(
  final Z value
) {
  return
   new Some<>(value);
}
```

none (OptionStatics)

```
// specific factory method
// not part of generic DSL
public static <Z>
Option<Z> none(
) {
  return
   new None<Z>();
}
```

identity (Option)

```
default public Option<Z> identity() {
  return
  fold(
    OptionStatics::some,
    OptionStatics::none
  );
}
```

length (Option)

```
default public int length() {
  return
  fold(
   z -> 1,
    () -> 0
  );
}
```

bindM (Option)

```
// binding is a fundamental
// (functional) programming concept
default public <Y>
Option<Y> bindM(
 final Function<Z, Option<Y>> z2oy
) {
 return
 fold(
  z2ov,
   OptionStatics::none
  );
```

one (OptionStatics)

```
// multiplicative method
public static <Z>
Option<Z> one(
  final Z z
) {
  return
  some(z);
}
```

bindF (Option)

```
// typically used at the end of a binding chain

default public <Y>
Option<Y> bindF(
  final Function<Z, Y> z2y
) {
  return
  bindM(z ->
    one(z2y._(z))
  );
}
```

bindA (Option)

```
// multiplicative method
// note: z is only used within the scope of bindF
default public <Y>
Option<Y> bindA(
 final Option<Function<Z, Y>> o_z2y
) {
 return
  bindM(z \rightarrow
   o_z2y.bindF(z2y ->
    z2v._{z}
```

join (OptionStatics)

```
public static <Z>
Function<Option<Option<Z>>, Option<Z>> join()
} {
  return
   ooz ->
    ooz.bindM(oz ->
    oz
   );
}
```

choice (Option)

```
default public Option<Z> choice(
 final Function<Z, Boolean> z2b,
 final Function<Z, Option<Z>> t_z2oz,
 final Function<Z, Option<Z>> f_z2oz
) {
 return
  bindM(z \rightarrow
   z2b._{z}
    ? t_z2oz._(z)
    : f_z2oz._(z)
  );
```

example01 (OptionApp)

```
// example01 = one(abc)

Option<String> example01 = one("a").bindM(a -> one("b").bindM(b -> one("c").bindM(c -> one(a + b + c) )
 )
);
```

example02 (OptionApp)

```
// example02 = one(abc)

Option<String> example02 = one("a").bindM(a -> one("b").bindM(b -> one("c").bindF(c -> a + b + c )
)
)
```

example03 (OptionApp)

```
// example03 = one(abc)

Option<String> example03 =
  one("a").bindA(
  one("b").bindA(
   one("c").bindF(c -> b -> a ->
        a + b + c
  )
  )
);
```

example06 (OptionApp)

```
// example06 = one(c)

Option<String> example06 = one("a").choice(a -> a.equals("b"), a -> one("b"), a -> one("c")
);
```

zero (OptionStatics)

```
// additive method
public static <Z>
Option<Z> zero(
) {
  return
  none();
}
```

example04 (OptionApp)

```
// example04 = zero

Option<String> example04 = one("a").bindM(a -> zero().bindM(z -> one("c").bindF(c -> a + z + c )
)
):
```

example05 (OptionApp)

```
// example05 = zero

Option<String> example05 =
  one("a").bindA(
   zero().bindA(
   one("c").bindF(c -> z -> a ->
    a + z + c
  )
  )
);
```

filter (Option)

```
default public Option<Z> filter(
  final Function<Z, Boolean> z2b
) {
  return
   choice(
    z2b,
    z -> one(z),
    z -> zero()
  );
}
```

example07 (OptionApp)

```
// example07 = zero
Option<String> example07 =
one("a").filter(a ->
   a.equals("b")
);
```

plus (Option)

```
// additive method

default public Option<Z> plus(
  final Cbn<Option<Z>> _2oz
) {
  return
  fold(
    OptionStatics::some,
    _2oz
  );
}
```

plus (OptionStatics)

```
// static version of plus
public static <Z>
Option<Z> plus(
  final Option<Z> oz1,
  final Cbn<Option<Z>> oz2
) {
  return
  oz1.plus(oz2);
}
```

someOptions (OptionApp)

```
private static final
Option<String> oneA_plus_oneB =
  one("a").plus(() -> one("b"));
private static final
Option<String> oneC_plus_oneD =
  one("c").plus(() -> one("d"));
```



someOptionsUsingZero (OptionApp)

```
private static final
Option<String> oneA_plus_zero =
  one("a").plus(() -> zero());
// note: sometimes we have to help the type inferencer
private static final
Option<String> zero_plus_oneA =
  OptionStatics.<String>zero().plus(() -> one("a"));
```

example08 (OptionApp)

```
// example08 = one(a)
Option<String> example08 =
  oneA_plus_oneB;
```

example09 (OptionApp)

```
// example09 = one(a)
Option<String> example09 =
  oneA_plus_zero;
```

example10 (OptionApp)

```
// example10 = one(a)
Option<String> example10 =
zero_plus_oneA;
```

example11 (OptionApp)

```
// example11 = one(ac)
Option<String> example11 =
  oneA_plus_oneB.bindM(apb ->
  oneC_plus_oneD.bindF(cpd ->
    apb + cpd
  )
);
```

example12 (OptionApp)

```
// example12 = one(a)
Option<String> example12 =
  oneA_plus_oneB.identity();
```

example13 (OptionApp)

```
// example13 = 1
int example13 =
  oneA_plus_oneB.length();
```

Stream

Stream



Stream

```
public interface Stream<Z> {
```



More

```
final public class More<Z>
  implements Stream<Z> {
  final Z current;
  final Cbn<Stream<Z>> next;
```



Done

```
final public class Done<Z>
  implements Stream<Z> {
```



fold (Stream)

```
// abstract method
// follows the recursive structure of Stream
public <Y>
Y fold(
  final BiFunction<Z, Cbn<Y>, Y> zny2y,
  final Cbn<Y> y
);
```

fold (More)

```
Onverride
public <Y>
Y fold(
 final BiFunction<Z, Cbn<Y>, Y> zny2y,
 final Cbn<Y> y
) {
 return
  zny2y._(
   current,
   () -> next._().fold(zny2y, y)
  );
```

fold (Done)

```
@Override
public <Y>
Y fold(
  final BiFunction<Z, Cbn<Y>, Y> zny2y,
  final Cbn<Y> y
) {
  return
   y._();
}
```

more (StreamStatics)

```
public static <Z>
Stream<Z> more(
  final Z current,
  final Cbn<Stream<Z>> next
) {
  return
   new More<>(current, next);
}
```

done (StreamStatics)

```
public static <Z>
Stream<Z> done(
) {
  return
  new Done<>();
}
```



identity (Stream)

```
default public Stream<Z> identity() {
  return
  fold(
    StreamStatics::more,
    StreamStatics::done
  );
}
```

length (Stream)

```
default public Integer length() {
  return
  fold(
    (z, 1) -> 1 + 1._(),
    () -> 0
  );
}
```

zero (StreamStatics)

```
public static <Z>
Stream<Z> zero(
) {
  return
  done();
}
```

plus (Stream)

```
default public Stream<Z> plus(
  final Cbn<Stream<Z>> sz
) {
  return
  fold(
    StreamStatics::more,
    sz
  );
}
```

bindM (Stream)

```
default public <Y>
Stream<Y> bindM(
  final Function<Z, Stream<Y>> z2sy
) {
  return
  fold(
    (z, sy) -> z2sy._(z).plus(sy),
    StreamStatics::zero
  );
}
```

one (StreamStatics)

```
public static <Z>
Stream<Z> one(
  final Z z
) {
  return
  more(z, StreamStatics::done);
}
```

example01 (StreamApp)

```
// example01 = one(abc) : zero
Stream<String> example01 =
  one("a").bindM(a ->
   one("b").bindM(b ->
   one("c").bindM(c ->
      one(a + b + c)
   )
  )
);
```

example02 (StreamApp)

```
// example02 = one(abc) : zero
Stream<String> example02 =
one("a").bindM(a ->
one("b").bindM(b ->
one("c").bindF(c ->
    a + b + c
)
));
```

example03 (StreamApp)

```
// example03 = one(abc) : zero
Stream<String> example03 =
  one("a").bindA(
  one("b").bindA(
   one("c").bindF(c -> b -> a ->
        a + b + c
  )
  )
);
```

example06 (StreamApp)

```
// example06 = one(c) : zero
Stream<String> example06 =
  one("a").choice(a ->
    a.equals("b"),
    a -> one("b"),
    a -> one("c")
);
```

example04 (StreamApp)

```
// example04 = zero
Stream<String> example04 =
one("a").bindM(a ->
  zero().bindM(z ->
  one("c").bindF(c ->
    a + z + c
  )
  )
):
```

example05 (StreamApp)

```
// example05 = zero

Stream<String> example05 =
  one("a").bindA(
   zero().bindA(
   one("c").bindF(c -> z -> a ->
        a + z + c
  )
  )
);
```

example07 (StreamApp)

```
// example07 = zero
Stream<String> example07 =
one("a").filter(a ->
   a.equals("b")
);
```

example08 (StreamApp)

```
// example08 = one(a) : one(b) : zero
Stream<String> example08 =
  oneA_plus_oneB;
```

example09 (StreamApp)

```
// example09 = one(a) : zero
Stream<String> example09 =
  oneA_plus_zero;
```

example10 (StreamApp)

```
// example10 = one(a) : zero
Stream<String> example10 =
  zero_plus_oneA;
```

example11 (StreamApp)

```
// example11 = one(ac) : one(ad) : one(bc) : one(bd) : zero
Stream<String> example11 =
  oneA_plus_oneB.bindM(apb ->
   oneC_plus_oneD.bindF(cpd ->
      apb + cpd
  )
  );
```

example12 (StreamApp)

```
// example12 = example12 = one(a) : one(b) : zero
Stream<String> example12 =
  oneA_plus_oneB.identity();
```

example13 (StreamApp)

```
// example13 = 2
int example13 =
  oneA_plus_oneB.length();
```

take (Stream)

```
// note: a stream can be infinite
public Stream<Z> take(
  int n
);
```

take (More)

```
@Override
public Stream<Z> take(
 int n
) {
 return
  (n > 0)
  ? more(
   current,
   () -> next._().take(n - 1)
   : done();
```

take (Done)

```
@Override
public Stream<Z> take(
  int n
) {
  return
  done();
}
```

infinitelyMany (StreamApp)

```
private static <Z>
Stream<Z> infinitelyMany(
   Z z
) {
   return
   one(z).plus(
      () -> infinitelyMany(z)
   );
}
```

example14 (StreamApp)

```
// example14 = one(a) : one(a) : one(a) : zero
Stream<String> example14 =
  infinitelyMany("a").take(4);
```

fibonacciNumbersFrom (StreamApp)

```
private static Stream<Integer> fibonacciNumbersFrom(
   Integer fib0,
   Integer fib1
) {
   return
   one(fib0).plus(
     () -> fibonacciNumbersFrom(fib1, fib0 + fib1)
     );
}
```

example15 (StreamApp)

```
// example15 = one(1) : one(2) : one(3) : one(5) : zero
Stream<Integer> example15 =
  fibonacciNumbersFrom(1, 2).take(4);
```

lift (StreamStatics)

```
// cbn version of one
public static <Z>
Cbn<Stream<Z>> lift(
  final Cbn<Z> z
) {
  return
  () -> one(z._());
}
```

liftF (StreamStatics)

```
// static version of bindF
public static <Z, Y>
Function<Stream<Z>, Stream<Y>> liftF(
  final Function<Z, Y> z2y
) {
  return
  sz ->
   sz.bindF(z2y);
}
```

liftA (StreamStatics)

```
// static version of bindA
public static <Z, Y>
Function<Stream<Z>, Stream<Y>> liftA(
  final Stream<Function<Z, Y>> s_z2y
) {
  return
  sz -> sz.bindA(s_z2y);
}
```

liftBF (StreamStatics)

```
public static <Z, Y, X>
BiFunction<Stream<Z>, Cbn<Stream<Y>>, Stream<X>> liftBF(
 final BiFunction<Z, Cbn<Y>, X> zny2x
) {
 return
  (sz, sy) ->
   sz.bindA(
    sy._().bindF(y \rightarrow z \rightarrow
     zny2x._(z, () \rightarrow y)
```

foreachDeclaration (Stream)

```
default public <Y, X, MY, MX>
Function<Function<Z, MY>, MX> foreach(
  final Cbn<X> x,
  final BiFunction<Y, Cbn<X>, X> ynx2x,
  final Function<Cbn<X>, Cbn<MX>> lift,
  final Function<
   BiFunction<Y, Cbn<X>, X>,
  BiFunction<MY, Cbn<MX>, MX>
  > liftBF
```

foreachDefinition (Stream)

```
{
  return
  z2my ->
  fold(
    (z, mx) -> liftBF._(ynx2x)._(z2my._(z), mx),
    lift._(x)
  );
}
```

sequenceOpDeclaration (OptionStatics)

```
public static <Z>
Function<Stream<Option<Z>>, Option<Stream<Z>>> sequenceOp(
  final Cbn<Stream<Z>> sz,
  final BiFunction<
    Stream<Z>, Cbn<Stream<Z>>,
    Stream<Z> > sznsz2sz
)
```

sequenceOpDefinition (OptionStatics)

```
return
 soz ->
  soz.foreach(
   SZ,
   sznsz2sz,
   OptionStatics::lift,
   OptionStatics::liftBF
  )._(
   liftF(StreamStatics::one)
  );
```

sequenceAccDeclaration (OptionStatics)

```
public static <Z>
Function<Stream<Option<Z>>, Option<Stream<Z>>> sequenceAcc(
  final Cbn<Stream<Z>> sz,
  final BiFunction<Z, Cbn<Stream<Z>>, Stream<Z>> znsz2sz
)
```

sequenceAccDefinition (OptionStatics)

```
return
 soz ->
  soz.foreach(
   SZ,
   znsz2sz,
   OptionStatics::lift,
   OptionStatics::liftBF
  )._(
   liftF(FunctionStatics::identity)
  );
```

someStreamsOfOptions (OptionApp)

```
private static final
Stream<Option<String>> oneOA_plus_oneOB =
 StreamStatics.one(one("a")).plus(() ->
  StreamStatics.one(one("b"))
private static final
Stream<Option<String>> oneZ_plus_oneOB =
 StreamStatics.<Option<String>>one(zero()).plus(() ->
  StreamStatics.one(one("b"))
 ):
private static final
Stream<Option<String>> oneOA_plus_oneZ =
 StreamStatics.one(one("a")).plus(() ->
  StreamStatics.one(zero())
 );
```

example14 (OptionApp)

```
// example14 = one(one(a) : one(b) : zero)

Option<Stream<String>> example14 =
    OptionStatics.<String>sequenceOp(
    StreamStatics::zero,
    StreamStatics::plus
)._(
    oneOA_plus_oneOB
);
```

example15 (OptionApp)

```
// example15 = zero

Option<Stream<String>> example15 =
    OptionStatics.<String>sequenceAcc(
    StreamStatics::done,
    StreamStatics::more
)._(
    oneZ_plus_oneOB
);
```

example16 (OptionApp)

```
// example16 = zero

Option<Stream<String>> example16 =
    OptionStatics.<String>sequenceAcc(
    StreamStatics::done,
    StreamStatics::more
)._(
    oneOA_plus_oneZ
);
```

example17 (OptionApp)

```
// example17 = one(one(A)) : zero
Stream<Option<String>> example17 =
 oneA_plus_oneB.<
  Option<String>, Option<String>,
  Stream<Option<String>>, Stream<Option<String>>
  >foreach(
  OptionStatics::zero, FunctionStatics::identity,
  StreamStatics::lift, StreamStatics::liftF
 )._(s ->
  StreamStatics.one(
   one(s.toUpperCase())
```

foreachDeclaration (Option)

```
default public <Y, X, MY, MX>
Function<Function<Z, MY>, MX> foreach(
  final Cbn<X> x,
  final Function<Y, X> y2x,
  final Function<Cbn<X>, Cbn<MX>> lift,
  final Function<Function<Y, X>, Function<MY, MX>> liftF)
```

foreachDefinition (Option)

```
{
  return
  z2my ->
  fold(
    z -> liftF._(y2x)._(z2my._(z)),
    lift._(x)
  );
}
```

sequenceFunDeclaration (StreamStatics)

```
public static <Z>
Function<Option<Stream<Z>>, Stream<Option<Z>>> sequenceFun(
  final Cbn<Option<Z>> oz,
  final Function<Option<Z>, Option<Z>> oz2oz
)
```

sequenceFunDefinition (StreamStatics)

```
return
 osz ->
  osz.foreach(
   oz,
   oz2oz,
   StreamStatics::lift,
   StreamStatics::liftF
  )._(
   liftF(OptionStatics::one)
  );
```



example16 (StreamApp)

```
// example16 = one(one(a)) : zero
Stream<Option<String>> example16 =
StreamStatics.<String>sequenceFun(
   OptionStatics::zero,
   FunctionStatics::identity
)._(
   oneSA_plus_oneSB
);
```

example17 (StreamApp)

```
// example17 = zero
Stream<Option<String>> example17 =
StreamStatics.<String>sequenceFun(
   OptionStatics::zero,
   FunctionStatics::identity
)._(
   oneZ_plus_oneSB
);
```



example18 (StreamApp)

```
// example18 = one(one(a)) : zero
Stream<Option<String>> example18 =
StreamStatics.<String>sequenceFun(
   OptionStatics::zero,
   FunctionStatics::identity
)._(
   oneSA_plus_oneZ
);
```



example19 (StreamApp)

```
// example19 = one(one(A) : one(B) : zero)
Option<Stream<String>> example19 =
 oneA_plus_oneB.<
  Stream<String>, Stream<String>,
  Option<Stream<String>>, Option<Stream<String>>
  >foreach(
  StreamStatics::zero, StreamStatics::plus,
  OptionStatics::lift, OptionStatics::liftBF
 )._(s ->
  OptionStatics.one(
   one(s.toUpperCase())
```

Tuple

Tuple



Tuple

```
// Tuple<Z, Y> zny = ...;
// Z z = zny._1;
// Y y = zny._2

public final class Tuple<Z, Y> {
  public final
  Z _1;
  public final
  Y _2;
```

TupleStatics

```
public final class TupleStatics {
  public static <Z, Y>
  Tuple<Z, Y> tuple(
    final Z z,
    final Y y
) {
    return
    new Tuple<>(z, y);
}
```

Unit

Unit



Unit

```
public final class Unit {
  @Override
  public String toString() {
   return "unit";
  }
}
```



UnitStatics

```
public final class UnitStatics {
  public final static
  Unit unit =
    new Unit();
}
```



State

State



State

```
// note: functional interface
public interface State<S, Z> {
  public Function<S, Tuple<Z, S>> open();
```



bindM (State)

```
// note: function literal
default public <Y>
State<S, Y> bindM(
 final Function<Z, State<S, Y>> z2sy
) {
 return
  () ->
   s -> {
    Tuple\langle Z, S \rangle zns = open()._(s);
    return
     z2sy._(zns._1).open()._(zns._2);
   };
```

one (StateStatics)

```
public static <S, Z>
State<S, Z> one(
  final Z z
) {
  return
  () ->
   s ->
    tuple(z, s);
}
```



get (StateStatics)

```
public static <S>
State<S, S> get(
) {
  return
  () ->
    s ->
    tuple(s, s);
}
```



set (StateStatics)

```
static <S>
State<S, Unit> set(
  final S newS
) {
  return
  () ->
   oldS ->
   tuple(unit, newS);
}
```

exec (StateStatics)

```
public static <S>
State<S, Unit> exec(
  final Function<S, S> s2s
) {
  return
   StateStatics.<S>get().bindM(s -> set(s2s._(s))
  );
}
```



Status (StateApp)

```
public enum Status {
  FREE, BUSY
}
```

Action (StateApp)

```
public enum Action {
  COIN, CANDY
}
```



Machine (StateApp)

```
public class Machine {
  Status status;
  int candies;
  int coins;
```



actions (StateApp)

```
private static final Stream<Action> coin =
 one(COIN);
private static final Stream<Action> candy =
 one(CANDY);
private static final Stream<Action> actions =
 coin.plus(
  () -> candy
 ).plus(
  () -> coin
 ).plus(
 () -> candy
 );
```



stateMachinePartOne (StateApp)

```
private static State<Machine, Unit> stateMachine(
  final Stream<Action> actions
) {
  return
  actions.<
    Unit, Unit,
    State<Machine, Unit>, State<Machine, Unit>
    >foreach(
    () -> unit, (u, v) -> unit,
    StateStatics::lift, StateStatics::liftBF
)
```

stateMachinePartTwo (StateApp)

```
. (a ->
exec(
 m ->
  m.candies == 0 | I |
   a == COIN && m.status == BUSY ||
   a == CANDY && m.status == FREE
   ? m
    : a == COIN && m.status == FREE
   ? new Machine(BUSY, m.candies, m.coins + 1)
    : a == CANDY && m.status == BUSY
   ? new Machine(FREE, m.candies - 1, m.coins)
    : null // this should never happen
```

main (StateApp)

```
public static void main(String[] args) {
   System.out.println(stateMachine(actions).open()._(
   new Machine(FREE, 10, 0)
   )._2
   );
}
```