The error in Bayesian phylogenetic reconstruction

when speciation is not instantaneous

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7 Abstract

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The tools for reconstructing phylogenetic relationships between taxonomic units (e.g. species) have become very advanced in the last three decades. Among the most popular tools are Bayesian approaches, such as BEAST, MrBayes and RevBayes, that use efficient tree sampling routines to create a posterior probability distribution of the phylogenetic tree. A feature of these approaches is the possibility to incorporate known or hypothesized structure of the phylogenetic tree through the tree prior. It has been shown that the effect of the prior on the posterior distribution of trees can be substantial.

Currently implemented tree priors assume that speciation is instantaneous, where we know that speciation can be a gradual process.

Here we explore the effects of ignoring the protractedness of the speciation process with an extensive simulation study.

We compare the inferred tree to the simulated tree, and find that \dots

Keywords: computational biology, evolution, phylogenetics, Bayesian analysis, tree prior

4 1 Introduction

The computational tools that are currently available to the phylogeneticists go beyond the wildest imagination of those living four decades ago. Advances in computational power allowed the first cladograms to be inferred from DNA alignments in 1981 (Felsenstein 1981), and the first Bayesian tools emerged in 1996 (Rannala & Yang 1996), providing unprecedented flexibility in the setup of a phylogenetic model.

31 Currently, the most popular Bayesian phylogenetics tools are

BEAST (Drummond & Rambaut 2007) and its offshoot BEAST2 (Bouckaert et al. 2014), MrBayes (Huelsenbeck & Ronquist 2001) and RevBayes (Höhna et al. 2016). They allow to incorporate known or hypothesized structure of a phylogenetic tree-to-be-inferred through model priors. With these priors and an alignment of DNA, RNA or protein sequences, they create a sample of the posterior distribution of phylogenies and parameter estimates (of the models used as a prior), in which more probable combinations are represented more often. Each of these tools use efficient tree sampling routines to rapidly create an informative posterior.

The model priors in Bayesian phylogenetic reconstruction can be grouped into three categories: (1) site model, specifying nucleotide substitutions, (2) clock model, specifying the rate of mutation per lineage in time, and (3) tree model, constituting the speciation model underlying branching events (speciation) and branch termination (extinction). The choice of site model (Posada & Buckley 2004), clock model (Baele et al. 2012) or tree prior (Möller et al. 2018; Yang & Rannala 2005) is known to affect the posterior.

Current phylogenetic tools use tree priors that assume speciation is instantaneous, whilst we know that, speciation is often a gradual process (Schluter
2009). The (constant-rate) birth-death (BD) model is a commonly used tree
prior, but it ignores this temporal aspect of speciation. The protracted birthdeath (PBD) model, an extension of the BD model, does incorporate the idea
that speciation takes time. In this model, a branching event does not give rise
to a new species, but to a new species-to-be, called an incipient species. Such an
incipient species may go extinct, finish its speciation to become a good species,
or give rise to new incipient species. Protracted speciation may explain observed
declines in lineage accumulation (Etienne & Rosindell 2012).

Unfortunately, a tree prior according to this model, providing the probability
of a species tree under the PBD model, is unavailable in current Bayesian phy-

Unfortunately, a tree prior according to this model, providing the probability of a species tree under the PBD model, is unavailable in current Bayesian phylogenetic tools. Whilst an approximate formula for this probability has been derived (Lambert et al. 2015) and the approximation is very good (Simonet 61 et al. 2018), it has not been implemented as tree prior yet. There are various reasons for this. First, the computation of this probability involves solving a set of non-linear differential equations, and while this computation is quite fast, it still takes much more time than the corresponding probability of the BD model which is a simple analytical formula. In a Bayesian MCMC chain, the tree prior probability must be calculated many times, and hence the total computation will take considerably longer with a PBD tree prior. Furthermore, the approximate probability is a probability for the species tree assuming an underlying incipient species tree. It can be safely used as tree prior when only one individual per species is sampled, but if one has multiple samples per species which is currently often the case - the methods to account for this such as the multi-species coalescent (Heled & Drummond 2009) may not be compatible with the underlying incipient species tree. More precisely, the phylogeny under the PBD model may contain paraphylies, while the multi-species coalescent was developed exactly to avoid these by explaining them as arising from incomplete lineage sorting. Because of these paraphylies there is no such thing as a true species tree in the PBD model. To get a species-level tree one must sample one incipient species per species. Which incipient species is sampled may therefore have an impact on the species tree.

Here we aim to explore the effect of using the BD prior on PBD simulated phylogenies, taking into account possible sampling effects. In brief, we simulate protracted phylogenies using the PBD process, from which we sample a species tree in two very different ways. Given this species tree, we simulate a DNA sequence alignment. Then, we use BEAST2 on these alignments to infer a posterior of phylogenies, using a BD prior. We quantify the difference between the (BD) posterior phylogenies and the simulated (PBD) species tree. Furthermore, while we evidently know the clock and site models used in the simulation, using a different clock and/or site model prior in inference may compensate or increase this difference between inferred and simulated tree. To study this, we also explore the effect of a different clock and site model prior in inference.

The PBD model has five biological parameters, depicted in table 2, which we explore in a factorial fashion, excluding - for computational reasons - the combinations in which the 95% quantile of the expected number of good species is more than 1250. This quantile is calculated with the pbd_numspec_quantile function we added to the PBD package (Etienne 2015). [RSE: I think we should release the new version with this function with this manuscript][RJCB: I would personally prefer 'release early, release often', but as lead maintainer you get to decide][RSE: Do you want to put the derivation here?][RJCB: Yes please, either here or at the PBD package (the functions pbd_geom and pbd_numspec_quantile) documentation.

Wherever you put it, I will transfer it to the other place. This calculation assumes $b = b_g = b_i$, we used $b = \max(b_g, b_i)$. We use 1000 good 103 species as a threshold, to prevent overly taxon-poor and taxon-rich phylogenies 104 respectively. The parameter values chosen are based on the parameter sets used 105 by Etienne et al. 2014, as these parameters were shown to result in reasonably 106 sized phylogenies and using the same set allows us to compare results. We use 107 a set of speciation initiation rates, $B = \{0.3, 0.5\}$, of which the speciation ini-108 tiation rate of good species $b_g \in B$ and incipient species $b_i \in B$. [RSE: your 109 units are not entirely correct, as these are probability rates.][RJCB: I 110 though I was correct in my units. If I am wrong, what are the correct 111 units then? In Etienne and Rosindell 2012, there is never 'probabil-112 ity rate' written. To be explicit, I think these sentences are all valid: 113 (1) the extinction rate of good species, mu_g is 1.2 extinction events per time unit (2) the speciation initiation rate of good species, b_g 115 is 2.3 speciation events per time unit, (3) the speciation completion 116 rate, lambda is 3.4 speciation completion events per time unit. What 117 would be the better unit? [RSE: Je hebt het over de eenheden van 118 de rates. Dat is subtiel omdat het om een stochastisch model gaat 119 en dus om kansen. Voorbeeld: mu * dt is de kans op een extinction 120 event per species in een tijdsinterval dt. 1/mu geeft de verwachte 121 tijd tot een extinctie event van een soort. mu is dus een probability 122 rate. The speciation completion rates we use are $\lambda = 0.1, 0.3, 1.0$ and 10^9 . 123 We use $10^9 \approx \infty$ to mimic the BD model, because the PBD model reduces to 124 the BD model for $\lambda = \infty$. This allows us to measure the baseline error, which is the difference between inferred tree and true species tree that arises purely 126 due to noise because the generating model and the model used in inference are 127 identical in this case. We use a set of extinction rates, $M = \{0.0, 0.1, 0.2, \infty\}$, of 128

which the extinction rate of good species $\mu_g \in M$ and incipient species $\mu_i \in M$.

From each biological parameter set, we simulate a protracted birth-death tree, using the PBD package (Etienne 2015) in the R programming language (R Core Team 2013), all with a crown age of 15 million years as used in Etienne et al. 2014. Each protracted birth-death tree uses a different random number generator seed, which makes all runs independent, resulting in a balanced data set.

From each incipient species tree, we construct a species tree, by sampling one 136 incipient/good species per good species. For example, when an incipient species branched off from its mother lineage, both of these subspecies are recognized 138 as representing the species, and hence both can be picked as an (equally good) representative of the species. Here, we use three sampling scenarios, in which 140 we pick the representative randomly or in such a way that this results in either the shortest or longest branch lengths. See the supplementary information for 142 a visualization of these sampling methods. RSE: Why not include that in 143 the paper here; I think it is essential RJCB: Because we are limited 144 to two figures 145

Based on the sampled species tree, we simulate a DNA alignment that has 146 the same history as this species tree, using the phangorn package (Schliep 2011). 147 We set the nucleotides of the DNA alignment to follow a Jukes-Cantor (Jukes et al. 1969) nucleotide substitution model, in which all nucleotide-to-nucleotide 149 transitions are equally likely. In our Bayesian inference (see below) we use the same site model as the (obviously correct) site model prior, but we also explore 151 the effect of assuming a more complex site model prior. We predict with the more complex substitution model, that there will be more noise and hence our 153 inference error will increase. On the other hand, we dare not rule out that 154 the inference error will decrease, due to more flexibility in the more complex 155

prior. We set the mutation rate in such a way to maximize the information contained in the alignment. To do so, we set the mutation rate such that we 157 expect on average one (possibly silent) mutation per nucleotide between crown 158 age and present, which equates to $\frac{1}{15}$ mutations per million years. The DNA 159 sequence length is chosen to provide a resolution of 10³ years, that is, to have 160 one expected nucleotide change per 10³ years per lineage on average. As one 161 nucleotide is expected to have on average one (possibly silent) mutation per 15 162 million years, $15 \cdot 10^3$ nucleotides result in 1 mutation per alignment per 10^3 163 years (which is coincidentally the same as Möller et al. 2018). The simulation of these DNA alignments follows a strict clock model, which we will specify as 165 one of the two clock models assumed in the Bayesian inference (see below).

From an alignment, we run a Bayesian analysis and create a posterior dis-167 tribution of trees and parameters using the babette (Bilderbeek & Etienne 2018) package that sets the input parameters similar to BEAUti 2 and then 169 runs BEAST2. For our site model, we assume either a Jukes-Cantor or GTR 170 nucleotide substitution model. The Jukes-Cantor model is the correct one, as it 17 is used for simulating that alignment, where the GTR model is the site model 172 that is picked as a default by most users. For our clock model, we assume either 173 a strict or relaxed log-normal clock model. Also here, the strict clock model 174 is the correct one, as it is used for simulating the alignment, but the relaxed 175 log-normal clock model is the one most commonly used. We set the BD model 176 as a tree prior, as gauging the effect of this incorrect assumption is the goal of 177 this study. We assume an MRCA prior with a tight normal distribution around 178 the crown age, by choosing the crown age as mean, and a standard deviation of $0.5 \cdot 10^{-3}$ time units, resulting in 95% of the crown ages inferred have the same 180 resolution (of 10^{-3} time units) as the alignment. We ran the MCMC chain to 181 generate 1111 states, of which we remove the first 10% (also called the 'burn-182

in'). Of the remaining 1000 MCMC states, the effective sample size (ESS) of the posterior must at least be 200 for a strong enough inference (Drummond & Bouckaert 2015). An ESS can be increased by increasing the number of samples or decreasing the autocorrelation between samples. If the ESS is less than 200, we decrease autocorrelation by doubling the MCMC sampling interval of that simulation, until the ESS exceeds 200.

We compare each posterior phylogeny to the (sampled) species tree using the

nLTT statistic (Janzen et al. 2015), from the nLTT package (Janzen 2015). The

nLTT statistic equals the area between the normalized lineages-through-time
plots of two phylogenies, which has a range from zero (for identical phylogenies)

to one. We use inference error and nLTT statistic interchangeably. Compar
ing the simulated species tree with each of the posterior species trees yields a

distribution of nLTT statistics.

We produce two data sets as a comma-separated file. The general data set 196 has 348 different combinations of biological parameter combinations, site and 197 clock models. The data set to investigate sampling has 552 different combi-198 nations of biological parameter combinations, site models, clock models and 199 sampling methods. The experiment is computationally intensive: pilot exper-200 iments show that the experiment takes roughly 100 days of CPU time and 20 201 days of wall clock time (which includes the queued waiting for computational re-202 sources) per replicate. Due to this, we choose to perform ten replicates, so that 203 the complete experiment will take an acceptable time of roughly seven months. For both data sets, we display the nLTT statistics distribution per biolog-205 ical parameter combination as a violin plot. We show combinations for which $b_g = b_i$ and $\mu_g = \mu_i$, to simplify the interpretation of the results, where the 207 other combinations are shown in the supplementary material. Additionally, we only show the nLTT distributions that were generated under the (correct) as-209

Term	Definition
Phylogenetics	The inference of evolutionary relationships of groups
	of organisms using genetics
Model prior	Knowledge or assumptions about the ontogeny of
	evolutionary histories
Posterior	A collection of phylogenies and parameter estimates,
	in which more probable combinations (determined
	by the data and the model prior) are presented more
	frequently
Protracted speciation	The process in which speciation takes two events:
	a speciation-initiation event and a speciation-
	completion event
Speciation initiation	The start of a speciation event creating an incipient
	species
Speciation completion	The end of a speciation event, in which an incipient
	species becomes or is recognized as a good species

Table 1: Glossary

- $_{\scriptsize 210}$ $\,$ sumptions of a Jukes-Cantor site model and a strict clock model, separated per
- $_{\rm 211}$ $\,$ sampling method used. We display the nLTT statistic distributions separated
- 212 per site or clock model in the supplementary information.

213 2 Results

3 Glossary

215 References

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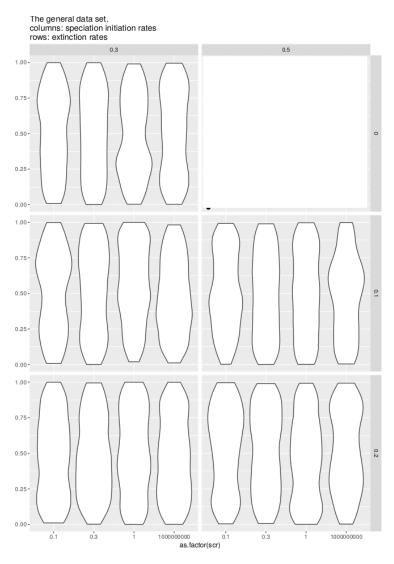


Figure 1: nLTT statistic distribution per biological parameter set, using the general data set, for the subset of combinations in which $b_g = b_i$, $\mu_g = \mu_i$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

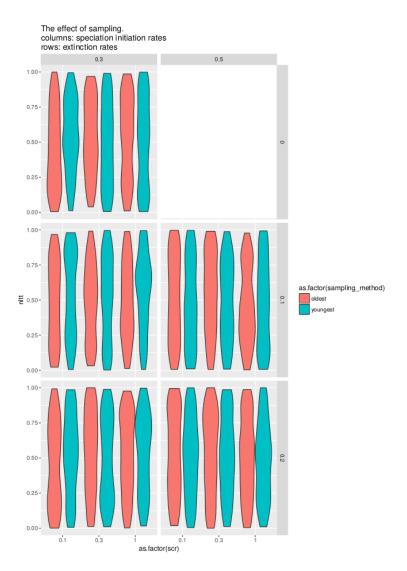


Figure 2: nLTT statistic distribution per biological parameter set per sampling regime, using the data set conditioned on sampling regime having an effect, for the subset of combinations in which $b_g = b_i$, $\mu_g = \mu_i$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

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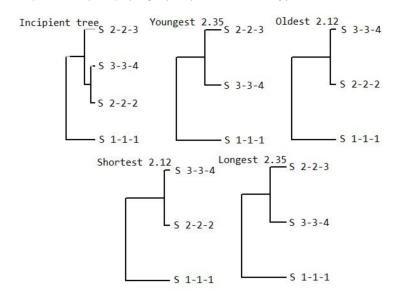


Figure 3: Sampling a species tree from an incipient species tree. At the top left, an incipient species tree is shown, of three different good species (the first and second number in the taxon label) and four different subspecies (the third number in the taxon tabel). The other four trees are species trees, that use a different sampling method to determine which sub-species is picked to represent a good species. These are: 'Youngest', 'Oldest', 'Shortest' and 'Longest'. With 'Youngest' the youngest sub-species is picked to represent the good species. With 'Oldest' the oldest sub-species is picked to represent the good species. 'Shortest' is the sampling method in which the sub-species are picked to assure the shortest branch lengths. 'Longest' is the sampling method in which the sub-species are picked to assure the longest branch lengths.

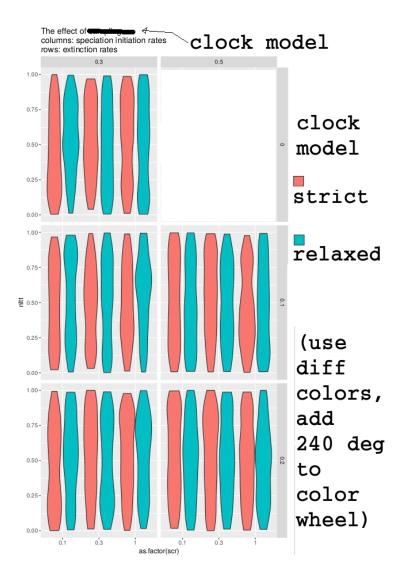


Figure 4: nLTT statistic distribution per biological parameter set per clock model, using the general data set, for the subset of combinations in which $b_g = b_i$, $\mu_g = \mu_i$, under the (correct) assumption of a Jukes-Cantor site model.

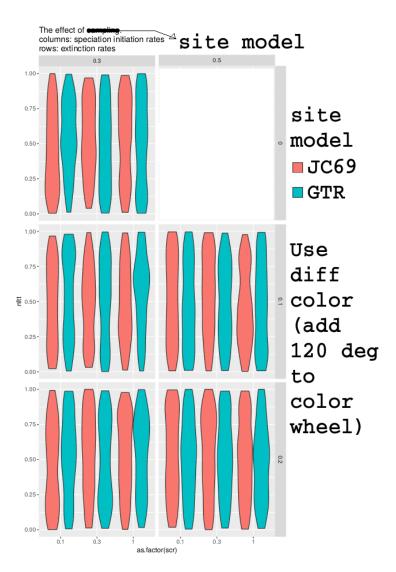


Figure 5: nLTT statistic distribution per biological parameter set per site model, using the general data set, for the subset of combinations in which $b_g = b_i$, $\mu_g = \mu_i$, under the (correct) assumption of a strict clock model.

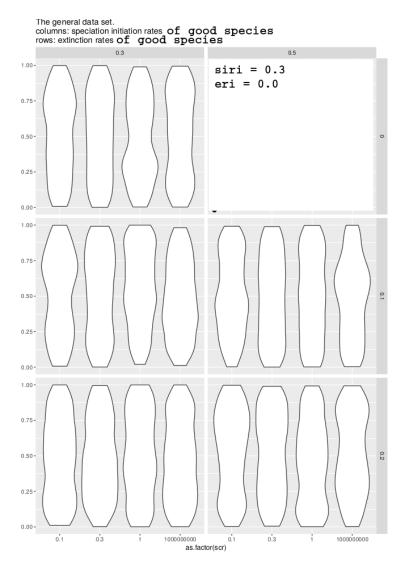


Figure 6: nLTT statistic distribution per biological parameter set, using the general data set, for $b_i = 0.3$ and $\mu_i = 0.0$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

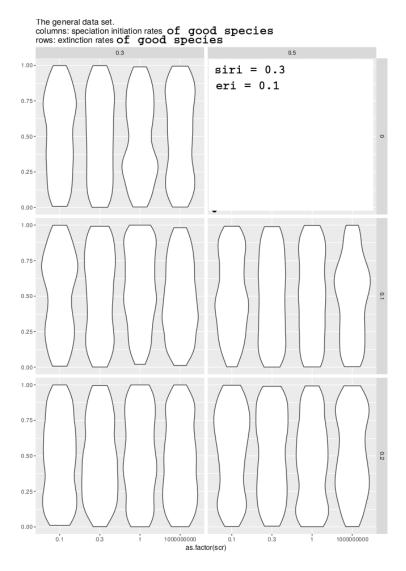


Figure 7: nLTT statistic distribution per biological parameter set, using the general data set, for $b_i = 0.3$ and $\mu_i = 0.1$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

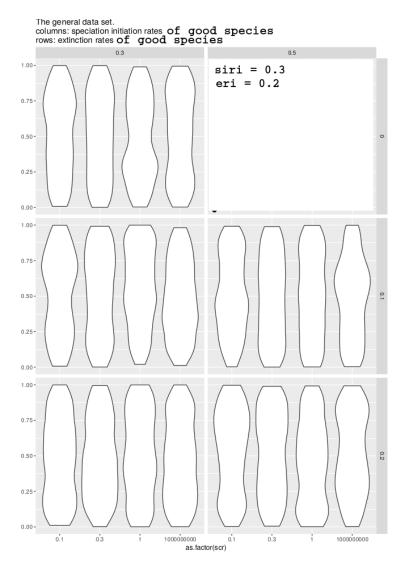


Figure 8: nLTT statistic distribution per biological parameter set, using the general data set, for $b_i = 0.3$ and $\mu_i = 0.2$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

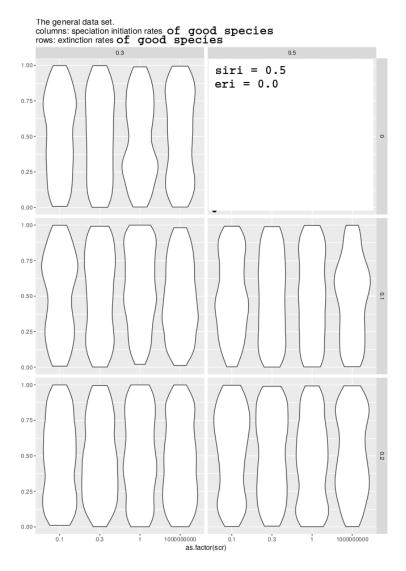


Figure 9: nLTT statistic distribution per biological parameter set, using the general data set, for $b_i = 0.5$ and $\mu_i = 0.0$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

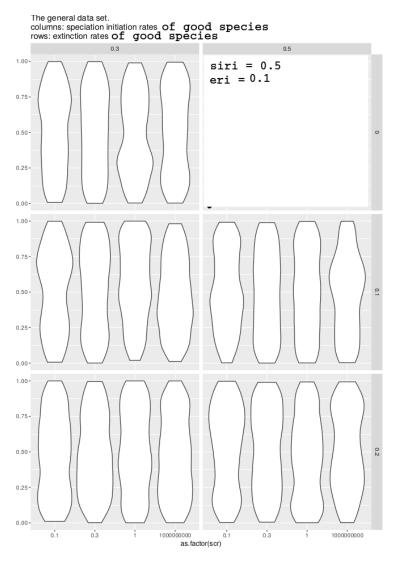


Figure 10: nLTT statistic distribution per biological parameter set, using the general data set, for $b_i = 0.5$ and $\mu_i = 0.1$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

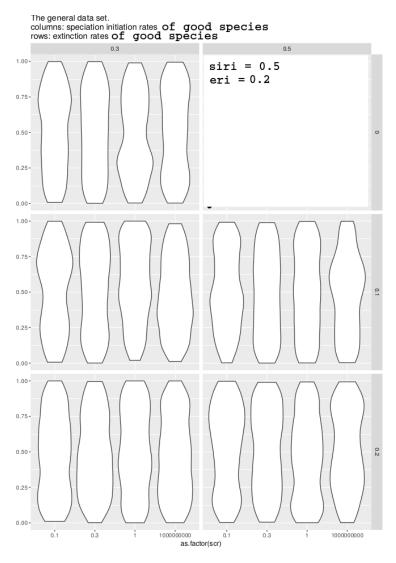


Figure 11: nLTT statistic distribution per biological parameter set, using the general data set, for $b_i = 0.5$ and $\mu_i = 0.2$, under the (correct) assumptions of a strict clock and Jukes-Cantor site model.

	Description	Values
$\overline{b_g}$	Speciation initiation rate of a good species	0.3, 0.5
b_i^-	Speciation initiation rate of an incipient species	0.3, 0.5
λ	Speciation completion rate	$0.1, 0.3, 1.0, \infty$
μ_g	Extinction rate of a good species	0.0, 0.1, 0.2
μ_i	Extinction rate of an incipient species	0.0, 0.1, 0.2
$\overline{t_c}$	Crown age	15
σ_c	Standard deviation around crown age	0.001
M_s	Sampling method	S, L, R
M_c	Clock model	S, RLN
M_t	Site model	JC69, GTR
r	Mutation rate	$\frac{1}{15}$
l_a	DNA alignment length	15K
f_i	MCMC sampling interval	1K or more
R_i	RNG seed incipient tree and randomly sampled	1, 2,
	species tree	
R_a	RNG seed alignment simulation	R_i
R_b	RNG seed BEAST2	R_i

Table 2: Overview of the simulation parameters. Above the horizontal line is the biological parameter set. The RNG seed R_i is 1 for the first simulation of the general data set, 2 for the next, and so on, up to and including 3480. The RNG seeds for the data set investigating the effect of sampling continue from there, but only those RNG seeds are used in which sampling has an effect. The sampling methods are abbreviated as such: 'R' denotes random sampling, 'S' is 'shortest' and 'L' is 'longest'. Sampling method M_s is random for the general data set. For the data set exploring the effect of sampling, we use 'shortest' and 'longest' for each value of R_i (which are random seeds in which sampling has an effect). The clock models are abbreviated as 'S' for a strict and 'RLN' for a relaxed log-normal model. The site models are abbreviated as 'JC69' for Jukes-Cantor (Jukes et al. 1969) and 'GTR' for the generalized time-reversible model (Tavaré 1986).

\overline{n}	Description
12	simulation parameters, see table 2
1000	nLTT statistic values
11	ESSes of all parameters estimated by BEAST2 (see specs below)

Table 3: Specification of the data sets. Each row will contain one experiment, where the columns contain parameters, measurements and diagnostics. This table displays the content of the columns. n denotes the number of columns a certain item will occupy, resulting in a table of 1023 columns and 20K rows.

#	Description
1	posterior
2	likelihood
3	prior
4	treeLikelihood
5	TreeHeight
6	BirthDeath
7	BDBirthRate
8	BDDeathRate
9	logP.mrca
10	mrcatime
11	clockRate

Table 4: Overview of the 11 parameters estimated by BEAST2 $\,$