

 This quiz has been regraded; your score was not affected.

## Homework 0 Part A

**Due** Sep 2 at 9am

**Points** 15

**Questions** 16

**Available** after Aug 29 at 12am

**Time Limit** None

## Instructions

This quiz on pre-requisite background is the first part of Homework 0. You must achieve a passing grade in order to continue in the course.

## Attempt History

	Attempt	Time	Score	Regraded
<b>LATEST</b>	<a href="#">Attempt 1</a>	5087 minutes	15 out of 15 *	15 out of 15 *

\* Some questions not yet graded

 Correct answers are hidden.

Score for this quiz: **15** out of 15 \*

Submitted Sep 2 at 2:21am

This attempt took 5087 minutes.

Probability and Statistics: Distributions

### Question 1

1 / 1 pts

Which of the following statements is true for the probability density function (pdf),  $f_X$ , of a continuous random variable,  $X$ , of one real-value? (Select all that applies)

☐ The range of  $f_X$  is  $[0, 1)$

☐ The range of  $f_X$  is  $(-\infty, \infty)$

☒  $\int_{-\infty}^{\infty} f_X(x) dx = 1$

☐ The domain of  $f_X$  is  $[0, 1]$

**Question 2****1 / 1 pts**

Which of the following statements is true for the cumulative distribution function (cdf),  $F_X$ , of a continuous random variable,  $X$ , of one real-value? (Select all that apply)

☒ The range of  $F_X$  is  $[0, 1)$

☐ The range of  $F_X$  is  $(-\infty, \infty)$

☐  $\int_{-\infty}^{\infty} F_X(x) dx = 1$

☒  $\int_{-\infty}^a f_X(x) dx = F_X(a)$ , where  $f_X$  is the pdf of  $X$

☐ The domain of  $F_X$  is  $[0, 1]$

**Question 3****1 / 1 pts**

For a continuous random variable  $X$ , the statement  $f_X(2) = 0.9$ , where  $f_X$  is the pdf of  $X$ , means... (Select all that apply)

☐ the probability of  $X = 2$  is 0.9

☐ the probability of  $X \leq 2$  is 0.9

☐ the probability of  $X = 2$  is very large, therefore we are very likely to observe  $X$  with a value of 2

☒ none of the above

## Question 4

1 / 1 pts

For a continuous random variable  $X$ , the statement  $F_X(2) = 0.9$ , where  $F_X$  is the cdf of  $X$ , means... (Select all that apply)

☐ the probability of  $X = 2$  is 0.9

☒ the probability of  $X \leq 2$  is 0.9

☐ the probability of  $X = 2$  is very small, therefore we are unlikely to observe  $X$  with a value of 2

☐ the probability of  $X = 2$  is very large, therefore we are very likely to observe  $X$  with a value of 2

☐ none of the above

## Question 5

1 / 1 pts

For a discrete random variable  $X$ , the statement  $p_X(2) = 0.9$ , where  $p_X$  is the probability mass function of  $X$ , means... (Select all that apply)

☒ the probability of  $X = 2$  is 0.9

☐ the probability of  $X \leq 2$  is 0.9

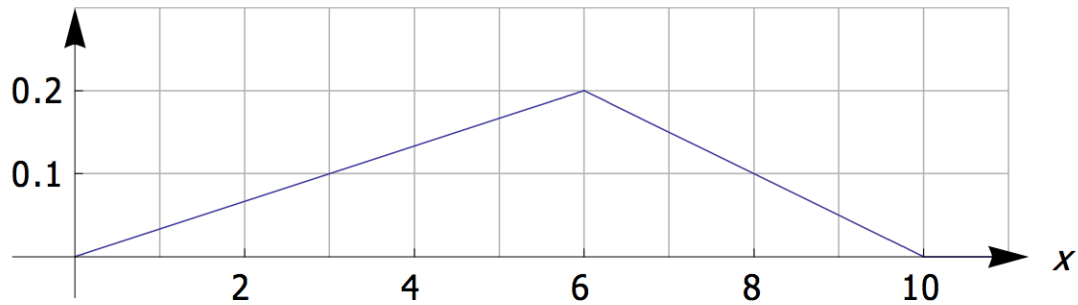
☐ the probability of  $X = 2$  is very small, therefore we are unlikely to observe  $X$  with a value of 2

☒ the probability of  $X = 2$  is very large, therefore we are very likely to observe  $X$  with a value of 2

☐ none of the above

## Probability and Statistics: Descriptive Statistics

The following is the pdf of a continuous random variable,  $X$ ,



Use the above graph to compute the following.

**Question 6****1 / 1 pts**

The mean of  $X$  is

☒  $\frac{16}{3}$

☐ 6

☐ 5

☐  $\sqrt{30}$

☐  $\frac{22}{3}$

**Question 7****1 / 1 pts**

The median of  $X$  is

☐  $\frac{16}{3}$

☐ 6☐ 5☒  $\sqrt{30}$ ☐  $\frac{22}{3}$ **Question 8****1 / 1 pts**The variance of  $X$  is☐  $\frac{258}{3}$ ☐ 45☐ 10☐ 30☒  $\frac{98}{3}$ **Question 9****1 / 1 pts**The mode of  $X$  is:☒  $\frac{16}{3}$ ☐ 6☐ 5☐  $\sqrt{30}$

☐  $\frac{22}{3}$

**Question 10****1 / 1 pts**

Suppose you're told that: "most of the single family homes in Worcester tend to be priced around \$150,000; although there are a significant number of listings ranging above \$150,000 into the million mark." In this case, it's reasonable to expect that:

- ☐ the median price of single family homes in Worcester is higher than the mean
- ☒ the mean price of single family homes in Worcester is higher than the median
- ☐ the mean and the median of single family homes in Worcester are equal
- ☐ there is insufficient information to make a statement about the mean and/or median

## Joint, Conditional and Marginal Probabilities

Suppose you have the following information regarding the FDA trials of an experimental Hep-C test:

- 80% of the participants were Hep-C positive
- 20% of the participants were Hep-C negative and were used as control
- 95% of the Hep-C patients tested positive
- 30% of the control patients tested positive

Let  $H$  the patient's actual Hep-C status and let  $T$  be the patient's test status. Compute the following probabilities. Please explain your reasoning and state all formulae, properties you use.

**Question 11****1 / 1 pts**

$$P(T = + | H = +)$$

☐  $0.8 \cdot 0.95$

☐  $\frac{0.8 \cdot 0.95}{0.95 \cdot 0.3}$

☐  $0.8 \cdot 0.3$

☐  $0.8 \cdot 0.95 + 0.2 \cdot 0.3$

☐  $0.95 \cdot 0.3$

☒  $0.95$

☐  $\frac{0.8 \cdot 0.8 \cdot 0.95}{0.8 \cdot 0.95 + 0.2 \cdot 0.3}$

☐  $0.8 \cdot 0.8 \cdot 0.95$

**Question 12****1 / 1 pts**

$P(T = +, H = +)$

☒  $0.8 \cdot 0.95$

☐  $\frac{0.8 \cdot 0.95}{0.95 \cdot 0.3}$

☐  $0.8 \cdot 0.3$

☐  $0.8 \cdot 0.95 + 0.2 \cdot 0.3$

☐  $0.95 \cdot 0.3$

☐  $0.95$

☐  $\frac{0.8 \cdot 0.8 \cdot 0.95}{0.8 \cdot 0.95 + 0.2 \cdot 0.3}$

☐  $0.8 \cdot 0.8 \cdot 0.95$

## Question 13

1 / 1 pts

$$P(T = +)$$

☐  $0.8 \cdot 0.95$

☐  $\frac{0.8 \cdot 0.95}{0.95 \cdot 0.3}$

☐  $0.8 \cdot 0.3$

☒  $0.8 \cdot 0.95 + 0.2 \cdot 0.3$

☐  $0.95 \cdot 0.3$

☐  $0.95$

☐  $\frac{0.8 \cdot 0.8 \cdot 0.95}{0.8 \cdot 0.95 + 0.2 \cdot 0.3}$

☐  $0.8 \cdot 0.8 \cdot 0.95$

## Question 14

1 / 1 pts

$$P(H = + | T = +)$$

☐  $0.8 \cdot 0.95$

☐  $\frac{0.8 \cdot 0.95}{0.95 \cdot 0.3}$

☐  $0.8 \cdot 0.3$

☐  $0.8 \cdot 0.95 + 0.2 \cdot 0.3$

☐  $0.95 \cdot 0.3$

☐  $0.95$



☒ 
$$\frac{0.8 \cdot 0.8 \cdot 0.95}{0.8 \cdot 0.95 + 0.2 \cdot 0.3}$$

☐  $0.8 \cdot 0.8 \cdot 0.95$

Incorrect

## Question 15

Original Score: 1 / 1 pts Regraded Score: 1 / 1 pts

 This question has been regraded.

In order to win FDA approval for commercial use, the Hep-C test must be 80% effective in indicating the existence of an Hep-C infection. Does the above experimental Hep-C test meet the standard for commercial usage?

☐ Yes

☒ No

☐ There is insufficient information to make this determination

## Question 16

Not yet graded / 1 pts

Suppose you are given a 2 by n table of US infant birth weight data, stored as a 2-dimensional array. The first column is the age of the mother at the time of birth and the second column is the birth weight of the infant.

Write a single function, in your language of choice, that takes as input:

1. the birth weight table
2. the number of rows in the table
3. a number min and a number max (in this order);

that then returns:

1. the average,
2. the median
3. the mode of the ages of the mothers whose infant has birth weight between min lbs and max lbs.

**Do not use any pre-defined or built-in functions (e.g. sort, filter, mean etc).**

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Quiz Score: **15** out of 15