

$$V_p = \sqrt{2} \left[\frac{-M}{r_1 + r_2} + \frac{M}{r_1} \right]^{\frac{1}{2}} = \left(\frac{M}{r_1} \right)^{\frac{1}{2}} \left[2 - \frac{2}{1 + r_2/r_1} \right]^{\frac{1}{2}} = V_{c1} \left[2 - \frac{2}{1 + r_2/r_1} \right]^{\frac{1}{2}}$$

$$\Delta V_1 = V_p - V_{c1} = V_{c1} \left\{ \left[2 - \frac{2}{1 + r_2/r_1} \right]^{\frac{1}{2}} - 1 \right\}$$

$$V_a = \sqrt{2} \left[\frac{M}{r_2} - \frac{M}{r_1 + r_2} \right]^{\frac{1}{2}} = \left(\frac{M}{r_2} \right)^{\frac{1}{2}} \left[2 - \frac{2}{1 + r_1/r_2} \right]^{\frac{1}{2}} = V_{c2} \left[2 - \frac{2}{1 + r_1/r_2} \right]^{\frac{1}{2}}$$

$$\Delta V_2 = V_{c2} - V_a = V_{c2} \left\{ 1 - \left[2 - \frac{2}{1 + r_1/r_2} \right]^{\frac{1}{2}} \right\}$$

$$\Delta V = \Delta V_1 + \Delta V_2$$

$$= V_{c1} \left\{ \left[2 - \frac{2}{1 + r_2/r_1} \right]^{\frac{1}{2}} - 1 \right\} + V_{c2} \left\{ 1 - \left[2 - \frac{2}{1 + r_1/r_2} \right]^{\frac{1}{2}} \right\}$$

$$= V_{c1} \left\{ \left[2 - \frac{2}{1 + r_2/r_1} \right]^{\frac{1}{2}} - 1 + \frac{V_{c2}}{V_{c1}} - \frac{V_{c2}}{V_{c1}} \left[2 - \frac{2}{1 + r_1/r_2} \right]^{\frac{1}{2}} \right\}$$

$$= V_{c1} \left\{ \left(2 - \frac{2}{1 + r_2/r_1} \right)^{\frac{1}{2}} + \sqrt{\frac{r_1}{r_2}} \left[1 - \left(2 - \frac{2}{1 + r_1/r_2} \right)^{\frac{1}{2}} \right] - 1 \right\}$$