Linear Systems

HW7

班級:航太四A

姓名: 吳柏勳

學號:407430635

座號:4

$$\begin{cases}
A = \sum_{k=0}^{l} \alpha_k A^k = \sum_{k=0}^{l} \alpha_k (V \wedge V^{-1})^k \\
= \sum_{k=0}^{l} \alpha_k V \wedge^k V^{-1} \\
= \sum_{k=0}^{l} V (\alpha_k \wedge^k) V^{-1} \\
= V \left(\sum_{k=0}^{l} \alpha_k \wedge^k \right) V^{-1}
\end{cases}$$

$$\Rightarrow \bigwedge^{\sim} = \sum_{k=0}^{\ell} \alpha_k \bigwedge^k$$

$$\Rightarrow \hat{\chi}_{\bar{i}} = \sum_{k=0}^{\ell} \alpha_k \lambda_{\bar{i}}^k = \int_{(\lambda_{\bar{i}})} \chi_{\bar{i}}^k = \int_{(\lambda_{\bar{i}$$

#2

-! A and B is similar matrices

$$B = P^{-1}AP$$

$$= P^{-1}V\Lambda V^{-1}P$$

$$= \widetilde{V}\Lambda \widetilde{V}^{-1}$$

The eigenvalue of B will equal to the A

The eigenvector of B will equal to P'vi #

#3

Let
$$X_1 \in S_1 \subseteq \mathbb{R}^n$$
, $X_2 \in S_2 \subseteq \mathbb{R}^n$

-- ' S_1 and S_2 are orthogonal

-- ' $(X_1, X_2) = 0$

If
$$x_1 = x_2$$
, then
$$\langle x_1, x_1 \rangle = 0$$

$$\Rightarrow x_1 = 0_{\mathbb{R}^n} \neq$$

$$\emptyset(\lambda) = \det(A - \lambda I) = (\lambda_1 - \lambda)(\lambda_2 - \lambda) \cdots (\lambda_n - \lambda)$$

$$\Rightarrow \emptyset(0) = \det(A) = \lambda_1 \lambda_2 \cdots \lambda_n$$