$$\Rightarrow A = \begin{bmatrix} -1 & -5 & -2 \\ 2 & 7 & 4 \\ -1 & 2 & 1 \end{bmatrix}$$

$$\begin{cases} \mathcal{C}_{1} = (0) \cdot \chi_{3} + (-1) \cdot \chi_{2} + (1) \cdot \chi_{3} \\ \mathcal{C}_{2} = (\lambda) \cdot \chi_{1} + (-1) \cdot \chi_{2} + (0) \cdot \chi_{3} \end{cases} \Rightarrow P = \begin{bmatrix} 0 & 2 & 1 \\ -1 & -1 & 0 \\ 1 & 0 & 0 \end{bmatrix}$$

$$\widetilde{A} \chi_{2} = y_{2} \Rightarrow \begin{bmatrix}
Q & Q_{12} & Q_{13} \\
-2 & Q_{22} & Q_{33} \\
-2 & Q_{33} & Q_{33}
\end{bmatrix}
\begin{bmatrix}
0 \\
1 \\
0
\end{bmatrix} = \begin{bmatrix}
2 \\
-2 \\
1
\end{bmatrix} \Rightarrow \begin{bmatrix}
Q_{12} \\
Q_{22} \\
Q_{32}
\end{bmatrix} = \begin{bmatrix}
2 \\
-2 \\
1
\end{bmatrix}$$

$$A = \begin{bmatrix} 9 & 2 & 5 \\ -2 & -2 & -3 \\ -2 & 1 & 0 \end{bmatrix} \#$$

$$\widetilde{A} = PAP^{-1} = \begin{bmatrix} 9 & 2 & 5 \\ -2 & -2 & -3 \\ -2 & 1 & 0 \end{bmatrix}$$

$$\{e\} \xrightarrow{A} \{e\}$$

$$P^{-1} \uparrow \qquad \downarrow Q^{-1}$$

$$\{x\} \qquad \{y\}$$

$$\begin{cases} e_{3} \xrightarrow{A} \\ \geqslant e_{3} \end{cases} \qquad \begin{cases} y_{1} = (-2)e_{1} + (4)e_{2} + (1)e_{3} \\ y_{2} = (1)e_{1} + (1)e_{2} + (0)e_{3} \Rightarrow Q = \begin{bmatrix} -2 & 1 & 0 \\ 4 & 1 & 3 \\ 1 & 0 & -1 \end{bmatrix} \end{cases}$$

$$\begin{cases} P^{-1} \land \qquad \qquad y_{3} = (0)e_{1} + (3)e_{2} + (-1)e_{3} \qquad \qquad 0 = \begin{bmatrix} -2 & 1 & 0 \\ 4 & 1 & 3 \\ 1 & 0 & -1 \end{bmatrix} \end{cases}$$

$$\overline{A} = Q^{-1}AP^{-1} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$\overline{A} \chi_{2} = y_{2} \Rightarrow \begin{bmatrix} 1 & a_{12} & a_{13} \\ 0 & a_{21} & a_{23} \\ 0 & a_{31} & a_{33} \end{bmatrix} \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix} \Rightarrow \begin{bmatrix} a_{12} \\ a_{22} \\ a_{32} \end{bmatrix} = \begin{bmatrix} 0 \\ 1 \\ 0 \end{bmatrix}$$

$$\overline{A}\chi_3 = Y_3 \Rightarrow \begin{bmatrix} 1 & 0 & a_{13} \\ 0 & 1 & a_{23} \\ 0 & 0 & a_{33} \end{bmatrix} \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \Rightarrow \begin{bmatrix} a_{13} \\ a_{23} \\ a_{23} \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}$$

$$\overline{A} = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

$$A = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \vdots \\ a_{m_1} & a_{n_2} & \cdots & a_{m_n} \end{bmatrix}_{m \times m} , \quad y = \begin{bmatrix} \frac{1}{m} (a_{m_1} + a_{12} + \cdots + a_{2m_n}) \\ \frac{1}{m} (a_{n_2} + a_{n_2} + \cdots + a_{2m_n}) \end{bmatrix}$$

$$Ay = \begin{bmatrix} a_{11} & a_{12} & \cdots & a_{1n} \\ a_{21} & a_{22} & \cdots & a_{2n} \\ \vdots & \vdots & \vdots \\ a_{m_1} & a_{n_2} & \cdots & a_{m_n} \end{bmatrix} \begin{bmatrix} \frac{1}{m} (a_{m_1} + a_{12} + \cdots + a_{2m_n}) \\ \frac{1}{m} (a_{m_1} + a_{n_2} + \cdots + a_{m_n}) \end{bmatrix}$$

$$\|Ay\|_{1} = \frac{1}{m} (|a_{11} + a_{12} + \cdots + a_{1n}| + |a_{11} + a_{22} + \cdots + a_{2m_n}| + \cdots + |a_{m_1} + a_{m_2} + \cdots + a_{m_n}|)$$

$$= \frac{1}{m} (\frac{m}{n}) \| x_0 \|_{1}$$

$$= x \times p (\frac{1}{m}) \| x_0 \|_{1}$$

$$= x \times p (\frac{1}{m}) \| x_0 \|_{1}$$

$$= x \times p (\frac{1}{m}) \| x_0 \|_{1}$$

$$= x \times p (\frac{1}{m}) \| x_0 \|_{1}$$

$$= ||a_{11} y_1 + a_{22} y_2 + \cdots + a_{m_n} y_m|_{1}$$

$$= ||a_{11} y_1 + a_{22} y_2 + \cdots + a_{m_n} y_m|_{1}$$

$$= ||a_{11} y_1 + ||a_{22} y_2 + \cdots + ||a_{n2} y_m||_{1}$$

$$= ||a_{11} y_1 + ||a_{22} y_2 + \cdots + ||a_{n2} y_m||_{1}$$

$$= ||a_{11} y_1 + ||a_{22} y_2 + \cdots + ||a_{n2} y_m||_{1}$$

$$= ||a_{11} y_1 + ||a_{22} y_2 + \cdots + ||a_{n2} y_m||_{1}$$

$$= ||a_{11} y_1 + ||a_{22} y_2 + \cdots + ||a_{n2} y_m||_{1}$$

$$= ||a_{11} y_1 + ||a_{12} y_m||_{1}$$

$$= ||a_{12} y_1 + ||a_{12} y_m||_{1}$$

$$= ||a_{12} y_m$$

$$\|A\| \leq \max_{\tilde{\ell}=1,2,\ldots,N} \|a_{\tilde{\ell}}\|_{1}$$

$$\#(h)$$
 $\left\| \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix} \right\|_{1} = 1$