

# Productivity Function

Mathematical foundation for Production Management in Construction

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## 1 Guidelines

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- 7000 Words

## 2 Abstract

The building construction industry faces challenges, such as increasing project complexity, and larger scope requirements but shorter deadlines. Additionally, the industry relies on practices based on intuition and experience, overlooking the dynamics of its production system. These approaches underestimate the influence of process repetitiveness, the size of the production run, the transient state (setup times), the variation of learning curves, and the conservation of processes properties. Consequently, construction adopts the manufacturing production model dismissing the application of approaches that accurately describe the characteristics of its production system. This chapter aims to provide a production theory to better understand the production mechanisms of repetitive processes in project-driven systems in construction. The chapter begins with an examination of the existing knowledge about production models, their characteristics, and the challenges to establishing a theoretical framework for controlling dynamic production systems management in construction projects. The chapter progresses to an analytical and scalable method (Productivity Function) to represent the behavior of production systems. The Productivity Function provides a mathematical foundation for the calculations of cycle times (average, best- and worst-cases), throughput at capacity, and the influence of the transient state time in the production variability. Productivity Function is applied in feedback loop control yielding a robust approach to plan, control, and optimize production. Finally, the chapter presents automated methods of data collection that feed the Productivity Function models, which are the foundation of the production theory and support the decision-making process on Lean Construction 4.0.

## 3 Introduction

Despite the name of the title of this chapter, you will not find equations here. Not because they do not exist, but because we believe that, at least for now, it is more important to understand what these equations represent than how they come to be. You are welcome to deep your knowledge and see the equations and their development on the referenced literature.

## 4 Lean principles and production theory [0/2]

### 4.1 Production in manufacturing (Factory Physics)

The manufacturing industry is knowable of its production. From early times when 'time and motion' has been developed on workers construction a brick wall (Reference here), manufacturing has being advancing on understanding and managing of its production. Mostly important on the context on this book, it was the creation and development of lean production that inspired lean construction. This chapter stands on further development of lean production: it's mathematical explanation of production. Such work has been conducted by TOYOTA dude, THE guy from MIT and mates from Factory Physics. Their work combined provide a set of equations that apply to manufacturing production systems. A production system consists into three main elements: inputs, process, outputs (Figure ). Inputs may not reflect the full range of requirements to create the output but on this system view they determine the output. The process can be determined on physical known equations or most often determined by evaluating the relationship between input and output. The mathematical representation of this relationship is main difference between manufacturing and construction.

### 4.2 The manufacturing theory does not apply directly to construction

Manufacturing is either a continuous or a repetitive process. Machinery and human resources are specialized and qualified. Production flow and material routes are established. Thus, most manufacturing processes can be automated. That scenario is different from construction. While capacity is known and measured in manufacturing, there was no way to measure it in construction. Increasing production in construction often means add more human resources. That often cause decrease of productivity due to lack of space, tools, skills, etc.

## 5 Productivity Function [0/2]

### 5.1 Production process system representation [100%]

- A SYSTEM VIEW (Source: Identification of repetitive processes at steady- and unsteady-state: Transfer function) Mathematical models have enabled a comprehensive understanding of production mechanisms supporting practices to improve production in manufacturing. Hopp and Spearman (1996) committed to the comprehension of the manufacturing production system. The system approach or system analysis was the problem-solving methodology of choice (Hopp2001). The first step of this methodology is a system view. In the system view, the problem is observed as a system established by a set of subsystems that interact with each other. Using the system approach, Hopp and Spearman elaborated significant laws to queue systems and the general production in manufacturing. The conservation of material and capacity laws (Hopp and Spearman, 1996) are particularly attractive, not only according to their importance, but also because they explicitly state one or more system restrictions.

In this system view, an input is applied to a process to produce an output. These three elements constitute a input/output system (Figure ??); which we will refer simply as system from now on. Input are, for instance, materials, tools, equipment, labor, management, time, and weather conditions (Blanchard and Fabrycky, 2011). **“Some of these factors, such as material, also become a part of the output product, while others are needed for control purposes (e.g., management). Still another category includes environmental impacts (e.g., weather conditions) (Remold, 1989).”** The outputs are (usually) the product of the processes, for example, absolute quantities such as squared meters of plastered wall, meters drilled or relative measurement of progress such as the percentage of activity completion (Antunes2016). This last may be especially useful for Lean Construction practitioners that utilize the Planned Percent Complete (PPC) as the tracking tool. The process is the transformation procedure, or operation that when applied the input will create the output. For instance, platerboards installation an drilling for the ouputs aforementioned. The Figure ?? shows a single output and single input (SISO) for simpicty purposes. A system can be composed by multiple inputs to single or multiple outputs (MISO and MIMO respectively) and also single input to multiple outputs. Regardless of the system composition in terms of how many inputs and outputs or what the input(s), output(s) and process are; there are a few restrictions to a system:

- There is no output on lack of input.
- There is no output without a process.



Figure 1: Simple system

- Project as cycle Most projects follow a cycle similar to plan-do-check-act (PDCA), also originally developed for manufacturing operations. PDCA applies to continuous process improvement (Rumane and Badiru, 2013, p.53) and consists of a four-stages infinite loop. First, the team establishing goals and develop the strategies to achieve them, creating a plan. Second, the plan is then implemented. The team carries out the actions addressing key points, according to the plan. Third, the team measures the outcomes of their actions comparing the results to the goals. Fourth, where the current process performance matches the goal, the team institutionalizes the new processs performance, thus setting a benchmark, as well as the actions performed to

achieve the goal, thus creating standard procedures. In the case where the actions are not effective, the team must return to the first cycle stage. The PDCA cycle restarts to implement further improvements. *In certain way, it means a system that is being constantly feedback by the current output state. If the current output state is no the one desired, the input will change to match achieve the output goal. The process improvement itself will alter the process as such the system will have increased the output using a constany input.* /In terms of system, it will look like figure ???. The 'plan' is desired output. 'Check' is a comparison between the 'plan' and the current output. The result is the measured 'deviation'. Based on the 'deviation' actions must be implemented. For example, the plan establish that an output of 50 square meters should be installed an hour to complete the job on time. Two workers are initially assigned to the job (input). If the two workers (input) are capable to install (process). That creates an action which for this example is to increase workers to increase output. On the other hand, if the workers produce a higher output than the plan, the deviation will work on the other way: decrease the number of workers to reduce output thus matching the plan. This configuration is a Closed-loop Control System or feedback control system in control theory.

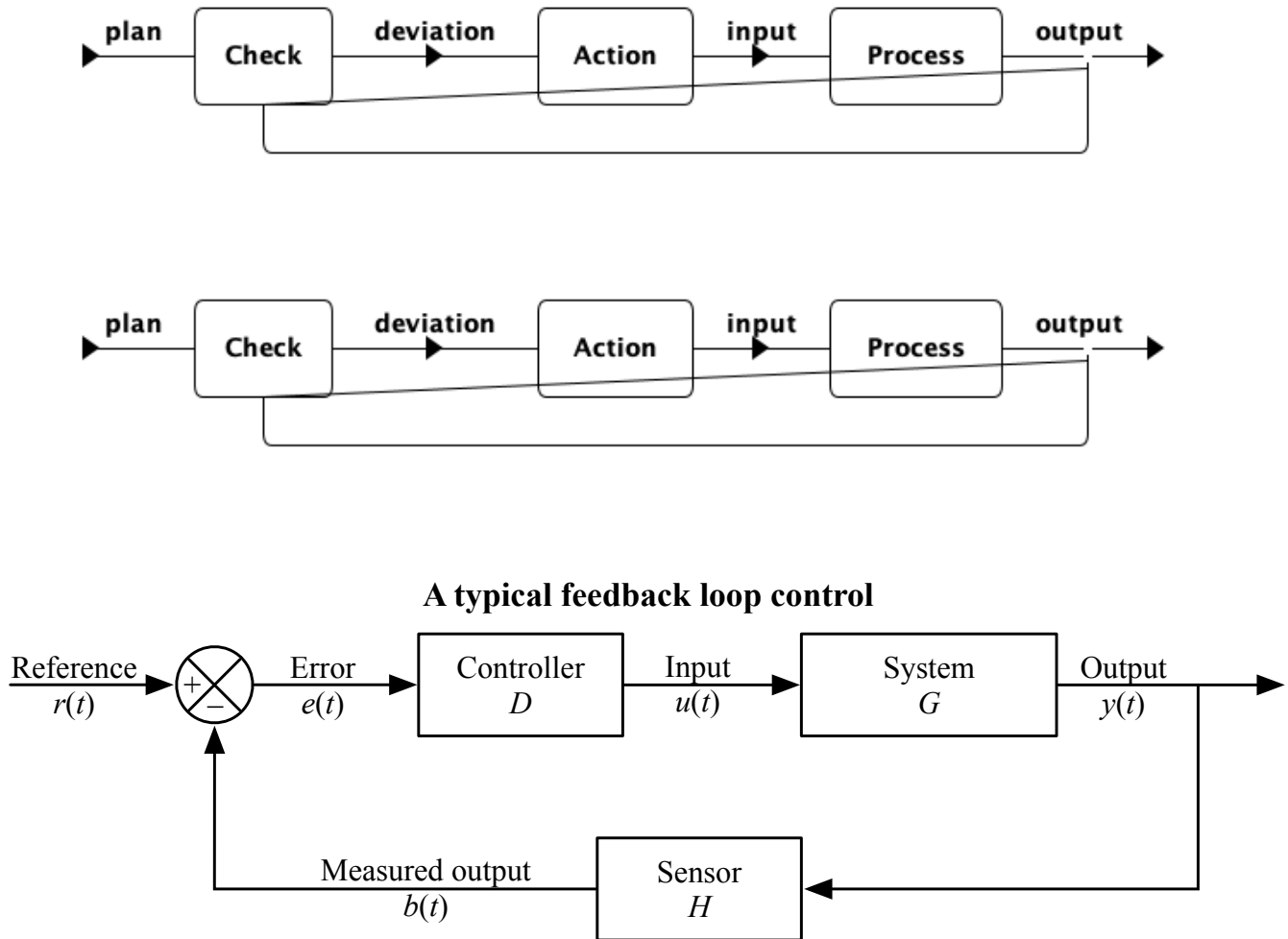


Figure 2: A typical feedback loop control

□ Construction System Source Paper07 Stays here

Several elements found in this literature review connect the characteristics of construction projects to the characteristics of a dynamic system. As shown in Figure ??, the interconnectivity is explicit between project stages, in the event that subsequent phases rely on the accomplishment and performance of previous ones. This dependent connection remains valid for divided n-substages or n-activities and also applies to the proposed framework. The dependence of processes and/or activities is well documented in the literature and well

known by practitioners. An activity or stage may impair or favour a successive action depending on the level of correlation and dependence. The interdependence of activities forms a conduit to the propagation of unsure events. Potential risks captured through the entire project life may impact project execution whenever not properly treated, resulting in project deviations. This sequence of events is represented in the system by the flow of uncertainty to risk and the occurrence of risk events, through risk management filtering actions—avoidance, acceptance, sharing, transference, mitigation, motivation—and, finally, to variability. This flow resembles an intrinsic characteristic of systems in the presence of disturbance or noise.

Control systems may transmit unfiltered noise across connections affecting vulnerable components and causing disturbances or unpredicted behaviour. Although the level of influence in this flow of sequential, parallel or overlapping relationships in the process or activity network have not been investigated at this point, understanding how risk transforms into variability, and especially how variability affects networked activities, propitiates an opportunity to develop methods aimed at avoiding and mitigating (filtering) the propagation of risk (noise). Regarding risk materialization in variability, different outcomes build on how concentrated or distributed the risk impact was. Operating on possibly the same conditions of linear/nonlinear, deterministic/stochastic, time-domain/frequency domain, direct/inverse problems, discrete/continuous models—control theory may create a proxy theory to explain the effects of variability in construction projects by extending the elements of the dynamic systems.

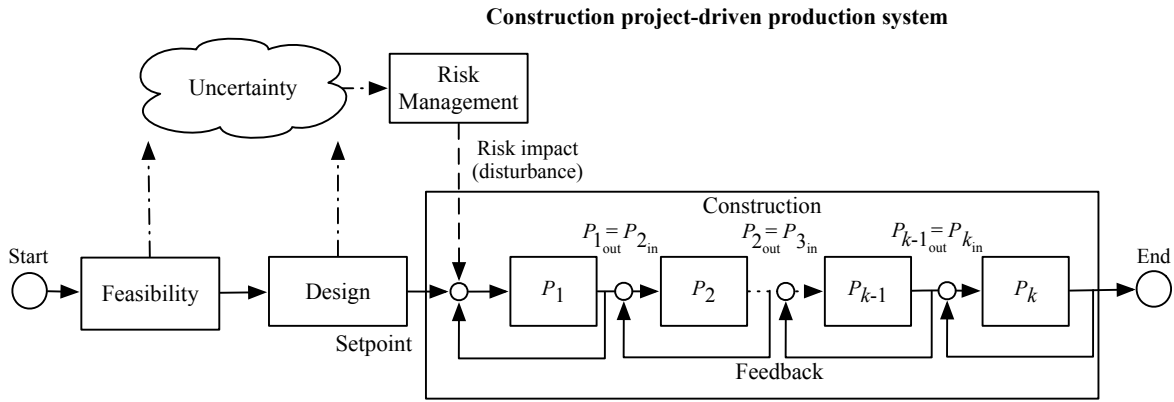


Figure 3: Construction project-driven production system

The simplest model of construction processes considers a closed conversion process where all factors affecting the work are steady state Drewin1982. In this model, the relationship between output and input, i.e., productivity, is given by a constant which is unaffected by external factors. This constant can be determined by, for instance, the linear curve fitting or the ratio of the sum of outputs to the sum of inputs. The linear scheduling method (LSM) (Harmelink1998,Su2016) and line-of-balance (LOB) (Lumsden1968,Su2016,ZolfagharDolabi2014) are examples of scheduling models for repetitive processes based on the steady state model. However, “because of the steady state nature of this model, the system more closely represents industrial production processes than construction processes (Thomas1990).” Short production runs Bashford2005, high levels of output and input variability **Gonzalez2009**, and nonlinear input-output relationships Bertelsen2003,Lutz1993 frequently prevent repetitive production processes in construction to reach steady state Antunes2015a,Walsh2007.

- Limitations of Manufacturing system view to construction These laws place reliance on stable systems, with long runs and at steady-state conditions. However, production in project-based systems, such as construction, involves a mix of processes in steady- and unsteady-state, short and long production runs, and different learning curves (Antunes2015) Hence, unless a construction process fulfills the stability and steady-state conditions, the manufacturing model and, consequently, the laws do not accurately represent production in construction. Alternatively, variants of manufacturing laws must be developed to production in project-based systems that not fulfill those requirements. In this scenario of variety, it is crucial distinguishing between project-based systems conditions, comprehending process dynamics and its behavior.

## 5.2 Mathematical foundation of the Productivity Function

(Explain differential equations, the frequency domain and transformation)

Although much work has been done on production management of repetitive construction processes, more studies need to be conducted to develop equations to quantify project-driven production systems in construction. The objective of this paper is to formulate variants of manufacturing production equations to calculate the production performance of repetitive construction processes for benchmarking purposes. Furthermore, this paper shows the calculation of theoretical production parameters such as capacity and cycle time, as well as the influence of transient time on productivity. The contribution of this paper to the body of knowledge are algebraic equations based on a generic model to calculate production parameters for repetitive processes in construction.

### 5.2.1 Step response: Transient and steady state (explain the equation, move it, or clean it)

The transient is the immediate system reaction of an input change from a rest state Ogata2010. If the system is stable, the response will tend to a constant value,  $y_{ssv}$ , when the time,  $t$ , goes to infinity (Equation~3). When the output reaches this value, the response is then at steady state. The time that the system response takes from the moment the input changes to the steady state Nise2010,Ogata2010, is the settling time,  $t_s$ , i.e., the duration of the transient state. Figure~?? shows the step analysis which is an artificial and controlled way to reproduce the transient, as well as determine the steady state response of a system represented by the Productivity Function. In the unitary-step function,  $u_{\text{step}}(t) \xleftrightarrow{\mathcal{L}} U_{\text{step}}(s) = 1/s$ , at a time  $t_0$  the input changes from 0 to 1 and then is kept constant at 1. At  $t_0$ , if there is no delay, the system will notice the change in the input generating the transient response. A physical interpretation of the step function is switching on a light by pressing a button. Finally, if the system is stable; the output will tend to the steady state value.

$$y_{ssv} = \lim_{t \rightarrow \infty} y(t) \quad (1)$$

The step function in the time domain is given by:

$$u_{\text{step}}(t) = \begin{cases} 0, & t = 0 \\ 1, & t \neq 0 \end{cases} \quad (2)$$

### 5.2.2 TODO Explain transient and steady-state (move to section above, foundation)

- Why the transient TRANSIENT STATE, STEADY-STATE, AND UNSTEADY-STATE RESPONSE Two parts compose a system response in the time domain, transient, and steady- or unsteady-state. Transient is the immediate system response to an input from an equilibrium state. After the transient state, a system response can assume a steady- or unsteady-state. In a stable system, the output tends to a constant value when  $t$  (Mandal, 2006). When the system response enters and stays in the threshold around the constant value the system reached the steady-state (Mandal, 2006). The time the stable system takes to reach the steady-state is the settling time,  $t_s$ . On the other hand, if the response never reaches a final value or oscillates surpassing the threshold when  $t$  the system is then at unsteady-state. Consequently, the system outputs at unsteady-state vary with time during the on-time interval even induced by an invariable input.

#### 1. Mathematical foundation of production (repeated title)

Repetitive construction projects falls into a fuzzy area where both project management and manufacturing overlap. Repetitive construction projects are constituted by several contractors executing processes that they are specialized in, as for instance plumbers and electricians, that in the end, build a one-of-a-kind product. The operations executed by several contractors are often performed repeatedly, and simultaneously at times, which stands for one of the peculiarities of repetitive projects. In project-driven production, the coexistent mix of characteristics from project management and manufacturing makes the management of project-driven production problematic. Project-driven production systems, such as repetitive construction, involve a combination of processes at transient, unsteady state, and-rarely-at steady state Antunes2015a,Antunes2015,Bashford2005,Walsh2007. However, traditional construction management, at this time, utilizes practices based on the manufacturing model that lacks the mathematical foundation to model and manage production in the project-driven systems Bertelsen2003,McCray2002,Pereira2013,Ko2016.

- The system steady-state. The steady-state of a system
- #### 2. Explain traditional methods of steady-state
- The transient is the immediate system reaction of an input change from a rest state Ogata2010. If the system is stable, the response will tend to a constant value,  $y_{ssv}$ , when

the time,  $t$ , goes to infinity (Equation~3). When the output reaches this value, the response is then at steady state. The time that the system response takes from the moment the input changes to the steady state Nise2010,Ogata2010, is the settling time,  $t_s$ , i.e., the duration of the transient state. Figure~4 shows the step analysis which is an artificial and controlled way to reproduce the transient, as well as determine the steady state response of a system represented by the Productivity Function. In the unitary-step function,  $u_{\text{step}}(t) \xleftrightarrow{\quad} U_{\text{step}}(s) = 1/s$ , at a time  $t_0$  the input changes from 0 to 1 and then is kept constant at 1. At  $t_0$ , if there is no delay, the system will notice the change in the input generating the transient response. A physical interpretation of the step function is switching on a light by pressing a button. Finally, if the system is stable; the output will tend to the steady state value.

$$y_{\text{ssv}} = \lim_{t \rightarrow \infty} y(t) \quad (3)$$

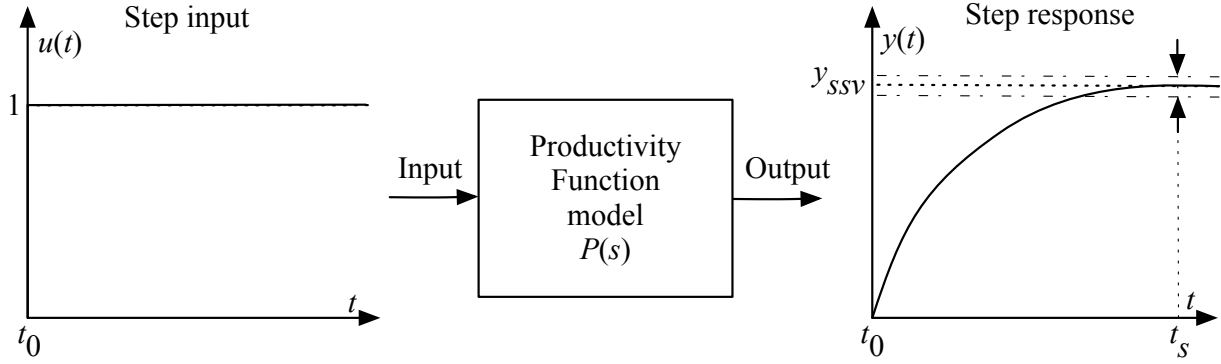


Figure 4: Transient analysis for unit step input

The step function in the time domain is given by:

$$u_{\text{step}}(t) = \begin{cases} 0, & t = 0 \\ 1, & t \neq 0 \end{cases} \quad (4)$$

The production of products or services designed to fulfill unique, or one-of-a-kind, specifications is the essence of project-driven production, also known as project-oriented manufacturing Martinez1997. “Repetitive construction projects are resource-driven, multi-unit projects characterized by activities which need to be performed in a sequence from unit to unit repeatedly Hajdasz2015.” That assumes a position in Product process matrix (Figure~??) between manufacturing and project management, hence mixing characteristics from both sides, following the manufacturing production structure on the make-to-order (or make-to-build) demand of projects. The product-process matrix (Figure~??) illustrates the relationship of different products regarding their workflow and volume. The most visible characteristic of the figure is a diagonal arrangement of the products showing a directly proportional relationship between production volume and workflow connection Kumar2009, and also a relationship between the degree of freedom and production focus.

At the lower end of the diagonal, products are produced in high volume units and with hardly any or no differentiation at all, e.g., commodities. Furthermore, the production process matches the characteristics of long run production [p.154]Baye2010 and economies of scale [p.185]Baye2010. The work stream is a continuous flow of specialized processes and equipment running at peak efficiency with stable and low variation processes [pp.8-10]Hopp2001 and relative short transients.

$$P(s) = \frac{Y(s)}{U(s)} = \frac{(\beta_m s^m + \beta_{m-1} s^{m-1} + \dots + \beta_0)}{(\alpha_n s^n + \alpha_{n-1} s^{n-1} + \dots + \alpha_0)} \quad (5)$$

□ Transfer Function (Source: Identification of repetitive processes at steady- and unsteady-state: Transfer function)

The transfer function of a system,  $G$ , is a transformation from an input function into an output function, capable of describing an output (or multiple outputs) by an input (or multiple inputs) change,  $y(t) = G(t) \star u(t)$ . Although generic, the application of the transfer function concept is restricted to systems that are represented by ordinary differential equations (Mandal, 2006). Ordinary differential equations can represent most dynamic systems in its entirety or at least in determined operational regions producing accurate results (Altmann and Macdonald, 2005; Mandal, 2006). As a consequence, the transfer function modeling is extensively applied in the analysis and design of systems (Ogata, 2010). A generic transfer function makes possible representing the system dynamics by algebraic equations in the frequency domain,  $s$ . In the frequency domain, the convolution operation transforms into an algebraic multiplication in  $s$ , which is simpler to manipulate. Mathematically, the transfer function of a linear system is defined as the ratio of the Laplace transform of the output,  $y(t)$ , to the Laplace transform of the input,  $u(t)$ , under the assumption that all initial conditions are zero (Mandal, 2006), Equation 1. Where the highest power of  $s$  in the denominator of the transfer function is equal to  $n$ , the system is called a  $n$ th-order system.

### 5.3 Modelling method [0/0]

- **SYSTEM IDENTIFICATION** (Source: Identification of repetitive processes at steady- and unsteady-state: Transfer function) (It should be moved after the system. To system Modelling approach.) The objective of system identification is to build mathematical models of dynamic systems using measured data from a system (Ljung, 1998). There are several system identification approaches to model different systems, for instance, transfer function. The transfer function is particularly useful because it provides an algebraic description of a system as well means to calculate parameters of the system dynamics and stability. Nevertheless, the modeling capability of the transfer function in construction must be evaluated and tested. In this study, the modeling approach, i.e., transfer function, focuses on replicating the input/output mapping observed in a sample data. When the primary goal is the most accurate replication of data, regardless of the mathematical model structure, a black-box modeling approach is useful. Additionally, black-box modeling supports a variety of models (Bapat, 2011; Billings, 2013), which have traditionally been practical for representing dynamic systems. It means that at the end of the modeling, a mathematical description represents the actual process performance rather than a structure biased by assumptions and restrictions. Black-box modeling is a trial-and-error method, where parameters of various models are estimated, and the output from those models is compared to the results with the opportunity for further refinement. The resulting models vary in complexity depending on the flexibility needed to account for both the dynamics and any disturbance in the data. The transfer function is used in order to show the system dynamics explicitly

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### 5.4 Production Theory for Construction

#### 5.4.1 Production forecast

Forecasting is a tool that allows managers to create and access different scenarios of production result of risk impact. Hence, forecasting supports both risk management practices for mitigating risk as the result of current progress on future completion. Even though forecasting in construction is often inadequate and one of the weakest project



controls functions ConstructionIndustryInstitute2012. “While there are many reasons for poor forecasting practice, one of the main causes may be the limited educational resources available on forecasting In many textbooks and manuals, education about forecasting starts and stops with a presentation of earned value and elementary trending calculations ConstructionIndustryInstitute2012a,” such as linear functions and averages. The numerical estimation approach of Productivity Function can be embedded in the Project Management software or used as a stand-alone tool to forecast, access and simulate critical processes that require in-depth project controls. As the Productivity Function models do not require anything else than the process’ inputs and outputs, e.g., labor hours used to produce square meters of plastered wall, the models can be used together with project control practices such as earned value or Planned Percent Complete (PPC). Simply by replacing the traditional steady state model by the Productivity Function, more accurate results should be obtained. Furthermore, Dynamics Simulation, which relies on the mathematical models defined by ordinary differential equations (as the Productivity Function), have a significant role in supply chain Higuchi2004 and production in manufacturing Forrester1997. The application of Dynamics Simulation in construction is rare, specifically due to the lacking of mathematical models to describe the production in construction. A gap that may be fulfilled by the Productivity Function. While the algebraic form of Productivity Function may support the development of equations that further explain the production of project-driven processes, such as equations for capacity and cycle time. Furthermore, the measurement and visualization of the transient state of project-driven processes support the quantitative and structured application of methods to reduce setup times, as for instance, Single Minute Exchange of Dices (SMED) and pre-fabrication Antunes2016.

This chapter initiated as an exploration of elements in the building construction project cycle and their effect on production behavior, resulting in theoretical framework structured as a system Antunes2015a. This system proposed a flow of uncertainty to risk and then risk impact risk impact that would cause variability. Following the framework, an analytical technique to describe the dynamic conditions of production in repetitive processes in projects was suggested Antunes2015, as well as the relationship between the model characteristics and flow variability Antunes2016. This study is a step forward towards the development of a mathematically driven production theory for construction project management and project-driven systems defining a modeling approach and pointing out that dynamical systems theory would be useful to describe the behavior of production in construction.

#### 5.4.2 Variability analysis

“Law (Variability): Increasing variability always degrades the performance of a production system Hopp2001.” In other words, the system will achieve its maximum performance when there is no variability. That becomes evident when analyzing CV (Equation~??): the greater the coefficient of variation,  $CV$ ; lower is the mean output,  $\bar{y}$ , i.e.,  $\bar{y} \sim CV^{-1}$ . Based on the knowledge of dynamic systems, the lowest level of variation in the output (indistinctly used in this paper as throughput once the outputs of dynamic systems are time dependent) happens when the system is at steady state Nise2010,Ogata2010. Productivity Function can be used to determine the theoretical output at steady state, and consequently the cycle time, using the stationary conditions as shown in Equation~??.

The output at steady state of a system represented by a Productivity Function in the frequency domain can be calculated using the final value theorem. “The final value theorem provides an easy-to-use technique for determining this value without having to first invert the Laplace transform to determine the time signal [p.97]Chen2007.” Equation~6 shows the final value theorem which gives the steady state value,  $y_{ssv}$ , in the frequency domain.

$$\lim_{t \rightarrow \infty} y(t) = \lim_{s \rightarrow 0} sY(s) \quad (6)$$

Replacing  $Y(s) = U_{\text{step}}(s) \times P(s)$ , where  $U_{\text{step}}(s)$  is the step function,  $1/s$ :  $Y(s) = 1/s \times P(s)$

$$\lim_{t \rightarrow \infty} y(t) = \lim_{s \rightarrow 0} s \frac{1}{s} \times P(s) \quad (7)$$

Replacing the left side of the Equation~7 by Equation~3 the result is the output at steady state, i.e., the system’s highest throughput with lowest variation: capacity.

$$y_{ssv} = \lim_{s \rightarrow 0} P(s) = P(0) \quad (8)$$

#### 5.4.3 Production benchmark

#### 5.4.4 Production plan, monitoring, and control

1. Throughput Throughput is the output (non-defective) of a production process in a defined period **Hopp2001**. Construction scheduling accuracy strongly depends on being able to coordinate resources to determine the

processes throughput **Cho2011**. When the relationship between resources and throughput can be established; it is possible to determine the necessary resources to achieve the desired performance **Cho2011**. The production workflow in construction is segmented, i.e., job shop, where “jobs arrive in different forms and require different tasks, and thus the equipment tends to be relatively general purpose **Hayes1979**,” equipment has different productivity/availability **Ok2006**, and the increased labor resource frequently causes site congestion **Cho2011**. There is an endless list of human factors that influence the labor output, such as the workers’ experience, skill, and age **El-Gohary2014**.

The open conversion model **Kellogg1981** considers internal, external, and also unknown influences to productivity in a hierarchical arrangement. Despite being generic and industry-comprehensive, at the operational level the complexity of inputs, such as the cost of labor, capital, energy, and materials; and output, e.g., dollars, makes the use of the open conversion model impractical **Thomas1990**. Explicitly incorporating all factors that influence productivity in a model is a challenging task.

“The relationship between inputs and outputs is very complex and, in many cases, includes some unknown combined effects **Ok2006**.” Simplifications and assumptions have to be made; however, the models are often over simplified.

## 2. Cycle-time

The accumulated throughput over time results in units of a service or product produced over time. The time taken to produce one output is the cycle time. In a continuous system, the function of the output produced is given by the integral of the output. At steady state, where the throughput is constant, the unitary area below the curve is given by the throughput,  $y_{ssv}$ , multiplied by the cycle time (Equation~14). In other words, the area results from the time when the last output was produced,  $t_{j-1}$ , minus the time when the production of the current output unit finishes  $t_j$ , where  $j$  is the denotation of an element and  $j \in N^+$ . Hence,  $\Delta t_j = t_j - t_{j-1}$  is the time taken to produce the  $j$ th-output, i.e., cycle time,  $CT_j$ . Therefore, Equation~13 is equivalent to Equation~14. As  $y_{ssv}$  should determine the capacity of the system, the cycle time at steady state is the shortest production time of the system while stable, i.e., cycle time (best).

$$y_{ssv} \times (t_j - t_{j-1}) = 1, \quad \text{or} \quad \Delta t_j = 1/y_{ssv} \quad (9)$$

Different to the steady state, the throughput of the production system varies while the system is in the transient. The unitary area under the throughput curve can be calculated by a limited integral, with  $t_{j-1}$  and  $t_j$  as lower and higher limits, respectively (Equation~10). As the throughput decreases, the cycle time increases. Hence, the maximum cycle time of the production system, i.e., cycle time (worst) is found at start-up when the throughput at time  $t_0$  is null.

$$\psi_j = \int_{t_{j-1}}^{t_j} y(t) dt \quad (10)$$

Considering that the production system will increase its throughput over time as per its transient curve; the cycle time (worst) is the time taken to produce the first output ( $j = 1$ ) from a rest state:  $\Delta t_m = t_1 - t_0$ , or simply  $\Delta t_j = t_1$ , once  $t_0 = 0$ , is given by Equation~11.

$$\psi_1 = \int_0^{t_1} y(t) dt \quad (11)$$

Consequently, if the process increases its throughput as described by its transient curve, the longer it will take to reach the steady state and the smaller will be the area under the curve; hence, smaller its average output produced per time. The average output per time can be calculated by the average function value given by Equation~12.

$$\psi_{t_s} = \frac{1}{t_s} \int_0^{t_s} y(t) dt \quad (12)$$

In other words, for processes with equal capacity,  $y_{ssv}$ , the longer the transient time,  $t_s$ , the longer is the average cycle time,  $CT$ . Also, for processes with equal transient time the greater the capacity, the smaller is the average cycle.

$$y_{ssv} \times (t_j - t_{j-1}) = 1, \quad \text{or} \quad \Delta t_j = 1/y_{ssv} \quad (13)$$

- (a) Average cycle-time
- (b) Worst cycle-time
- (c) Best cycle-time

3. Capacity “Law (Capacity): In steady state, all plants will release work at an average rate that is strictly less than the average capacity [p.]Hopp2001.” Furthermore, in most cases, releasing work into the system above the capacity causes the system to become unstable Hopp2001. According to these definitions, it would be correct to state that a process’ capability is the highest throughput achievable without the process becoming unstable. Thus, at capacity, the process operates with optimal productivity Kisi2017. “The theoretical maximum productivity that would be achieved under absolutely perfect conditions in all respects (perfect weather, highly motivated, and productive labor with perfect workmanship, optimal materials, optimal equipment, no interferences from other trades, no design errors, perfect understanding of design intend, etc . . . ) [p.150]Son2011.” However, the variation in the efficiency of workers and equipment, actual demand, and scheduling planning and control~**Kumar2009** may prevent processes from achieving the system design capacity. Design capacity in a manufacturing system is engineered to full-scale operating conditions. However, the system capacity is less than the design capacity, because the full-scale operating conditions are rarely met Kumar2009.

The capacity of project-driven processes is not engineered but based on intuition McCray2002,ProjectManagementInstitute2011. Regardless of the equation used for productivity measurement Thomas1990, determining the system capacity is crucial to settling a benchmark and elaborating what the level of productivity the actual performance should be compared to Abdel-Razek2007,Olomolaiye1998,Zhao2014.

$$y_{ssv} = \lim_{s \rightarrow 0} P(s) = P(0) \quad (14)$$

## 6 Applicability

### 6.1 Automation and technology

#### 6.1.1 Supervisory control and data acquisition (SCADA)

#### 6.1.2 Challenges

### 6.2 Decision-making support

### 6.3 Benefits and impacts

## 7 Discussion

## 8 Conclusion

## 9 Plan

Section	Words	Current	Effort	Current
Plan			1	1
Introduction	500		4	
Lean principles and production theory	1500		5	
Productivity Function	2000		5	5
Applicability	1500		5	
Discussion	1000		5	
Conclusion	500		5	
Review			5	
Total	7000	0	35	3

9.1 6 Section

10 References