COMP 2402 Class Notes

Java Collections Framework (JCF)

The Java Collections Framework (JCF) is a unified architecture for representing and manipulating collections.

A collection — sometimes called a container — is simply an object that groups multiple elements into a single unit. Collections are used to store, retrieve, manipulate, and communicate aggregate data. Typically, they represent data items that form a natural group, such as a poker hand (a collection of cards), a mail folder (a collection of letters), or a telephone directory (a mapping of names to phone numbers). If you have used the Java programming language — or just about any other programming language — you are already familiar with collections.

In order to use the JCF you can import it like this.

```
import java.util.*
```

Sorting

This is how to sort strings based on length by using anonymous object [Comparator].

```
Collections.sort(list, new Comparator<String>() {
    public int compare(String x, String y) {
        return x.length() - y.length();
    }
});

// or you can use lambda function
list.sort( (String o1, String o2) -> o1.compareTo(o2)
```

```
// if you want to sort by length and also
alphabetically
Collections.sort(list,new Comparator<String>() {
    public int compare(String x, String y) {
        // if not same length, use length
        if(x.length() != y.length()) {
            return x.length() - y.length();
        }
        // else compare as strings
        return x.compareTo(y);
    }
});
```

The **compare(x,y)** method works by moving an element left if the **compare(x,y)** method returns a negative integer, and moves the element right if the **compare(x,y)** returns a positive integer. [difference between x and y]

```
(-) x < y
(0) x = y
(+) x > y
```

Maps [Hashmap]

Also known as dictionaries in Swift or C#...

Cannot have duplicate entries

```
Map<String, Integer> map = new HashMap<>();
map.put("Java", 6);
map.put("Swift", 10);
map.put("C#", 7);
map.put("Ruby", 9);
```

```
// this will print out every value in the map [foreach]
for(String str : map.keySet()) {
    System.out.println(str + " : " + map.get(str))
}
map.get(key); // fast operation, returns null if no key
found
```

List

Continuing from previous example...

Map.Entry is just a key-value pair

```
List<Map.Entry<String,Integer>> entryList = new
ArrayList<>();
entryList.addAll(map.entrySet); // set containing all
the elements

for(Map.Entry<String,Integer> entry : entrylist) {
    System.out.println(entry.getKey() + " : " +
entry.getValue() );
}
```

Deque [ArrayDeque]

Fast for reading/writing at *start* or *end* of list. Basically just a flexible stack/queue.

```
Deque<String> dq = new ArrayDeque<>>();
dq.addFirst("second");
dq.addFirst("first");
dq.addLast("penultimate");
dq.addLast("last");
```

Priority Queue

Essentially: uses a heap instead of a tree, in order to keep a certain one on top. So first element is 'sorted' and then rest is unsorted.

Not good for sorting, or random access.

```
Queue<String> pq = new PriorityQueue<>();
pq.addAll(list);

System.out.println(pq.remove()); // remove smallest
element
```

If alphabetical, one that starts with 'a' will be removed. After first element, the queue is not sorted. Removing one will promote next smallest to the top

Asymptotic Notation [Big O]

Used to analyze complexity of algorithms, to find faster, or which ones requires more space.

Comparing data structures

- Time
- Space
- Correctivenes

Growth rates proportioanl to n

• If input doubles in size, how much will runtime increase?

Runtime as a count of primative operation

This is machine independent

Proportional to exact runtimess

```
for(int i = 0; i < n; i++) {
    arr[i] = i;
}</pre>
```

Runtime:

- 1: assignment [int i = 0]
- **n+1**: comparisons [i < n]
- **n**: increments [i++]
- n: array offset calculations [arr[i]]
- **n**: n indirect assignments [arr[i] = i]

Definition of Big O

After a certain point, g(x) will grow as fast [or faster] than f(x)

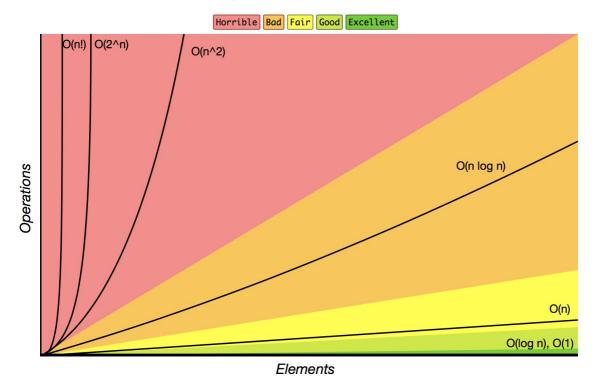
• g(x) is the upper limit to f(x)

$O(g(n)) \ \forall \ (f(n) < c \bullet g(n))$

Orders of growth

Complexity	Name
O(1)	Constant
O(log n)	Logarithmic
O(n)	Linear
O(n log n)	Quasilinear
O(n^2)	Quasilinear
O(2^n)	Exponential
O(n!)	Factorial

Big-O Complexity Chart



Tips

- Only largest values matter
- Drop all coefficient
- Log bases are all equivalent

Example

Array-based Data Structures

ArrayStack [ArrayList]

- Implements **List** interface with an array
- Similar to ArrayList
- Efficient only for stack operations [back]
- superceded by ArrayDeque
- get(), set() in O(1)
- add(), remove() in O(1 + n-i)
 - o good for write at the back

Stacks vs List

Stack	List
push(x)	add(n,x)
pop()	remove(n-1)
size()	size()
peek(x)	get(n-1)

List Interface

- get(i) / set(i,x)
 - Access element i, and return/replace it

- size()
 - o number of items in list
- add(i,x)
 - o insert new item x at position i
- remove(i)
 - o remove the element from position i

dereferencing: getting the address of a data item

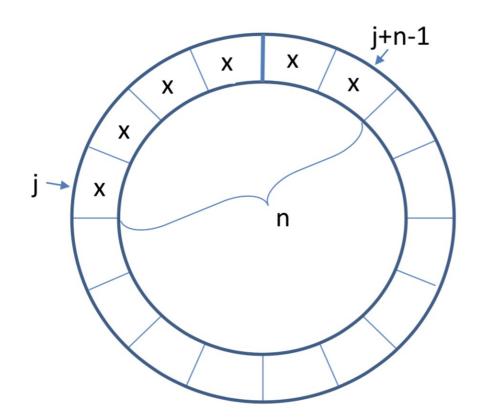
Amortized Cost

When an algorithm has processes that may be much longer but usually is quick, so you take the average. [roughly]

e.g. resizing an an array when adding/removing

ArrayQueue & ArrayDeque

Allow for efficient access at front and backs.



ArrayQueue

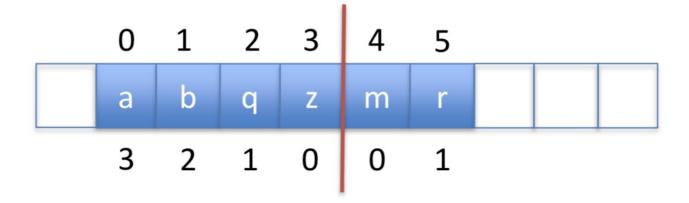
- Implements Queue and List interfaces with an array
- Cyclic array, (n: number of elements, j: 'index' of last element)
- get(), set() in O(1)
- add(), remove () in O(1 + min(i, n-i))
 - quick to write at front or back
 - cannot access anywhere else
- resize is O(n)

ArrayDeque

- Implements List interface with an array
- get(), set() in O(1)
- add(), remove() in O(1 + min(i, n-i))
 - quick to write at front or back
 - not so quick to access middle
- resize is O(n)

DualArrayDeque

- Implements List interface
- Uses two ArrayStacks front-to-front
- Since arrays are quick to add to the end, this makes front and back operations fast
- May be rebalanced if one array is much larger than the other
- Use Potential Function to decide when to rebalance
- get(), set() in O(1)
- add(), remove() in O(1 + min(i, n-i))
 - o quick to write at front or back, but not middle



Potential Function

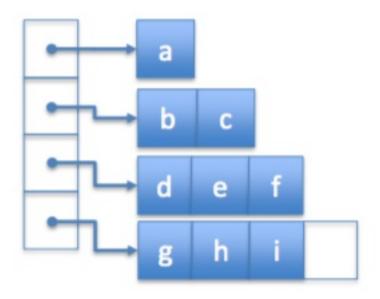
Define a potential function for the data structure to be the absolute difference of the sizes of the two stacks

P = | front_array.size - back_array.size |

 Adding or removing an element can only increase/decrease 1 to this function

RootishArrayStack

- Implements the **List** interface using multiple backing arrays
- Reduces 'wasted space' [unused space]
- At most: sqrt(n) unused array locations
- Good for space efficiency
- get(), set() in O(1)
- add(), remove() in O(1 + n-i)
 - quick to write at the back



Linked Lists

- Recursive data structure made up of nodes
- Pointers to head and tail, and each node points to the next node
- Efficient add/remove but slow read/write

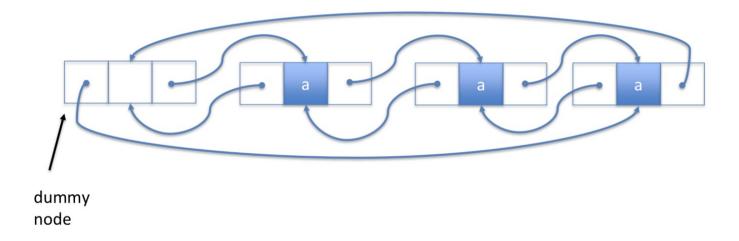
SLList [Singly-Linked List]

- Implements the Stack and Queue interfaces
- push(), pop() in O(1)
- add(), remove() in O(1)



DSList [Doubly-Linked List]

- Forward and backwards pointers at each node
- Implements the List interfaces
- get(), set() in O(1 + min(i, n-i))
- add(), remove() in O(1 + min(i, n-i))



SELList [Space-Efficient Linked List]

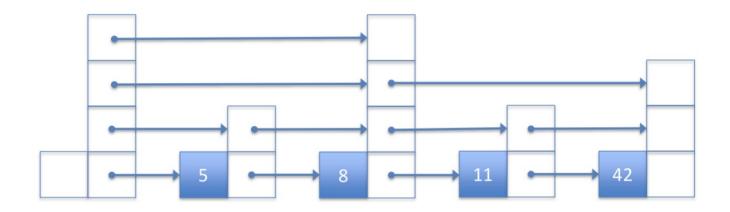
- Like a doubly-linked list, but uses block size b
- Is a series of **ArrayDeque** with *next* and *prev* pointers
- Implements the **List** interfaces
- get(), set() in O(1 + min(i, n-i)/b)
- add(), remove() in O(1 + min(i, n-i)/b)
 - o is quicker because you can skip blocks of data

Skiplist

- Like a singly-linked list, with 'skips'
- Randomly generated structure
- Faster searches than linked lists

SSet Interface

- Additional nodes with pointers that allow 'skipping'
- Successor search: find(x) will return smallest value ≥ x
- find(), add(), remove() in O(log n)



List Implementations

	get/set	add/remove
Arrays	O(1)	O(1 + min(i,n-i))
LinkedList	O(1 + min(i,n-i))	O(1)
Skiplist	O(log n)	O(log n)

^{*} given a pointer to a location

Definitions

Random variable: a random sample from a group of values

Expected value: average value of a random variable

Indicator variable: random variable with values of 0 or 1

Linearity of Expectation: the expected value of a sum is equal to the sum of expected values

Expected height of node [if coin flips were used]:

```
P(x = 1) = 1/2 // prob. that tails on first flip P(x = 2) = 1/4 // prob. that tails on second flip P(x = 3) = 1/8 // prob. that tails on third flip P(x = i) = 1/(2^i)
```

```
Thus,
E[x] = i*Sum(1/2^i) // for all natural numbers
E[x] = Sum(E[I j])
E[x] = Sum(P(I_j = i))
Indicator variable: 1 if tails, 0 is heads
P(I 1 = 1) = 1
P(I_2 = 1) = 1/2
P(I j = 1) = 1/(2^{(i-1)})
let S = Sum(P(x = i)) = 1 + 1/2 + 1/4 + ...
therefore,
S/2 = 1/2 + 1/4 + 1/8 + ...
S - S/2 = 1
=> S = 2
E[x] = Sum(P(I_j = i)) = S = 1 + 1/2 + 1/4 + ...
E[x] = 2
```

Expected number of elements in the skiplist:

```
h = # of levels in list
I_i = 1 if level is not empty, 0 if level empty
// expected value of sum of indicator(level not empty)
E[h] = E[Sum(I_i)] // from 0...infinity [no
max height]
E[h] = Sum(E[I_i])
I_i ≤ n_i // if level exists, less likely than number
of nodes
E[I_i] \le E[n_i] = n/(2^i)
// use log(n) since we know to prove O(log n)
E[h] = E[I_i] \{ from [0] to [log(n)] \}
      + E[ I_i ]{ from [log(n) + 1] to [infinity] }
E[h] = [log(n) + 1] + [1] // because math
E[h] = \log(n) + 2 \le \log(n) + 3
```

Average length of skiplist:

```
R_i = \# of horizontal steps at level \leq n_i l = Sum(R_i) E[R_i] \leq E[\# node height not promoted] E[R_i] \leq E[\# node height promoted] - 1 E[R_i] \leq S - 1  // S = 2 from above E[R_i] \leq 1 let sp = total length of search path <math>E[sp] = E[h] + E[l] E[sp] = (log(n) + 3) + E[Sum(R_i)]
```

```
\begin{split} \mathsf{E}[\mathsf{sp}] &= (\ \mathsf{log}(\mathsf{n}) \, + \, 3 \ ) \, + \, \mathsf{Sum}(\ \mathsf{E}[\ \mathsf{R}\_i\ ] \ ) \\ &= \{ (\ \mathsf{log}(\mathsf{n}) \, + \, 3 \ ) \\ &\quad + \, \mathsf{Sum}(1) \{ \ \mathsf{from}\ [\emptyset] \ \mathsf{to}\ [\mathsf{log}(\mathsf{n})] \ \} \\ &\quad + \, \mathsf{Sum}(\ \mathsf{E}[\ \mathsf{n}\_i\ ] \ ) \{ \ \mathsf{from}\ [\mathsf{log}(\mathsf{n}) \, + \, 1] \ \mathsf{to}\ \mathsf{n} \ \} \\ &= \{ (\ \mathsf{log}(\mathsf{n}) \, + \, 3 \ ) \\ &\quad + \, \mathsf{log}(\mathsf{n}) \\ &\quad + \, \mathsf{Sum}(\ \mathsf{n}/(2^{\mathsf{h}}i) \ ) \{ \ \mathsf{from}\ [\mathsf{log}(\mathsf{n}) \, + \, 1] \ \mathsf{to}\ \mathsf{n} \ \} \\ &= \{ \mathsf{log}(\mathsf{n}) \, + \, 6 \ \} \\ &= \{ \mathsf{log}(\mathsf{n}) \, + \, 0(1) \end{split}
```

HashTables

- Unordered sets with fast access
- Associative array
 - Index elements into a range of int
 - for non-integer elements, use hashCode()

Binary Trees

Nodes:

• Root: top-most node

• Internal: nodes that have children

• Leaf: nodes with no children

• External: null nodes [children of leaf nodes]

Definitions:

• Depth: distance from root

• level: set of nodes at same depth

height: largest depth for subtree at node

• size: number of nodes for subtree at node

How to calculate the size of a subtree [recursively]

```
int size(Node u) {
   if(u == null) return 0; // external node
   // add one each time, count this node
   return size(u.left) + size(u.right) + 1;
}
```

How to calculate the height of a subtree [recursively]

```
int height(Node u) {
    if(u == null) return -1; // external node went too
far
    // add one each time, count this node
    return max( height(u.left) + height(u.right) ) + 1;
}
```

How to calculate the depth of a node [recursively]

```
int depth(Node u) {
   if(u == null) return -1; // external node went too
far
   // add one each time, count this node
   return depth(u.parent) + 1;
}
```