

# Data Structure Summary

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A data structure is an implementation of an [abstract] interface.

- List
- Queue
- Stack
- Deque [double ended queue]
- Unordered Set [set]
- Sorted Set
- Map [set of key-value pairs]
- Sorted Map [sorted set of key-value pairs (kvp)]

## Access and Modification Characteristics

	get/set	add/remove
Arrays	$O(1)$	$O(1 + \min(i, n-i))$
LinkedList	$O(1 + \min(i, n-i))$	$O(1)^*$
Skiplist	$O(\log n)$	$O(\log n)$

\*given a pointer to the location, else traversal is necessary

## Set

Efficient for contains().

## SortedSet

Efficient for find().

- Does a successor search [closest value  $\geq$  to value]

## Maps

Efficient for contains() [kvp]

## SortedMap

Efficient for find() [kvp]

## Array-based

Efficient for read / write. Expensive insertion / deletion.

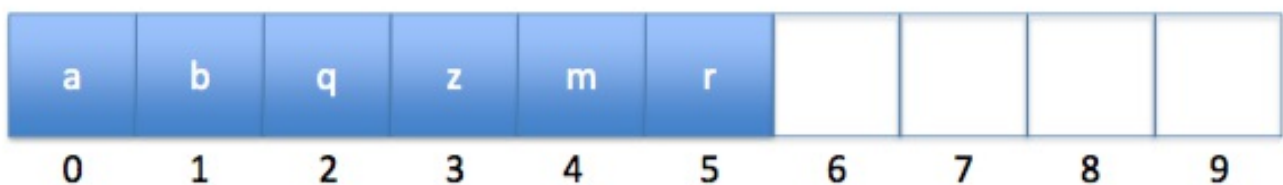
### ArrayList / ArrayStack

Efficient access anywhere. Efficient insertion / deletion at back [think stack].

- Implements **List** interface with an array
- superceded by ArrayDeque
- **get(), set() in  $O(1)$**
- **add(), remove() in  $O(1 + n-i)$**
- **resize is  $O(n)$  [amortized]**

// for  $m \geq 1$  add() / remove() calls, resize() will copy at most  $2m$

// the amortized cost of resize() for  $m$  calls is  $2m/m = O(1)$



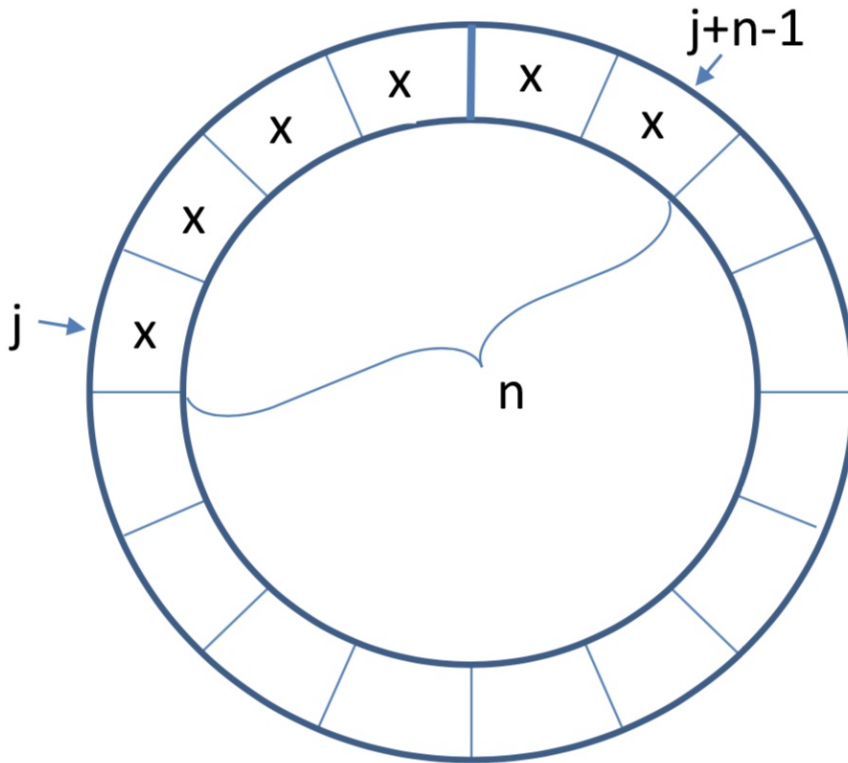
### ArrayQueue / ArrayDeque

Efficient access anywhere. Efficient insertion / deletion at front and back [think deque].

- Implements **List** interface with an array
- **get(), set() in  $O(1)$**

- **add(), remove()** in  $O(1 + \min(i, n-i))$
- **resize** is  $O(n)$  [amortized]

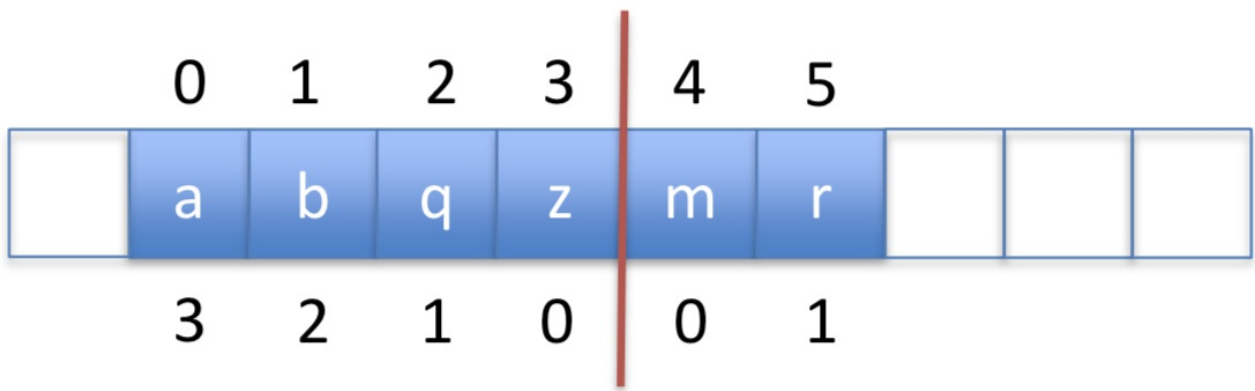
// since **ArrayQueue** only supports **addLast()** and **removeFirst()**, these are  $O(1)$



## DualArrayDeque

Efficient access anywhere. Efficient insertion / deletion at front and back [think deque].

- Implements **List** interface
- Uses two **ArrayStacks** front-to-front
- May be rebalanced if one array is much larger than the other
- **get(), set()** in  $O(1)$
- **add(), remove()** in  $O(1 + \min(i, n-i))$

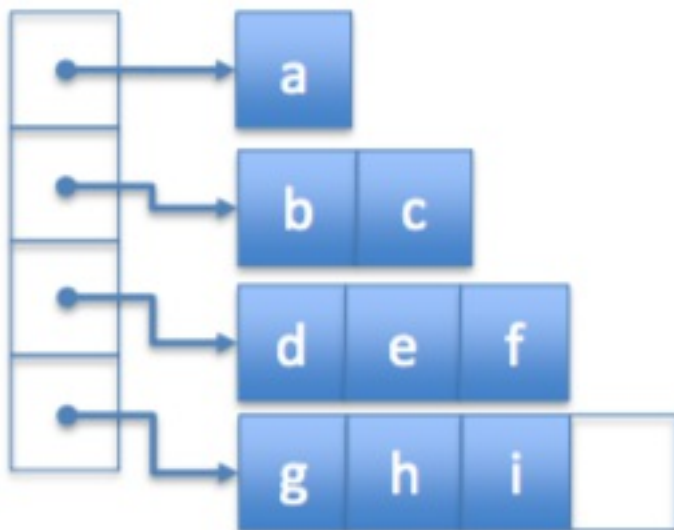


## RootishArrayStack

List of Lists, of increasing size. Efficient space [ $\sqrt{n}$ ] wasted space. Efficient access anywhere. Efficient insertion / deletion at back.

- Implements the **List** interface using multiple backing arrays
- Reduces 'wasted space' [unused space]
- At most:  $\sqrt{n}$  unused array locations
- Good for space efficiency
- **get(), set() in  $O(1)$**
- **add(), remove() in  $O(1 + \sqrt{n-i})$**

//  $m \geq 1$  add() / remove() calls, results on  $O(m)$  time on resize()



## Linked Lists

Efficient insertion / deletion. Expensive access.

## Singly Linked List [SLList]

Nodes with pointer to next node. Efficient insertion / deletion. Expensive access.

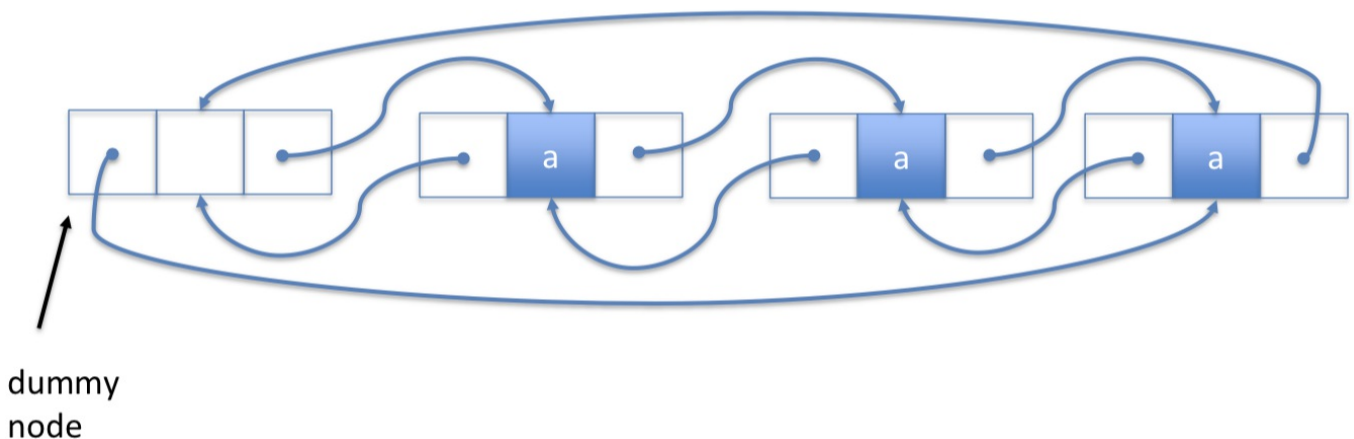
- Implements the Stack and Queue **interfaces**.
- **get(), set()** in  $O(1 + i)$
- **add(), remove()** in  $O(1)$



## Doubly Linked List [DLList]

Nodes with pointers to previous and next nodes. Efficient insertion / deletion. Expensive access.

- Implements the Stack and Queue **interfaces**.
- **get(), set()** in  $O(1 + \min(i, n-i))$
- **add(), remove()** in  $O(1 + \min(i, n-i))$



## SELList [Space-Efficient Linked List]

Nodes with pointers to previous and next nodes. Values stored as blocks in each node. [you can skip data] Efficient insertion / deletion. Expensive access.

- Implements the **List** interfaces

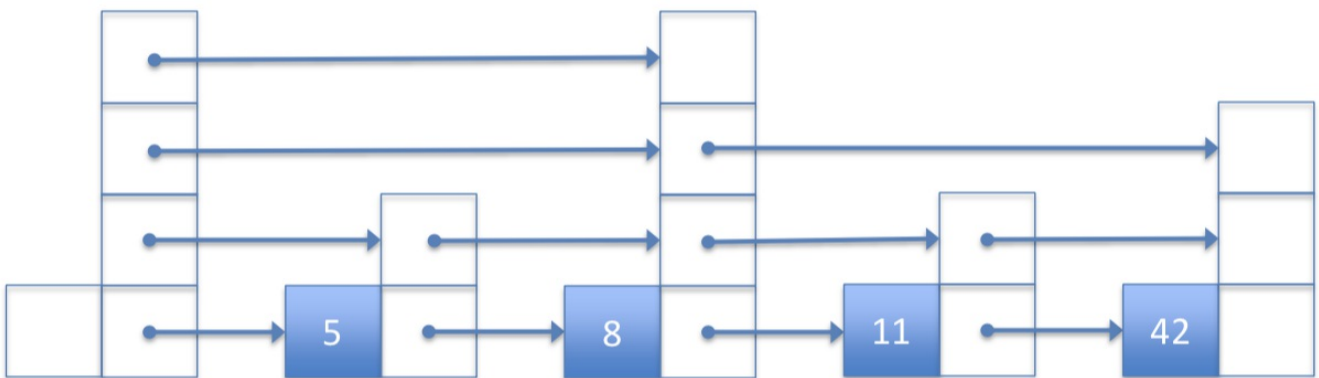
- wasted space:  $\{ n + O(b + n/b) \}$
- **get(), set()** in  $O(1 + \min(i, n-i)/b)$
- **add(), remove()** in  $O(1 + \min(i, n-i)/b)$

//  $m \geq 1$  add() / remove() calls, results in  $O(b \cdot m)$  time on **resize()**

## SkipLists

SLL with additional skipping pointers. Randomly generated structure. Allows for faster searches.

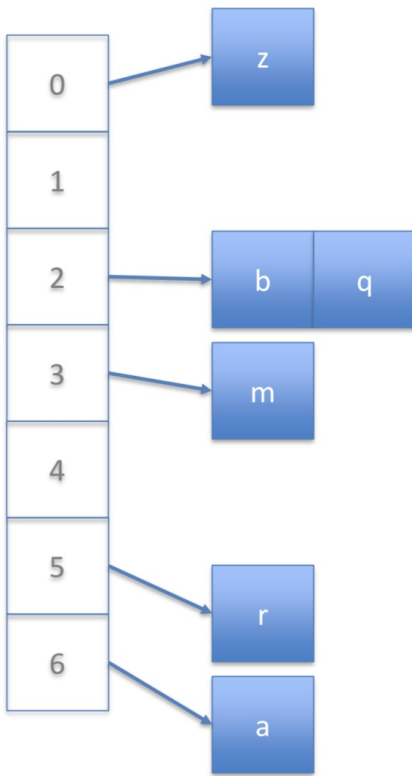
- Implements the **SortedSet** interface
- Successor search: **find(x)** will return **smallest value  $\geq x$**
- **get(), set()** in  $O(\log n)$
- **add(), remove()** in  $O(\log n)$



## After Midterm

## HashTable

- Unordered sets with fast access
- Associative array
  - Index elements into a range of int
  - for non-integer elements, use `hashCode()`



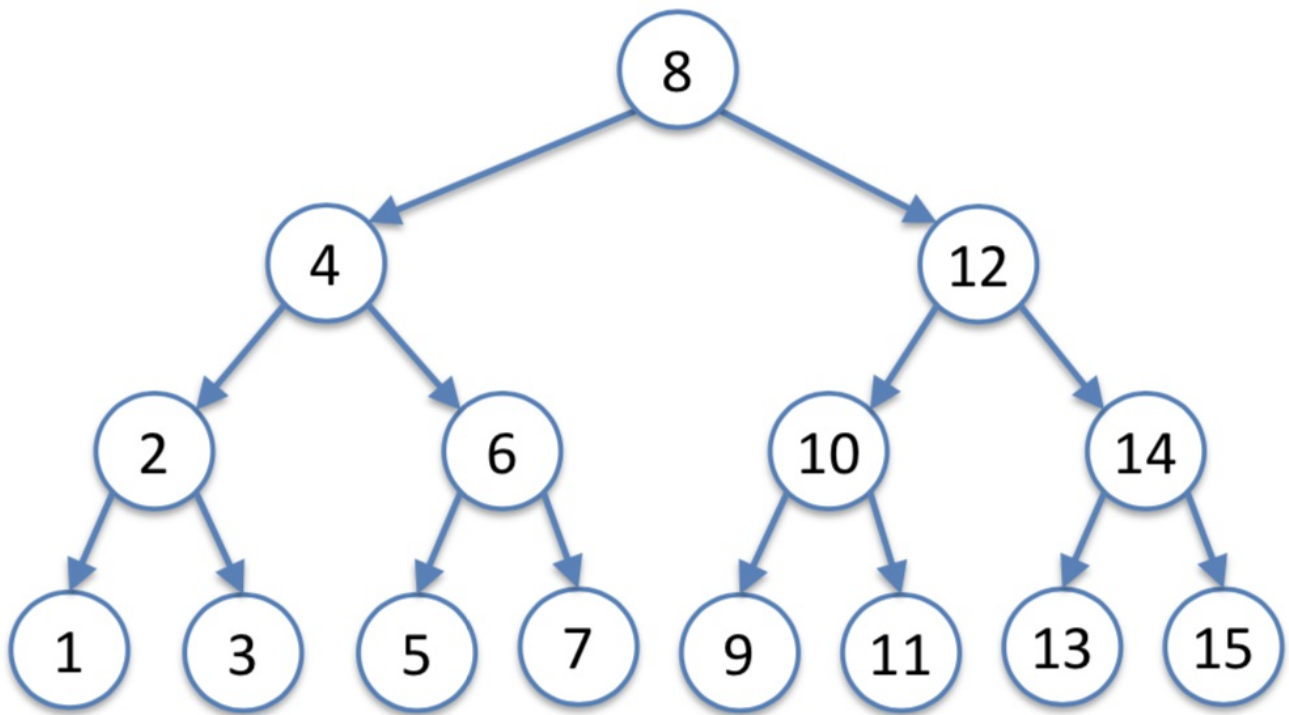
## ChainedHashTable

- Implements the **USet** interface
- **find(), add(), remove()** in  $O(n_i)$ 
  - where  $n_i$  is based of size of list at index

//  $m \geq 1$  add() / remove() calls, results in  $O(m)$  time on resize()

## Binary Tree

- Nodes with up to two child nodes



## BinarySearchTree

- Implements the **SSet** interface
- **find()**, **add()**, **remove()** in  $O(n)$

## Random Binary Search Trees

Balanced trees are statistically more likely

- Implements the **SSet** interface
- **constructed** in  $O(n \log n)$
- **add()**, **remove()** in  $O(n)$
- **find()** in  $O(\log n)$

// search path is at most  $2 \log(n) + O(1)$

## Treaps

**Has an extra priority:**

Parent priority should be less than child priority.

This has the property of bounding the height of the tree.

- Implements the **SSet** interface



- Priorities are randomly applied
- constructed in  $O(n \log n)$
- `find()`, `add()`, `remove()` in  $O(\log n)$

