Data Structure Summary

A data structure is an implementation of an [abstract] interface.

- List
- Queue
- Stack
- Deque [double ended queue]
- Unordered Set [set]
- Sorted Set
- Map [set of key-value pairs]
- Sorted Map [sorted set of key-value pairs (kvp)]

Access and Modifification Characteristics

	get/set	add/remove
Arrays	O(1)	O(1 + min(i,n-i))
LinkedList	O(1 + min(i,n-i))	O(1)*
Skiplist	O(log n)	O(log n)

*given a pointer to the location, else traversal is necessary

Set

Efficient for contains().

SortedSet

Efficient for find().

Does a successor search [closest value ≥ to value]

Maps

Efficient for contains() [kvp]

SortedMap

Efficient for find() [kvp]

Array-based

Efficient for read / write. Expensive insertion / deletion.

ArrayList / ArrayStack

Efficient access anywhere. Efficient insertion / deletion at back [think stack].

- Implements **List** interface with an array
- superceded by ArrayDeque
- get(), set() in O(1)
- add(), remove() in O(1 + n-i)
- resize is O(n) [amortized]

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// for m ≥ 1 add() / remove() calls, resize() will copy at
most 2m
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// the amortized cost of resize() for m calls is 2m/m = 0(1)

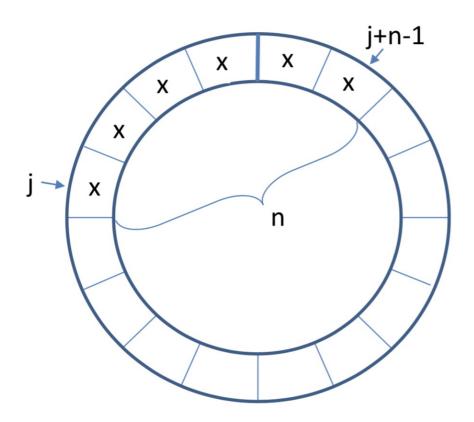


ArrayQueue / ArrayDeque

Efficient access anywhere. Efficient insertion / deletion at front and back [think deque].

- Implements **List** interface with an array
- get(), set() in O(1)
- add(), remove() in O(1 + min(i, n-i))
- resize is O(n) [amortized]

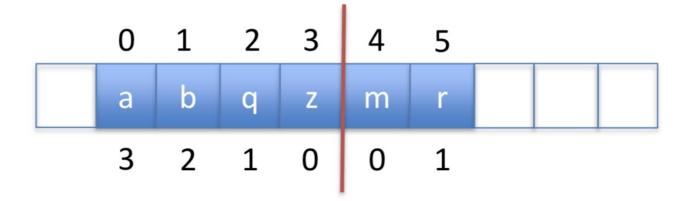
// since ArrayQueue only supports addLast() and
removeFirst(), these are 0(1)



DualArrayDeque

Efficient access anywhere. Efficient insertion / deletion at front and back [think deque].

- Implements List interface
- Uses two **ArrayStacks** front-to-front
- May be rebalanced if one array is much larger than the other
- get(), set() in O(1)
- add(), remove() in O(1 + min(i, n-i))

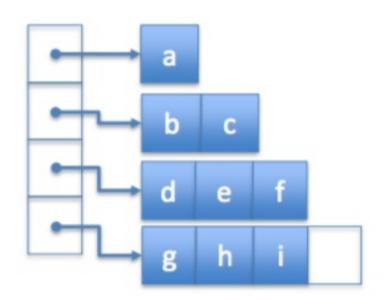


RootishArrayStack

List of Lists, of increasing size. Efficient space [sqrt(n) wasted space. Efficient access anywhere. Efficient insertion / deletion at back.

- Implements the **List** interface using multiple backing arrays
- Reduces 'wasted space' [unused space]
- At most: *sqrt(n)* unused array locations
- Good for space efficiency
- get(), set() in O(1)
- add(), remove() in O(1 + n-i)

// $m \ge 1$ add() / remove() calls, results on O(m) time on resize()



Linked Lists

Efficient insertion / deletion. Expensive access.

Singly Linked List [SLList]

Nodes with pointer to next node. Efficient insertion / deletion. Expensive access.

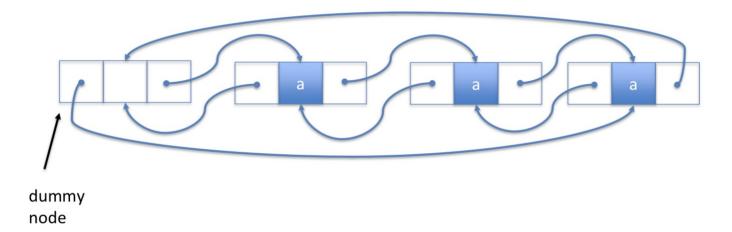
- Implements the Stack and Queue interfaces.
- get(), set() in O(1 + i)
- add(), remove() in O(1)



Doubly Linked List [DLList]

Nodes with pointers to previous and next nodes. Efficient insertion / deletion. Expensive access.

- Implements the Stack and Queue interfaces.
- get(), set() in O(1 + min(i, n-i))
- add(), remove() in O(1 + min(i, n-i))



SELList [Space-Efficient Linked List]

Nodes with pointers to previous and next nodes. Values stored as blocks in each node. [you can skip data] Efficient insertion / deletion. Expensive

access.

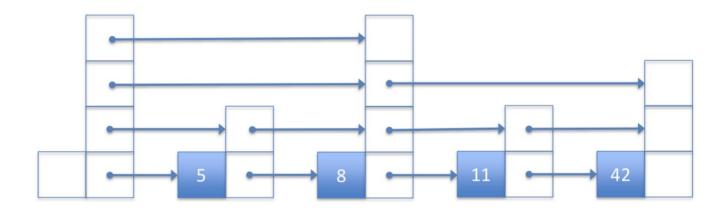
- Implements the List interfaces
- wasted space: $\{ n + O(b + n/b) \}$
- get(), set() in O(1 + min(i, n-i)/b)
- add(), remove() in O(1 + min(i, n-i)/b)

// $m \ge 1$ add() / remove() calls, results in $O(b \cdot m)$ time on resize()

SkipLists

SLL with additional skipping pointers. Randomly generated structure. Allows for faster searches.

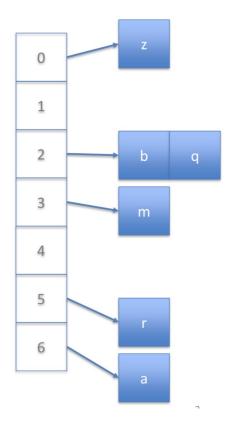
- Implements the **SortedSet** interface
- Successor search: find(x) will return smallest value ≥ x
- get(), set() in O(log n)
- add(), remove() in O(log n)



After Midterm

HashTable

- Unordered sets with fast access
- Associative array
 - o Index elements into a range of int
 - for non-integer elements, use hashCode()



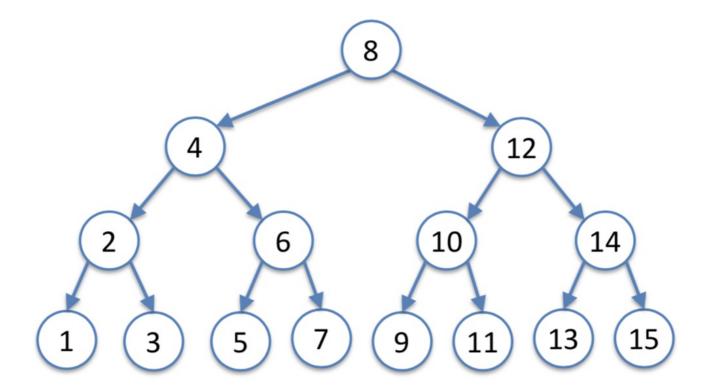
ChainedHashTable

- Implements the **USet** interface
- find(), add(), remove() in O(n_i)
 - where *n_i* is based of size of list at index

```
// m \ge 1 add() / remove() calls, results in O(m) time on resize()
```

Binary Tree

• Nodes with up to two child nodes



Binary Search Tree [BST]

- Implements the **SSet** interface
- find(), add(), remove() in O(n)

Random Binary Search Trees [RBST]

Balanced trees are statistically more likely

- Implements the SSet interface
- contructed in O(n•log(n))
- ** in O(n)**
- find(), add(), remove() in O(log n)

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// search path is at most 2•log(n) + 0(1)
```

Treaps

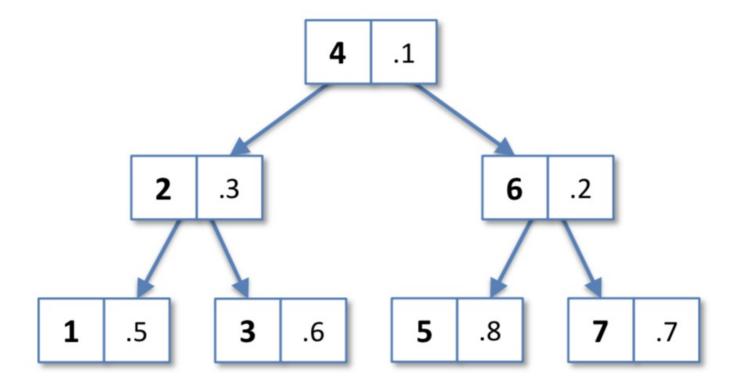
Has an extra priority:

Parent priority should be less than child priority.

This has the property of bounding the height of the tree.

• Implements the **SSet** interface

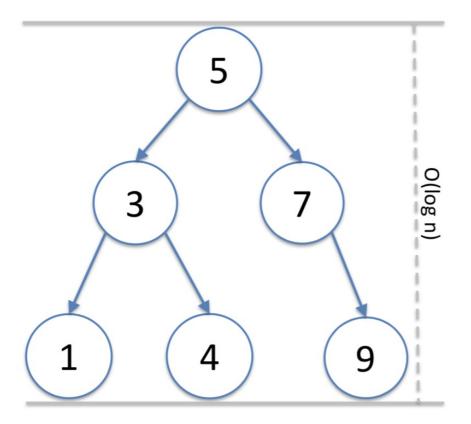
- Priorities are randomly applied
- contructed in O(n●log(n))
- find(), add(), remove() in O(log n)



Scapegoat Tree

BST that with height maintained within O(log n), rebuilt if too unbalanced. Limited with integer q, where height $\leq \log_{3/2}(q)$

- Implements the **SSet** interface
- Rebuild only one search path that triggered rebuild
 - this ensures that not entire tree is rebuilt
- rebuild() in O(log n) amortized
- find(), add(), remove() in O(log n)

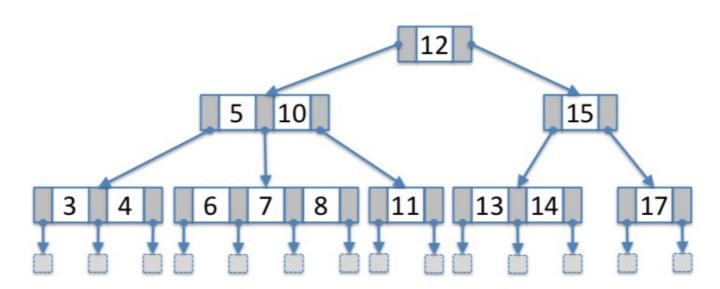


// m calls to add() / remove (), results in O(m•log(n) time
spent on rebuild()

2-4 Tree

Tree where every leaf has the same depth.

- Implements the **SSet** interface
- All leaves have equal depth
- All internal nodes have 2-4 children
- find(), add(), remove() in O(log n) [worst-case]



RedBlack Tree

A self-balancing binary search tree, built off a 2-4 Tree, where each node has a 'colour'.

- Implements the **SSet** interface
- Uses colour to remain balanced when adding / removing
 - There is the same number of black nodes on every root to leaf path
 - o i.e. equal sum of colours on any root to leaf path
- No red nodes can be adjacent
 - red nodes must have black parent
- left-leaning: if left node is black, then right node must be black
- Maximum height of 2•log(n)
- find(),add(), remove() in O(log n) [worst-case]

Binary Search Tree Implementations

	find()	add()	remove()
BST	O(n)	O(n)	O(n)
RBST / Treaps	<i>O(log n)</i>	<i>O(log n)</i>	<i>O(log n)</i>
	[expected]	[expected]	[expected]
Scapegoat	<i>O(log n)</i>	<i>O(log n)</i>	<i>O(log n)</i>
Trees	[amortized]	[amortized]	[amortized]
2-4 / RedBlack	O(log n)	O(log n)	O(log n) [worst-case]
Trees	[worst-case]	[worst-case]	

Sorted Set Implementations

	Runtime
Skiplists	O(log n) [expected]
Treaps	O(log n) [expected]

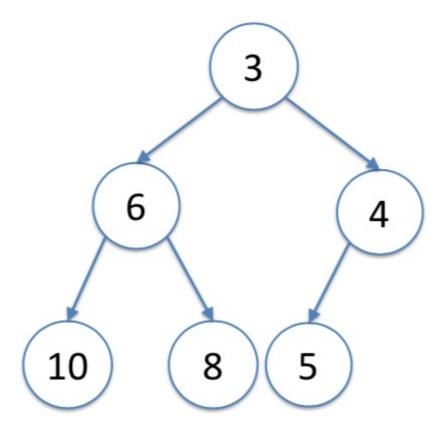
Scapegoat Trees	O(log n) [amortized]
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2-4 / **RedBlack Trees** *O(log n)* [worst-case]

Binary Heaps

A complete Binary Tree that also maintains the heap property.

- Implements the [priority] Queue Interface
- Allows to find / remove most extreme node with peek() / remove()
- add(), remove() in O(log n)
- peek() in O(1)



// $m \ge 1$ add() / remove() calls, results in O(m) time on resize()