Important declarations

Please remove this info from manuscript text if it is also present there.

Associated Data

Data supplied by the author:

All data, scripts and full results are available here: https://osf.io/my8pc/

Required Statements

Competing Interest statement:

The authors declare that they have no competing interests.

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Exact integer linear programming solvers outperform simulated annealing for solving conservation planning problems

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The resources available for conserving biodiversity are limited, and so protected areas need to be established in places that will achieve objectives for minimal cost. Two of the main algorithms for solving systematic conservation planning problems are Simulated Annealing (SA) and exact integer linear programming (EILP) solvers. Using a case study in British Columbia, Canada, we compare the cost-effectiveness and processing times of SA used in Marxan versus EILP using both commercial and open-source algorithms. Plans for expanding protected area systems based on EILP algorithms were 12 to 30% cheaper than plans using SA, due to EILP's ability to find optimal solutions as opposed to approximations. The best EILP solver we examined was on average 1071 times faster than the SA algorithm tested. The performance advantages of EILP solvers were also observed when we aimed for spatially compact solutions by including a boundary penalty. One practical advantage of using EILP over SA is that the analysis does not require calibration, saving even more time. Given the performance of EILP solvers, they can be used to generate conservation plans in real-time during stakeholder meetings and can facilitate rapid sensitivity analysis, and contribute to a more transparent, inclusive, and defensible decision-making process.

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Abstract

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integer linear programming (EILP) solvers. Using a case study in British Columbia, Canada, we
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decision-making process.



Introduction

Area-based systematic conservation planning aims to provide a rigorous, repeatable, and
structured approach for designing new protected areas that efficiently meet conservation
objectives (Margules and Pressey 2000). Historically, spatial conservation decision-making ofter
evaluated parcels opportunistically as they became available for purchase, donation, or under
threat (Pressey et al. 1993, Pressey and Bottrill 2008). Although purchasing such areas may
improve the status quo, such decisions may not substantially and cost-effectively enhance the
long-term persistence of species or communities (Joppa and Pfaff 2009, Venter et al. 2014).
Systematic conservation planning, on the other hand, is a multi-step process that involves
framing conservation planning problems as optimization problems with clearly defined
objectives (e.g. minimize acquisition cost) and constraints (Margules and Pressey 2000). These
optimization problems are then solved to obtain candidate reserve designs (termed solutions),
which are used to guide protected area acquisitions and land policy (Schwartz et al. 2018). Due
to the systematic, evidence-based nature of these tools, they can help contribute to a transparent,
inclusive, and more defensible decision-making process (Margules and Pressey 2000).
Today, Marxan is the most widely used systematic conservation planning software,
having been used in 184 countries to design marine and terrestrial reserve systems (Ball et al.
2009). Although Marxan supports several algorithms for solving conservation planning
problems, most conservation planning exercises use its implementation of simulated annealing
(SA), an iterative, stochastic metaheuristic algorithm for approximating global optima of
complex functions (Kirkpatrick et al. 1983). By conducting thousands of simulations to
determine the impact of different candidate solutions, Marxan aims to generate solutions that are
near-optimal. One of the reasons why Marxan uses SA instead of exact integer linear



programming (EILP) solvers, is that EILP solvers were historically not well suited to solve
problems with nonlinear constraints and penalties, such as problems trying to create spatially
compact or connected solutions (i.e. compactness and connectivity goals) and generally took
considerably longer than SA to solve problems (Sarkar et al. 2006, Haight and Snyder 2009).
However, the SA approach provides no guarantee on solution quality, and conservation scientists
and practitioners have no way of knowing how close to optimal their solutions are. In this case,
"optimal" refers to the configuration of protected areas that delivers the desired benefits and the
lowest cost. The discussion about the relative merits of linear programming versus heuristics
such as SA in conservation planning spans more than two decades (Cocks and Baird 1989,
Underhill 1994, Church et al. 1996, Rodrigues and Gaston 2002, Önal 2004), but the EILP
shortcomings mentioned above have largely been overcome in recent years (Beyer et al. 2016).
In a recent simulation study, Beyer et al. (2016) found that Marxan with simulated
annealing can deliver solutions that are orders of magnitude below optimality. They compared
Marxan to exact integer linear programming (EILP) (Wolsey and Nemhauser 1999), which
minimizes or maximizes an objective function (a mathematical equation describing the
relationship between actions and outcomes) subject to a set of constraints and conditional on the
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relationship between actions and outcomes) subject to a set of constraints and conditional on the
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relationship between actions and outcomes) subject to a set of constraints and conditional on the decision variables (the variables corresponding to the selection of actions to implement) being integers (Beyer et al. 2016). Unlike metaheuristic methods such as SA, prioritization using EILP will find the optimal solution or can be instructed to return solutions within a defined level of



the Marxan-like systematic conservation planning problems with EILP for large problems
 (Haight and Snyder 2009, Beyer et al. 2016).

Here we compare exact integer linear programming solvers with simulated annealing as used in Marxan, for solving minimum set systematic conservation planning problems (Rodrigues et al. 2000) using real-world data from Western North America. The goal of solving the minimum set problem is to find the places that maximize biodiversity, while minimizing reserve cost. We found that EILP generated high quality solutions 1,000 times faster than simulated annealing that could save over \$100 million (or 13%) for realistic conservation scenarios when compared to solutions obtained from simulated annealing. These results also hold true for problems aiming for spatially compact solutions. Our findings open up new possibilities for scenario generation to quickly explore and compare different conservation prioritization scenarios in real-time.

Material and Methods

91 Study area

We focused on a 27,250 km² portion of the Georgia Basin, Puget Trough and Willamette Valley of the Pacific Northwest region spanning the US and Canada, corresponding to the climate envelope indicative of the Coastal Douglas-fir (CDF) Biogeoclimatic zone in southwestern British Columbia (Meidinger and Pojar 1991) (Supplementary Information Figure S1). Land cover in the region is diverse, with approximately 57% of the land in forest, 8% as savanna or grassland, 5% in cropland, 10% being urban or built and the rest in wetland, water or barren.



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Biodiversity data.

We used species distribution models for 72 bird species as our conservation features at a 1-ha grid cell resolution (Supplementary Table 1). The distribution models were based on data from eBird, a citizen-science effort that has produced the largest and most rapidly growing biodiversity database in the world (Hochachka et al. 2012, Sullivan et al. 2014). From the 2013 eBird Reference Dataset (http://ebird.org/ebird/data/download) we used a total of 12,081 checklists in our study area, then filtered these checklists to retain only those from March – June to capture the breeding season, <1.5 hours in duration, <5 km travelled, and a maximum of 10 visits to a given location to improve model fit. Sampling locations <100 m apart were collapsed to one location, yielding 5,470 checklists from 2,160 locations, visited from 1-10 times and 2.53 times on average. The R package unmarked (version 0.9-9; Fiske and Chandler 2011) provided the framework for all species distribution models, which necessarily include two parts: occupancy and detection (Mackenzie et al. 2002). This form of distribution modelling, also known as occupancy modelling, uses the information from repeat visits to a site to infer estimates of detectability of a species as well as estimates of probability of occurrence. For further details on biodiversity data see (Rodewald et al. 2019).

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Property layer and land cost.

We incorporated spatial heterogeneity in land cost (Ando et al. 1998, Polasky et al. 2001, Ferraro 2003, Naidoo et al. 2006) in our plans by using property data and 2012 land value assessments from the Integrated Cadastral Information Society of British Columbia (BC). This process resulted in 193,623 properties for BC which were subsequently used as planning units (Schuster et al. 2014). Property data, including tax assessment land values from Washington





(https://depts.washington.edu/wagis/projects/parcels/; Version:

StatewideParcels_v2012n_e9.2_r1.3; Date accessed: 2015/04/30), as well as San Juan County
Parcel Data with separate signed user agreement. The combined property layer included 1.92
million polygons. Property data, including tax assessment land values from Oregon State had to
be sourced from individual counties, which included Benton, Clackamas, Columbia, Douglas,
Lane, Linn, Marion, Multnomah, Polk, Washington and Yamhill. The combined property layer
for Oregon included 605,425 polygons. We converted the polygon cost values to 1-ha raster cells
for consistency with the biodiversity data by calculating area weighted mean values of cost per
raster cell. Using tax assessment values as an estimate of conservation cost is an underestimate
because tax assessment values are often lower than market value, but estimates of market values
over larger areas are rarely available and tax assessments do provide a good general
approximation.

State came from the University of Washington's Washington State Parcel Database

Spatial prioritization

We compared EILP and SA for solving the minimum set spatial prioritization problem (Ball et al. 2009). In this formulation, the landscape is divided into a set of discrete planning units. Each planning unit is assigned a financial cost (here we use the assessed land value) and a conservation value for a set of features that we wish to protect (here the occupancy probability for a set of species). We also define representation targets for each species as the amount of habitat we hope to protect for that species. The goal of this prioritization problem is to optimize the trade-off between conservation benefit and financial cost (McIntosh et al. 2017). Achieving this goal involves finding the set of planning units that meets the conservation targets for the



minimum possible cost (i.e. min cost: such that conservation value ≥ target). Details on the Marxan problem formulation can be found in Ball et al. (2009) and the EILP formulation in Beyer et al. (2016) and SI Appendix S2. Three key parameters that are important for Marxan analysis, which we also use here are: species penalty factor, number of iterations, and number of restarts (Ardron et al. 2010). Briefly, the species penalty factor is the penalty given to a reserve system for not adequately representing a feature, the number of iterations determines how long the annealing algorithms will run, and the number of restarts determines how many different solutions Marxan will generate (for more details see SI Appendix S1). For all scenarios, we used 1 km² planning units, generated by aggregating the species and cost data to this coarser resolution from the original 1-ha cells. Aggregation was accomplished by taking the sum of cost data and the mean of species data for all 1-ha cells within the larger 1 km² cells.

EILP solvers (commercial vs open source)

A variety of EILP solvers currently exist, and both commercial and open source solvers are available. All solvers yield optimal solutions to EILP problems, but there are substantial differences in performance (i.e. time taken to solve a problem) and in the size of problems that can be solved (Lin et al. 2017). For the purposes of performance testing we opted for one of the best commercial solvers currently available, Gurobi (Gurobi Optimization Inc. 2017). In a recent benchmark study, Gurobi outperformed other solver packages for more complex formulations and a practical use-case (Luppold et al. 2018). To investigate solver performance of packages that are freely available to everyone, we also tested the open source solver SYMPHONY (Ralphs et al. 2019). Both Gurobi and SYMPHONY can be used from R. For Gurobi we used the R package provided with the software (Gurobi version 8.1-0) and for SYMPHONY the



Rsymphony package (version 0.1-28; Harter et al. 2017). We used the prioritizr R package to solve EILP problems for both Gurobi and SYMPHONY solvers (Hanson et al. 2019).

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Scenarios investigated

We investigated a range of scenarios that were computationally feasible for this study. For both Marxan and prioritzr we created the following range of scenarios: i) vary conservation targets between 10 and 90% protection of features in 10% increments (9 variations), using ii) 10 - 72 features (5 variations) as targets, and iii) with spatial extents of 9,282 planning units, 37,128 planning units, and 148,510 planning units (3 variations), resulting in a total of 135 scenarios created (Table 1). For Marxan, we also varied two additional parameters, i) the number of iterations ranged from 10⁴ to 10⁸ (5 variations) and ii) species penalty factors (SPF) of 1, 5, 25, and 125 were explored (4 variations, roughly spanning two orders of magnitude) for a total of 2,700 scenarios investigated in Marxan (Table 1). Exploring ranges of values for number of iterations and SPF is recommended for calibration of Marxan to increase its ability to approximate the optimal solution (Ardron et al. 2010). As the processing time for the most complex problem in Marxan (90% target, 72 features, 148,510 planning units, 108 iterations) was >8 hours, we restricted the full range of scenarios to those mentioned above. The maximum number of planning units we used is within the range of previous studies using Marxan (e.g. Venter et al. 2014; Runge et al. 2016), although using more than 50,000 planning units with SA is discouraged without extensive parameter calibration, as near optimal solutions will be hard to find for problems of that size (Ardron et al. 2010). To allow for a fair contrast between SA and EILP that focuses on algorithmic comparisons and not within SA variation, we focused our results and discussion on the best solution achieved with Marxan across 10 repeat runs.



As systematic conservation planners often aim for spatially compact solutions to their problems, we also investigated a range of scenarios using a term called boundary length modified (BLM), which is used to improve the clustering and compactness of a solution (McDonnell et al. 2002). We randomly selected a 225 x 225 pixel region of the study area to generate a problem with 50, 625 planning units, the maximum recommended for Marxan. After initial calibration we set the number of features/species to 72, SPF to 25 and number of iterations for Marxan to 10⁸. We varied targets between 10 and 90% protection of features in 10% increments, and used the following BLM values: 0.1; 1; 10; 100; 1,000 for a total of 45 scenarios. Both Marxan and prioritzr allow a user to specify BLM values as presented here. For details on the mathematical formulation of the spatial compactness constraint in ILP, please see SI Appendix S2 and (Beyer et al. (2016).

All analyses were conducted on a desktop computer with an Intel Core i7-7820X Processor and 128 GB RAM running Ubuntu 18.04 and R v 3.5.3. All data, scripts and full results are available online (https://osf.io/my8pc/) and will be archived in a persistent repository with a DOI pending acceptance of the manuscript.

Results

EILP algorithms (Gurobi, SYMPHONY) outperformed SA (Marxan) in terms of their ability to find minimal cost solutions across all scenarios that met conservation targets. Summarizing across calibrated Marxan scenarios (number of iterations > 100,000 and species penalty factor 5 or 25), the range of savings ranged from 0.8% to 52.5% (median 12.6%, SI Figure S2) when comparing EILP results to the best (cheapest) solution for a Marxan scenario. For example, at the 30% protection target EILP solvers resulted in solutions that were \$55





million cheaper than SA (Figure 1a), because the EILP solvers selected cheaper and fewer parcels in the optimal solution. With these savings an additional 961 ha could be protected (13,897 ha vs 12,936 ha) using an EILP algorithm by raising the representation targets until the cost of the resulting solution matched that of the Marxan solution using SA. In general, SA performed reasonably well at smaller problem sizes, fewer planning units and features and low targets, but as the problem size and complexity increased SA was less consistent in finding good solutions (SI Figure S2). Cost profiles across targets, number of features and number of planning units are shown in SI Figures S3-5.

The shortest processing times were achieved using the prioritizr package and the commercial solver Gurobi, followed by prioritizr and the open source solver SYMPHONY, and lastly Marxan (Figure 1b). Gurobi had the shortest processing times across all scenarios investigated, SYMPHONY tied with Gurobi in some scenarios and took up to 78 times longer than Gurobi in other scenarios (mean = 14 times, SI Figure S6), and Marxan took between 1.8 and 1995 times longer than Gurobi (mean = 281 times, SI Figure S7). The longest processing times for Gurobi, SYMPHONY and Marxan for a single scenario were 40 seconds, 31 minutes, and 8 hours respectively. For the most complex problem (i.e. targets = 90%, 72 features; 148,510 planning units), Marxan calibration across the 5 number of iterations and 4 species penalty factor values took a total of 5 days 7 hours, compared to 30 seconds using Gurobi and 28 minutes using SYMPHONY. Time profiles across targets, number of features and number of planning units are shown in SI Figures S8-10.

BLM to achieve more compact solutions. This was true for objective function values (Figure 2a)

EILP algorithms (Gurobi, SYMPHONY) also outperformed SA (Marxan) when using a



as well as for processing times (Figure 2b). Through finding optimal solutions, using EILP resulted in objective function values 5.65 to 149% (mean 22.7%) lower than SA values. Gurobi was the fastest solver to find solutions to problems including BLM in 44 of 45 scenarios, in one case SYMPHONY was faster. SYMPHONY outperformed Marxan in 44 of 45 scenarios, and took on average 13.7 times as long as Gurobi to find a solution (range -0.31 to 42.6). Marxan was never faster than Gurobi and took on average 104.6 times as long as Gurobi to find a solution (range 3.09 to 190.8). An example of the spatial representation of the solutions for a 10% target is shown in SI Figure S11.

Discussion

We found that EILP algorithms outperformed SA both in terms of cost-effectiveness and processing times, even when including linearized non-linear problem formulations, when planning for spatially compact solutions. There have been calls for using EILP in solving conservation planning problems in the past (Underhill 1994, Rodrigues and Gaston 2002), but we are now at a point where making this switch is both advisable and computationally feasible, where technical capacity exists. Our study provides a systematic test, using real world data to build on the findings of (Beyer et al. 2016), and shows that their results hold for a realistic case study. We further expanded the scope of testing to include assessed land values in order to give estimates of how much better optimal solution can perform in terms of cost savings, compared to SA solutions. Finally, we showcase that even open source EILP solvers are much faster than SA algorithms as implemented in Marxan, which is very encouraging for non-academic user that would otherwise have to buy Gurobi licenses (Gurobi is free for academic use). The combination of the superior performance findings by both (Beyer et al. 2016) and this study indicates that



EILP approaches should be strongly considered as improvements for minimum set conservation planning problems, currently solved using SA. This improvement is especially important in real world applications as the speed of generating solutions can be advantageous in iterative and dynamic planning processes that usually occur when planning for conservation (Sarkar et al. 2006). Given Marxan's flexibility to use optimization methods other than SA, we hope that a future version of Marxan will include EILP solvers.

One practical advantage of using EILP over SA is that the analysis does not require parameter calibration. Unlike EILP, parameter calibration is a crucial task in every Marxan/SA project and the species penalty factors, number of SA iterations, and number of SA restarts must be calibrated to improve solution quality (Ardron et al. 2010). This task can be very time consuming, especially for larger problems (e.g. 50,000 planning units). Ideally all possible combinations of parameters should be explored, but this further increases processing time. For instance, exploring three different parameter values would result in 27 different scenarios to explore (i.e. $3 \times 3 \times 3$). Although we omitted calibration runs prior to finalizing and presenting results in this study, the parameter calibration step took several days for the most complex problem we investigated in this study. Yet none of this calibration time is necessary using EILP. An added benefit is that the somewhat subjective process of setting values for these three parameters can be eliminated using EILP as well.

Recommended practices for Marxan analyses caution against using SA for conservation planning exercises with more than 50,000 planning units (Ardron et al. 2010). Such large-sized problems have occurred in the past and, as increasingly high resolution data become available, may become more common in the future (e.g. Venter et al. 2014; Runge et al. 2016). Unlike SA, EILP/prioritizr can solve problem sizes with more than one million planning units (Hanson 2018,



Schuster et al. 2019). Realistically, as problem sizes grow beyond what was intended for Marxan/SA projects, EILP will run into problems solving very large problems (>1 million planning units) that include non-linear constraints, such as optimizing compactness or connectivity, as those problem formulations need to be linearized for EILP to work. A potential future solution to this issue could be the use of nonlinear integer programming for more problems including non-linear constraints (Grossmann 2002, Lee and Leyffer 2011). Whether EILP would also outperform SA for more complex problem formulations, such as dynamic problems or problems with multiple objectives, still needs to be explored. Potential solutions would be to linearize the problem, or incorporate algorithms like Mixed Integer Quadratically Constrained Programming (Franco et al. 2014).

Finally, we argue that another strength of EILP solvers, especially Gurobi, is that they can be used to quickly explore and compare different conservation prioritization scenarios in real-time. This ability could be used to great advantage during stakeholder meetings, to explore various scenarios and undertake rapid sensitivity analysis.

Conclusion

EILP algorithms substantially outperform SA as used in minimum set systematic conservation planning, both in terms of solution cost, as well as in terms of time required to find near optimal or optimal solutions. Using an EILP algorithm, as implemented in the R package prioritizr, has the added benefit that users do not need to worry about or set parameters such as species penalty factors or number of iterations, which significantly reduces the time a user spends on finding suitable values for these parameters. Given the potential EILP is showing for





- 306 conservation planning, we recommend users consider adding this modified approach to solving
- 307 systematic conservation planning problems.





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(<u>https://osf.io/my8pc/</u>) and will be archived in a persistent repository with a DOI pending
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Table 1(on next page)

Scenarios investigated in our analysis

The total number of scenarios tested for both Gurobi and SYMPHONY are 135. For Marxan analysis, we included calibration steps as well, which brought the total number of scenarios to 2700 for that algorithm.



Parameter	Value range	variations	Scenarios
targets	10 - 90%	9	
# features	10, 26, 41, 56, 72	5	
# planning units	9,282, 37,128, 148,510	3	135 (ILP)
Marxan iterations	10^4 , 10^5 , 10^6 , 10^7 , 10^8	5	
Marxan SPF	1, 5, 25, 125	4	2,700 (SA)



Figure 1

Solution cost and time comparisons

a) The lines represent costs compared to the Gurobi cost baseline. The numbers on the blue line represent total cost of a solution in million \$ and the numbers on the green line represent how much more expensive, again in million \$, the SA/Marxan solution is compared to the ILP solutions. b) Time to solution comparisons between solvers. Marxan parameters used are: 72 features, 37,128 planning units, 10^7 iterations, using mean cost and time, across all Marxan runs that met their target for a given scenario (max = 10). Note that in a) gurobi (red) and Rsymphony (blue) yielded optimal solutions for all target values and so their lines are plotted exactly on top of each other.



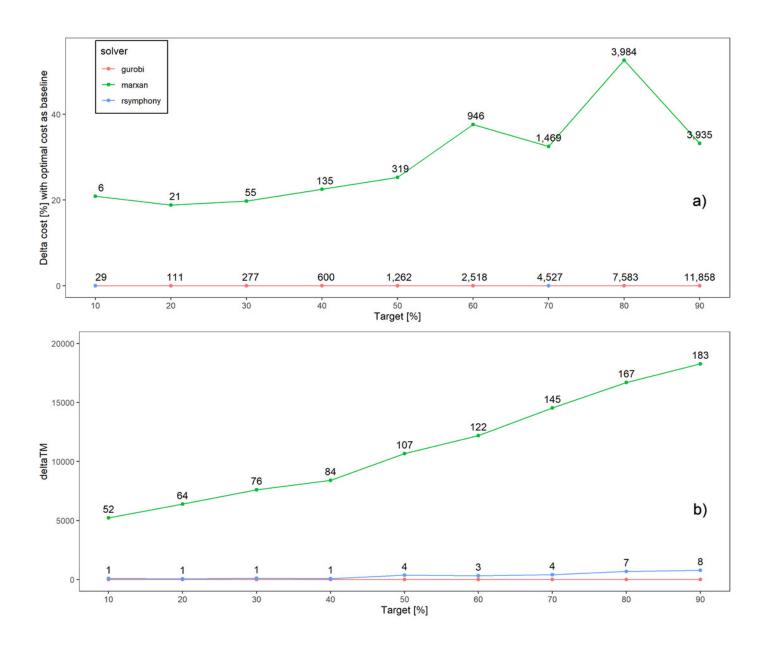




Figure 2

Objective function value and time comparisons using a boundary penalty to achieve spatially compact solutions

a) Deviation from lowest objective function value for solvers used and over a range of boundary penalty or boundary length modifier values (BLM); zero deviation indicates optimal solution. b) Time to solution comparisons between solvers and across BLM values. Note that in a) gurobi (red) and Rsymphony (blue) yielded optimal solutions for all target values and so their lines are plotted exactly on top of each other.



