

The following is the original dataset downloaded from the UCI Repository:

Modified Dataset:

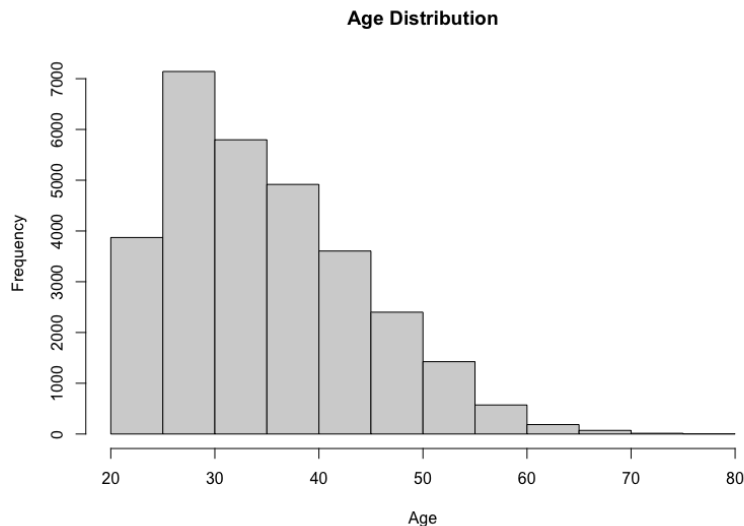
- [illegible]

Summary Statistics Table:

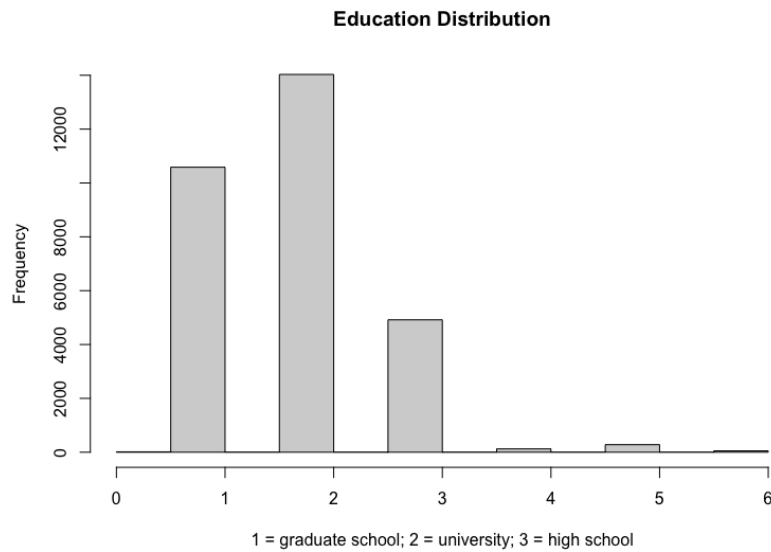
ID	LIMIT_BAL	SEX	EDUCATION	MARRIAGE	AGE
Min. : 1	Min. : 10000	Min. : 1.000	Min. : 0.000	Min. : 0.000	Min. : 21.00
1st Qu.: 7501	1st Qu.: 50000	1st Qu.: 1.000	1st Qu.: 1.000	1st Qu.: 1.000	1st Qu.: 28.00
Median : 15000	Median : 140000	Median : 2.000	Median : 2.000	Median : 2.000	Median : 34.00
Mean : 15000	Mean : 167484	Mean : 1.604	Mean : 1.853	Mean : 1.552	Mean : 35.49
3rd Qu.: 22500	3rd Qu.: 240000	3rd Qu.: 2.000	3rd Qu.: 2.000	3rd Qu.: 2.000	3rd Qu.: 41.00
Max. : 30000	Max. : 1000000	Max. : 2.000	Max. : 6.000	Max. : 3.000	Max. : 79.00
PAY_0	PAY_2	PAY_3	PAY_4	PAY_5	PAY_6
Min. : -2.0000	Min. : -2.0000	Min. : -2.0000	Min. : -2.0000	Min. : -2.0000	Min. : -2.0000
1st Qu.: -1.0000	1st Qu.: -1.0000	1st Qu.: -1.0000	1st Qu.: -1.0000	1st Qu.: -1.0000	1st Qu.: -1.0000
Median : 0.0000	Median : 0.0000	Median : 0.0000	Median : 0.0000	Median : 0.0000	Median : 0.0000
Mean : -0.0167	Mean : -0.1338	Mean : -0.1662	Mean : -0.2207	Mean : -0.2662	Mean : -0.2911
3rd Qu.: 0.0000	3rd Qu.: 0.0000	3rd Qu.: 0.0000	3rd Qu.: 0.0000	3rd Qu.: 0.0000	3rd Qu.: 0.0000
Max. : 8.0000	Max. : 8.0000	Max. : 8.0000	Max. : 8.0000	Max. : 8.0000	Max. : 8.0000
BILL_AMT1	BILL_AMT2	BILL_AMT3	BILL_AMT4	BILL_AMT5	BILL_AMT6
Min. : -165580	Min. : -69777	Min. : -157264	Min. : -170000	Min. : -81334	Min. : -339603
1st Qu.: 3559	1st Qu.: 2985	1st Qu.: 2666	1st Qu.: 2327	1st Qu.: 1763	1st Qu.: 1256
Median : 22382	Median : 21200	Median : 20088	Median : 19052	Median : 18104	Median : 17071
Mean : 51223	Mean : 49179	Mean : 47013	Mean : 43263	Mean : 40311	Mean : 38872
3rd Qu.: 67091	3rd Qu.: 64006	3rd Qu.: 60165	3rd Qu.: 54506	3rd Qu.: 50190	3rd Qu.: 49198
Max. : 964511	Max. : 983931	Max. : 1664089	Max. : 891586	Max. : 927171	Max. : 961664
PAY_AMT1	PAY_AMT2	PAY_AMT3	PAY_AMT4	PAY_AMT5	PAY_AMT6
Min. : 0	Min. : 0	Min. : 0	Min. : 0	Min. : 0.0	Min. : 0.0
1st Qu.: 1000	1st Qu.: 833	1st Qu.: 390	1st Qu.: 296	1st Qu.: 252.5	1st Qu.: 117.8
Median : 2100	Median : 2009	Median : 1800	Median : 1500	Median : 1500.0	Median : 1500.0
Mean : 5664	Mean : 5921	Mean : 5226	Mean : 4826	Mean : 4799.4	Mean : 5215.5
3rd Qu.: 5006	3rd Qu.: 5000	3rd Qu.: 4505	3rd Qu.: 4013	3rd Qu.: 4031.5	3rd Qu.: 4000.0
Max. : 873552	Max. : 1684259	Max. : 896040	Max. : 621000	Max. : 426529.0	Max. : 528666.0
default.payment.next.month					
Min. : 0.0000					
1st Qu.: 0.0000					
Median : 0.0000					
Mean : 0.2212					
3rd Qu.: 0.0000					
Max. : 1.0000					

Exploratory Data Analysis

1. Since the variables for Sex, Education, and Marriage are numeric, there is no need for factorization and the variables can be used in the regression models directly.
2. We check for missing values using `any_missing <- any(is.na(d))` and it outputs FALSE. Which means there are no missing values in the dataset.
3. Plotting a histogram to understand age distribution of credit card clients.



4. Plotting a graph to understand the distribution of the level of education.



Choosing predictor variables:

LIMIT_BAL: Credit card limit balance tells how likely people are to default, as clients with higher credit limits might be more likely.

EDUCATION: Education level can also be a crucial factor. Higher education level might correlate with lower default rates.

AGE: Age can also be an important factor since younger individuals might default more while older clients can have lower default rates with experience.

PAY_0 to PAY_6: These variables are repayment status numbered by month. They can be a strong predictor since clients with a greater number of delayed months or consistently delayed payments can be more likely to default.

BILL_AMT1 to BILL_AMT6: Higher bill amount can lead to more chances of default since it means higher financial stress. Hence it is a strong predictor too.

PAY_AMT1 to PAY_AMT6: Monthly payment amounts can also talk strongly about the possibility of default for a client. If the client has had consistently low payments or shows a trend of decreasing monthly payment amounts, they have higher chances of default.

Thus, the above variables will be used in the models.

Logit Regression

Summary:

```
Coefficients:
              Estimate Std. Error z value Pr(>|z|)
(Intercept) -1.253e+00  6.694e-02 -18.725 < 2e-16 ***
LIMIT_BAL   -7.163e-07  1.560e-07  -4.592 4.39e-06 ***
EDUCATION    -9.491e-02  2.080e-02  -4.564 5.03e-06 ***
AGE          1.128e-02  1.629e-03   6.924 4.38e-12 ***
PAY_0        5.779e-01  1.768e-02  32.681 < 2e-16 ***
PAY_2        8.548e-02  2.016e-02   4.239 2.25e-05 ***
PAY_3        7.247e-02  2.258e-02   3.209 0.00133 **
PAY_4        2.419e-02  2.499e-02   0.968 0.33305
PAY_5        3.500e-02  2.687e-02   1.303 0.19260
PAY_6        7.074e-03  2.212e-02   0.320 0.74912
BILL_AMT1    -5.475e-06  1.136e-06  -4.817 1.46e-06 ***
BILL_AMT2    2.388e-06  1.501e-06   1.590 0.11177
BILL_AMT3    1.324e-06  1.322e-06   1.002 0.31654
BILL_AMT4   -1.832e-07  1.350e-06  -0.136 0.89208
BILL_AMT5    6.161e-07  1.518e-06   0.406 0.68488
BILL_AMT6    3.715e-07  1.192e-06   0.312 0.75534
PAY_AMT1    -1.363e-05  2.306e-06  -5.912 3.38e-09 ***
PAY_AMT2    -9.612e-06  2.098e-06  -4.580 4.64e-06 ***
PAY_AMT3    -2.755e-06  1.726e-06  -1.596 0.11045
PAY_AMT4    -4.013e-06  1.790e-06  -2.243 0.02493 *
PAY_AMT5    -3.415e-06  1.777e-06  -1.921 0.05469 .
PAY_AMT6    -2.101e-06  1.300e-06  -1.616 0.10602
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 31705  on 29999  degrees of freedom
Residual deviance: 27911  on 29978  degrees of freedom
AIC: 27955

Number of Fisher Scoring iterations: 6
```

According to the logistic regression summary, coefficients like LIMIT_BAL, EDUCATION, AGE, payment history (PAY_0, PAY_2) bill amount for first month (BILL_AMT1) and payment amounts for first two months (PAY_AMT1, PAY_AMT2) are significant. AIC Score is 27955, which is reasonable for the model.

Marginal Effects Analysis:

```
Marginal Effects:
              df/dx   Std. Err.      z    P>|z|
LIMIT_BAL -1.0932e-07 2.3760e-08 -4.6010 4.204e-06 ***
EDUCATION -1.4485e-02 3.1721e-03 -4.5663 4.964e-06 ***
AGE        1.7208e-03 2.4856e-04  6.9232 4.415e-12 ***
PAY_0      8.8185e-02 2.6838e-03 32.8579 < 2.2e-16 ***
PAY_2      1.3044e-02 3.0812e-03  4.2334 2.301e-05 ***
PAY_3      1.1059e-02 3.4464e-03  3.2090 0.001332 **
PAY_4      3.6913e-03 3.8132e-03  0.9680 0.333035
PAY_5      5.3420e-03 4.1002e-03  1.3029 0.192623
PAY_6      1.0796e-03 3.3759e-03  0.3198 0.749119
BILL_AMT1 -8.3547e-07 1.7311e-07 -4.8261 1.392e-06 ***
BILL_AMT2  3.6436e-07 2.2900e-07  1.5911 0.111593
BILL_AMT3  2.0213e-07 2.0178e-07  1.0017 0.316475
BILL_AMT4 -2.7960e-08 2.0607e-07 -0.1357 0.892076
BILL_AMT5  9.4024e-08 2.3169e-07  0.4058 0.684871
BILL_AMT6  5.6695e-08 1.8194e-07  0.3116 0.755335
PAY_AMT1 -2.0807e-06 3.4951e-07 -5.9533 2.627e-09 ***
PAY_AMT2 -1.4668e-06 3.1852e-07 -4.6050 4.125e-06 ***
PAY_AMT3 -4.2040e-07 2.6325e-07 -1.5970 0.110275
PAY_AMT4 -6.1243e-07 2.7290e-07 -2.2442 0.024821 *
PAY_AMT5 -5.2115e-07 2.7111e-07 -1.9223 0.054571 .
PAY_AMT6 -3.2056e-07 1.9822e-07 -1.6172 0.105840
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

df/dx represents marginal effects or the change in probability for default.

According to the marginal effects table, the significant variables have the following interpretation:

1. LIMIT_BAL: Decrease in credit limit balance shows increase in default probability.
2. EDUCATION: Lower level of education indicates increase in default probability.
3. AGE: Higher clients have slightly higher probability of default
4. PAY_0 to PAY_3: Higher chances of default for payments that are more delayed.
5. BILL_AMT1: Higher billing amounts are associated with higher probability of default in next month.
6. PAY_AMT1, PAY_AMT2, PAY_AMT4, PAY_AMT5: Higher pay amounts can show a decrease in the probability of default whereas lower can indicate higher default probability.

Probit Regression

Summary:

```

Coefficients:
      Estimate Std. Error z value Pr(>|z|)
(Intercept) -7.649e-01  3.804e-02 -20.108 < 2e-16 ***
LIMIT_BAL   -3.907e-07  8.600e-08  -4.543 5.56e-06 ***
EDUCATION    -5.195e-02  1.166e-02  -4.457 8.29e-06 ***
AGE          6.706e-03  9.340e-04   7.180 6.99e-13 ***
PAY_0        3.120e-01  1.017e-02  30.675 < 2e-16 ***
PAY_2        5.183e-02  1.184e-02   4.378 1.20e-05 ***
PAY_3        3.891e-02  1.303e-02   2.986 0.00283 **
PAY_4        1.113e-02  1.445e-02   0.770 0.44109
PAY_5        2.026e-02  1.560e-02   1.298 0.19417
PAY_6        3.086e-03  1.281e-02   0.241 0.80970
BILL_AMT1    -2.612e-06  5.709e-07  -4.575 4.76e-06 ***
BILL_AMT2     9.157e-07  7.765e-07   1.179 0.23828
BILL_AMT3     5.731e-07  7.071e-07   0.811 0.41761
BILL_AMT4     3.304e-08  7.218e-07   0.046 0.96350
BILL_AMT5     2.744e-07  8.120e-07   0.338 0.73538
BILL_AMT6     6.350e-08  6.355e-07   0.100 0.92041
PAY_AMT1     -6.204e-06  1.093e-06  -5.676 1.38e-08 ***
PAY_AMT2    -4.207e-06  9.913e-07  -4.244 2.19e-05 ***
PAY_AMT3    -1.454e-06  8.825e-07  -1.647 0.09954 .
PAY_AMT4    -1.774e-06  9.029e-07  -1.965 0.04940 *
PAY_AMT5    -1.452e-06  9.057e-07  -1.603 0.10891
PAY_AMT6    -8.820e-07  6.595e-07  -1.337 0.18110
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

(Dispersion parameter for binomial family taken to be 1)

    Null deviance: 31705  on 29999  degrees of freedom
Residual deviance: 28113  on 29978  degrees of freedom
AIC: 28157

Number of Fisher Scoring iterations: 6

```

Coefficients like LIMIT_BAL, EDUCATION, AGE, payment history (PAY_0, PAY_2) bill amount for first month (BILL_AMT1) and payment amounts for first two months (PAY_AMT1, PAY_AMT2) are highly significant here too, as in logit.

AIC Score is 28157, which is greater than logit.

Marginal Effects:

```

Marginal Effects:
      dF/dx   Std. Err.      z    P>|z|
LIMIT_BAL -1.0854e-07 2.3876e-08 -4.5460 5.468e-06 ***
EDUCATION -1.4435e-02 3.2375e-03 -4.4586 8.251e-06 ***
AGE        1.8631e-03 2.5954e-04 7.1786 7.045e-13 ***
PAY_0      8.6682e-02 2.8238e-03 30.6968 < 2.2e-16 ***
PAY_2      1.4401e-02 3.2913e-03 4.3754 1.212e-05 ***
PAY_3      1.0811e-02 3.6209e-03 2.9858 0.002829 **
PAY_4      3.0934e-03 4.0156e-03 0.7704 0.441088
PAY_5      5.6275e-03 4.3344e-03 1.2983 0.194174
PAY_6      8.5732e-04 3.5601e-03 0.2408 0.809701
BILL_AMT1 -7.2563e-07 1.5849e-07 -4.5785 4.684e-06 ***
BILL_AMT2 2.5442e-07 2.1571e-07 1.1795 0.238215
BILL_AMT3 1.5924e-07 1.9644e-07 0.8106 0.417591
BILL_AMT4 9.1784e-09 2.0054e-07 0.0458 0.963495
BILL_AMT5 7.6244e-08 2.2559e-07 0.3380 0.735377
BILL_AMT6 1.7643e-08 1.7657e-07 0.0999 0.920405
PAY_AMT1 -1.7237e-06 3.0274e-07 -5.6936 1.244e-08 ***
PAY_AMT2 -1.1689e-06 2.7479e-07 -4.2538 2.102e-05 ***
PAY_AMT3 -4.0385e-07 2.4513e-07 -1.6475 0.099455 .
PAY_AMT4 -4.9298e-07 2.5080e-07 -1.9656 0.049341 *
PAY_AMT5 -4.0341e-07 2.5160e-07 -1.6034 0.108855
PAY_AMT6 -2.4504e-07 1.8319e-07 -1.3376 0.181016
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

The marginal effects for probit is very similar to logit. Positive value represents an increase in the probability of default (for example PAY_0 to PAY_6).

Prediction Model:

Dataset size = 30000

Predictors = 21

Cross validation number of folds = 5

tune length = 10

1. **KNN Model:** It gives an accuracy of 77.74% with the final value of k = 23.

k-Nearest Neighbors

```

30000 samples
 21 predictor
 2 classes: '0', '1'

```

No pre-processing

Resampling: Cross-Validated (5 fold)

Summary of sample sizes: 24000, 24000, 24000, 24000, 24000

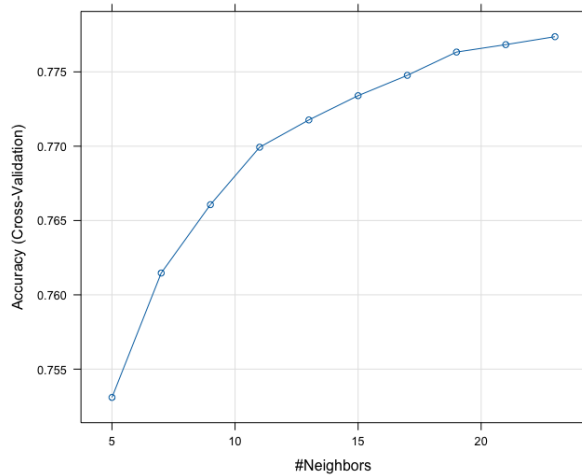
Resampling results across tuning parameters:

k	Accuracy	Kappa
5	0.7531000	0.11605658
7	0.7614667	0.11173715
9	0.7660667	0.10847952
11	0.7699333	0.10798225
13	0.7717667	0.10205788
15	0.7734000	0.10084118
17	0.7747667	0.09925668
19	0.7763333	0.09844912
21	0.7768333	0.09391628
23	0.7773667	0.09114417

Accuracy was used to select the optimal model using the largest value.

The final value used for the model was k = 23.

Plotting accuracy vs number of neighbors



2. **Naïve Bayes Model:** It gives an accuracy of 79.56% and the optimal model is chosen with `laplace = 0`, `usekernel = TRUE` and `adjust = 1`.

Naive Bayes

30000 samples
 21 predictor
 2 classes: '0', '1'

No pre-processing

Resampling: Cross-Validated (5 fold)

Summary of sample sizes: 23999, 24001, 24000, 24000, 24000

Resampling results across tuning parameters:

usekernel	Accuracy	Kappa
FALSE	0.7098011	0.3106027
TRUE	0.7956000	0.1835265

Tuning parameter 'laplace' was held constant at a value of 0

Tuning parameter 'adjust' was
 held constant at a value of 1

Accuracy was used to select the optimal model using the largest value.

The final values used for the model were `laplace = 0`, `usekernel = TRUE` and `adjust = 1`.

Thus, based on the accuracy, Naïve Bayes will be the optimal model for predicting default for credit card clients.