THE LOAD UP TO NOW ...

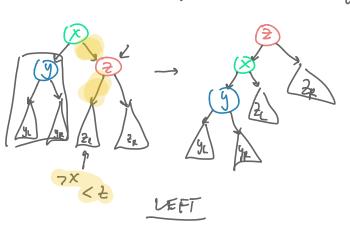
- Recursive data structures (Linked List, Trees)
- Operations on data structures + Time complexity (Search for number in tree? O(logn))

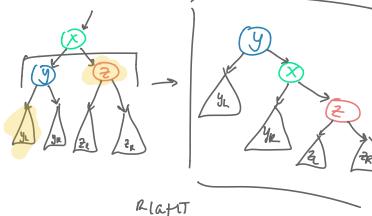
rotalek (The Nocle -L)

SOME RASIC PLIMITIVES: Potation.

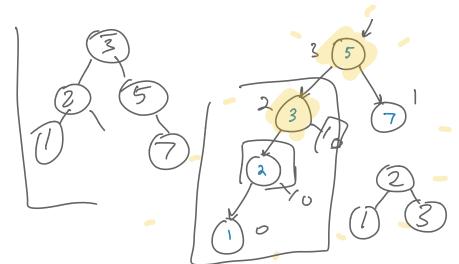
auAL- reorganise he tree whilst maintaining the search tree condition, FAST - 0(1)

VARIANTS - left notation and right notation.





Constant number of pointers change in each notation => CONSTANT TIME. USEFUCNESS? - One side is taller han he oher, notate in apposition!



MEGHT balance me tree.

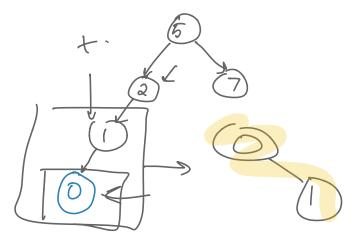
 $|h_L - h_R| \leq 1$

YOU KNOW: INSERT AT LEAF

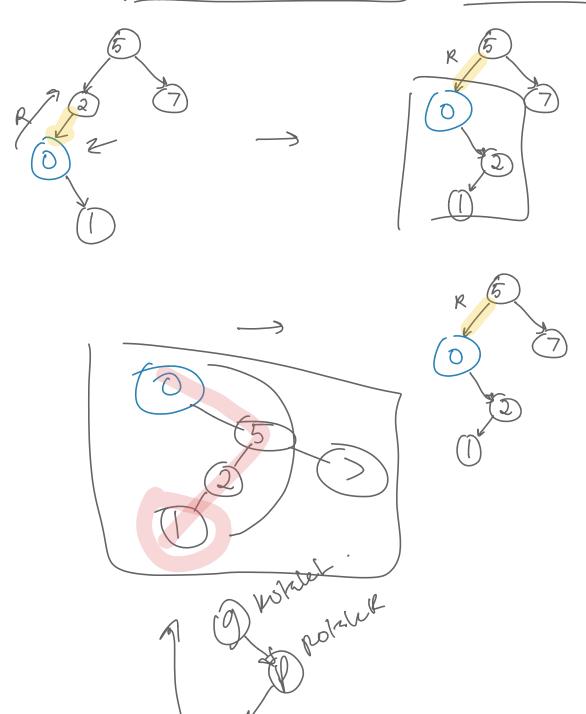
as a luf following BST condition.

INSERTAT KOOT:

1 INSERT VALUE AT LEAF.



(2) kotate in opposition to what side you recured on e.g (+ - left = insert (v,1 - left) => ROTATE RIGHT!



Same inversion netwood as insurtion at voot.

EXCEPT!



(1) Rotate right on g node (notates on g-sp edge)

THEN

1 Rotate right on p node (rotates on p -> x edge)

What would an invertion at noot do?

WE CALL THIS MODIFIED VEKSION OF AMENDING THE TREE THE SPLAY OPERATION.

On insertion of a value -> inext at leas -> perform SPLAY.

On finding a node -> perform SPLAY to closest tayet.



VS

- Localit "non livery"
 to search again.
- O (logn) "amortized" time.
- Not all cases you get he scauch for all under in a scenery.

AUGMENTING DATA STRUCTURES

Adding some EXTRA data on an existing structure for efficient implementation of ops. e.g. POUBLY LINKED LISTS.

The AVLTREE

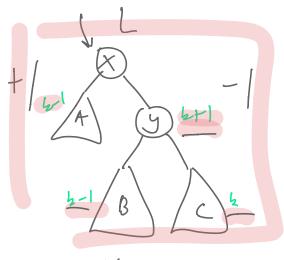
Motivation - if we can keep he height of the tree "h' bounded above by log In I then subsequent operations on the tree proportional to 'h' are bounded by log In () what CASE OCLOG In () operation!

aore - Insert Oblogn > Oth) OBS ERVATION - For all nodes in the three search Oblogn = Oth) let he = height (node -> left)

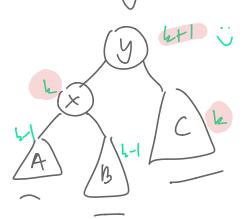
hr = height (node -> night)

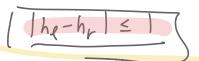
then maintain invariant:

consider thee







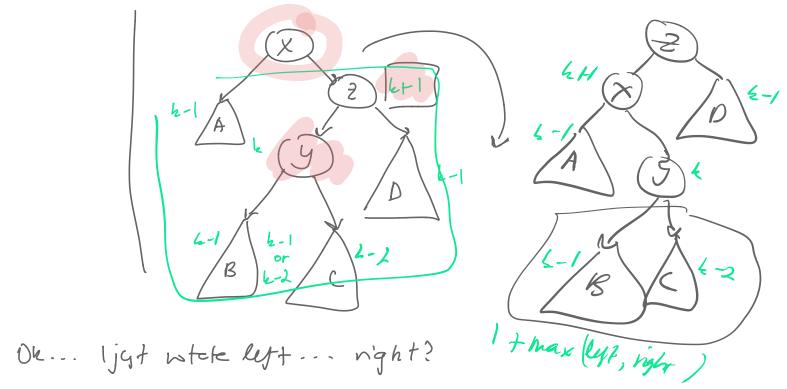


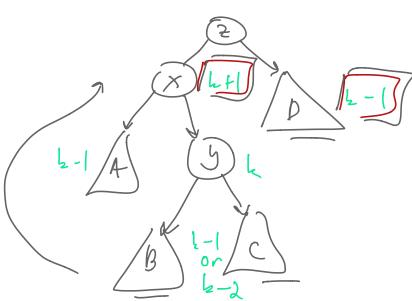
- O let x betweenode that fint violates the Au condition.
- (2) Assume x is right heavy (taker on Length)
- 3 person left notation to countract
- 4) Similar idea if x is left herey (Symnetric)

HANG ON ...

Done just notale inopposition to the side that's taker?

- most cases yes, but wasider ...





Notice hefore ne whate left, it would be good to rehalance the 2-39 edge. Here O votate R(2) 2) notale L(x)

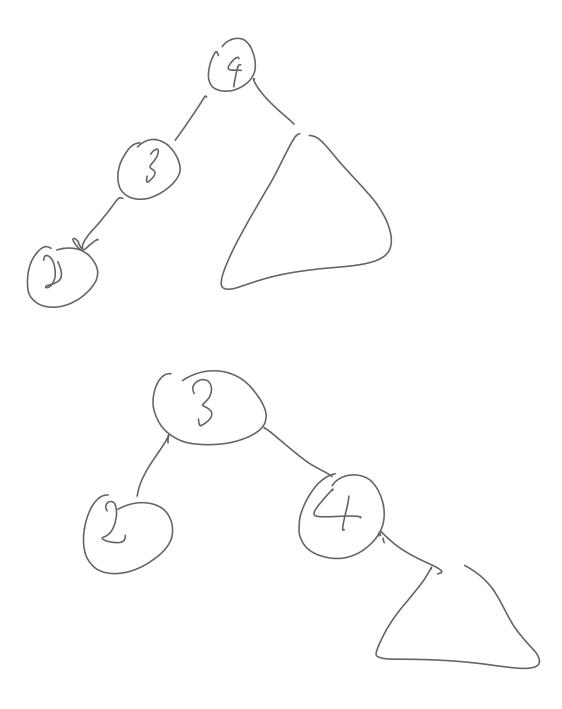
Dh. . . does this do anything?

would case when every node has he and he aughtrby I. Let NH Le number of nodes in height-h AVG true.

$$N_{h} = N_{h-1} + N_{h-2} + N_{h-2$$

7 2 N. . (solve the recurring)

 $N_{H} > 2^{h/2}$ $\log (N_{H}) > \log (2^{h/2})$ $2 \log (N_{H}) > h \Rightarrow h < 2 \log (N_{H})$ $\log (N_{H})$



1,5000