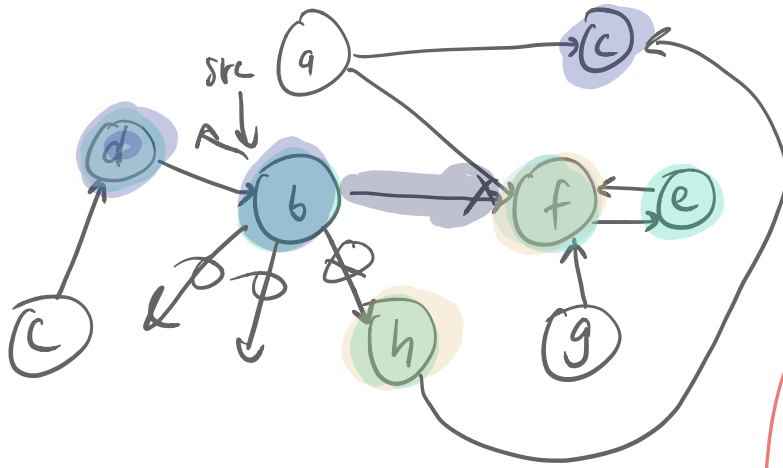


REACHABILITY



reachable set from a traversal on a .

$\{a, b, d, f, e\}$

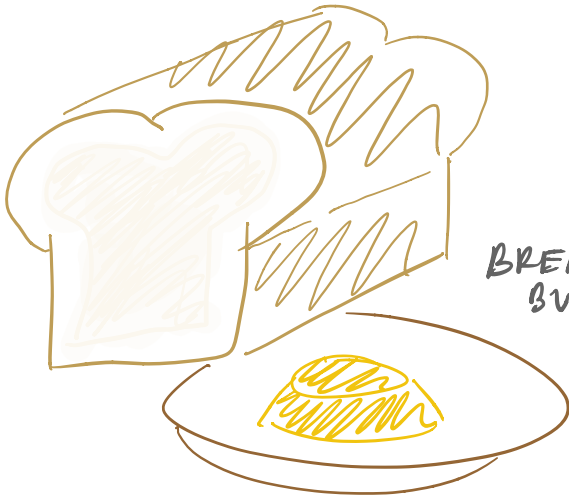
reflexivity? $x \rightarrow x$ ✓

symmetric? $x \rightarrow y \Rightarrow y \rightarrow x$ (undirected)

transitive? $x \rightarrow y \wedge y \rightarrow z \Rightarrow x \rightarrow z$ ✓.

Equivalence relation defined on graphs! ;

not assessable.



BREAD and BUTTER

of GRAPH ALGORITHMS.

→ BFS / DFS ;

Pseudo code: (Recursive DFS)

bool reachable (Graph g, Vertex src, Vertex dst)

Set s = newSet(); //preamble setup.

return reachableRec(g, src, dst, s)

h
is Member :: Bool
add to set

bool reachableRec (Graph g, Vertex src, Vertex dst, Set seen)

or
wid

if (src == dst) return 1

// src ≠ dst: do a step to each of the neighbours of our src.

addToSet(seen, src)

for (int i = 0; i < g → n; i++):

g → edges[src][i]

if (g → edges[src][i] ∧ isInSet(seen, i) ∧ reachableRec)

(return 1;

Ok... ^{return 0} what IF we want to print out a path from src \rightarrow dest?

AUGMENT SET TO BE A PARENT STRUCTURE

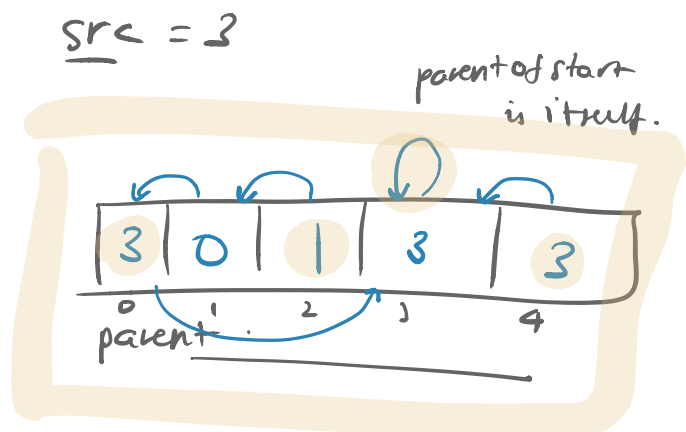
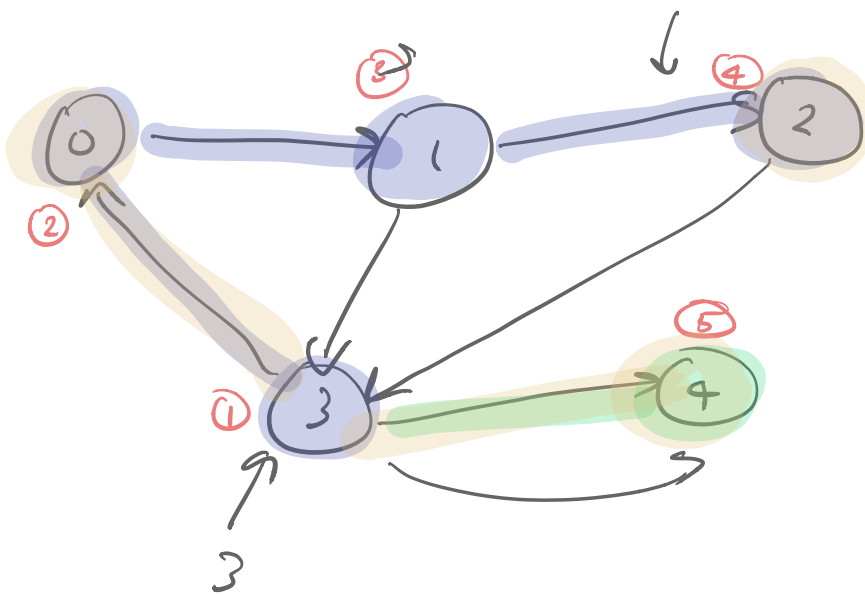
IDEA: Instead of querying if we've seen a vertex.

QUERY for the "PARENT" of a node in our current path.

Q: Do we still need a 'seen' set?

A!

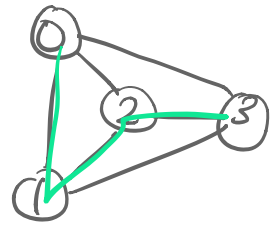
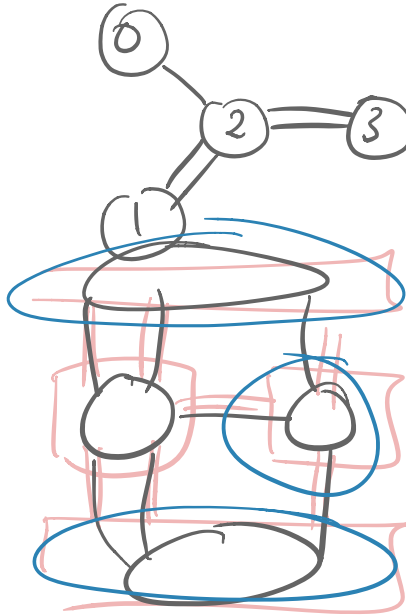
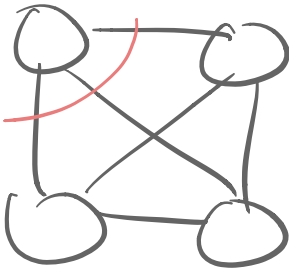
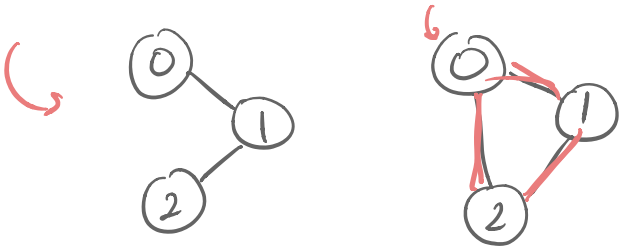
* Below diagram only works for integer labelled vertices.



Given a node you want to print a path for, how can you use parent to print a path?

next lab you'll get to practice this technique!

(vertices) (edges)
Hamiltonian / Euler Paths / Circuits



KONIGSBERG
PROBLEM?

→ MAY two vertices with
odd degree!