How are AVL Trees constructed?

## AULTREE INVARIANTS:

- + Search Tree Invariant
- + Height invariant.

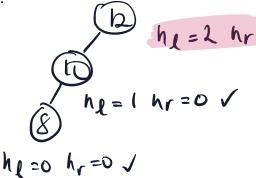
## Q2 from tutes

"Show how an AVI tree would be constructed if the following values were inserted in order"

2.

1 Me-hr/>1?

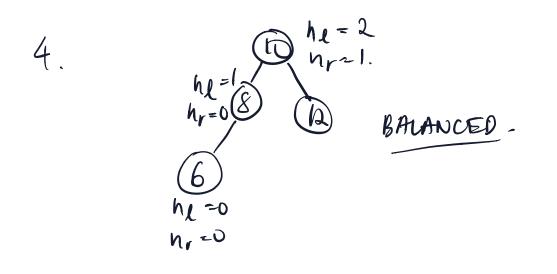
3.

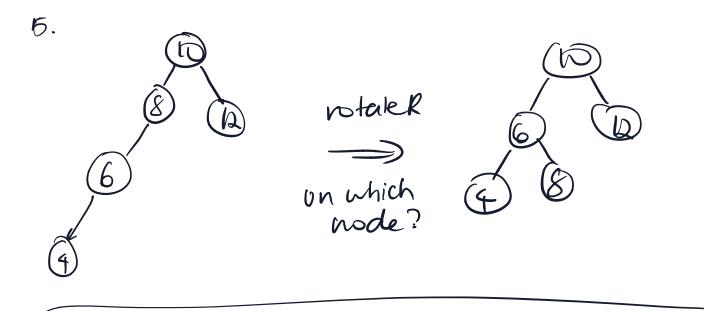


rotales right: isounter leptheavy)



We only ever do one notate and then its abalance tree, why is that?





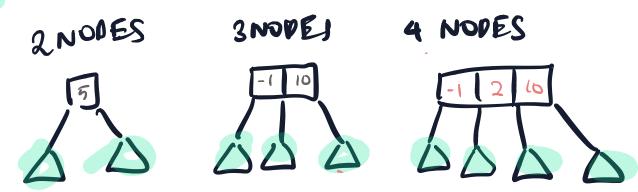
6. (1) balanced.

We only ever do a maximum of one rotate / node, and then we move on. How can we guarantee that it's balanced at the end.

Revelop an algorithm that checks it atree is an AVI tre. > what doy it mean to be an AVL tree?

Say rehave a BST that may or may not be an AVL 75126 tree. Buelop an algorithm to AVLify it. 5/2 (we) (2)

4 TREES.



Invariants:

- Every non-leaf node is a 2/3 node
- All leaves are on the same level.

Why? Checkout itset.

(1) Find the position that you'd like to Inject the value X.

- (2) If we have overflow venoue original middle node and push up. Inkat our element as a leaf.
- (3) Repeat overfrom theek for parent, doing steps (2-3) on parent.

It root, the redian node is the new root.

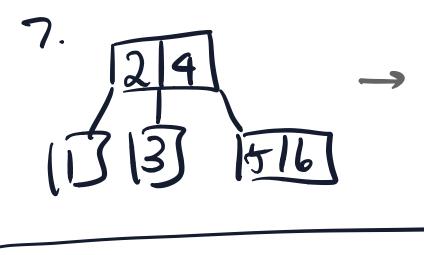
2. Inode 
$$2 \text{ node}$$

$$3. \sqrt{3}$$

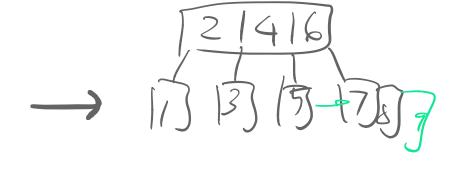
$$3. \sqrt{3}$$

1

4. 213 take median and push up! (why?) 3 14 15

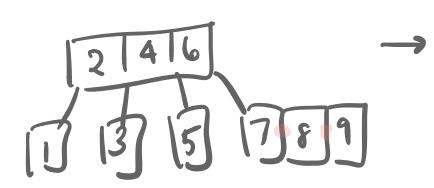


8-



9.

(O.



search for Derin in inherval (-20, 4]? YES!

in inherval (-20, 2]? YES!

in inherval (-20, 1]? YES!

3 LOMI.

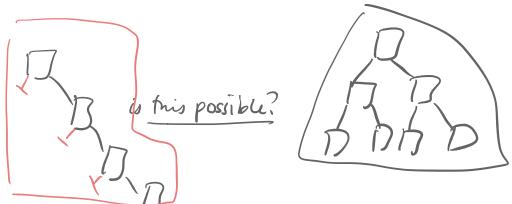
Senoth for  $\mathcal{D}$  can check if  $2 \operatorname{noole}$  can check if  $2 \operatorname{noole}$   $\mathcal{D}$  or explicit range check. If  $(-\infty, 4)? \times [4, 7)? \vee (-\infty, 6) \times (6, 7) \vee (-\infty, 6) \times (-$ 

## 3/ 7

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Some make to derive the most case time complexitis.

- 1) Suppose I had a Bree with n nodes, then inorder to find norsteen (fire) the most possible height of this tree w.r.t. n.
- 2 Each node has at nost 4 children orat west 2 children.
- 3) The nont case is when each mode has 2 children. Cuty?)



4) If every mode has exactly 2 children in cost cose => Ollog\_(n)) height.

(balaved here).

All LEAVES same bel:

push one up -> leaves go one down the tree.

-> subhees go down one but only by wonstruction.