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1 ; FindMax(Square, N, M)
2 ; Input Parameters
3 ;   $a0: Square is the address of first element of 2D matrix
4 ;   $a1: N is the number of rows in Square
5 ;   $a2: M is the number of columns in Square
6 ; Return Value:
7 ;   $v0: value of maximum element in Square
8 ;
9 0x1FFF FFB0 FindMax:    li      $v0, -1          # max <-- -1
10 0x1FFF FFB4           move    $t0, $zero        # i <-- 0
11 0x1FFF FFB8 NextRow:  slt     $t7, $a1, $t0      # if N<i then $t7 <-- 1
12 0x1FFF FFBC           bne     $t7, $zero, Return # if i>=N Return
13 0x1FFF FFC0           move    $t5, $a0          # p <-- Square
14 0x1FFF FFC4           move    $t1, $zero        # j <-- 0
15 0x1FFF FFC8 NextColumn: slt    $t7, $a2, $t1     # if M<j then $t7 <-- 1
16 0x1FFF FFCC           bne     $t7, $zero, RowDone # if j>=M RowDone
17 0x1FFF FFD0           mul     $t3, $t0, $a1      # $t3 <-- i*N
18 0x1FFF FFD4           add     $t4, $t3, $t1      # $t4 <-- i*N+j
19 0x1FFF FFD8           sll     $t5, $t4, 2        # $t5 <-- 4*(i*N+j)
20 0x1FFF FFDC           lw      $t6, 0($t5)        # $t6 <-- Square[i][j]
21 0x1FFF FFE0           slt     $t7, $v0, $t6      # if(max < Square[i][j]) then $t7 <-- 1
22 0x1FFF FFE4           beq     $t7, $zero, NoChange
23 0x1FFF FFE8           move    $v0, $t6          # max <-- Square[i][j]
24 0x1FFF FFEC NoChange: addi    $t1, $t1, 1        # j <-- j+1
25 0x1FFF FFF0           j       NextColumn
26 0x1FFF FFF4 RowDone:  addi    $t0, $t0, 1        # i <-- i+1
27 0x1FFF FFF8           j       NextRow           # if i != N goto NextRow
28 0x1FFF FFFC Return:   jr      $ra

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Figure 1: MIPS Assembly code for FindMax procedure.

In this part of the exam we will study the MIPS assembly code for the FindMax procedure shown in Figure 1.

**Question 1 (20 points):** In this question we will explore the binary representation of instructions that appear in the code for the FindMax procedure shown in Figure 1. Here is some review of relevant information that we know about branches and jump instructions in MIPS:

**Branches** The binary representation of the Opcode for a `bne` instruction in MIPS is 000101, `$t7` is register 15, and `$zero` is register 0. The binary format of a branch instruction in MIPS, from the most-significant to the least-significant bit, starts with the Opcode, followed by the specification of the two registers that are compared by the instruction in the same order that they appear in the assembly instruction, followed by a 16-bit address field. To compute the address of the target instruction, the MIPS branch instruction shifts this 16-bit address field to the left by two bits, sign extends it to 32 bits, and then adds to the value of `PC+4`, where `PC` is the memory address of the branch instruction.

**Jumps** The binary representation of the Opcode for a jump instruction in MIPS is 000010. The binary format of a jump instruction in MIPS, from the most-significant to the least-significant bit, starts with the Opcode, followed by a 26-bit address field. To compute the address of the target of the jump, the MIPS jump instruction concatenates the four most-significant bits of `PC+4`, where `PC` is the memory address of the jump instruction, with the 26-bit address field of the instruction, and then shifts the result to the left by two.

- a. (10 points) What is the hexadecimal representation of the branch instruction that appears at address 0x1FFF FFC8 in the code of the FindMax procedure shown in Figure 1?

The 16 most significant bits are given by the opcode and the number of the registers:

$$000101\ 01111\ 00000 = 0001\ 0101\ 1110\ 0000 = 0x15E0$$

The 16 least significant bits must be calculated based on the address of the branch instruction and on the address of the target instruction. The 6 most-significant hexadecimal digits of the branch instruction and the target instruction are identical. Therefore we can work only with the two least-significant hexadecimal digits:

$$\begin{array}{rcl} 0x\ F4 & = & 1111\ 0100 \\ -\ 0x\ D0 & = & 1101\ 0000 \end{array}$$

The easiest way to subtract in binary is to compute the negative of the second operand and then convert the subtraction to an addition. This is equivalent to adding the complement of the second operand and then adding 1:

$$\begin{array}{r} 1111\ 0100 \\ +\ 0010\ 1111 \\ +\ \phantom{0000}\ 1 \\ \hline 0010\ 0100 \end{array}$$

Now we need to shift this value to the right by two and represent it in 16 bits:

$$0000\ 0000\ 0000\ 1001 = 0x0009$$

Therefore the hexadecimal representation of that branch instruction is:

$$0x\ 15E0\ 0009$$

Another, much simpler, way to find out the value that goes in the offset field of the branch instruction is to count the number of instructions between PC+4 and the target and figure out that we need to add  $9 \times 4$  to PS+4.

- b. (10 points) What is the hexadecimal representation of the jump instruction that appears at address 0x1FFF FFF0 in the code of the FindMax procedure shown in Figure 1?

All we have to do is to take the target address:

$$0x1FFF\ FFC8 = 0001\ 1111\ 1111\ 1111\ 1111\ 1111\ 1100\ 1000$$

Shift it right by two:

$$0000\ 0111\ 1111\ 1111\ 1111\ 1111\ 1111\ 0010$$

Then concatenate the Opcode of the jump instruction with the 26 lowest significant bits of the number above:

$$0000\ 1011\ 1111\ 1111\ 1111\ 1111\ 1111\ 0010 = 0x\ 0BFF\ FFF2$$