Question 2 (30 points): The 16-bit half precision floating point representation has the following specification:

_	15	14	10	9	0
	S	exponent		fraction	

$$N = \begin{cases} (-1)^S \times 0.fraction \times 2^{-14} & \text{if } exponent = 0\\ (-1)^S \times 1.fraction \times 2^{exponent-15} & \text{if } 0 < exponent < 31\\ (-1)^S \times \infty & \text{if } exponent = 31 \text{ and } fraction = 0\\ NaN & \text{if } exponent = 31 \text{ and } fraction \neq 0 \end{cases}$$

a) (4 points) What is the binary representation of -37.375 in the half-precision floating-point representation?  $-37.375_{10} = -100101.011_2 \Rightarrow 1.00101011 \times 25$ Sign = 1 exponent =  $5+15=20 \Rightarrow 10100$ 

- b) (6 points) A = 0x6404 and B = 0x4790 are two half-precision floating-point numbers. What is the true value of A + B expressed in decimal notation? That is, if we have infinite precision to do the addition and store the result, what is A + B?  $A = 0110 \ 0100 \ 0000 \ 0100 \ 0$
- c) (5 points) What is the decimal value of A + B computed on a machine with one guard bit, one round bit and one sticky bit?

1.00000001  
+ 0.0000001111001  
1.00000010111001  
fraction guard 
$$\Rightarrow$$
 1.0000001100 × 2<sup>10</sup>  
sticky=1  
= [10.3610]

d) (15 points) MIPS has division instructions for single and double precision floating point values, but not for half-precision. Write a MIPS procedure to implement division of a half-precision floating point by an integer multiple of 2. The input to your procedure is the address of a half-precision floating point value (in \$a0), and the unsigned integer representation of a power of 2 (in \$a1). Your procedure should perform the division and update the value in memory at the address in \$a0.

Your code should follow calling conventions and should not use any pseudoinstructions. You may assume that the result of the division can be represented as a half-precision floating point value.

Note that if \$al contains the unsigned intrepresentation of 2k, then it will contain a I followed by k 0's. We need to count the 0's, then subtract that from the half's exponent.

```
addi $ +0, $ zero, -1
halfdiv:
          beg $al, $zero, next # repeats until we
loop:
                              # have made k+1
          srital, tal, 1
          addi $ t0, $ t0, 1
                                # shifts
          loop
          Thu $11,0($00)
                               # load the half
next:
          andi $12, $11, 0x7000 # mask out exponent
          srl $+2, $4.2, 10
                                #shift, add k, and
    5Ub Dat $+2, $-12, $to
                                # shift back
          SII $ tz, $ tz, 10
          andi $t1, $t1, 0x83FF # clear exponent
                                # update exponent
          or $11, $11, $t2
                               # update memory
          shu $61,0($00)
          ir sta
```