

E2 prediction

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This notebook analyzes prediction using Bayesian binomial generalized linear mixed effects models (GLMMs).

Set up

```
set.seed(15000)

data <- read_csv('../data/E1-E2-E4/prediction.csv')

## Rows: 3210 Columns: 6
## -- Column specification -----
## Delimiter: ","
## chr (3): response, scramble, Musician
## dbl (3): exp_subject_id, Trial_Nr, yrs_mus_exp
##
## i Use `spec()` to retrieve the full column specification for this data.
## i Specify the column types or set `show_col_types = FALSE` to quiet this message.
```

Convert variables to factors.

```
data %<>%
  mutate(exp_subject_id = as.factor(exp_subject_id),
         response = ifelse(response == 'Correct', TRUE, FALSE),
         scramble = factor(scramble, levels = c('8B', '2B', '1B')),
         Musician = factor(Musician, levels = c('Yes', 'No'))) %>%
  filter(!is.na(response))
```

Set the contrast for condition.

```
contrasts(data$scramble) <- contr.treatment(3)
print(contrasts(data$scramble))
```

```
##      2 3
## 8B 0 0
## 2B 1 0
## 1B 0 1
```

```
contrasts(data$Musician)
```

```
##      No
## Yes  0
## No   1
```

Main analysis

Priors

Priors are expressed in log(odds) space.

Intercept: Given that chance is 50%, we assume that participants will perform somewhere between chance and ceiling. We expect the center of the distribution of accuracy to be somewhere around 75% or 80%. If we use a center of 80% and an SD of 1, 95% of the values fall between 35.1% and 96.7%.

```
prior_intercept <- set_prior('normal(log(0.8 / (1 - 0.8)), 1)', class = 'Intercept')
```

Group: We might expect musicians to do slightly better than non-musicians, on average.

In this range, a difference in 0.25 log odds gives us about a 5% decrease in accuracy.

```
prior_mus <- set_prior('normal(-0.25, 1)', coef = 'MusicianNo')
```

Scramble: We expect performance to improve as scramble level decreases. If we code 8B as reference level, then we expect $8B > 2B$ and $8B > 1B$.

Since we're keeping the musician slope at $SD = 1$, we'll keep these (and the interactions) at $SD = 1$. This seems to be a pretty weak prior.

```
prior_scramble2B <- set_prior('normal(-0.1, 1)', coef = 'scramble2')  
prior_scramble1B <- set_prior('normal(-0.2, 1)', coef = 'scramble3')
```

Interaction: We expect no interaction between group and scramble.

```
prior_int2B <- set_prior('normal(0, 1)', coef = 'MusicianNo:scramble2')  
prior_int1B <- set_prior('normal(0, 1)', coef = 'MusicianNo:scramble3')
```

Random slope for subjects: *Leave this as default for now, may update.*

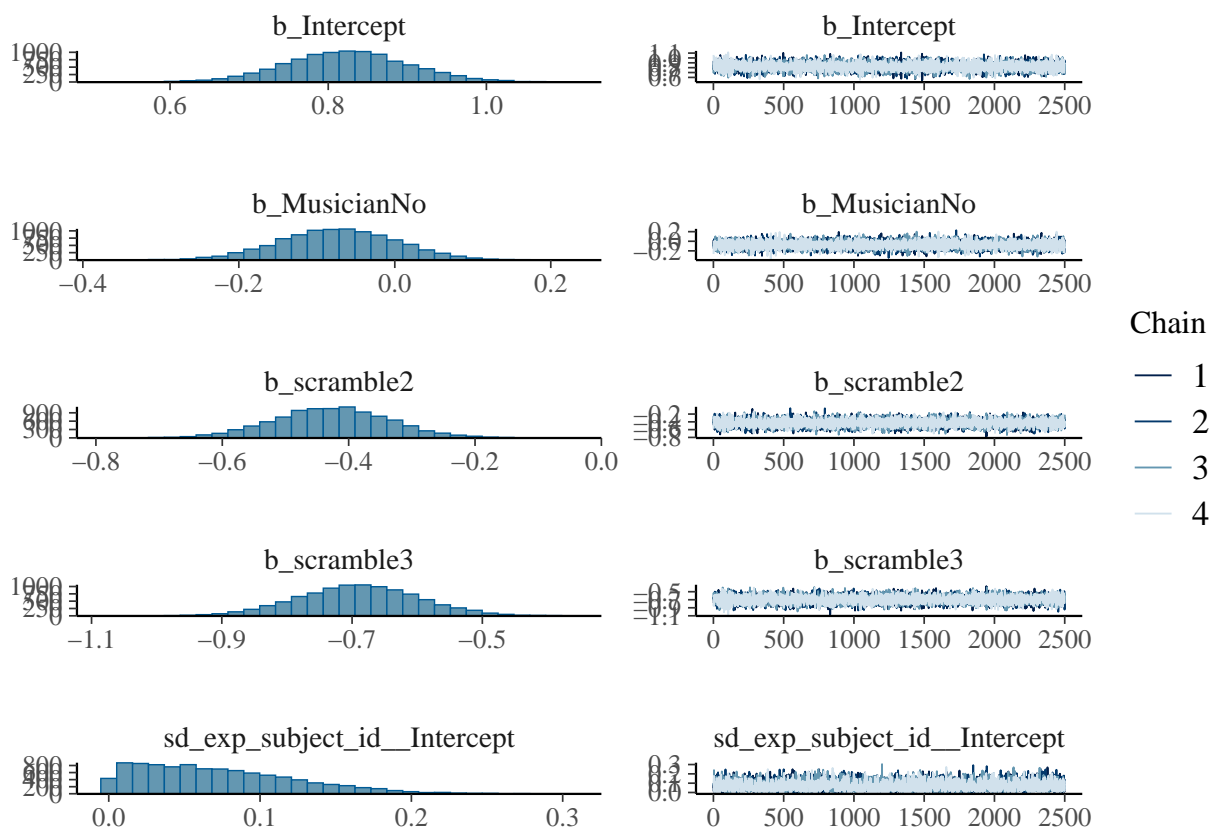
Main model with group and condition

```
get_prior(response ~ Musician + scramble + (1 | exp_subject_id), data = data)

##           prior      class      coef      group resp dpar nlpar lb ub
##           (flat)         b              0
##           (flat)         b MusicianNo
##           (flat)         b  scramble2
##           (flat)         b  scramble3
## student_t(3, 0, 2.5) Intercept
## student_t(3, 0, 2.5)      sd              0
## student_t(3, 0, 2.5)      sd      exp_subject_id      0
## student_t(3, 0, 2.5)      sd Intercept exp_subject_id      0
## student_t(3, 0, 2.5)      sigma              0
##      source
##      default
## (vectorized)
## (vectorized)
## (vectorized)
##      default
##      default
## (vectorized)
## (vectorized)
##      default

mus_scram <- brm(response ~ Musician + scramble + (1 | exp_subject_id), data = data,
  family = bernoulli(),
  prior = c(prior_intercept, prior_mus,
    prior_scramble2B, prior_scramble1B),
  save_pars = save_pars(all = TRUE), iter = 5000,
  file = 'models/E2_mus_scram')

plot(mus_scram)
```



```
print(summary(mus_scram), digits = 4)
```

```
## Warning: There were 1 divergent transitions after warmup. Increasing
## adapt_delta above 0.8 may help. See
## http://mc-stan.org/misc/warnings.html#divergent-transitions-after-warmup

## Family: bernoulli
## Links: mu = logit
## Formula: response ~ Musician + scramble + (1 | exp_subject_id)
## Data: data (Number of observations: 3158)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 105)
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
sd(Intercept)	0.0723	0.0510	0.0032	0.1866	1.0012	3170	4111

```
##
## Regression Coefficients:
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
Intercept	0.8244	0.0776	0.6738	0.9791	1.0007	9598	6847
MusicianNo	-0.0726	0.0749	-0.2196	0.0717	1.0000	12486	6999
scramble2	-0.4270	0.0912	-0.6051	-0.2464	1.0004	9666	8092
scramble3	-0.6900	0.0920	-0.8697	-0.5119	1.0005	9341	7771

```
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

```
emm_mus_scram_s <- emmeans(mus_scram, specs = "scramble")
summary(emm_mus_scram_s)
```

```
##  scramble emmean lower.HPD upper.HPD
##  8B      0.7877   0.6573   0.922
##  2B      0.3615   0.2354   0.482
##  1B      0.0986  -0.0215   0.222
##
## Results are averaged over the levels of: Musician
## Point estimate displayed: median
## Results are given on the logit (not the response) scale.
## HPD interval probability: 0.95
```

```
contrast(emm_mus_scram_s, method = "pairwise")
```

```
##  contrast estimate lower.HPD upper.HPD
##  8B - 2B      0.427   0.2486   0.607
##  8B - 1B      0.690   0.5118   0.869
##  2B - 1B      0.264   0.0868   0.434
##
## Results are averaged over the levels of: Musician
## Point estimate displayed: median
## Results are given on the log odds ratio (not the response) scale.
## HPD interval probability: 0.95
```

```
emm_mus_scram_ms <- emmeans(mus_scram, specs = c("Musician", "scramble"))
summary(emm_mus_scram_ms)
```

```
##  Musician scramble emmean lower.HPD upper.HPD
##  Yes      8B      0.824   0.66884   0.973
##  No       8B      0.752   0.60539   0.905
##  Yes      2B      0.397   0.25214   0.535
##  No       2B      0.325   0.18342   0.470
##  Yes      1B      0.135  -0.00177   0.275
##  No       1B      0.062  -0.07678   0.210
##
## Point estimate displayed: median
## Results are given on the logit (not the response) scale.
## HPD interval probability: 0.95
```

```
contrast(emm_mus_scram_ms, method = "pairwise")
```

```
##  contrast          estimate lower.HPD upper.HPD
##  Yes 8B - No 8B      0.0725  -0.0738   0.216
##  Yes 8B - Yes 2B     0.4271   0.2486   0.607
##  Yes 8B - No 2B      0.5002   0.2679   0.737
##  Yes 8B - Yes 1B     0.6899   0.5118   0.869
##  Yes 8B - No 1B      0.7634   0.5348   1.000
##  No 8B - Yes 2B      0.3548   0.1208   0.578
##  No 8B - No 2B       0.4271   0.2486   0.607
##  No 8B - Yes 1B      0.6177   0.3935   0.842
##  No 8B - No 1B      0.6899   0.5118   0.869
##  Yes 2B - No 2B      0.0725  -0.0738   0.216
##  Yes 2B - Yes 1B     0.2637   0.0868   0.434
##  Yes 2B - No 1B      0.3359   0.1035   0.553
##  No 2B - Yes 1B      0.1898  -0.0357   0.415
```

```
## No 2B - No 1B      0.2637    0.0868    0.434
## Yes 1B - No 1B     0.0725   -0.0738    0.216
##
## Point estimate displayed: median
## Results are given on the log odds ratio (not the response) scale.
## HPD interval probability: 0.95
```

Main effects

```
main_BF <- describe_posterior(mus_scram,  
                               estimate = "median", dispersion = TRUE,  
                               ci = .95, ci_method = "HDI",  
                               test = c("bayes_factor"))
```

```
## Warning: Bayes factors might not be precise.  
##   For precise Bayes factors, sampling at least 40,000 posterior samples is  
##   recommended.
```

```
print(main_BF, digits = 5)
```

```
## Summary of Posterior Distribution
```

```
##
```

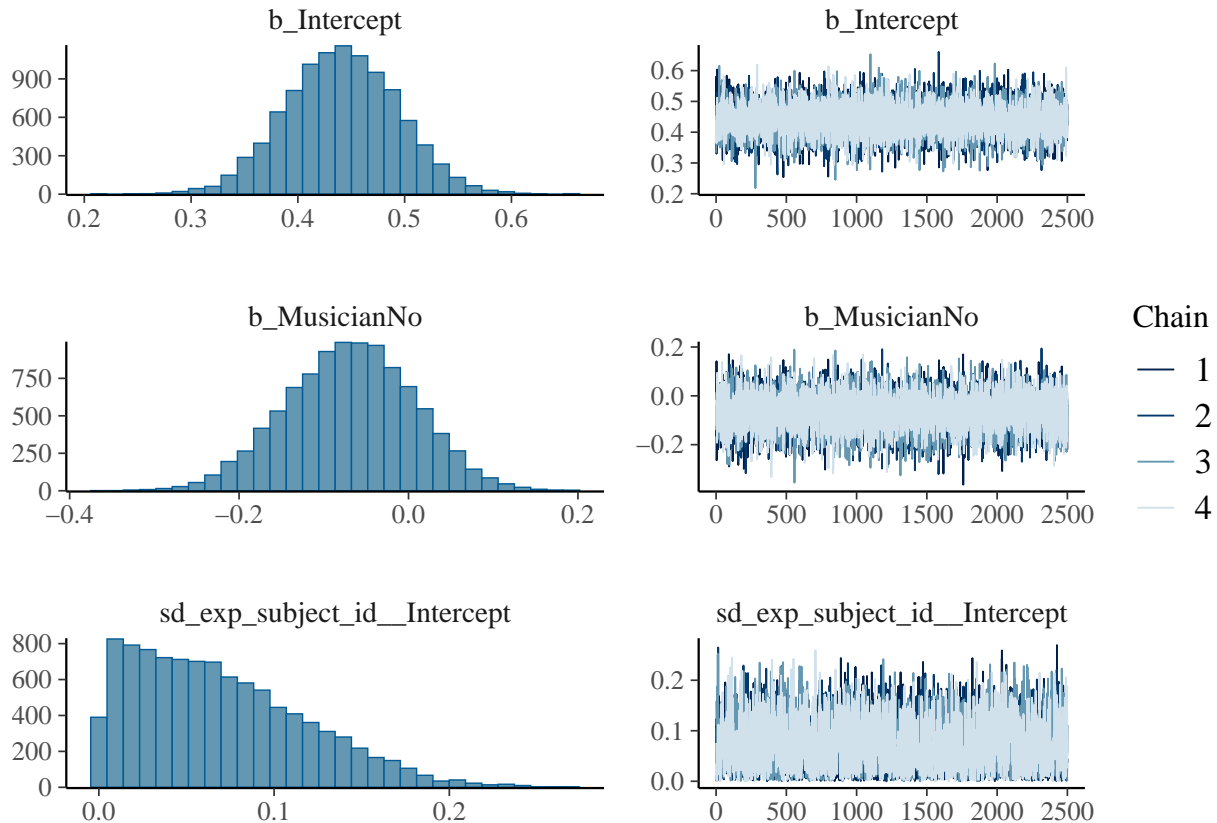
## Parameter		Median		MAD		95% CI		BF		Rhat		ESS
##	-----		-----		-----		-----		-----		-----	
## (Intercept)		0.82360		0.07590		[0.67, 0.97]		8.58e+09		1.000		9632.00000
## MusicianNo		-0.07245		0.07581		[-0.22, 0.07]		0.114		1.000		12615.00000
## scramble2		-0.42709		0.09068		[-0.61, -0.25]		648.50		1.000		9634.00000
## scramble3		-0.68986		0.09222		[-0.87, -0.51]		1.38e+06		1.000		9300.00000

Strong evidence against a main effect of group.

To get the main effect of scramble level, fit the “null” model with group only to compare.

```
mus_only <- brm(response ~ Musician + (1 | exp_subject_id), data = data,
  family = bernoulli(),
  prior = c(prior_intercept, prior_mus),
  save_pars = save_pars(all = TRUE), iter = 5000,
  file = 'models/E2_mus_only')
```

```
plot(mus_only)
```



```
print(summary(mus_only), digits = 4)
```

```
## Family: bernoulli
## Links: mu = logit
## Formula: response ~ Musician + (1 | exp_subject_id)
## Data: data (Number of observations: 3158)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 105)
## Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept) 0.0693 0.0488 0.0029 0.1774 1.0006 3401 4362
##
## Regression Coefficients:
## Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept 0.4410 0.0522 0.3403 0.5426 0.9999 13508 7350
## MusicianNo -0.0688 0.0755 -0.2168 0.0746 1.0005 13455 7340
##
```



```

## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
BF_scramble <- bayes_factor(mus_scram, mus_only)

## Iteration: 1
## Iteration: 2
## Iteration: 3
## Iteration: 4
## Iteration: 5
## Iteration: 6
## Iteration: 1
## Iteration: 2
## Iteration: 3
## Iteration: 4
print(BF_scramble)

## Estimated Bayes factor in favor of mus_scram over mus_only: 72700233010.60995
Very strong evidence for a main effect of scramble condition.

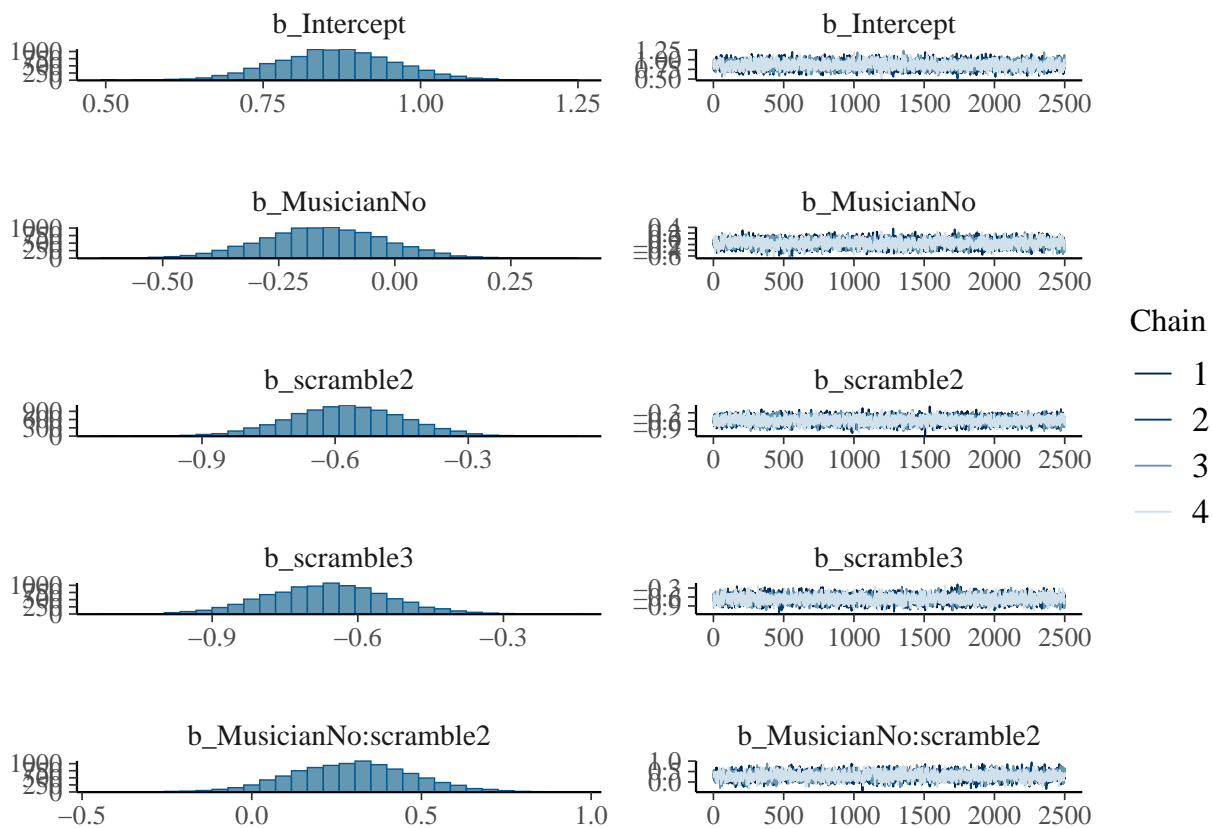
```

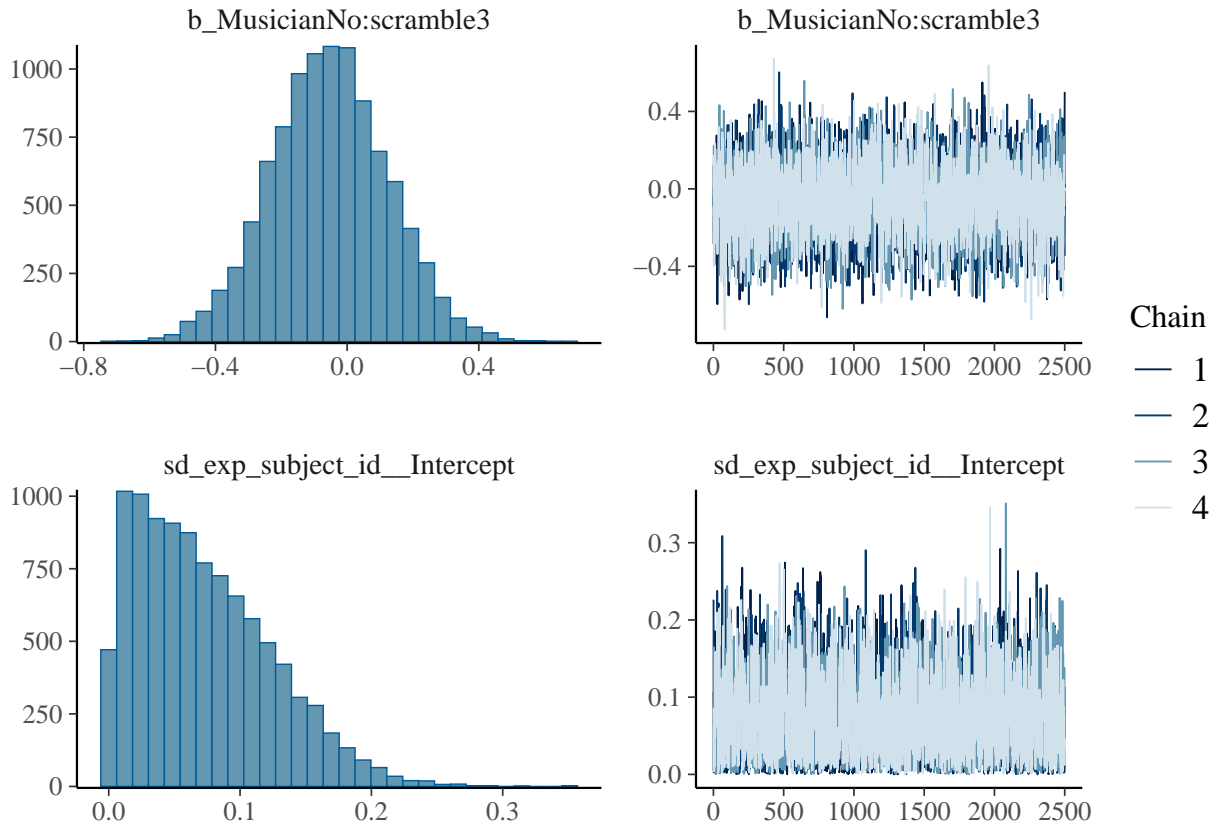
Interaction between group and condition?

Add an interaction between group and condition, and compare the model with the interaction to the one without.

```
mus_scram_int <- brm(response ~ Musician*scramble + (1 | exp_subject_id), data = data,
  family = bernoulli(),
  prior = c(prior_intercept, prior_mus,
    prior_scramble2B, prior_scramble1B,
    prior_int2B, prior_int1B),
  save_pars = save_pars(all = TRUE), iter = 5000,
  file = 'models/E2_mus_scram_int')
```

```
plot(mus_scram_int)
```





```
print(summary(mus_scram_int), digits = 4)
```

```
## Family: bernoulli
## Links: mu = logit
## Formula: response ~ Musician * scramble + (1 | exp_subject_id)
## Data: data (Number of observations: 3158)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 105)
##
```

	Estimate	Est.Error	1-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
sd(Intercept)	0.0725	0.0513	0.0030	0.1878	1.0005	3258	4589

```
##
## Regression Coefficients:
##
```

	Estimate	Est.Error	1-95% CI	u-95% CI	Rhat	Bulk_ESS
Intercept	0.8665	0.0941	0.6844	1.0559	1.0005	5201
MusicianNo	-0.1543	0.1311	-0.4120	0.0998	1.0002	4588
scramble2	-0.5752	0.1281	-0.8276	-0.3277	1.0001	5845
scramble3	-0.6636	0.1252	-0.9095	-0.4141	1.0004	5707
MusicianNo:scramble2	0.2957	0.1781	-0.0511	0.6444	1.0007	5023
MusicianNo:scramble3	-0.0544	0.1770	-0.4008	0.2934	1.0000	4856

```
##
## Tail_ESS
## Intercept 7176
## MusicianNo 6067
## scramble2 7095
## scramble3 6800
## MusicianNo:scramble2 6670
```

```

## MusicianNo:scramble3      6214
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
BF_int <- bayes_factor(mus_scram_int, mus_scram)

## Iteration: 1
## Iteration: 2
## Iteration: 3
## Iteration: 4
## Iteration: 5
## Iteration: 6
## Iteration: 7
## Iteration: 1
## Iteration: 2
## Iteration: 3
## Iteration: 4
## Iteration: 5
print(BF_int)

## Estimated Bayes factor in favor of mus_scram_int over mus_scram: 0.27155
Strong evidence against an interaction between group and condition.

```

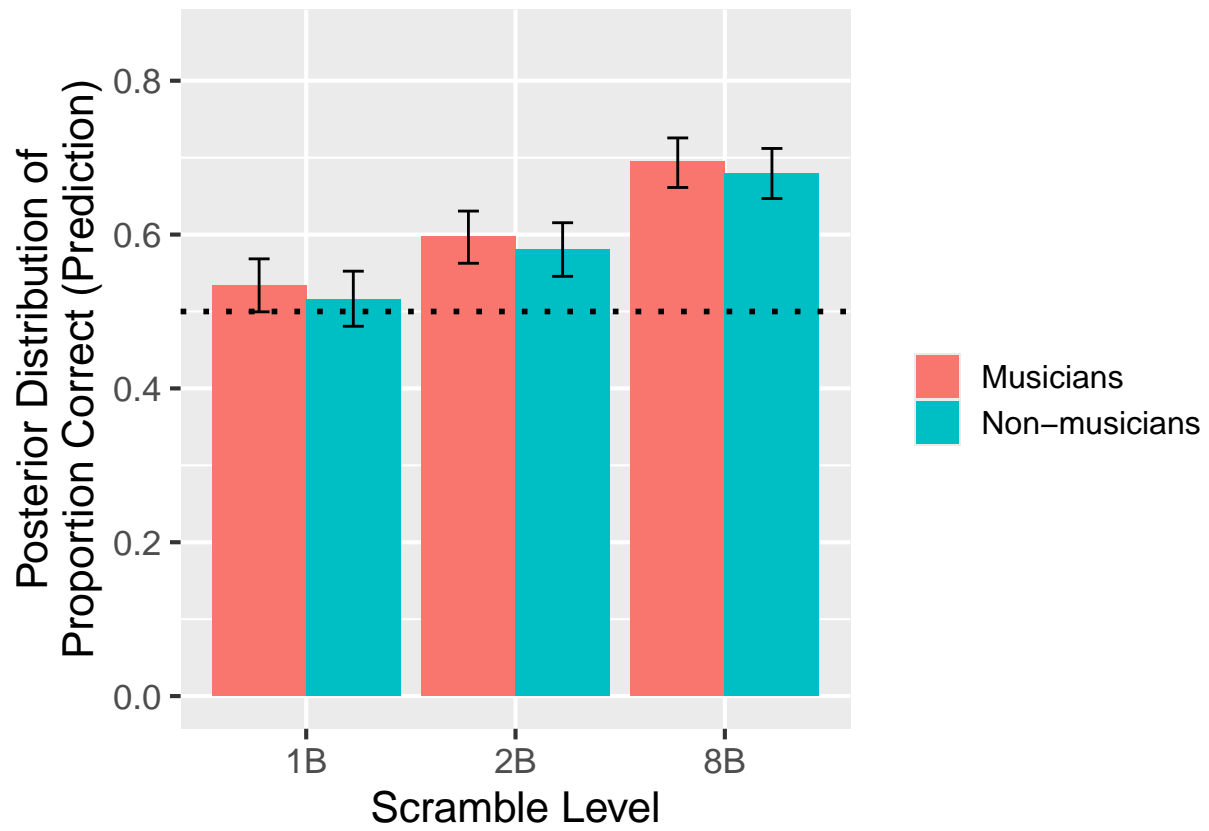
Figure 2B

Create a helper function for the conversion from log odds to probability.

```
calculate_prob_from_logodds <- function(logodds) {  
  return(exp(logodds) / (1 + exp(logodds)))  
}
```

Visualize with posterior estimates and 95% CrI on the scale of accuracy.

```
posterior_est <- as.data.frame(emm_mus_scram_ms)  
  
ggplot() +  
  geom_col(aes(x = scramble, y = calculate_prob_from_logodds(emmean), fill = Musician),  
    data = posterior_est,  
    position = "dodge") +  
  geom_errorbar(aes(x = scramble,  
    ymin = calculate_prob_from_logodds(lower.HPD),  
    ymax = calculate_prob_from_logodds(upper.HPD),  
    fill = Musician),  
    data = posterior_est, position = position_dodge(width = 0.9), width = 0.2) +  
  geom_hline(yintercept = 0.5, linetype = "dotted", color = "black", linewidth = 1) +  
  theme_gray(base_size = 16) +  
  scale_x_discrete(limits = rev) +  
  ylim(0, 0.85) +  
  xlab('Scramble Level') +  
  ylab('Posterior Distribution of\nProportion Correct (Prediction)') +  
  scale_fill_discrete(name="", labels=c('Musicians', 'Non-musicians')) +  
  theme(legend.text = element_text(size = 12))  
  
## Warning in geom_errorbar(aes(x = scramble, ymin =  
## calculate_prob_from_logodds(lower.HPD), : Ignoring unknown aesthetics: fill
```



```
ggsave('../figures/Fig2B_prediction.png', width = 7, height = 5)
```

1B condition at chance?

There is technically no “right” answer, so performance in the 1B condition should be at chance.

```
data1B <- filter(data, scramble == '1B')
```

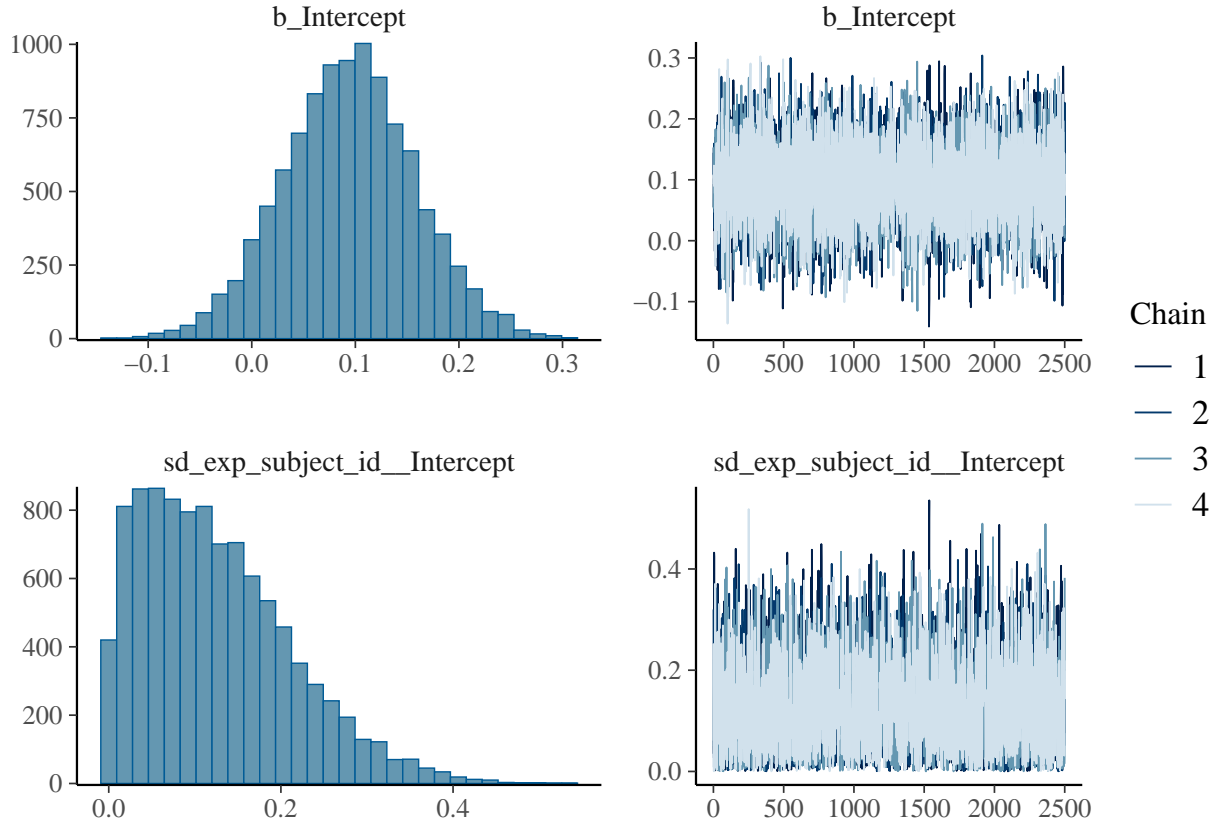
```
get_prior(response ~ 1 + (1 | exp_subject_id), data = data1B)
```

```
##           prior      class      coef      group resp dpar nlpar lb ub
## student_t(3, 0, 2.5) Intercept
## student_t(3, 0, 2.5)      sd
## student_t(3, 0, 2.5)      sd      exp_subject_id
## student_t(3, 0, 2.5)      sd Intercept exp_subject_id
## student_t(3, 0, 2.5)      sigma
##      source
##      default
##      default
## (vectorized)
## (vectorized)
##      default
```

(Leave the default prior for this intercept.)

```
only1B <- brm(response ~ 1 + (1 | exp_subject_id), data = data1B,
  family = bernoulli(),
  save_pars = save_pars(all = TRUE), iter = 5000,
  file = 'models/E2_only1B')
```

```
plot(only1B)
```



```
print(summary(only1B), digits = 4)
```

```
## Family: bernoulli
## Links: mu = logit
## Formula: response ~ 1 + (1 | exp_subject_id)
## Data: data1B (Number of observations: 1054)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 105)
##      Estimate Est.Error l-95% CI u-95% CI   Rhat Bulk_ESS Tail_ESS
## sd(Intercept)  0.1247    0.0872   0.0055   0.3286 1.0004    3804    5028
##
## Regression Coefficients:
##      Estimate Est.Error l-95% CI u-95% CI   Rhat Bulk_ESS Tail_ESS
## Intercept  0.0944    0.0637  -0.0310   0.2206 1.0002    15621    6872
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

Is intercept different from 0?

```
bf_pointnull(only1B, null = 0)
```

```
## Sampling priors, please wait...
## Warning: Bayes factors might not be precise.
## For precise Bayes factors, sampling at least 40,000 posterior samples is
## recommended.
## Bayes Factor (Savage-Dickey density ratio)
##
## Parameter | BF
## -----
## (Intercept) | 0.072
##
## * Evidence Against The Null: 0
```

There is strong evidence that performance in the 1B condition is at chance.

What if we just look at 8B and 2B?

The main thing here is to see if the interaction we see between group and condition (that we see visually) shows up when we take out 1B.

```
data_no1B <- filter(data, scramble != '1B')
```

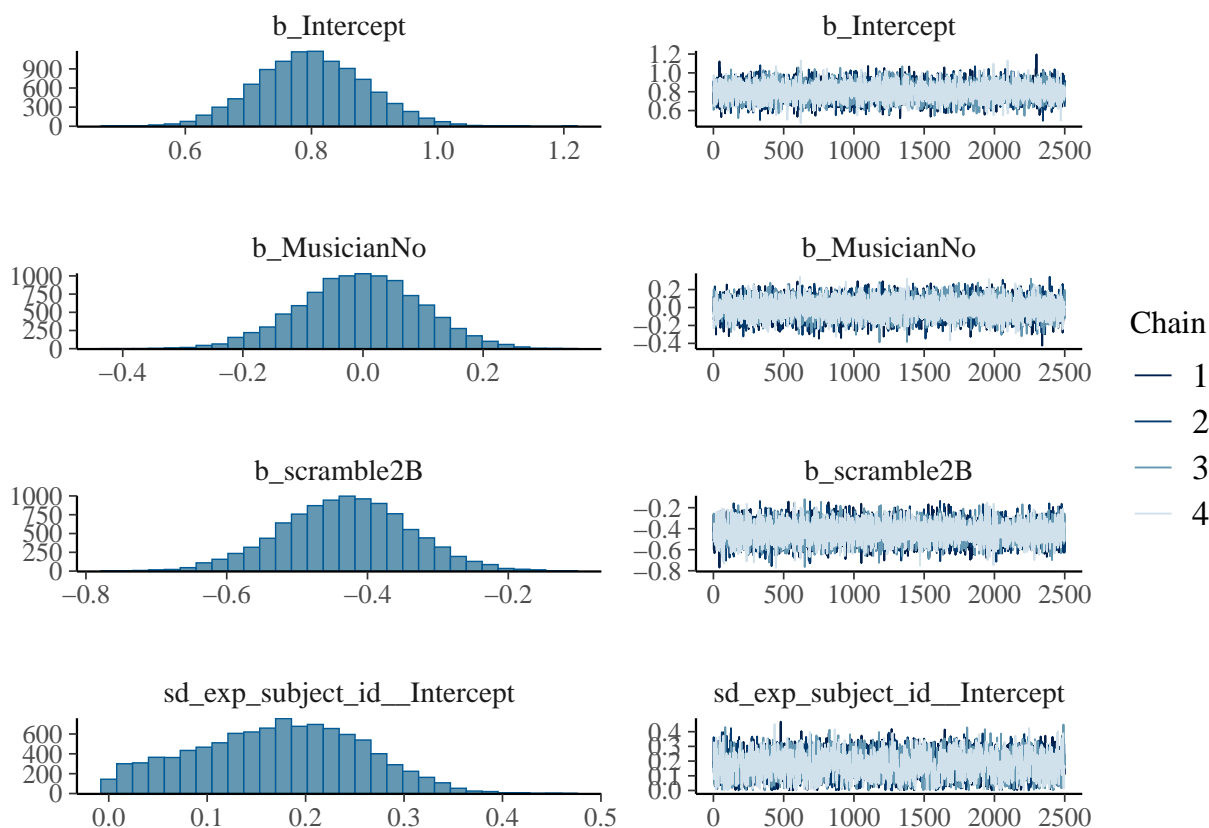
```
get_prior(response ~ Musician + scramble + (1 | exp_subject_id), data = data_no1B)
```

```
## Warning: contrasts dropped from factor scramble due to missing levels
```

```
##           prior      class      coef      group resp dpar nlpar lb ub
##           (flat)         b
##           (flat)         b MusicianNo
##           (flat)         b scramble2B
## student_t(3, 0, 2.5) Intercept
## student_t(3, 0, 2.5)      sd
## student_t(3, 0, 2.5)      sd      exp_subject_id
## student_t(3, 0, 2.5)      sd Intercept exp_subject_id
## student_t(3, 0, 2.5)      sigma
##      source
##      default
## (vectorized)
## (vectorized)
##      default
##      default
## (vectorized)
## (vectorized)
##      default
```

```
no1B <- brm(response ~ Musician + scramble + (1 | exp_subject_id), data = data_no1B,
  family = bernoulli(),
  prior = c(
    prior_intercept, prior_mus, set_prior('normal(-0.1, 1)', coef = 'scramble2B')
  ),
  save_pars = save_pars(all = TRUE), iter = 5000,
  file = 'models/E2_no1B')
```

```
plot(no1B)
```



```
print(summary(no1B), digits = 4)
```

```
## Family: bernoulli
## Links: mu = logit
## Formula: response ~ Musician + scramble + (1 | exp_subject_id)
## Data: data_no1B (Number of observations: 2104)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 105)
## Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept) 0.1708 0.0843 0.0140 0.3284 1.0013 2069 2631
##
## Regression Coefficients:
## Estimate Est.Error 1-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept 0.7995 0.0862 0.6359 0.9701 1.0006 9772 6942
## MusicianNo -0.0048 0.1004 -0.2056 0.1879 1.0012 10390 7624
## scramble2B -0.4315 0.0913 -0.6143 -0.2526 1.0008 13723 7301
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

```
get_prior(response ~ Musician*scramble + (1 | exp_subject_id), data = data_no1B)
```

```
## Warning: contrasts dropped from factor scramble due to missing levels
```

```
## prior class coef group resp dpar
```



```

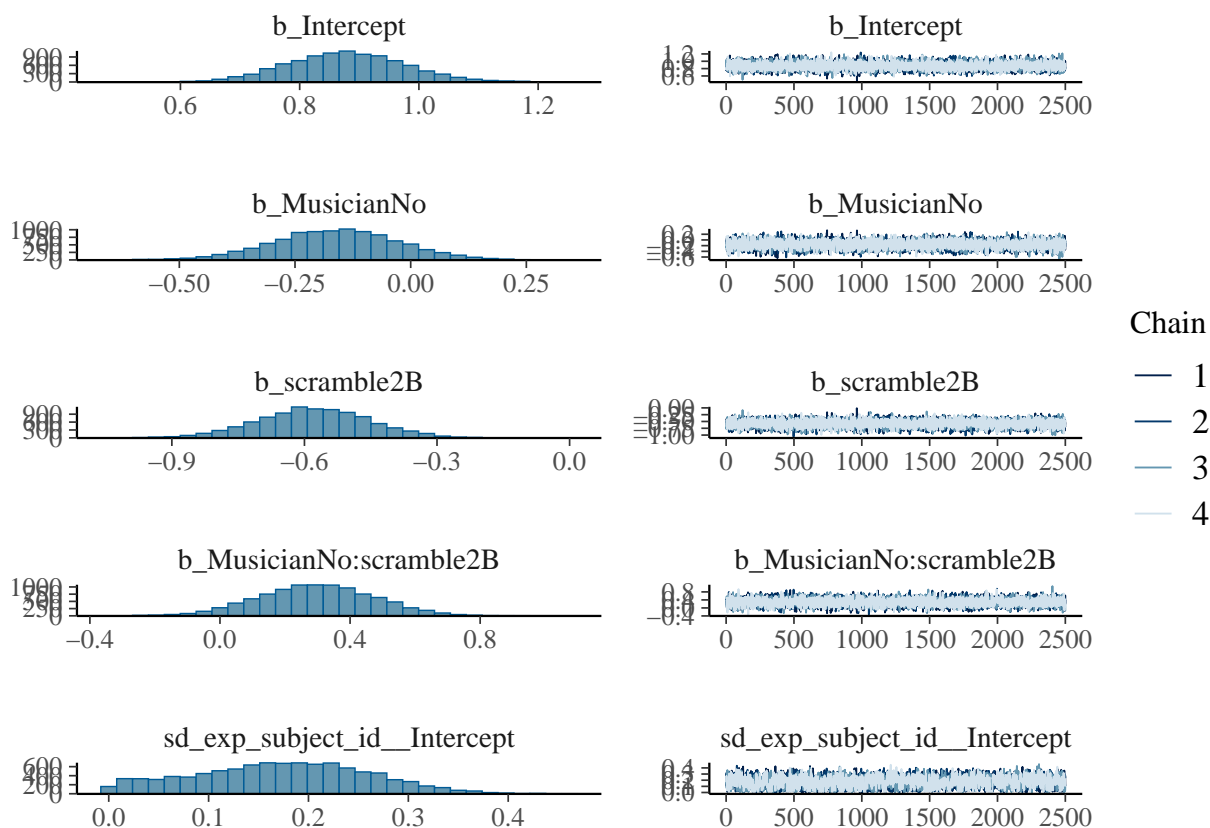
## Chain 1: Adjust your expectations accordingly!
## Chain 1:
## Chain 1:
## Chain 1: Iteration:    1 / 5000 [  0%] (Warmup)
## Chain 1: Iteration:   500 / 5000 [ 10%] (Warmup)
## Chain 1: Iteration:  1000 / 5000 [ 20%] (Warmup)
## Chain 1: Iteration:  1500 / 5000 [ 30%] (Warmup)
## Chain 1: Iteration:  2000 / 5000 [ 40%] (Warmup)
## Chain 1: Iteration:  2500 / 5000 [ 50%] (Warmup)
## Chain 1: Iteration:  2501 / 5000 [ 50%] (Sampling)
## Chain 1: Iteration:  3000 / 5000 [ 60%] (Sampling)
## Chain 1: Iteration:  3500 / 5000 [ 70%] (Sampling)
## Chain 1: Iteration:  4000 / 5000 [ 80%] (Sampling)
## Chain 1: Iteration:  4500 / 5000 [ 90%] (Sampling)
## Chain 1: Iteration:  5000 / 5000 [100%] (Sampling)
## Chain 1:
## Chain 1: Elapsed Time: 3.598 seconds (Warm-up)
## Chain 1:                2.764 seconds (Sampling)
## Chain 1:                6.362 seconds (Total)
## Chain 1:
##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 2).
## Chain 2:
## Chain 2: Gradient evaluation took 7.6e-05 seconds
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.76 seconds.
## Chain 2: Adjust your expectations accordingly!
## Chain 2:
## Chain 2:
## Chain 2: Iteration:    1 / 5000 [  0%] (Warmup)
## Chain 2: Iteration:   500 / 5000 [ 10%] (Warmup)
## Chain 2: Iteration:  1000 / 5000 [ 20%] (Warmup)
## Chain 2: Iteration:  1500 / 5000 [ 30%] (Warmup)
## Chain 2: Iteration:  2000 / 5000 [ 40%] (Warmup)
## Chain 2: Iteration:  2500 / 5000 [ 50%] (Warmup)
## Chain 2: Iteration:  2501 / 5000 [ 50%] (Sampling)
## Chain 2: Iteration:  3000 / 5000 [ 60%] (Sampling)
## Chain 2: Iteration:  3500 / 5000 [ 70%] (Sampling)
## Chain 2: Iteration:  4000 / 5000 [ 80%] (Sampling)
## Chain 2: Iteration:  4500 / 5000 [ 90%] (Sampling)
## Chain 2: Iteration:  5000 / 5000 [100%] (Sampling)
## Chain 2:
## Chain 2: Elapsed Time: 3.953 seconds (Warm-up)
## Chain 2:                2.761 seconds (Sampling)
## Chain 2:                6.714 seconds (Total)
## Chain 2:
##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 3).
## Chain 3:
## Chain 3: Gradient evaluation took 7.5e-05 seconds
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.75 seconds.
## Chain 3: Adjust your expectations accordingly!
## Chain 3:
## Chain 3:
## Chain 3: Iteration:    1 / 5000 [  0%] (Warmup)

```

```

## Chain 3: Iteration: 500 / 5000 [ 10%] (Warmup)
## Chain 3: Iteration: 1000 / 5000 [ 20%] (Warmup)
## Chain 3: Iteration: 1500 / 5000 [ 30%] (Warmup)
## Chain 3: Iteration: 2000 / 5000 [ 40%] (Warmup)
## Chain 3: Iteration: 2500 / 5000 [ 50%] (Warmup)
## Chain 3: Iteration: 2501 / 5000 [ 50%] (Sampling)
## Chain 3: Iteration: 3000 / 5000 [ 60%] (Sampling)
## Chain 3: Iteration: 3500 / 5000 [ 70%] (Sampling)
## Chain 3: Iteration: 4000 / 5000 [ 80%] (Sampling)
## Chain 3: Iteration: 4500 / 5000 [ 90%] (Sampling)
## Chain 3: Iteration: 5000 / 5000 [100%] (Sampling)
## Chain 3:
## Chain 3: Elapsed Time: 3.664 seconds (Warm-up)
## Chain 3: 2.763 seconds (Sampling)
## Chain 3: 6.427 seconds (Total)
## Chain 3:
##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 4).
## Chain 4:
## Chain 4: Gradient evaluation took 7.6e-05 seconds
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.76 seconds.
## Chain 4: Adjust your expectations accordingly!
## Chain 4:
## Chain 4:
## Chain 4: Iteration: 1 / 5000 [ 0%] (Warmup)
## Chain 4: Iteration: 500 / 5000 [ 10%] (Warmup)
## Chain 4: Iteration: 1000 / 5000 [ 20%] (Warmup)
## Chain 4: Iteration: 1500 / 5000 [ 30%] (Warmup)
## Chain 4: Iteration: 2000 / 5000 [ 40%] (Warmup)
## Chain 4: Iteration: 2500 / 5000 [ 50%] (Warmup)
## Chain 4: Iteration: 2501 / 5000 [ 50%] (Sampling)
## Chain 4: Iteration: 3000 / 5000 [ 60%] (Sampling)
## Chain 4: Iteration: 3500 / 5000 [ 70%] (Sampling)
## Chain 4: Iteration: 4000 / 5000 [ 80%] (Sampling)
## Chain 4: Iteration: 4500 / 5000 [ 90%] (Sampling)
## Chain 4: Iteration: 5000 / 5000 [100%] (Sampling)
## Chain 4:
## Chain 4: Elapsed Time: 4.172 seconds (Warm-up)
## Chain 4: 2.796 seconds (Sampling)
## Chain 4: 6.968 seconds (Total)
## Chain 4:
plot(no1B_int)

```



```
print(summary(no1B_int), digits = 4)
```

```
## Family: bernoulli
## Links: mu = logit
## Formula: response ~ Musician * scramble + (1 | exp_subject_id)
## Data: data_no1B (Number of observations: 2104)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 105)
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
sd(Intercept)	0.1714	0.0863	0.0125	0.3354	1.0029	1920	2082

```
##
## Regression Coefficients:
##
```

	Estimate	Est.Error	l-95% CI	u-95% CI	Rhat	Bulk_ESS	Tail_ESS
Intercept	0.8786	0.0978	0.6925	1.0734	1.0003	6837	
MusicianNo	-0.1605	0.1351	-0.4267	0.1016	1.0009	6718	
scramble2B	-0.5794	0.1262	-0.8297	-0.3347	0.9999	7641	
MusicianNo:scramble2B	0.2971	0.1768	-0.0456	0.6387	1.0001	6225	

```
##
## Tail_ESS
## Intercept 5842
## MusicianNo 6715
## scramble2B 8120
## MusicianNo:scramble2B 7327
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
```

```
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

```
BF_no1B_int <- bayes_factor(no1B_int, no1B)
```

```
## Iteration: 1
```

```
## Iteration: 2
```

```
## Iteration: 3
```

```
## Iteration: 4
```

```
## Iteration: 5
```

```
## Iteration: 6
```

```
## Iteration: 7
```

```
## Iteration: 1
```

```
## Iteration: 2
```

```
## Iteration: 3
```

```
## Iteration: 4
```

```
## Iteration: 5
```

```
## Iteration: 6
```

```
## Iteration: 7
```

```
print(BF_no1B_int)
```

```
## Estimated Bayes factor in favor of no1B_int over no1B: 0.80461
```

Still moderate evidence against an interaction between group and condition.

Years of experience

Keep only the subjects for which we have years of experience data and average accuracy per condition.

```
yrs_exp <- data %>%  
  filter(!is.na(yrs_mus_exp)) %>%  
  group_by(exp_subject_id, scramble, yrs_mus_exp) %>%  
  summarize(count = n(),  
            n_correct = sum(response),  
            accuracy = n_correct / count)
```

```
## `summarise()` has grouped output by 'exp_subject_id', 'scramble'. You can  
## override using the `.groups` argument.
```

Priors

For this analysis, we're operating on the scale of accuracy. Because we don't see ceiling effects (i.e. participants aren't getting too close to perfect accuracy), a linear model is appropriate enough.

```
these_priors <- c(  
  set_prior('normal(0.75, 0.1)', class = 'Intercept'),  
  set_prior('normal(-0.1, 0.1)', coef = 'scramble2'),  
  set_prior('normal(-0.2, 0.1)', coef = 'scramble3'),  
  set_prior('normal(0, 0.1)', coef = 'yrs_mus_exp')  
)
```



```
years_mus_scram <- brm(accuracy ~ scramble + yrs_mus_exp + (1|exp_subject_id), data = yrs_
prior = these_priors,
save_pars = save_pars(all = TRUE), iter = 5000,
file = 'models/E2_years')
```

25

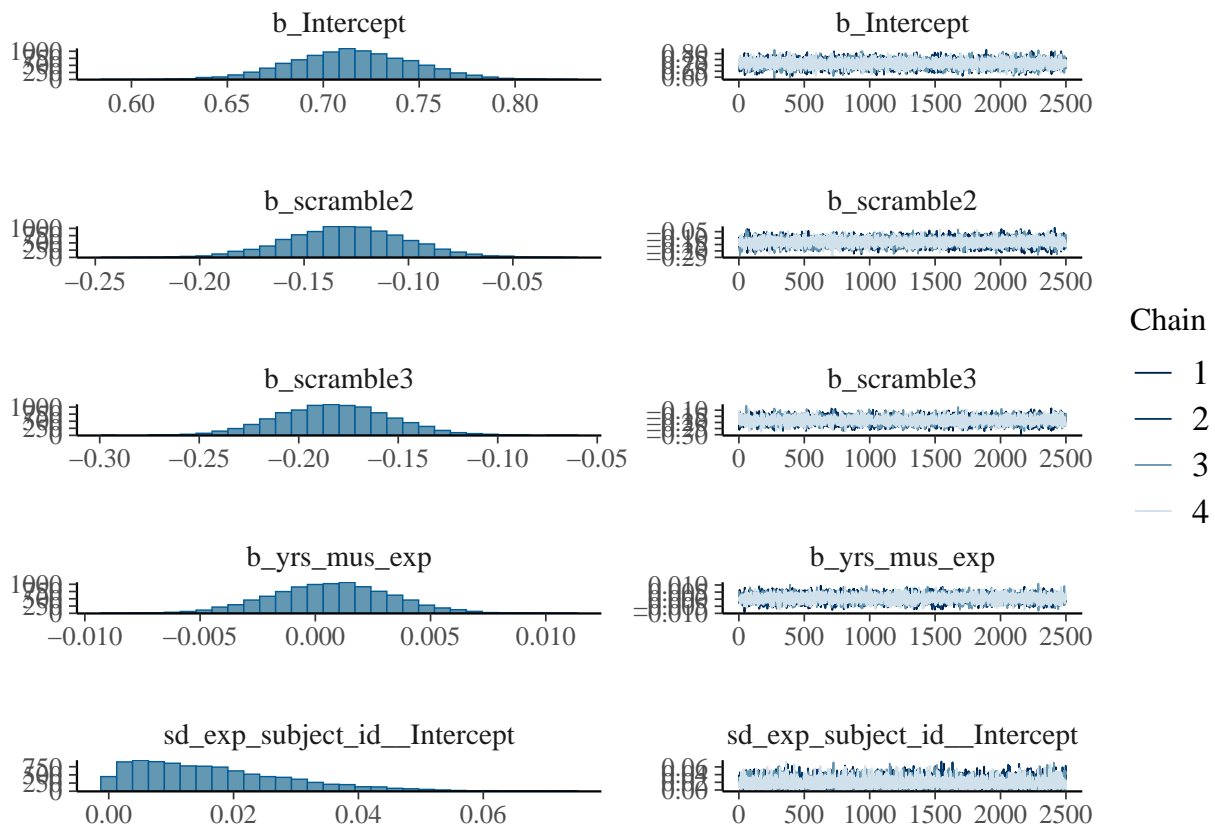
```

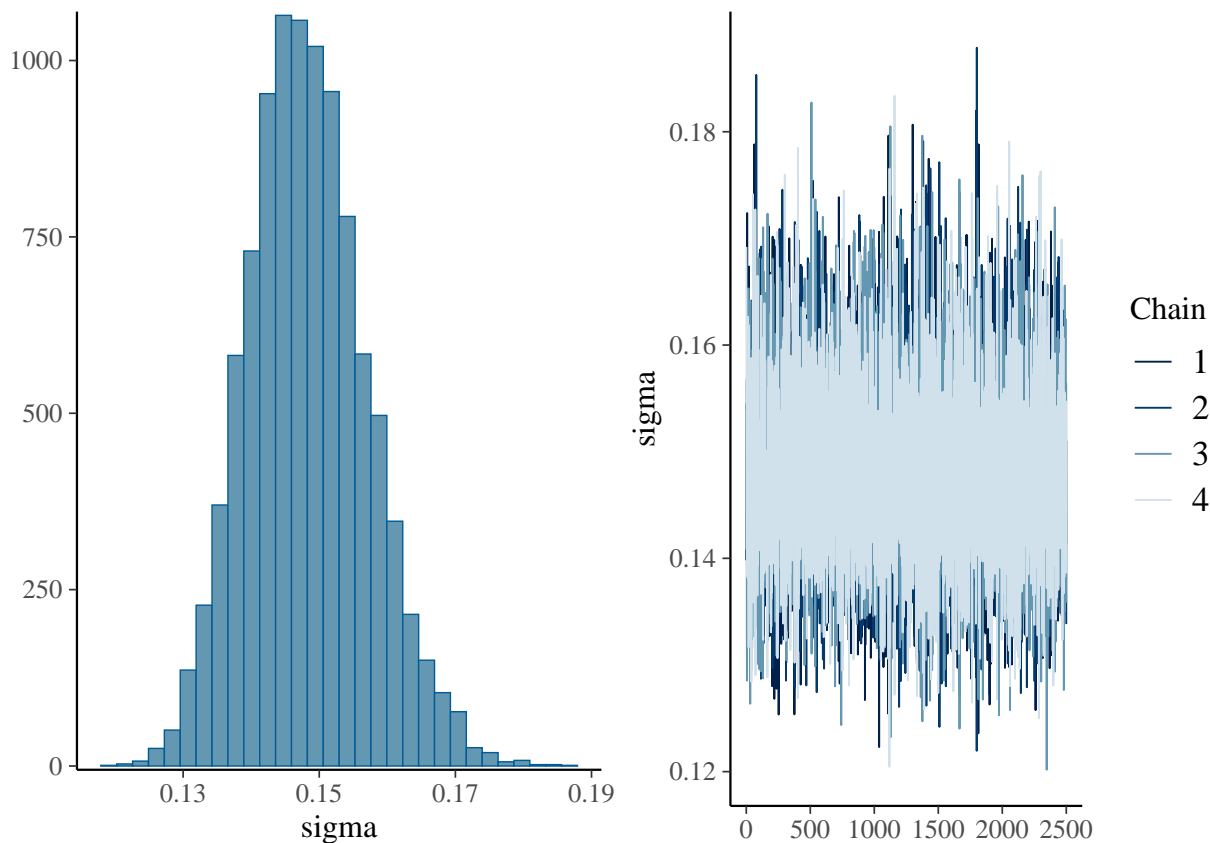
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.07 seconds.
## Chain 2: Adjust your expectations accordingly!
## Chain 2:
## Chain 2:
## Chain 2: Iteration:    1 / 5000 [  0%] (Warmup)
## Chain 2: Iteration:   500 / 5000 [ 10%] (Warmup)
## Chain 2: Iteration:  1000 / 5000 [ 20%] (Warmup)
## Chain 2: Iteration:  1500 / 5000 [ 30%] (Warmup)
## Chain 2: Iteration:  2000 / 5000 [ 40%] (Warmup)
## Chain 2: Iteration:  2500 / 5000 [ 50%] (Warmup)
## Chain 2: Iteration: 2501 / 5000 [ 50%] (Sampling)
## Chain 2: Iteration:  3000 / 5000 [ 60%] (Sampling)
## Chain 2: Iteration:  3500 / 5000 [ 70%] (Sampling)
## Chain 2: Iteration:  4000 / 5000 [ 80%] (Sampling)
## Chain 2: Iteration:  4500 / 5000 [ 90%] (Sampling)
## Chain 2: Iteration:  5000 / 5000 [100%] (Sampling)
## Chain 2:
## Chain 2: Elapsed Time: 1.09 seconds (Warm-up)
## Chain 2:                0.264 seconds (Sampling)
## Chain 2:                1.354 seconds (Total)
## Chain 2:
##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 3).
## Chain 3:
## Chain 3: Gradient evaluation took 1.2e-05 seconds
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.12 seconds.
## Chain 3: Adjust your expectations accordingly!
## Chain 3:
## Chain 3:
## Chain 3: Iteration:    1 / 5000 [  0%] (Warmup)
## Chain 3: Iteration:   500 / 5000 [ 10%] (Warmup)
## Chain 3: Iteration:  1000 / 5000 [ 20%] (Warmup)
## Chain 3: Iteration:  1500 / 5000 [ 30%] (Warmup)
## Chain 3: Iteration:  2000 / 5000 [ 40%] (Warmup)
## Chain 3: Iteration:  2500 / 5000 [ 50%] (Warmup)
## Chain 3: Iteration: 2501 / 5000 [ 50%] (Sampling)
## Chain 3: Iteration:  3000 / 5000 [ 60%] (Sampling)
## Chain 3: Iteration:  3500 / 5000 [ 70%] (Sampling)
## Chain 3: Iteration:  4000 / 5000 [ 80%] (Sampling)
## Chain 3: Iteration:  4500 / 5000 [ 90%] (Sampling)
## Chain 3: Iteration:  5000 / 5000 [100%] (Sampling)
## Chain 3:
## Chain 3: Elapsed Time: 0.771 seconds (Warm-up)
## Chain 3:                0.25 seconds (Sampling)
## Chain 3:                1.021 seconds (Total)
## Chain 3:
##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 4).
## Chain 4:
## Chain 4: Gradient evaluation took 7e-06 seconds
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.07 seconds.
## Chain 4: Adjust your expectations accordingly!
## Chain 4:
## Chain 4:

```

```
## Chain 4: Iteration: 1 / 5000 [ 0%] (Warmup)
## Chain 4: Iteration: 500 / 5000 [ 10%] (Warmup)
## Chain 4: Iteration: 1000 / 5000 [ 20%] (Warmup)
## Chain 4: Iteration: 1500 / 5000 [ 30%] (Warmup)
## Chain 4: Iteration: 2000 / 5000 [ 40%] (Warmup)
## Chain 4: Iteration: 2500 / 5000 [ 50%] (Warmup)
## Chain 4: Iteration: 2501 / 5000 [ 50%] (Sampling)
## Chain 4: Iteration: 3000 / 5000 [ 60%] (Sampling)
## Chain 4: Iteration: 3500 / 5000 [ 70%] (Sampling)
## Chain 4: Iteration: 4000 / 5000 [ 80%] (Sampling)
## Chain 4: Iteration: 4500 / 5000 [ 90%] (Sampling)
## Chain 4: Iteration: 5000 / 5000 [100%] (Sampling)
## Chain 4:
## Chain 4: Elapsed Time: 0.705 seconds (Warm-up)
## Chain 4: 0.256 seconds (Sampling)
## Chain 4: 0.961 seconds (Total)
## Chain 4:
```

```
plot(years_mus_scam)
```





```
print(summary(years_mus_scram), digits = 5)
```

```
## Family: gaussian
## Links: mu = identity; sigma = identity
## Formula: accuracy ~ scramble + yrs_mus_exp + (1 | exp_subject_id)
## Data: yrs_exp (Number of observations: 147)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 49)
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept) 0.01696 0.01257 0.00071 0.04705 1.00025 6157 5414
##
## Regression Coefficients:
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept 0.71535 0.03197 0.65312 0.77851 1.00018 14423 8004
## scramble2 -0.12931 0.02867 -0.18591 -0.07305 1.00061 15820 7708
## scramble3 -0.18209 0.02872 -0.23763 -0.12551 0.99990 14682 7968
## yrs_mus_exp 0.00070 0.00262 -0.00442 0.00586 1.00013 14731 7747
##
## Further Distributional Parameters:
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sigma 0.14825 0.00874 0.13233 0.16689 1.00030 17240 6916
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
```

```
## scale reduction factor on split chains (at convergence, Rhat = 1).
```

Null model (for plotting purposes)

```
years_mus <- brm(accuracy ~ yrs_mus_exp + (1|exp_subject_id), data = yrs_exp,
  prior = c(
    set_prior('normal(0.75, 0.1)', class = 'Intercept'),
    set_prior('normal(0, 0.1)', coef = 'yrs_mus_exp')),
  save_pars = save_pars(all = TRUE), iter = 5000,
  file = 'models/E2_years_null')
```

```
## Compiling Stan program...
```

```
## Trying to compile a simple C file
```

```
## Running /Library/Frameworks/R.framework/Resources/bin/R CMD SHLIB foo.c
```

```
## using C compiler: 'Apple clang version 16.0.0 (clang-1600.0.26.6)'
```

```
## using SDK: 'MacOSX15.2.sdk'
```

```
## clang -arch arm64 -I"/Library/Frameworks/R.framework/Resources/include" -DNDEBUG -I"/Library/Frame
```

```
## In file included from <built-in>:1:
```

```
## In file included from /Library/Frameworks/R.framework/Versions/4.3-arm64/Resources/library/StanHeaders
```

```
## In file included from /Library/Frameworks/R.framework/Versions/4.3-arm64/Resources/library/RcppEigen,
```

```
## In file included from /Library/Frameworks/R.framework/Versions/4.3-arm64/Resources/library/RcppEigen,
```

```
## /Library/Frameworks/R.framework/Versions/4.3-arm64/Resources/library/RcppEigen/include/Eigen/src/Cor
```

```
## 679 | #include <cmath>
```

| ^ ~ ~ ~ ~ ~

```
## 1 error generated.
```

```
## make: *** [foo.o] Error 1
```

```
## Start sampling
```

##

```
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 1).
```

```
## Chain 1:
```

```
## Chain 1: Gradient evaluation took 5.5e-05 seconds
```

```
## Chain 1: 1000 transitions using 10 leapfrog steps per transition would take 0.55 seconds.
```

```
## Chain 1: Adjust your expectations accordingly!
```

```
## Chain 1:
```

```
## Chain 1:
```

```
## Chain 1: Iteration:    1 / 5000 [  0%] (Warmup)
```

```
## Chain 1: Iteration: 500 / 5000 [ 10%] (Warmup)
```

```
## Chain 1: Iteration: 1000 / 5000 [ 20%] (Warmup)
```

```
## Chain 1: Iteration: 1500 / 5000 [ 30%] (Warmup)
```

```
## Chain 1: Iteration: 2000 / 5000 [ 40%] (Warmup)
```

```
## Chain 1: Iteration: 2500 / 5000 [ 50%] (Warmup)
```

```
## Chain 1: Iteration: 2501 / 5000 [ 50%] (Sampling)
```

```
## Chain 1: Iteration: 3000 / 5000 [ 60%] (Sampling)
```

```
## Chain 1: Iteration: 3500 / 5000 [ 70%] (Sampling)
```

```
## Chain 1: Iteration: 4000 / 5000 [ 80%] (Sampling)
```

```
## Chain 1: Iteration: 4500 / 5000 [ 90%] (Sampling)
```

```
## Chain 1: Iteration: 5000 / 5000 [100%] (Sampling)
```

```
## Chain 1:
```

```
## Chain 1: Elapsed Time: 0.67 seconds (Warm-up)
```

```
## Chain 1: 0.246 seconds (Sampling)
```

```
## Chain 1: 0.916 seconds (Sample)
```

```
## Chain 1:
```

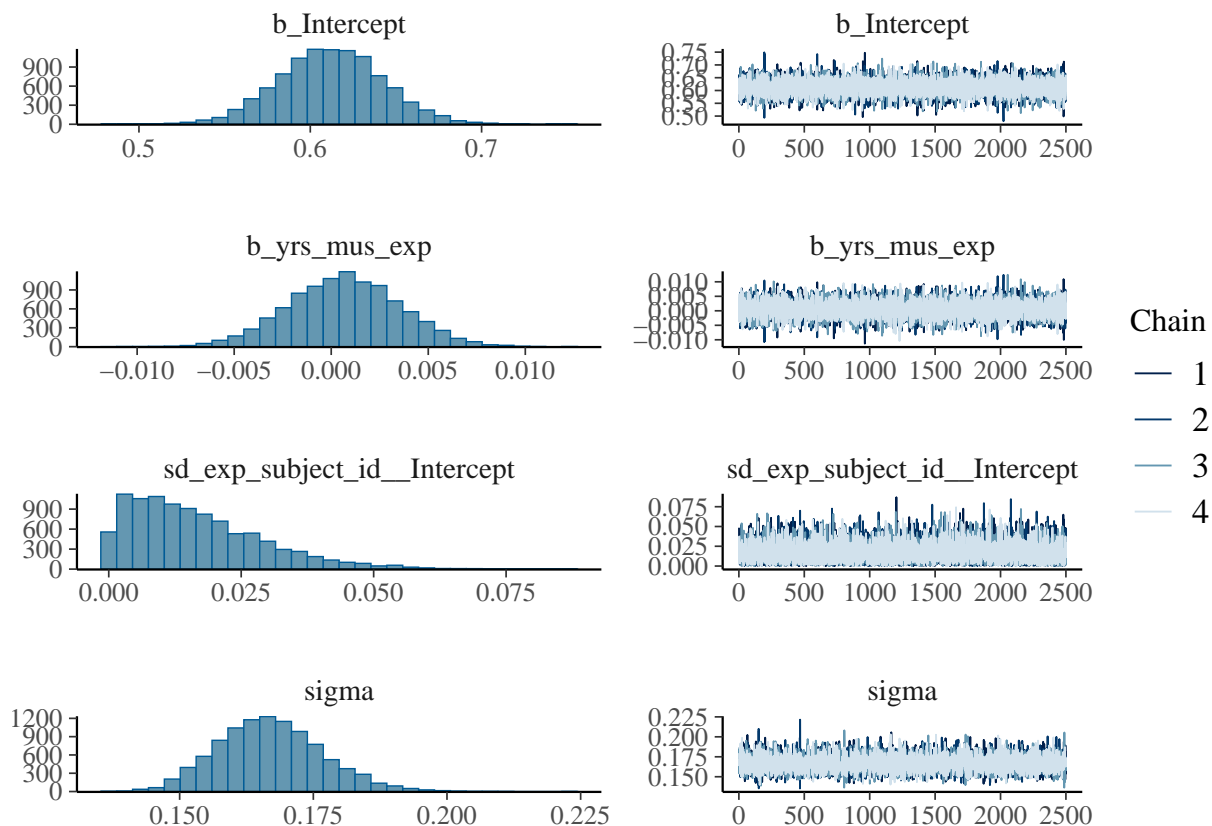
```

##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 2).
## Chain 2:
## Chain 2: Gradient evaluation took 7e-06 seconds
## Chain 2: 1000 transitions using 10 leapfrog steps per transition would take 0.07 seconds.
## Chain 2: Adjust your expectations accordingly!
## Chain 2:
## Chain 2:
## Chain 2: Iteration:    1 / 5000 [  0%] (Warmup)
## Chain 2: Iteration:   500 / 5000 [ 10%] (Warmup)
## Chain 2: Iteration:  1000 / 5000 [ 20%] (Warmup)
## Chain 2: Iteration:  1500 / 5000 [ 30%] (Warmup)
## Chain 2: Iteration:  2000 / 5000 [ 40%] (Warmup)
## Chain 2: Iteration:  2500 / 5000 [ 50%] (Warmup)
## Chain 2: Iteration:  2501 / 5000 [ 50%] (Sampling)
## Chain 2: Iteration:  3000 / 5000 [ 60%] (Sampling)
## Chain 2: Iteration:  3500 / 5000 [ 70%] (Sampling)
## Chain 2: Iteration:  4000 / 5000 [ 80%] (Sampling)
## Chain 2: Iteration:  4500 / 5000 [ 90%] (Sampling)
## Chain 2: Iteration:  5000 / 5000 [100%] (Sampling)
## Chain 2:
## Chain 2: Elapsed Time: 0.662 seconds (Warm-up)
## Chain 2:                0.251 seconds (Sampling)
## Chain 2:                0.913 seconds (Total)
## Chain 2:
##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 3).
## Chain 3:
## Chain 3: Gradient evaluation took 9e-06 seconds
## Chain 3: 1000 transitions using 10 leapfrog steps per transition would take 0.09 seconds.
## Chain 3: Adjust your expectations accordingly!
## Chain 3:
## Chain 3:
## Chain 3: Iteration:    1 / 5000 [  0%] (Warmup)
## Chain 3: Iteration:   500 / 5000 [ 10%] (Warmup)
## Chain 3: Iteration:  1000 / 5000 [ 20%] (Warmup)
## Chain 3: Iteration:  1500 / 5000 [ 30%] (Warmup)
## Chain 3: Iteration:  2000 / 5000 [ 40%] (Warmup)
## Chain 3: Iteration:  2500 / 5000 [ 50%] (Warmup)
## Chain 3: Iteration:  2501 / 5000 [ 50%] (Sampling)
## Chain 3: Iteration:  3000 / 5000 [ 60%] (Sampling)
## Chain 3: Iteration:  3500 / 5000 [ 70%] (Sampling)
## Chain 3: Iteration:  4000 / 5000 [ 80%] (Sampling)
## Chain 3: Iteration:  4500 / 5000 [ 90%] (Sampling)
## Chain 3: Iteration:  5000 / 5000 [100%] (Sampling)
## Chain 3:
## Chain 3: Elapsed Time: 0.646 seconds (Warm-up)
## Chain 3:                0.216 seconds (Sampling)
## Chain 3:                0.862 seconds (Total)
## Chain 3:
##
## SAMPLING FOR MODEL 'anon_model' NOW (CHAIN 4).
## Chain 4:
## Chain 4: Gradient evaluation took 7e-06 seconds

```

```
## Chain 4: 1000 transitions using 10 leapfrog steps per transition would take 0.07 seconds.
## Chain 4: Adjust your expectations accordingly!
## Chain 4:
## Chain 4:
## Chain 4: Iteration: 1 / 5000 [ 0%] (Warmup)
## Chain 4: Iteration: 500 / 5000 [ 10%] (Warmup)
## Chain 4: Iteration: 1000 / 5000 [ 20%] (Warmup)
## Chain 4: Iteration: 1500 / 5000 [ 30%] (Warmup)
## Chain 4: Iteration: 2000 / 5000 [ 40%] (Warmup)
## Chain 4: Iteration: 2500 / 5000 [ 50%] (Warmup)
## Chain 4: Iteration: 2501 / 5000 [ 50%] (Sampling)
## Chain 4: Iteration: 3000 / 5000 [ 60%] (Sampling)
## Chain 4: Iteration: 3500 / 5000 [ 70%] (Sampling)
## Chain 4: Iteration: 4000 / 5000 [ 80%] (Sampling)
## Chain 4: Iteration: 4500 / 5000 [ 90%] (Sampling)
## Chain 4: Iteration: 5000 / 5000 [100%] (Sampling)
## Chain 4:
## Chain 4: Elapsed Time: 0.647 seconds (Warm-up)
## Chain 4: 0.241 seconds (Sampling)
## Chain 4: 0.888 seconds (Total)
## Chain 4:
```

```
plot(years_mus)
```



```
print(summary(years_mus), digits = 4)
```

```
## Family: gaussian
## Links: mu = identity; sigma = identity
## Formula: accuracy ~ yrs_mus_exp + (1 | exp_subject_id)
```

```

## Data: yrs_exp (Number of observations: 147)
## Draws: 4 chains, each with iter = 5000; warmup = 2500; thin = 1;
## total post-warmup draws = 10000
##
## Multilevel Hyperparameters:
## ~exp_subject_id (Number of levels: 49)
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sd(Intercept) 0.0166 0.0125 0.0006 0.0471 1.0003 6184 5124
##
## Regression Coefficients:
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## Intercept 0.6120 0.0306 0.5531 0.6728 1.0000 15649 7815
## yrs_mus_exp 0.0007 0.0029 -0.0050 0.0063 0.9999 15083 6873
##
## Further Distributional Parameters:
## Estimate Est.Error l-95% CI u-95% CI Rhat Bulk_ESS Tail_ESS
## sigma 0.1670 0.0098 0.1494 0.1872 1.0005 17413 7186
##
## Draws were sampled using sampling(NUTS). For each parameter, Bulk_ESS
## and Tail_ESS are effective sample size measures, and Rhat is the potential
## scale reduction factor on split chains (at convergence, Rhat = 1).

```



```
yrs_BF <- describe_posterior(years_mus_scram,
  estimate = "median", dispersion = TRUE,
  ci = .95, ci_method = "HDI",
  test = c("bayes_factor"))
```

Warning: Bayes factors might not be precise.
For precise Bayes factors, sampling at least 40,000 posterior samples is
recommended.

```
print(yrs_BF, digits = 4)
```

Summary of Posterior Distribution

## Parameter	Median	MAD	95% CI	BF	Rhat	ESS
## (Intercept)	0.7150	0.0319	[0.65, 0.78]	1.76e+23	1.000	14188.0000
## scramble2	-0.1292	0.0284	[-0.19, -0.07]	790.53	1.000	15842.0000
## scramble3	-0.1823	0.0286	[-0.24, -0.13]	2.30e+04	1.000	14605.0000
## yrs_mus_exp	0.0007	0.0026	[0.00, 0.01]	0.028	1.000	14554.0000

```
yrs_null_BF <- describe_posterior(years_mus,
  estimate = "median", dispersion = TRUE,
  ci = .95, ci_method = "HDI",
  test = c("bayes_factor"))
```

Warning: Bayes factors might not be precise.
For precise Bayes factors, sampling at least 40,000 posterior samples is
recommended.

```
print(yrs_null_BF, digits = 4)
```

Summary of Posterior Distribution

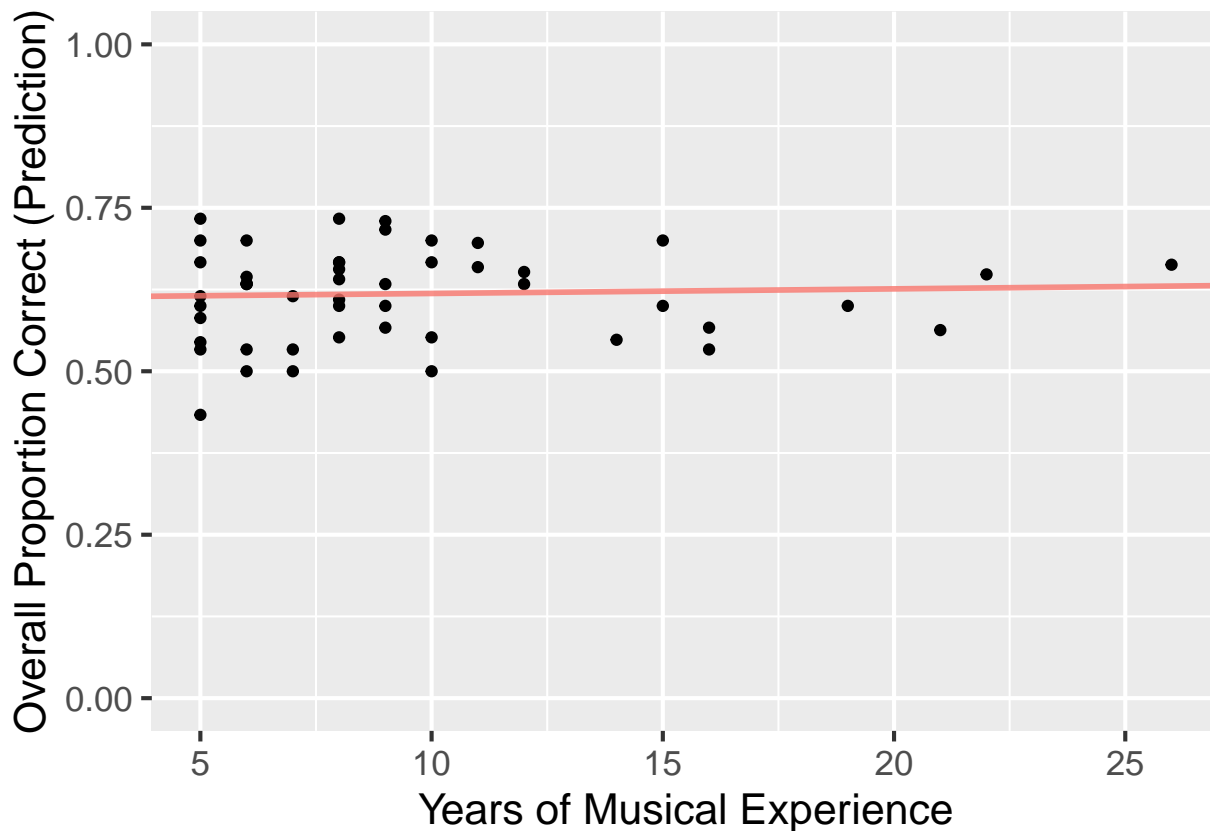
## Parameter	Median	MAD	95% CI	BF	Rhat	ESS
## (Intercept)	0.6119	0.0303	[0.55, 0.67]	9.83e+20	1.000	15621.0000
## yrs_mus_exp	0.0007	0.0029	[0.00, 0.01]	0.030	1.000	15081.0000

Strong evidence against an effect of years of musical experience.

Figure S1B

```
yrs_exp %>%
  group_by(exp_subject_id, yrs_mus_exp) %>%
  summarize(mean_acc = mean(accuracy)) %>%
  ggplot(aes(yrs_mus_exp, mean_acc)) +
  geom_point() +
  geom_abline(intercept = yrs_null_BF$Median[1], slope = yrs_null_BF$Median[2],
              color = '#F8766D', linewidth = 1, alpha = 0.8) +
  xlab('Years of Musical Experience') +
  ylab('Overall Proportion Correct (Prediction)') +
  scale_x_continuous(breaks = seq(5,30,5)) +
  scale_y_continuous(breaks = seq(0, 1, 0.1)) +
  ylim(0,1) +
  theme_gray(base_size = 16)
```

```
## `summarise()` has grouped output by 'exp_subject_id'. You can override using
## the `groups` argument.
## Scale for y is already present. Adding another scale for y, which will replace
## the existing scale.
```



```
ggsave('../figures/FigS1B_prediction.png', width = 5, height = 5)
```