E3_compute_precision_sensitivity

October 31, 2024

```
[1]: #Python version 3.11.7
    #Jupyter Notebook version 7.0.8
    import numpy as np # version 1.26.4
    from scipy import stats # version 1.11.4
    import pandas as pd # version 2.1.4
    import matplotlib.pyplot as plt # version 3.8.0

plt.rcParams["font.family"] = "Arial"
    plt.rcParams["font.size"] = 12
```

The following levels are considered: - scramble boundaries: 1 bar (2 seconds) - scramble boundaries: 2 bars (4 seconds) - every 3 bars (6 seconds) - half-phrase: 4 bars (8 seconds) - every 5 bars (10 seconds) - phrase: 8 bars (16 seconds) - half-section: 16 bars (32 seconds)

Final alignment plot (figure 4): each panel in the final plot will show all of the above levels. Each condition is a different color. Musicians and non-musicians will be in separate subplots.

1 Load the data and ground truth

Load the timestamps.

```
[2]: timestamps = pd.read_csv('../data/timestamps_filtered_long.csv')
print(timestamps)
```

	<pre>exp_subject_id</pre>	Musician	stimulus_set	scramble	${\tt stim_num}$	value
0	377777	No	1	2B	1	6.924
1	377777	No	1	2B	1	27.737
2	377777	No	1	2B	1	37.522
3	377777	No	1	2B	1	45.708
4	377777	No	1	2B	1	61.284
•••	•••	•••		•••	•••	
3547	611455	No	3	2B	12	52.989
3548	611455	No	3	2B	12	63.226
3549	611455	No	3	Intact	1	32.335
3550	611455	No	3	Intact	1	58.304
3551	611455	No	3	Intact	2	32.814

[3552 rows x 6 columns]

```
[4]: # load ground truths
gts = pd.read_csv('../data/combined/ground_truths.csv')
# remove last column (NaNs - IDK why it's there)
gts = gts.drop("Unnamed: 5", axis=1)
print(gts)
```

stimulus_set	scramble	$stim_num$	level	boundary_time
1	Intact	1	16	34
1	Intact	1	16	66
1	Intact	1	8	18
1	Intact	1	8	34
1	Intact	1	8	50
•••	•••			•••
4	1B	16	1	52
4	1B	16	1	54
4	1B	16	1	56
4	1B	16	1	58
4	1B	16	1	60
	1 1 1 1 1 4 4 4	1 Intact 4 1B 4 1B 4 1B 4 1B	1 Intact 1 4 IB 16 4 IB 16 4 IB 16 4 IB 16	1 Intact 1 16 1 Intact 1 8 1 Intact 1 8 1 Intact 1 8 1 Intact 1 8 4 1B 16 1 4 1B 16 1 4 1B 16 1 4 1B 16 1

[3176 rows x 5 columns]

2 Functions

```
[5]: def compute_ps_chance(data, gt, window_before=0.25, window_after=1.0,_
      ⇒samples=1000):
         Computes precision, sensitivity, and alignment (F) for single subject, \Box

¬single condition - used within `ps_wrapper`

         Default window before is 0.25 seconds, default window after is 1.0 seconds. \Box
      →Number of samples used to make null distribution is 1000.
         levels = pd.unique(gt['level'])
         trials = pd.unique(data['stim_num'])
         output = np.zeros([3, len(levels)]) # first dim is precision, sensitivity,
      \hookrightarrow F; second dim is each level
         for level in range(len(levels)):
             # what are the ground truth boundary times for this level?
             these_gt_vals_both = gt[gt['level'] == levels[level]]
             # set up list to hold both trials
             precision = []
             sensitivity = []
             avg_chance_precision = []
             avg_chance_sensitivity = []
```

```
for tr in trials:
           # grab the responses for this trial
           these_responses = data[data['stim_num'] == tr]['value'].to_numpy()
           total_responses = np.shape(these_responses)[0]
           these_gt_vals = these_gt_vals_both[these_gt_vals_both['stim_num']_u
←== tr]['boundary_time'].to_numpy()
           # compute the number of "in window responses"
           # for each GT boundary, is there a response in the window around \square
\rightarrow that?
           in_window_response_by_bound = np.zeros(these_gt_vals.shape[0])
           for w in range(len(these gt vals)):
               # define the "in-window" range
               range_before = these_gt_vals[w] - window_before
               range_after = these_gt_vals[w] + window_after
               # for each response, check if the response is in the range
               for r in these_responses:
                   if r > range_before and r <= range_after:</pre>
                       # if it is, set the corresponding in-window count to 1
                       in_window_response_by_bound[w] = 1 # this prevents_
⇔double-counting
                   # otherwise do nothing
           in_window_responses = np.sum(in_window_response_by_bound)
           # compute precision and sensitivity
           precision.append(in_window_responses / total_responses)
           sensitivity.append(in_window_responses / np.shape(these_gt_vals)[0])
           # compute chance using a bootstrap approach
           # lists to hold results from many samples
           chance_precision = []
           chance_sensitivity = []
           for sample in range(samples):
               # generate random responses
               responses_random = np.random.rand(total_responses) * 68 # to_
→account for length of trial
               # compute the number of "in window responses"
               # for each GT boundary, is there a response in the window_
→around that?
               in_window_response_by_bound = np.zeros(these_gt_vals.shape[0])
               for w in range(len(these_gt_vals)):
                   # define the "in-window" range
                   range_before = these_gt_vals[w] - window_before
```

```
range_after = these_gt_vals[w] + window_after
                        # for each response, check if the response is in the range
                        for r in responses_random:
                           if r > range_before and r <= range_after:</pre>
                                # if it is, set the corresponding in-window count_
     \hookrightarrow t_0 1
                                in window response by bound[w] = 1 # this prevents.
      \hookrightarrow double-counting
                            # otherwise do nothing
                    in window responses = np.sum(in window response by bound)
                    chance_precision.append(in_window_responses / total_responses)
                    chance_sensitivity.append(in_window_responses / np.
     ⇒shape(these_gt_vals)[0])
                avg_chance_precision.append(np.mean(chance_precision))
                avg_chance_sensitivity.append(np.mean(chance_sensitivity))
            # take the mean and adjust for chance
            precision_mean_adj = np.mean(precision) - np.mean(avg_chance_precision)
            sensitivity mean adj = np.mean(sensitivity) - np.
      →mean(avg_chance_sensitivity)
            ⇔output array
            output[0,level] = precision mean adj
            output[1,level] = sensitivity_mean_adj
            # compute and save F
            if precision_mean_adj == 0.0 and sensitivity_mean_adj == 0.0:
      \rightarrowoutput[2,level] = 0.0
            else: output[2,level] = (2 * precision_mean_adj * sensitivity_mean_adj)_u
      return output
[6]: def ps_wrapper(data, gt, group, stimulus_set, window_before=0.25,__
     →window_after=1.0, samples=1000):
        # all the data gets passed, so first have to filter by group and stimulus_
        this_data = data[data['Musician'] == group]
        this_data = this_data[this_data['stimulus_set'] == stimulus_set]
        # pull out subject ids
```

```
sub_ids = pd.unique(this_data['exp_subject_id'])
  # the conditions array should be defined earlier in the notebook, but copy_
→it here for sanity
  conditions = ['Intact', '8B', '2B', '1B']
  # pull out the levels (compute_ps also does this)
  levels = pd.unique(gt['level'])
  # initialize the output array
  \# 3 (P,S,F) x number of subjects x number of conditions x number of levels
  output = np.zeros([3, np.shape(sub_ids)[0], len(conditions), len(levels)])
  # each subject individually
  for s in range(sub_ids.shape[0]):
      this_sub_data = this_data[this_data['exp_subject_id'] == sub_ids[s]]
      # further, filter by condition
      for c in range(len(conditions)):
          this_cond_data = this_sub_data[this_sub_data['scramble'] ==_
⇔conditions[c]]
          if this_cond_data.empty:
               #print("Subject %s is missing data." %sub_ids[s])
              continue
          this_gt = gt[gt['scramble'] == conditions[c]]
          output[:,s,c,:] = compute_ps_chance(this_cond_data, this_gt,
                                               window_before=window_before,_
→window after=window after, samples=samples)
  return output
```

3 Compute precision, sensitivity, and overall alignment

ps_wrapper takes one group (musician/non-musician) and one stimulus set at a time.

```
[7]: psf_M_1 = ps_wrapper(timestamps, gts, group='Yes', stimulus_set=1)
psf_M_3 = ps_wrapper(timestamps, gts, group='Yes', stimulus_set=3)
psf_M_4 = ps_wrapper(timestamps, gts, group='Yes', stimulus_set=4)
psf_NM_1 = ps_wrapper(timestamps, gts, group='No', stimulus_set=1)
psf_NM_3 = ps_wrapper(timestamps, gts, group='No', stimulus_set=3)
psf_NM_4 = ps_wrapper(timestamps, gts, group='No', stimulus_set=4)
# this cell takes a bit
```

Combine all stimulus sets.

```
[9]: psf_M_all = np.concatenate((psf_M_1, psf_M_3, psf_M_4), axis = 1)
    psf_NM_all = np.concatenate((psf_NM_1, psf_NM_3, psf_NM_4), axis = 1)
```

```
[10]: print(np.shape(psf_M_all))
print(np.shape(psf_NM_all))
```

```
(3, 45, 4, 7)
(3, 45, 4, 7)
```

Data structure is P/S/F x number of subjects x condition x levels.

3.1 Save alignment values

Wrangle F values into a long form with labels so we can read it in R. If anyone has any suggestions for how to do this more efficiently, please let me know:)

```
[14]: levels = ['16', '8', '5', '4', '3', '2', '1']
```

```
[16]: f = psf_M_all[2,:,:,:]
```

Separate each condition and save as a separate dataframe

```
[17]: f_I = pd.DataFrame(f[:,0,:], columns = levels)
    f_I.insert(0, 'scramble', 'Intact')
    f_8B = pd.DataFrame(f[:,1,:], columns = levels)
    f_8B.insert(0, 'scramble', '8B')
    f_2B = pd.DataFrame(f[:,2,:], columns = levels)
    f_2B.insert(0, 'scramble', '2B')
    f_1B = pd.DataFrame(f[:,3,:], columns = levels)
    f_1B.insert(0, 'scramble', '1B')
```

```
[18]: # concatenate
f_M = pd.concat([f_I, f_8B, f_2B, f_1B])
# reset index so we have a subject column
f_M = f_M.reset_index()
f_M = f_M.rename(columns = {"index": "sub"})
# add a group column
f_M.insert(0, 'Musician', 'Yes')
```

```
[19]: print(f_M)
```

```
Musician
           sub scramble
                                      8
                                              5
                            16
0
                 Intact 0.092180 0.029338 -0.052741 -0.013109 0.008378
       Yes
                 Intact 0.076953 -0.065617 -0.039501 -0.129176 -0.071079
1
       Yes
             1
2
       Yes
             2
                Intact -0.056000 -0.062857 -0.063950 -0.069115 -0.068206
3
       Yes
             3
                Intact 0.447246 0.222488 -0.014428 0.085393 0.024988
4
             4
                Intact -0.045513 -0.049706 -0.049871 -0.051598 -0.051099
       Yes
. .
                    175
       Yes
            40
       Yes
            41
                    176
177
       Yes
            42
                    1B 0.198519 0.208151 -0.016299 0.233151 -0.086834
178
       Yes
            43
                    1B 0.074500 -0.011125 0.033000 -0.012333 0.063667
179
       Yes
            44
                    1B 0.114200 0.310857 0.302111 0.117364 0.048929
```

```
1
         -0.111014 -0.079989
     2
         -0.070340 -0.051410
     3
          0.009150 0.019770
     4
         -0.014525 -0.024580
     . .
     175 0.000000 0.000000
     176 0.063928 0.042361
     177
          0.049953 -0.008668
     178 -0.069650 0.024676
     179 0.191000 0.083694
     [180 rows x 10 columns]
     Repeat for non-musicians
[20]: f = psf_NM_all[2,:,:,:]
      f_I = pd.DataFrame(f[:,0,:], columns = levels)
      f_I.insert(0, 'scramble', 'Intact')
      f 8B = pd.DataFrame(f[:,1,:], columns = levels)
      f_8B.insert(0, 'scramble', '8B')
      f 2B = pd.DataFrame(f[:,2,:], columns = levels)
      f_2B.insert(0, 'scramble', '2B')
      f_1B = pd.DataFrame(f[:,3,:], columns = levels)
      f_1B.insert(0, 'scramble', '1B')
      # concatenate
      f_NM = pd.concat([f_I, f_8B, f_2B, f_1B])
      # reset index so we have a subject column
      f_NM = f_NM.reset_index()
      f_NM = f_NM.rename(columns = {"index": "sub"})
      # add a group column
      f_NM.insert(0, 'Musician', 'No')
[21]: print(f_NM)
                   sub scramble
                                                                                 3 \
         Musician
                                       16
                                                  8
                                                             5
                     0
                         Intact -0.031429 -0.030462 -0.036842 -0.034240 -0.033636
     0
               No
     1
               No
                         Intact -0.046273 -0.050119 -0.050346 -0.051160 -0.053852
     2
               No
                         Intact -0.094570 0.058013 -0.057804 0.016128 0.072560
     3
                     3
                         Intact 0.184605 0.067875 -0.079070 -0.004863 -0.085352
               No
     4
                     4
               No
                         Intact -0.065915 -0.142856 0.018058 -0.067925 0.108733
                    40
                             1B 0.073097 0.120352 -0.148001 0.108612
     175
                                                                        0.040119
               No
     176
               No
                    41
                             1B -0.029418 0.053685 0.027600 -0.007265
                                                                          0.250436
                             1B -0.030400 -0.030000 0.119538 -0.032000 0.053304
     177
               No
                    42
```

2

0.007587 0.007182

0

```
178
          No
               43
                        1B -0.052000 -0.056800 -0.059714 -0.062020 0.021518
                        1B 0.075264 -0.165842 0.025425 -0.112314 -0.034047
179
          No
               44
            2
                      1
   -0.034776 -0.035253
0
   -0.054053 -0.033572
1
    0.047997 0.008747
3
   -0.045718 -0.061631
     0.070121 0.114615
175 0.124664 0.043521
176 0.189848 0.118477
177 -0.036364 0.023015
178 0.055352 -0.008931
179 -0.066093 -0.076170
[180 rows x 10 columns]
```

Concatenate across both groups and save

```
[23]: f_all = pd.concat([f_M, f_NM])
f_all.to_csv('alignment.csv', index = False)
```

Only issue is that both musicians and non-musicans are both labelled 0-44. This is addressed in E3_alignment.Rmd

4 Plot alignment values

```
[24]: conditions = ['Intact', '8B', '2B', '1B']
  cond_colors = ['red', 'orange', 'green', 'blue']
  cond_jitter = [-.225, -.075, .075, .225]
  levels = np.asarray([1,2,3,4,5,8,16])
  levels = np.flip(levels)
```

```
ax[1].plot(levels + cond_jitter[c], np.nanmean(psf_NM_all[2,:,c,:],_
 ⇒axis=0), color = cond_colors[c], alpha = 1,
               label = conditions[c])
   ax[1].scatter(levels + cond_jitter[c], np.nanmean(psf_NM_all[2,:,c,:],__
 ⇒axis=0), color = cond_colors[c], alpha = 1)
    ax[1].errorbar(levels + cond_jitter[c], np.nanmean(psf_NM_all[2,:,c,:],_
 ⇔axis=0),
                   yerr = stats.sem(psf_NM_all[2,:,c,:], axis=0, nan_policy =__
 color = cond_colors[c], capsize = 3, alpha = 0.4)
ax[0].set_ylabel('Overall Alignment', fontsize = 22)
ax[0].set_title('Musicians', fontsize = 20)
ax[1].set_title('Non-musicians', fontsize = 20)
for col in range(2):
    ax[col].set_xlim(0, 17)
   ax[col].hlines(0,17,0, color = 'black', alpha = 0.2)
   ax[col].set_xticks(levels)
   ax[col].set xticklabels(levels, fontsize = 16)
   ax[col].tick_params(axis='y', which='major', labelsize=14)
   ax[col].set xlabel('Level (Bars)', fontsize = 18)
   ax[col].legend(fontsize=16)
#plt.savefiq('alignment.png', dpi=500)
```



