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## 1 Number theory

### 1.1 Bigmod, Inverse Mod

```

1 ll bigmod(ll a, ll b, ll mod){
2     ll res = 1;
3     while (b > 0){
4         if (b & 1) res = (res * a) % mod;
5         a = (a * a) % mod;
6         b >>= 1;
7     }
8     return res;
9 }
10
11 ll inverse_mod(ll a, ll b) {
12     return 1 < a ? b - inverse_mod(b % a, a) * b / a : 1;
13 }
14 ll inv[N]; // inverse modulo pre calculate
15 void imod() {
16     inv[1] = 1;
17     for (ll i = 2; i < N; i++) inv[i] = (mod - (mod / i) * inv[mod % i]) % mod;
18 }
19 // another way to find inverse modulo of n is
20 ll inv_of_n = bigmod(n, mod - 2, mod);

```

### 1.2 inclusion-exclusion - number of multiples of divs in [l, r]

```

1 ll iep(int l, int r) {
2     if (l > r) return 0;
3     ll sum = 0, sz = divs.size();
4     for (ll j = 1; j < (1LL << sz); j++) {
5         ll gun = 1, one = 0;
6         for (ll i = 0; i < sz; i++)
7             if (j & (1LL << i)) {
8                 one++; gun *= divs[i];
9             }
10        ll mult = (r / gun) - ((l - 1) / gun);
11        if (one % 2 == 1) sum += mult;
12        else sum -= mult;
13    }
14    return sum;
15 }
16

```

### 1.3 Linear Sieve

```

1 const ll N = 10000000;
2 vector<ll> lp(N+1), pr;
3
4 for (ll i=2; i <= N; ++i) {
5     if (lp[i] == 0) {
6         lp[i] = i; pr.push_back(i);
7     }
8     for (ll j=0; j < (ll)pr.size() && pr[j] <= lp[i] && i*pr[j] <= N; ++j) {
9         lp[i * pr[j]] = pr[j];
10    }
11 }

```

### 1.4 Phi Function[n]/ Phi Sieve[1 to n]

```

1 int phi(int n) {
2     int result = n;
3     for (int i = 2; i * i <= n; i++) {
4         if (n % i == 0) {
5             while (n % i == 0) n /= i;
6             result -= result / i;
7         }
8     }
9     if (n > 1)
10        result -= result / n;
11    return result;
12 }
13
14 void phi_1_to_n(int n) {
15     vector<int> phi(n + 1);
16     for (int i = 0; i <= n; i++)
17         phi[i] = i;
18
19     for (int i = 2; i <= n; i++)
20         if (phi[i] == i)
21             for (int j = i; j <= n; j += i)
22                 phi[j] -= phi[j] / i;
23 }

```

### 1.5 Extended Euclid

```

1 ll extended_euclid(ll a, ll b, ll &x, ll &y) {
2     if (b == 0) {
3         x = 1; y = 0;
4         return a;
5     }

```

```

6   ll x1, y1;
7   ll d = extended_euclid(b, a % b, x1, y1);
8   x = y1;
9   y = x1 - y1 * (a / b);
10  return d;
11 }

```

```

40      Matrix single = Matrix();
41      single.a[0][0] = 1 ; single.a[0][1] = 1 ; single.a[1][0] = 1 ;
↪      single.a[1][1] = 0 ;
42      Matrix ans = expo_power(single,k);
43  }
44
45

```

## 1.6 MatExpo

```

1  const ll mod = 1e9 + 7;
2  #define REP(i, n) for(int i = 0; i < (n); i++)
3  ll sz ;
4  struct Matrix {
5      vector<vector<ll>> a = vector<vector<ll>>(sz,vector<ll>(sz)) ;
6      Matrix() {
7          REP(i, sz) {
8              REP(j, sz) {
9                  a[i][j] = 0;
10             }
11         }
12     }
13     Matrix operator *(Matrix other) {
14         Matrix product = Matrix();
15         REP(i, sz) {
16             REP(j, sz) {
17                 REP(k, sz) {
18                     product.a[i][k] += a[i][j] *
↪      other.a[j][k];
19                 }
20                 product.a[i][k] %= mod;
21             }
22         }
23         return product;
24     }
25 };
26 Matrix expo_power(Matrix a, long long n) {
27     Matrix res = Matrix();
28     for (ll i = 0 ; i < sz ; i++) res.a[i][i] = 1 ;
29     while(n) {
30         if(n % 2) {
31             res = res * a;
32         }
33         n /= 2;
34         a = a * a;
35     }
36     return res;
37 }
38 int main() {
39     sz = 2 ; ll k = 7 ;

```

## 1.7 CRT

```

1  using T = __int128;
2  // ax + by = __gcd(a, b)
3  // returns __gcd(a, b)
4  T extended_euclid(T a, T b, T &x, T &y) {
5      T xx = y = 0;
6      T yy = x = 1;
7      while (b) {
8          T q = a / b;
9          T t = b; b = a % b; a = t;
10         t = xx; xx = x - q * xx; x = t;
11         t = yy; yy = y - q * yy; y = t;
12     }
13     return a;
14 }
15 // finds x such that x % m1 = a1, x % m2 = a2. m1 and m2 may not be coprime
16 // here, x is unique modulo m = lcm(m1, m2). returns (x, m). on failure, m = -1.
17 pair<T, T> CRT(T a1, T m1, T a2, T m2) {
18     T p, q;
19     T g = extended_euclid(m1, m2, p, q);
20     if (a1 % g != a2 % g) return make_pair(0, -1);
21     T m = m1 / g * m2;
22     p = (p % m + m) % m;
23     q = (q % m + m) % m;
24     return make_pair((p * a2 % m * (m1 / g) % m + q * a1 % m * (m2 / g) % m) % m,
↪      m);
25 }
26 //cout << (int)CRT(1, 31, 0, 7).first << '\n';

```

## 1.8 Miller Rabin Primality Test

```

1  /* Miller Rabin Primality Test for <= 10^18 */
2  #define ll long long
3
4  ll mulmod(ll a, ll b, ll c) {
5      ll x = 0, y = a % c;
6      while (b) {
7          if (b & 1) x = (x + y) % c;

```

```

8         y = (y << 1) % c;
9         b >>= 1;
10    }
11    return x % c;
12 }
13 ll fastPow(ll x, ll n, ll MOD) {
14     ll ret = 1;
15     while (n) {
16         if (n & 1) ret = mulmod(ret, x, MOD);
17         x = mulmod(x, x, MOD);
18         n >>= 1;
19     }
20     return ret % MOD;
21 }
22 bool isPrime(ll n) {
23     if (n == 2 || n == 3) return true;
24     if (n == 1 || !(n & 1)) return false;
25     ll d = n - 1;
26     int s = 0;
27     while (d % 2 == 0) {
28         s++;
29         d /= 2;
30     }
31
32     int a[9] = { 2, 3, 5, 7, 11, 13, 17, 19, 23 };
33     for (int i = 0; i < 9; i++) {
34         if (n == a[i]) return true;
35         bool comp = fastPow(a[i], d, n) != 1;
36         if (comp) for (int j = 0; j < s; j++) {
37             ll fp = fastPow(a[i], (1LL << (11)j) * d, n);
38             if (fp == n - 1) {
39                 comp = false;
40                 break;
41             }
42         }
43         if (comp) return false;
44     }
45     return true;
46 }

```

## 1.9 FFT

```

1  /**
2  * Multiply (7x^2 + 8x^1 + 9x^0) with (6x^1 + 5x^0)
3  * ans = 42x^3 + 83x^2 + 94x^1 + 45x^0
4  * A = {9, 8, 7}
5  * B = {5, 6}
6  * V = multiply(A,B)
7  * V = {45, 94, 83, 42}

```

```

8  /**/
9  /** Tricks
10 * Use vector < bool > if you need to check only the status of the sum
11 * Use bigmod if the power is over same polynomial && power is big
12 * Use long double if you need more precision
13 * Use long long for overflow
14 */
15 typedef vector<int> vi;
16 const double PI = 2.0 * acos(0.0);
17 using cd = complex<double>;
18 void fft(vector<cd> &a, bool invert = 0) {
19     int n = a.size();
20     for (int i = 1, j = 0; i < n; i++) {
21         int bit = n >> 1;
22         for (; j & bit; bit >>= 1)
23             j ^= bit;
24         j ^= bit;
25
26         if (i < j)
27             swap(a[i], a[j]);
28     }
29     for (int len = 2; len <= n; len <= 1) {
30         double ang = 2 * PI / len * (invert ? -1 : 1);
31         cd wlen(cos(ang), sin(ang));
32         for (int i = 0; i < n; i += len) {
33             cd w(1);
34             for (int j = 0; j < len / 2; j++) {
35                 cd u = a[i + j], v = a[i + j + len / 2] * w;
36                 a[i + j] = u + v;
37                 a[i + j + len / 2] = u - v;
38                 w *= wlen;
39             }
40         }
41     }
42     if (invert) {
43         for (cd &x : a)
44             x /= n;
45     }
46 }
47
48 void ifft(vector<cd> &p) { fft(p, 1); }
49
50 vi multiply(vi const &a, vi const &b) {
51     vector<cd> fa(a.begin(), a.end()), fb(b.begin(), b.end());
52     int n = 1;
53     while (n < a.size() + b.size())
54         n <= 1;
55     fa.resize(n);
56     fb.resize(n);

```

```

57     fft(fa);
58     fft(fb);
59     for (int i = 0; i < n; i++)
60         fa[i] *= fb[i];
61     ifft(fa);
62
63     vi result(n);
64     for (int i = 0; i < n; i++)
65         result[i] = round(fa[i].real());
66     return result;
67 }
68

```

## 1.10 NTT

```

1  /**
2   Iterative Implementation of Number Theoretic Transform
3   Complexity: O(N log N)
4   Slower than regular fft
5   Possible Optimizations:
6   1. Remove trailing zeroes
7   2. Keep the mod const
8
9   Suggested mods (mod, root, inv, pw) :
10  7340033, 5, 4404020, 1<<20
11  13631489, 11799463, 6244495, 1<<20
12  23068673, 177147, 17187657, 1<<21
13  463470593, 428228038, 182429, 1<<21
14  415236097, 73362476, 247718523, 1<<22
15  918552577, 86995699, 324602258, 1<<22
16  998244353, 15311432, 469870224, 1<<23
17  167772161, 243, 114609789, 1<<25
18  469762049, 2187, 410692747, 1<<26
19  If required mod is not above, use nttdata function OFFLINE.
20  If pw=1<<k, a polynomial can have at most (1<<k) degree.
21  */
22  #include<bits/stdc++.h>
23  using namespace std;
24
25  namespace ntt {
26      int N;
27      vector<int> perm;
28      vector<int> wp[2][30];
29      const int mod = 998244353, root = 15311432, inv = 469870224, pw = 1<<23;
30
31      int power(int a, int p) {
32          if (p==0) return 1;
33          int ans = power(a, p/2);
34          ans = (ans * 1LL * ans)%mod;

```

```

35         if (p%2) ans = (ans * 1LL * a)%mod;
36         return ans;
37     }
38
39     void precalculate() {
40         perm.resize(N);
41         perm[0] = 0;
42
43         for (int k=1; k<N; k<=1) {
44             for (int i=0; i<k; i++) {
45                 perm[i] <= 1;
46                 perm[i+k] = 1 + perm[i];
47             }
48         }
49
50         for (int b=0; b<2; b++) {
51             for (int idx = 0, len = 2; len <= N; idx++, len <= 1) {
52                 int factor = b ? inv : root;
53                 for (int i = len; i < pw; i <= 1)
54                     factor = (factor*1LL*factor)%mod;
55
56                 wp[b][idx].resize(N);
57                 wp[b][idx][0] = 1;
58                 for (int i = 1; i < len; i++)
59                     wp[b][idx][i] = (wp[b][idx][i-1]*1LL*factor)%mod;
60             }
61         }
62     }
63
64     void fft(vector<int> &v, bool invert = false) {
65         if (v.size() != perm.size()) {
66             N = v.size();
67             assert(N && (N&(N-1)) == 0);
68             precalculate();
69         }
70
71         for (int i=0; i<N; i++)
72             if (i < perm[i])
73                 swap(v[i], v[perm[i]]);
74
75         for (int idx = 0, len = 2; len <= N; idx++, len <= 1) {
76             for (int i=0; i<N; i+=len) {
77                 for (int j=0; j<len/2; j++) {
78                     int x = v[i+j];
79                     int y = (wp[invert][idx][j]*1LL*v[i+j+len/2])%mod;
80                     v[i+j] = (x+y>=mod ? x+y-mod : x+y);
81                     v[i+j+len/2] = (x-y>=0 ? x-y : x-y+mod);
82                 }
83             }

```

```

84     }
85     if (invert) {
86         int n1 = power(N, mod-2);
87         for (int &x : v) x = (x*1LL*n1)%mod;
88     }
89 }
90
91 vector<int> multiply(vector<int> a, vector<int> b) {
92     int n = 1;
93     while(a.back() == 0 && !a.empty()) a.pop_back();
94     while(b.back() == 0 && !b.empty()) b.pop_back();
95
96     while (n < a.size()+ b.size()) n<=1;
97     a.resize(n), b.resize(n);
98
99     fft(a), fft(b);
100    for (int i=0; i<n; i++) a[i] = (a[i] * 1LL * b[i])%mod;
101    fft(a, true);
102    return a;
103 }
104 };
105
106 const int M = 998244353, N = 2e6;
107 int main() {
108     std::ios_base::sync_with_stdio(false);
109     cin.tie(NULL); cout.tie(NULL);
110     vector<int> a(N), b(N);
111     long long asum = 0, bsum = 0, csum = 0;
112     for (int i=0; i<N; i++) asum += (a[i] = rand()%M);
113     for (int i=0; i<N; i++) bsum += (b[i] = rand()%M);
114
115     vector<int> c = NTT::multiply(a, b);
116     for (int x: c) csum += x;
117     cout<<csum<<endl;
118 }
119
120 int power(int a, int p, int mod) {
121     if (p==0) return 1;
122     int ans = power(a, p/2, mod);
123     ans = (ans * 1LL * ans)%mod;
124     if (p%2) ans = (ans * 1LL * a)%mod;
125     return ans;
126 }
127 /** Find primitive root of p assuming p is prime.
128 if not, we must add calculation of phi(p).
129 Complexity : O(Ans * log (phi(n)) * log n + sqrt(p)) (if exists)
130              O(p * log (phi(n)) * log n + sqrt(p)) (if does not exist)
131 Returns -1 if not found.
132 */
133 int primitive_root(int p) {

```

```

134     if (p == 2) return 1;
135     vector<int> factor;
136     int phi = p-1, n = phi;
137
138     for (int i=2; i*i<=n; ++i)
139         if (n%i == 0) {
140             factor.push_back(i);
141             while (n%i==0) n/=i;
142         }
143
144     if (n>1) factor.push_back(n);
145
146     for (int res=2; res<=p; ++res) {
147         bool ok = true;
148         for (int i=0; i<factor.size() && ok; ++i)
149             ok &= power(res, phi/factor[i], p) != 1;
150         if (ok) return res;
151     }
152     return -1;
153 }
154 /**
155 Generates necessary info for NTT (for offline usage :3).
156 Returns maximum k such that 2^k % mod = 1,
157 NTT can only be applied for arrays not larger than this size.
158 mod MUST BE PRIME!!!!
159 We use the fact that if primes have the form p=c*2^k+1,
160 there always exists the 2^k-th root of unity.
161 It can be shown that g^c is such a 2^k-th root
162 of unity, where g is a primitive root of p.
163 */
164 int nttdata(int mod, int &root, int &inv, int &pw) {
165     int c = 0, n = mod-1;
166     while (n%2 == 0) c++, n/=2;
167     pw = (mod-1)/n;
168     int g = primitive_root(mod);
169     if(g == -1) return -1; // No primitive root exists
170     root = power(g, n, mod);
171     inv = power(root, mod-2, mod);
172     return c;
173 }

```

## 2 Data Structure

### 2.1 BIT

```

1 ll bit[N]; //Add(0)--> RTE
2 void Add(ll x,ll v) { for(;x < N;x += x & (-x)) bit[x] = (bit[x] + v) ; }
3 ll Sum(ll x) { ll r = 0; for(;x; x -= x & (-x)) r = (r + bit[x]) ; return r; }

```

## 2.2 Sack

```

1  int cnt[maxn];
2  bool big[maxn];
3  void add(int v, int p, int x){
4      cnt[ col[v] ] += x;
5      for(auto u: g[v])
6          if(u != p && !big[u])
7              add(u, v, x)
8  }
9  void dfs(int v, int p, bool keep){
10     int mx = -1, bigChild = -1;
11     for(auto u : g[v])
12         if(u != p && sz[u] > mx)
13             mx = sz[u], bigChild = u;
14     for(auto u : g[v])
15         if(u != p && u != bigChild)
16             dfs(u, v, 0); // run a dfs on small childs and clear them from cnt
17     if(bigChild != -1)
18         dfs(bigChild, v, 1), big[bigChild] = 1; // bigChild marked as big and
↪ not cleared from cnt
19     add(v, p, 1);
20     //now cnt[c] is the number of vertices in subtree of vertex v that has color
↪ c. You can answer the queries easily.
21     if(bigChild != -1)
22         big[bigChild] = 0;
23     if(keep == 0)
24         add(v, p, -1);
25 }

```

## 2.3 Centroid Decomposition

```

1  /// decompose(1, -1) //For 1 rooted tree
2
3  #define ll long long
4  #define pb push_back
5  const ll MAX = 1e5;
6  vector<ll> g[MAX + 9];
7  ll del[MAX + 9], sz[MAX + 9], par[MAX + 9], curSize;
8
9  void dfs(ll u, ll p)
10 {
11     sz[u] = 1;
12     for(ll i = 0; i < g[u].size(); i++) {

```

```

14         ll nd = g[u][i];
15         if(nd == p || del[nd])
16             continue;
17         dfs(nd, u);
18         sz[u] += sz[nd];
19     }
20 }
21
22 ll findCentroid(ll u, ll p)
23 {
24     for(ll i = 0; i < g[u].size(); i++) {
25         ll nd = g[u][i];
26         if(nd == p || del[nd] || sz[nd] <= curSize / 2)
27             continue;
28     }
29     return findCentroid(nd, u);
30 }
31 return u;
32 }
33
34 void decompose(ll u, ll p)
35 {
36     dfs(u, -1);
37     curSize = sz[u];
38     ll cen = findCentroid(u, -1);
39     if(p == -1) p = cen;
40     par[cen] = p, del[cen] = 1;
41
42     for(ll i = 0; i < g[cen].size(); i++) {
43         ll nd = g[cen][i];
44
45         if(!del[nd])
46             decompose(nd, cen);
47     }
48 }
49
50 }

```

## 2.4 Lca with Sparse Table

```

1  int n, l, timer;
2  vector<vector<int>> adj, up;
3  vector<int> tin, tout;
4  void dfs(int v, int p) {
5      tin[v] = ++timer;
6      up[v][0] = p;
7      for (int i = 1; i <= l; ++i)
8          up[v][i] = up[up[v][i-1]][i-1];
9  }

```

```

10     for (int u : adj[v]) {
11         if (u != p)
12             dfs(u, v);
13     }
14     tout[v] = ++timer;
15 }
16 bool is_ancestor(int u, int v){
17     return tin[u] <= tin[v] && tout[u] >= tout[v];
18 }
19 int lca(int u, int v){
20     if (is_ancestor(u, v)) return u;
21     if (is_ancestor(v, u)) return v;
22     for (int i = 1; i >= 0; --i) {
23         if (!is_ancestor(up[u][i], v))
24             u = up[u][i];
25     }
26     return up[u][0];
27 }
28 void preprocess(int root) {
29     tin.resize(n); tout.resize(n);
30     timer = 0; l = ceil(log2(n));
31     up.assign(n, vector<int>(l + 1));
32     dfs(root, root);
33 }
34

```

## 2.5 PBDS/Ordered Set

```

1  #include <ext/pb_ds/assoc_container.hpp>
2  #include <ext/pb_ds/tree_policy.hpp>
3  using namespace __gnu_pbds;
4  template <typename T> using ordered_set = tree<T, null_type, less<T>,
   ↳ rb_tree_tag, tree_order_statistics_node_update>;
5
6  ordered_set <pair<int,int>> st;
7  st.insert({10, 1});
8
9  cout << (st.find_by_order(2) -> first) << endl; //print element in k-th
   ↳ index
10  cout << st.order_of_key({10, 2}) << endl; //print number of items < k
11  auto print = [&] () {
12      for (auto z : st) cout << z.first << ' ';
13  };
14  print();
15  st.erase(st.lower_bound({0, 1}));
16
17  // #define ordered_set tree<int, null_type, less<int>, rb_tree_tag,
   ↳ tree_order_statistics_node_update>

```

```

18  // #define ordered_set tree<int, null_type, less_equal<int>, rb_tree_tag,
   ↳ tree_order_statistics_node_update>
19  //less than or equal -> use less_equal<int>
20  // #define ordered_set tree<pair<int,int>, null_type, pair<int,int>,
   ↳ rb_tree_tag, tree_order_statistics_node_update>
21  //to use multiset -> use pair<int, int> where first element is value and second
   ↳ element is index
22

```

## 2.6 DSU

```

1  void make_set(int v) {
2      parent[v] = v;
3  }
4  int find_set(int v) {
5      if (v == parent[v]) return v;
6      return parent[v] = find_set(parent[v]);
7  }
8  void union_sets(int a, int b) {
9      a = find_set(a); b = find_set(b);
10     if (a != b)
11         parent[b] = a;
12 }

```

## 2.7 Mo's Algo/ Sqrt decomposition

```

1  void remove(idx); // TODO: remove value at idx from data structure
2  void add(idx);    // TODO: add value at idx from data structure
3  int get_answer(); // TODO: extract the current answer of the data structure
4  int block_size;
5  struct Query {
6      int l, r, idx;
7      bool operator<(Query other) const
8      {
9          return make_pair(l / block_size, r) <
10                 make_pair(other.l / block_size, other.r);
11     }
12 };
13 vector<int> mo_s_algorithm(vector<Query> queries) {
14     vector<int> answers(queries.size());
15     sort(queries.begin(), queries.end());
16
17     // TODO: initialize data structure
18
19     int cur_l = 0;
20     int cur_r = -1;
21     // invariant: data structure will always reflect the range [cur_l, cur_r]

```



```

22     for (Query q : queries) {
23         while (cur_l > q.l) {
24             cur_l--;
25             add(cur_l);
26         }
27         while (cur_r < q.r) {
28             cur_r++;
29             add(cur_r);
30         }
31         while (cur_l < q.l) {
32             remove(cur_l);
33             cur_l++;
34         }
35         while (cur_r > q.r) {
36             remove(cur_r);
37             cur_r--;
38         }
39         answers[q.idx] = get_answer();
40     }
41     return answers;
42 }
43

```

### 3 Graph Theory

#### 3.1 0-1 BFS

```

1  vector<int> d(n, INF);
2  d[s] = 0;
3  deque<int> q;
4  q.push_front(s);
5  while (!q.empty()) {
6      int v = q.front();
7      q.pop_front();
8      for (auto edge : adj[v]) {
9          int u = edge.first;
10         int w = edge.second;
11         if (d[v] + w < d[u]) {
12             d[u] = d[v] + w;
13             if (w == 1)
14                 q.push_back(u);
15             else
16                 q.push_front(u);
17         }
18     }
19 }

```

#### 3.2 Bellman Ford Algorithm to find Negative Cycle

```

1  //bellman ford with negative cycle print
2  struct edge {
3      ll v, w;
4  };
5  const ll N = 3e3 + 6, inf = 1LL << 60;
6  ll n, m, dis[N], par[N];
7  vector<edge> g[N];
8
9  int bellman_ford() {
10     lop(n + 1) dis[i] = inf;
11     dis[1] = 0;
12     int cy;
13
14     lop(n + 1) {
15         cy = -1;
16         for (int u = 1; u <= n; u++) {
17             for (auto z : g[u]) {
18                 ll v = z.v, w = z.w;
19                 if (dis[u] + w < dis[v]) {
20                     dis[v] = dis[u] + w;
21                     par[v] = u;
22                     cy = v; // if(u == n) negative cycle;
23                 }
24             }
25         }
26     }
27     return cy; //cy is a adjacent node or a node of negative cycle
28 }
29
30 int main() {
31     cin >> n >> m;
32     lop(m) {
33         ll u, v, w;
34         cin >> u >> v >> w;
35         g[u].pb({v, w});
36     }
37
38     int x = bellman_ford();
39     if (x == -1) {
40         //no negative cycle
41         return 0;
42     }
43
44     //x can be not a part of cycle, so if we go through //path sometimes, x will be
45     ↪ a node of cycle
46     lop(n) x = par[x];
47     vector<int> cycle;
48     int i = x;

```

```

48 while (i != x or cycle.size() <= 1) {
49     cycle.pb(i); //retrieving cycle
50     i = par[i];
51 }
52 cycle.pb(i);
53 reverse(all(cycle));
54 for (int z : cycle)
55     cout << z << ' ';
56 return 0;
57 }

```

### 3.3 Kruskal MST

```

1 struct edge {
2     int u, v, w;
3     bool operator < (const edge &b) const {
4         return w > b.w;
5     }
6 };
7
8 const int N = 2e5;
9 int n, m, par[N];
10 vector <edge> eg;
11
12 int findpar(int x) {
13     return par[x] = par[x] == x ? x : findpar(par[x]);
14 }
15
16 void Union(int u, int v) {
17     par[findpar(u)] = findpar(v);
18 }
19
20 int kruskal() {
21     sort(eg.begin(), eg.end());
22     iota(par, par + n, 0);
23
24     int cost = 0, connected = 0;
25     while (connected != n - 1) {
26         edge z = eg.back();
27         eg.pop_back();
28
29         int x = findpar(z.u), y = findpar(z.v);
30         if (x != y) {
31             connected++;
32             cost += z.w;
33             Union(x, y);
34         }
35     }
36 }

```

```

37     return cost;
38 }
39
40
41 int main()
42 {
43     ios_base::sync_with_stdio(0); cin.tie(0);
44
45     cin >> n >> m;
46     for (int i = 0; i < m; i++) {
47         int u, v, w;
48         cin >> u >> v >> w;
49         eg.push_back({u, v, w});
50     }
51
52     cout << kruskal() << '\n';
53
54     return 0;
55 }

```

### 3.4 Articulation Bridge and Point

```

1 const int N = 1e4 + 10;
2 int n, m, root, Time, low[N], d[N];
3 bool vis[N], is_arti[N]; // is articulation point
4 vector <int> g[N];
5 vector <pair <int, int>> arti_bridge;
6
7 void dfs(int p, int u) {
8     Time++;
9     vis[u] = 1;
10    d[u] = low[u] = Time;
11
12    int child = 0;
13    for (int v : g[u]) {
14        if (v == p) continue;
15
16        if (vis[v]) low[u] = min(low[u], d[v]);
17        else {
18            child++;
19            dfs(u, v);
20
21            low[u] = min(low[u], low[v]);
22            if (low[v] >= d[u] and u != root)
23                is_arti[u] = 1;
24
25            if (d[u] < low[v])
26                arti_bridge.push_back({min(u, v), max(u, v)});

```

```

27     }
28 }
29
30     if (u == root and child > 1)
31         is_arti[u] = 1;
32 }
33
34 int main () {
35     cin >> n >> m;
36     for (int i = 0; i < m; i++) {
37         int u, v; cin >> u >> v;
38         g[u].push_back(v);
39         g[v].push_back(u);
40     }
41
42     Time = root = 1;
43     memset(vis, 0, sizeof vis);
44     memset(is_arti, 0, sizeof is_arti);
45     dfs(root, root);
46 }

```

### 3.5 Online Articulation Bridge Finding

```

1 vector<int> par, dsu_2ecc, dsu_cc, dsu_cc_size;
2 int bridges;
3 int lca_iteration;
4 vector<int> last_visit;
5
6 void init(int n) {
7     par.resize(n);
8     dsu_2ecc.resize(n);
9     dsu_cc.resize(n);
10    dsu_cc_size.resize(n);
11    lca_iteration = 0;
12    last_visit.assign(n, 0);
13    for (int i = 0; i < n; ++i) {
14        dsu_2ecc[i] = i;
15        dsu_cc[i] = i;
16        dsu_cc_size[i] = 1;
17        par[i] = -1;
18    }
19    bridges = 0;
20 }
21
22 int find_2ecc(int v) {
23     if (v == -1)
24         return -1;
25     return dsu_2ecc[v] == v ? v : dsu_2ecc[v] = find_2ecc(dsu_2ecc[v]);
26 }

```

```

27
28 int find_cc(int v) {
29     v = find_2ecc(v);
30     return dsu_cc[v] == v ? v : dsu_cc[v] = find_cc(dsu_cc[v]);
31 }
32
33 void make_root(int v) {
34     v = find_2ecc(v);
35     int root = v;
36     int child = -1;
37     while (v != -1) {
38         int p = find_2ecc(par[v]);
39         par[v] = child;
40         dsu_cc[v] = root;
41         child = v;
42         v = p;
43     }
44     dsu_cc_size[root] = dsu_cc_size[child];
45 }
46
47 void merge_path (int a, int b) {
48     ++lca_iteration;
49     vector<int> path_a, path_b;
50     int lca = -1;
51     while (lca == -1) {
52         if (a != -1) {
53             a = find_2ecc(a);
54             path_a.push_back(a);
55             if (last_visit[a] == lca_iteration) {
56                 lca = a;
57                 break;
58             }
59             last_visit[a] = lca_iteration;
60             a = par[a];
61         }
62         if (b != -1) {
63             b = find_2ecc(b);
64             path_b.push_back(b);
65             if (last_visit[b] == lca_iteration) {
66                 lca = b;
67                 break;
68             }
69             last_visit[b] = lca_iteration;
70             b = par[b];
71         }
72     }
73 }
74
75 for (int v : path_a) {

```

```

76     dsu_2ecc[v] = lca;
77     if (v == lca)
78         break;
79     --bridges;
80 }
81 for (int v : path_b) {
82     dsu_2ecc[v] = lca;
83     if (v == lca)
84         break;
85     --bridges;
86 }
87 }
88
89 void add_edge(int a, int b) {
90     a = find_2ecc(a);
91     b = find_2ecc(b);
92     if (a == b)
93         return;
94
95     int ca = find_cc(a);
96     int cb = find_cc(b);
97
98     if (ca != cb) {
99         ++bridges;
100         if (dsu_cc_size[ca] > dsu_cc_size[cb]) {
101             swap(a, b);
102             swap(ca, cb);
103         }
104         make_root(a);
105         par[a] = dsu_cc[a] = b;
106         dsu_cc_size[cb] += dsu_cc_size[a];
107     } else {
108         merge_path(a, b);
109     }
110 }

```

### 3.6 Strongly Connected Components

```

1  const int N = 3e5 + 9;
2
3  // given a directed graph return the minimum number of edges to be added so that
4  ⇨ the whole graph become an SCC
5  bool vis[N];
6  vector<int> g[N], r[N], G[N], vec; //G is the condensed graph
7  void dfs1(int u) {
8      vis[u] = 1;
9      for (auto v : g[u]) if (!vis[v]) dfs1(v);
10     vec.push_back(u);

```

```

11
12     vector<int> comp;
13     void dfs2(int u) {
14         comp.push_back(u);
15         vis[u] = 1;
16         for (auto v : r[u]) if (!vis[v]) dfs2(v);
17     }
18
19     int idx[N], in[N], out[N];
20     int main() {
21         ios_base::sync_with_stdio(0);
22         cin.tie(0);
23
24         int n, m;
25         cin >> n >> m;
26         for (int i = 1; i <= m; i++) {
27             int u, v;
28             cin >> u >> v;
29             g[u].push_back(v);
30             r[v].push_back(u);
31         }
32         for (int i = 1; i <= n; i++) if (!vis[i]) dfs1(i);
33         reverse(vec.begin(), vec.end());
34         memset(vis, 0, sizeof vis);
35         int scc = 0;
36         for (auto u : vec) {
37             if (!vis[u]) {
38                 comp.clear();
39                 dfs2(u);
40                 scc++;
41                 for (auto x : comp) idx[x] = scc;
42             }
43         }
44         for (int u = 1; u <= n; u++) {
45             for (auto v : g[u]) {
46                 if (idx[u] != idx[v]) {
47                     in[idx[v]]++, out[idx[u]]++;
48                     G[idx[u]].push_back(idx[v]);
49                 }
50             }
51         }
52         int needed_in = 0, needed_out = 0;
53         for (int i = 1; i <= scc; i++) {
54             if (!in[i]) needed_in++;
55             if (!out[i]) needed_out++;
56         }
57         int ans = max(needed_in, needed_out);
58         if (scc == 1) ans = 0;
59         cout << ans << '\n';

```

```

60     return 0;
61 }

```

### 3.7 2 SAT

```

1  const int N = 3e5 + 9;
2
3  /*
4  zero Indexed
5  we have vars variables
6  F=(x_0 XXX y_0) and (x_1 XXX y_1) and ... (x_{vars-1} XXX y_{vars-1})
7  here {x_i,y_i} are variables
8  and XXX belongs to {OR,XOR}
9  is there any assignment of variables such that F=true
10 */
11 struct twosat {
12     int n; // total size combining +, -. must be even.
13     vector< vector<int> > g, gt;
14     vector<bool> vis, res;
15     vector<int> comp;
16     stack<int> ts;
17     twosat(int vars = 0) {
18         n = vars << 1;
19         g.resize(n);
20         gt.resize(n);
21     }
22
23     //zero indexed, be careful
24     //if you want to force variable a to be true in OR or XOR combination
25     //add addOR (a,1,a,1);
26     //if you want to force variable a to be false in OR or XOR combination
27     //add addOR (a,0,a,0);
28
29     //(x_a or (not x_b))-> af=1,bf=0
30     void addOR(int a, bool af, int b, bool bf) {
31         a += a + (af ^ 1);
32         b += b + (bf ^ 1);
33         g[a ^ 1].push_back(b); // !a => b
34         g[b ^ 1].push_back(a); // !b => a
35         gt[b].push_back(a ^ 1);
36         gt[a].push_back(b ^ 1);
37     }
38     //(!x_a xor !x_b)-> af=0, bf=0
39     void addXOR(int a, bool af, int b, bool bf) {
40         addOR(a, af, b, bf);
41         addOR(a, !af, b, !bf);
42     }
43     //add this type of condition->
44     //add(a,af,b,bf) means if a is af then b must need to be bf

```

```

45     void add(int a, bool af, int b, bool bf) {
46         a += a + (af ^ 1);
47         b += b + (bf ^ 1);
48         g[a].push_back(b);
49         gt[b].push_back(a);
50     }
51     void dfs1(int u) {
52         vis[u] = true;
53         for (int v : g[u]) if (!vis[v]) dfs1(v);
54         ts.push(u);
55     }
56     void dfs2(int u, int c) {
57         comp[u] = c;
58         for (int v : gt[u]) if (comp[v] == -1) dfs2(v, c);
59     }
60     bool ok() {
61         vis.resize(n, false);
62         for (int i = 0; i < n; ++i) if (!vis[i]) dfs1(i);
63         int scc = 0;
64         comp.resize(n, -1);
65         while (!ts.empty()) {
66             int u = ts.top();
67             ts.pop();
68             if (comp[u] == -1) dfs2(u, scc++);
69         }
70         res.resize(n / 2);
71         for (int i = 0; i < n; i += 2) {
72             if (comp[i] == comp[i + 1]) return false;
73             res[i / 2] = (comp[i] > comp[i + 1]);
74         }
75         return true;
76     }
77 };
78
79 int main() {
80     int n, m; cin >> n >> m;
81     twosat ts(n);
82     for (int i = 0; i < m; i++) {
83         int u, v, k; cin >> u >> v >> k;
84         --u; --v;
85         if (k) ts.add(u, 0, v, 0), ts.add(u, 1, v, 1), ts.add(v, 0, u, 0), ts.add(v,
↵ 1, u, 1);
86         else ts.add(u, 0, v, 1), ts.add(u, 1, v, 0), ts.add(v, 0, u, 1), ts.add(v,
↵ 1, u, 0);
87     }
88     int k = ts.ok();
89     if (!k) cout << "Impossible\n";
90     else {
91         vector<int> v;

```

```

92     for (int i = 0; i < n; i++) if (ts.res[i]) v.push_back(i);
93     cout << (int)v.size() << '\n';
94     for (auto x : v) cout << x + 1 << ' ';
95     cout << '\n';
96 }
97 return 0;
98 }

```

## 4 Dynamic Programming

### 4.1 LIS

```

1 int lis(vector<int> const& a) {
2     int n = a.size();
3     const int INF = 1e9; //INF must be > max(a)
4     vector<int> d(n + 1, INF);
5     d[0] = -INF;
6     for (int i = 0; i < n; i++) {
7         int j = upper_bound(d.begin(), d.end(), a[i]) - d.begin();
8         if (d[j - 1] <= a[i] && a[i] <= d[j]) d[j] = a[i];
9     }
10    int ans = 0;
11    for (int i = 0; i <= n; i++) {
12        if (d[i] < INF) ans = i;
13    }
14    return ans;
15 }
16

```

### 4.2 SOS DP

```

1 for(int i = 0; i < (1 << N); ++i)
2     F[i] = A[i];
3 for(int i = 0; i < N; ++i) for(int mask = 0; mask < (1 << N); ++mask){
4     if(mask & (1 << i))
5         F[mask] += F[mask ^ (1 << i)];
6 }
7 // The above algorithm runs in O(N^2N) time.

```

### 4.3 Digit DP

```

1 // How many numbers x are there in the range a to b, where the digit d occurs
2 ↪ exactly k times in x?
3 vector<int> num;
4 int a, b, d, k;
5 int DP[12][12][2];

```

```

5 // DP[p][c][f] = Number of valid numbers <= b from this state
6 // p = current position from left side (zero based)
7 // c = number of times we have placed the digit d so far
8 // f = the number we are building has already become smaller than b? [0 = no, 1
9 ↪ = yes]
10 int call(int pos, int cnt, int f){
11     if(cnt > k) return 0;
12     if(pos == num.size()){
13         if(cnt == k) return 1;
14         return 0;
15     }
16     if(DP[pos][cnt][f] != -1) return DP[pos][cnt][f];
17     int res = 0; int LMT;
18     if(f == 0) LMT = num[pos]; else LMT = 9;
19     for(int dgt = 0; dgt <= LMT; dgt++){
20         int nf = f; int ncnt = cnt;
21         if(f == 0 && dgt < LMT) nf = 1; // The number is getting smaller at
22 ↪ this position
23         if(dgt == d) ncnt++;
24         if(ncnt <= k) res += call(pos+1, ncnt, nf);
25     }
26     return DP[pos][cnt][f] = res;
27 }
28 int solve(int b){
29     num.clear();
30     while(b > 0){
31         num.push_back(b%10);
32         b/=10;
33     }
34     reverse(num.begin(), num.end());
35     memset(DP, -1, sizeof(DP));
36     int res = call(0, 0, 0);
37     return res;
38 }
39
40 int main () {
41     cin >> a >> b >> d >> k;
42     int res = solve(b) - solve(a-1);
43     cout << res << endl;
44 }

```

## 5 String

### 5.1 Hashing

```

1  const ll N = 1e6 + 10, mod = 2e9 + 63, base1 = 1e9 + 21, base2 = 1e9 + 181;
2  ll pw1[N], pw2[N], hp1[N], hp2[N], hs1[N], hs2[N], n, q;
3  string s;
4
5  void pw_cal() {
6      pw1[0] = pw2[0] = 1;
7      for (int i = 1; i < N; i++) {
8          pw1[i] = (pw1[i - 1] * base1) % mod;
9          pw2[i] = (pw2[i - 1] * base2) % mod;
10     }
11 }
12 void init() {
13     hp1[0] = hp2[0] = hs1[n + 1] = hs2[n + 1] = 0;
14     for (int i = 1; i <= n; i++) {
15         hp1[i] = (hp1[i - 1] * base1 + s[i - 1]) % mod;
16         hp2[i] = (hp2[i - 1] * base2 + s[i - 1]) % mod;
17     }
18     for (int i = n; i > 0; i--) {
19         hs1[i] = (hs1[i + 1] * base1 + s[i - 1]) % mod;
20         hs2[i] = (hs2[i + 1] * base2 + s[i - 1]) % mod;
21     }
22 }
23
24 ll hashp(int l, int r) {
25     ll hash1 = (hp1[r] - hp1[l - 1] * pw1[r - l + 1]) % mod;
26     if (hash1 < 0) hash1 += mod;
27     ll hash2 = (hp2[r] - hp2[l - 1] * pw2[r - l + 1]) % mod;
28     if (hash2 < 0) hash2 += mod;
29     return (hash1 << 32) | hash2;
30 }
31
32 ll hashs(int l, int r) {
33     ll hash1 = (hs1[l] - hs1[r + 1] * pw1[r - l + 1]) % mod;
34     if (hash1 < 0) hash1 += mod;
35     ll hash2 = (hs2[l] - hs2[r + 1] * pw2[r - l + 1]) % mod;
36     if (hash2 < 0) hash2 += mod;
37     return (hash1 << 32) | hash2;
38 }
39
40 bool ispal(int l, int r) {
41     int mid = (r + l) / 2;
42     ll x = hashp(l, mid), y = hashs(mid, r);
43     return x == y;
44 }

```

### 5.2 Trie

```

1  const int N = 1e5+10, M = 26;
2  int trie[N][M], nnode;
3  bool isword[N];
4
5  void reset(int k) {
6      for (int i = 0; i < M; i++)
7          trie[k][i] = -1;
8  }
9
10 void Insert(string &s) {
11     int n = s.size(), node = 0;
12     for (int i = 0; i < n; i++) {
13         if (trie[node][s[i] - 'a'] == -1) {
14             trie[node][s[i] - 'a'] = ++nnode;
15             reset(nnode);
16         }
17         node = trie[node][s[i] - 'a'];
18     }
19     isword[node] = 1;
20 }
21
22 bool Search(string &s) {
23     int n = s.size(), node = 0;
24     for (int i = 0; i < s.size(); i++) {
25         if (trie[node][s[i] - 'a'] == -1) return 0;
26         node = trie[node][s[i] - 'a'];
27     }
28     return isword[node];
29 }
30
31 //find maximum subarray xor sum
32 int doxor(int s) {
33     int nw = 0, t = 0;
34     for (int i = 31; i >= 0; i--) {
35         bool p = (1 << i) & s;
36         if (node[nw][p ^ 1] != -1) {
37             t |= 1 << i;
38             nw = node[nw][p ^ 1];
39         } else
40             nw = node[nw][p];
41     }
42     return t;
43 }
44
45 //minimum subarray xor sum
46 int doxor2(int s) {
47     int nw = 0, t = 0;
48     for (int i = 31; i >= 0; i--) {
49         bool p = (1 << i) & s;

```

```

49     if (node[nw][p] != -1) nw = node[nw][p];
50     else {
51         t |= 1 << i;
52         nw = node[nw][p ^ 1];
53     }
54 }
55 return t;
56 }
57 //at first insert(0), then calculate xor before inserting each element of the
58 ↪ array
59 //calculate number of subarray having xor>=k
60 int doxor(int s) {
61     int nw = 0, t = 0;
62     for (int i = 31; i >= 0; i--) {
63         bool p = (1 << i) & s;
64         bool q = (1 << i) & k;
65         if (!q) {
66             t += (node[nw][p ^ 1] != -1 ? word[node[nw][p ^ 1]] : 0);
67             nw = node[nw][p];
68         } else {
69             nw = node[nw][p ^ 1];
70             if (nw == -1)
71                 break;
72         }
73     }
74     if (nw != -1)
75         t += word[nw];
76     return t;
77 }
78 //insert(0), sum returned value, insert prefix xor
79 int main() {
80     reset(0);
81     int n; cin >> n;
82     for (int i = 0; i < n; i++) {
83         string s;
84         cin >> s;
85         Insert(s);
86     }
87     int q; cin >> q;
88     while (q--) {
89         string s;
90         cin >> s;
91         cout << Search(s) << endl;
92     }
93 }

```

### 5.3 Z- Algo //0-based Indexing

```

1  vector<int> z_function(string s) {
2      int n = (int) s.length();
3      vector<int> z(n);
4      for (int i = 1, l = 0, r = 0; i < n; ++i) {
5          if (i <= r)
6              z[i] = min (r - i + 1, z[i - l]);
7          while (i + z[i] < n && s[z[i]] == s[i + z[i]])
8              ++z[i];
9          if (i + z[i] - 1 > r)
10             l = i, r = i + z[i] - 1;
11     }
12     return z;
13 }

```

- The Z-function for this string  $s$  is an array of length  $n$  where the  $i$ -th element is equal to the greatest number of characters starting from the position  $i$  that coincides with the first characters of  $s$ .

### 5.4 KMP

```

1  #include <iostream>
2  using namespace std;
3  int pattern[200005],text[200005],f[200005]/*failure_table*/;
4  int pattern_size,text_size;
5  void build_table(){
6      f[0]=0;
7      f[1]=0;
8      int i,j;
9      for(i=2; i<=pattern_size; i++){
10         j=f[i-1];
11         while(1){
12             if(pattern[j]==pattern[i-1]){
13                 f[i]=j+1;
14                 break;
15             }
16             if(j==0){
17                 f[i]=0;
18                 break;
19             }
20             j=f[j];
21         }
22     }
23 }
24 int kmp(){
25     build_table();
26     int i=0,j=0,ret=0;
27     while(1){

```



```

28     if(j==text_size){
29         break;
30     }
31     if(text[j]==pattern[i]){
32         i++;
33         j++;
34         if(i==pattern_size) {
35             ret++;
36             i=f[i];
37         }
38     }
39     else{
40         if(i==0){
41             j++;
42         }
43         else{
44             i=f[i];
45         }
46     }
47 }
48 return ret;
49 }
50
51 int main(){
52     text_size=3;
53     pattern_size=2;
54     text[0]=1;
55     text[1]=1;
56     text[2]=2;
57     pattern[0]=1;
58     pattern[1]=2;
59
60     cout<<kmp();
61 }
62
63

```

## 5.5 Aho-Corasick

```

1  int nxt[N][26],cnt[N],f[N],vis[N],num;
2  vector<int> g[N]; //fail node tree
3
4  char s[1000005],pat[505]; //given string and pattern
5
6  //adding patterns to the trie
7  void add(){
8      int node=0,i,len=strlen(pat);
9
10     for(i=0 ; i<len ; i++){

```

```

11     int ch=pat[i]-'a';
12
13     if(nxt[node][ch]){
14         node=nxt[node][ch];
15     }
16     else{
17         nxt[node][ch] = ++num;
18         node = num;
19     }
20
21 }
22 qnode.pb(node);
23 }
24
25 //building automaton
26 void build_aho(){
27     queue<int> q;
28     int i,u,v,curr;
29
30     for(i=0 ; i<26 ; i++){
31         if(nxt[0][i]) q.push(nxt[0][i]);
32     }
33
34     while(q.size()){
35         curr = q.front();
36         q.pop();
37
38         for(i=0 ; i<26 ; i++){
39             if(nxt[curr][i]){
40                 u=nxt[curr][i];
41                 q.push(u);
42                 v=f[curr];
43                 while(v && nxt[v][i]==0){
44                     v=f[v];
45                 }
46                 f[u]=nxt[v][i];
47                 g[f[u]].pb(u);
48             }
49         }
50     }
51 }
52
53 //searching the string
54 void search(){
55     int j=0,i,len=strlen(s);
56
57     for(i=0 ; i<len ; i++){
58         int ch=s[i]-'a';
59

```

```

60     while(j && nxt[j][ch]==0){
61         j = f[j];
62     }
63
64     j=nxt[j][ch];
65
66     cnt[j]++;
67 }
68 }
69 //dfs to add cnts of fail node subtree of a node
70 void dfs(int node){
71     vis[node]=1;
72     for(auto to : g[node]){
73         if(!vis[to]) dfs(to);
74         cnt[node]+=cnt[to];
75     }
76 }
77
78 }

```

## 5.6 Palindromic Tree

## 5.7 Suffix Array

```

1  #define MAX_N 1000020
2  int n, t;
3  // char s[500099];
4  string s;
5  int SA[MAX_N], LCP[MAX_N];
6  int RA[MAX_N], tempRA[MAX_N];
7  int tempSA[MAX_N];
8  int c[MAX_N];
9  int Phi[MAX_N], PLCP[MAX_N];
10 // second approach: O(n log n)
11 // the input string, up to 100K characters
12 // the length of input string
13 // rank array and temporary rank array
14 // suffix array and temporary suffix array
15 // for counting/radix sort
16 void countingSort(int k) { // O(n)
17     int i, sum, maxi = max(300, n);
18     // up to 255 ASCII chars or length of n
19     memset(c, 0, sizeof c);
20     // clear frequency table
21     for (i = 0; i < n; i++)
22         // count the frequency of each integer rank
23         c[i + k < n ? RA[i + k] : 0]++;
24     for (i = sum = 0; i < maxi; i++) {
25         int t = c[i]; c[i] = sum; sum += t;

```

```

26     }
27     for (i = 0; i < n; i++)
28         // shuffle the suffix array if necessary
29         tempSA[c[SA[i] + k < n ? RA[SA[i] + k] : 0]++] = SA[i];
30
31     for (i = 0; i < n; i++)
32         // update the suffix array SA
33         SA[i] = tempSA[i];
34 }
35
36 void buildSA() {
37     int i, k, r;
38     for (i = 0; i < n; i++) RA[i] = s[i];
39     // initial rankings
40     for (i = 0; i < n; i++) SA[i] = i;
41     // initial SA: {0, 1, 2, ..., n-1}
42     for (k = 1; k < n; k <= 1) {
43         // repeat sorting process log n times
44         countingSort(k); // actually radix sort: sort based on the second item
45         countingSort(0);
46         // then (stable) sort based on the first item
47         tempRA[SA[0]] = r = 0;
48         // re-ranking; start from rank r = 0
49         for (i = 1; i < n; i++)
50             // compare adjacent suffixes
51             tempRA[SA[i]] = // if same pair => same rank r; otherwise, increase
52                             (RA[SA[i]] == RA[SA[i - 1]] && RA[SA[i] + k] == RA[SA[i - 1] +
53                             k]) ? r : ++r;
54         for (i = 0; i < n; i++)
55             // update the rank array RA
56             RA[i] = tempRA[i];
57
58         if (RA[SA[n - 1]] == n - 1) break;
59         // nice optimization trick
60     }
61 }
62
63 void buildLCP() {
64     int i, L;
65     Phi[SA[0]] = -1;
66     // default value
67     for (i = 1; i < n; i++)
68         // compute Phi in O(n)
69         Phi[SA[i]] = SA[i - 1];
70     // remember which suffix is behind this suffix
71     for (i = L = 0; i < n; i++) {
72         // compute Permuted LCP in O(n)
73         if (Phi[i] == -1) { PLCP[i] = 0; continue; }

```

```

73 // special case
74 while (s[i + L] == s[Phi[i] + L]) L++;
75 // L increased max n times
76 PLCP[i] = L;
77 L = max(L - 1, 0);
78 // L decreased max n times
79 }
80 for (i = 0; i < n; i++)
81 // compute LCP in O(n)
82 LCP[i] = PLCP[SA[i]];
83 // put the permuted LCP to the correct position
84 }
85 // n = string length + 1
86 // s = the string
87 // memset(LCP, 0, sizeof(LCP)); setting all index of LCP to zero
88 // buildSA(); for building suffix array
89 // buildLCP(); for building LCP array
90 // LCP is the longest common prefix with the previous suffix here
91 // SA[0] holds the empty suffix "\0".
92
93 int main()
94 {
95     s = "banana";
96     s += "$";
97     n = s.size();
98
99     memset(LCP, 0, sizeof(LCP));
100     buildSA();
101     buildLCP();
102
103     for (int i = 0; i < n; i++) cout << SA[i] << ' ' << s.substr(SA[i], n -
↵ SA[i]) << endl;
104     printf("\n");
105     for (int i = 0; i < n; i++) printf("%d ", LCP[i]);
106     printf("\n");
107
108     return 0;
109 }

```

## 6 Geometry

### 6.1 Convex Hull

```

1 struct pt {
2     double x, y;
3 };
4
5 int orientation(pt a, pt b, pt c) {
6     double v = a.x*(b.y-c.y)+b.x*(c.y-a.y)+c.x*(a.y-b.y);

```

```

7     if (v < 0) return -1; // clockwise
8     if (v > 0) return +1; // counter-clockwise
9     return 0;
10 }
11
12 bool cw(pt a, pt b, pt c, bool include_collinear) {
13     int o = orientation(a, b, c);
14     return o < 0 || (include_collinear && o == 0);
15 }
16 bool ccw(pt a, pt b, pt c, bool include_collinear) {
17     int o = orientation(a, b, c);
18     return o > 0 || (include_collinear && o == 0);
19 }
20
21 void convex_hull(vector<pt>& a, bool include_collinear = false) {
22     if (a.size() == 1)
23         return;
24
25     sort(a.begin(), a.end(), [](pt a, pt b) {
26         return make_pair(a.x, a.y) < make_pair(b.x, b.y);
27     });
28     pt p1 = a[0], p2 = a.back();
29     vector<pt> up, down;
30     up.push_back(p1);
31     down.push_back(p1);
32     for (int i = 1; i < (int)a.size(); i++) {
33         if (i == a.size() - 1 || cw(p1, a[i], p2, include_collinear)) {
34             while (up.size() >= 2 && !cw(up[up.size()-2], up[up.size()-1], a[i],
↵ include_collinear))
35                 up.pop_back();
36             up.push_back(a[i]);
37         }
38         if (i == a.size() - 1 || ccw(p1, a[i], p2, include_collinear)) {
39             while (down.size() >= 2 && !ccw(down[down.size()-2],
↵ down[down.size()-1], a[i], include_collinear))
40                 down.pop_back();
41             down.push_back(a[i]);
42         }
43     }
44
45     if (include_collinear && up.size() == a.size()) {
46         reverse(a.begin(), a.end());
47         return;
48     }
49     a.clear();
50     for (int i = 0; i < (int)up.size(); i++)
51         a.push_back(up[i]);
52     for (int i = down.size() - 2; i > 0; i--)
53         a.push_back(down[i]);

```

```
54 }

```

## 6.2 Polar Sort

```

1 inline bool up (point p) {
2     return p.y > 0 or (p.y == 0 and p.x >= 0);
3 }
4
5 sort(v.begin(), v.end(), [] (point a, point b) {
6     return up(a) == up(b) ? a.x * b.y > a.y * b.x : up(a) < up(b);
7 });

```

## 7 Miscellaneous

### 7.1 C++17 Sublime Build

```

1 {
2     "cmd": ["g++ -std=c++17 -Wall -fsanitize=address $file_name -o
3         $file_base_name && timeout 10s ./$file_base_name <in>out"],
4     "selector": "source.cpp",
5     "shell": true,
6     "working_dir": "$file_path"
7 }

```

### 7.2 Test Case Generator with FASTIO

```

1 #pragma GCC optimize("Ofast,unroll-loops")
2 #pragma GCC target("avx,avx2,fma")
3
4 //generator to generate testcase
5 #include <bits/stdc++.h>
6 using namespace std;
7 #define ll long long
8 mt19937_64 rng(chrono::steady_clock::now().time_since_epoch().count());
9 // return a random number in [l, r] range
10 ll rand(ll l, ll r) {
11     return uniform_int_distribution<ll>(l, r)(rng);
12 }
13 void tree() {
14     int n = rand(1, 10);
15     int t = rand(1, 5);
16
17     vector<int> p(n);
18     for (int i = 0; i < n; i++)
19         if (i > 0) p[i] = rand(i, t);
20

```

```

21     printf("%d\n", n);
22     vector<int> perm(n);
23     for (int i = 0; i < n; i++) perm[i] = i;
24     shuffle(perm.begin() + 1, perm.end(), rng);
25     vector<pair<int, int> > edges;
26
27     for (int i = 1; i < n; i++)
28         if (rand(0, 1))
29             edges.push_back(make_pair(perm[i], perm[p[i]]));
30         else
31             edges.push_back(make_pair(perm[p[i]], perm[i]));
32
33     shuffle(edges.begin(), edges.end(), rng);
34     for (int i = 0; i + 1 < n; i++)
35         printf("%d %d\n", edges[i].first + 1, edges[i].second + 1);
36 }
37
38 int main(int argc, char* argv[]) {
39     ios_base::sync_with_stdio(0); cin.tie(0);
40
41     ll t = rand(1, 1);
42     cout << t << endl;
43     while (t--) {
44         ll n = rand(1, 15);
45         cout << n << endl;
46     }
47     return 0;
48 }

```

### 7.3 Output Checker Bash Script

```

1 //Bash script to auto check output
2 for((i = 1; ; ++i)); do
3     echo $i
4     ./gen $i > in
5     # ./a < in > out1
6     # ./brute < in > out2
7     # diff -w out1 out2 || break
8     diff -w <./sol < in < ./brute < in || break
9 done
10 echo case
11 cat in
12 #create and build a brute force code named brute.cpp, main solution code sol.cpp
   ↳ and a random test case generator gen.cpp. To make this script runnable, run
   ↳ this command chmod +x s.sh (s.sh is this bash script name). Then run the
   ↳ script by ./s.sh or bash s.sh

```

## 7.4 Custom Hash for unordered map

```

1 // To prevent collision in unordered_map
2 #include <bits/stdc++.h>
3 using namespace std;
4 struct custom_hash {
5     static uint64_t splitmix64(uint64_t x) {
6         // http://xorshift.di.unimi.it/splitmix64.c
7         x += 0x9e3779b97f4a7c15;
8         x = (x ^ (x >> 30)) * 0xbf58476d1ce4e5b9;
9         x = (x ^ (x >> 27)) * 0x94d049bb133111eb;
10        return x ^ (x >> 31);
11    }
12    size_t operator()(uint64_t x) const {
13        static const uint64_t FIXED_RANDOM =
14            chrono::steady_clock::now().time_since_epoch().
15            count();
16        return splitmix64(x + FIXED_RANDOM);
17    }
18 };
19 /// Declaration: unordered_map <int, int, custom_hash > numbers;
20 /// Usage: same as normal unordered_map
21 /// Ex: numbers[5] = 2;
22 /// *** To use gp_hash_table (faster than unordered_map) **** ///
23 /// Add these extra two lines:
24 /// #include <ext/pb_ds/assoc_container.hpp>
25 /// using namespace __gnu_pbds;
26 /// Declaration: gp_hash_table<int, int, custom_hash > numbers;
27 /// Usage: Same as unordered_map

```

## 7.5 Release vector memory

```

1 vector<int> Elements ;
2 // fill the vector up
3 vector<int>().swap(Elements);

```

## 7.6 Set of Structure [Operator overload]

```

1 struct seg{
2     ll l , r , c;
3     bool operator < (const seg &S) const {
4         return l < S.l ;
5     }
6 };
7 set<seg> s ; s.insert({0,0,0}) ;

```

## 7.7 Graph and Bitmask Operation

```

1 #pragma GCC optimize("Ofast,unroll-loops")
2 #pragma GCC target("avx,avx2,fma")
3 /* Infos */
4 ~ 4 Direction
5 int dr[] = {1, -1, 0, 0};
6 int dc[] = {0, 0, 1, -1};
7 ~ 8 Direction
8 int dr[] = {1, -1, 0, 0, 1, 1, -1, -1};
9 int dc[] = {0, 0, 1, -1, 1, -1, 1, -1};
10 ~ Knight Direction
11 int dr[] = {1, -1, 1, -1, 2, 2, -2, -2};
12 int dc[] = {2, 2, -2, -2, 1, -1, 1, -1};
13 ~ Hexagonal Direction
14 int dr[] = {2, -2, 1, 1, -1, -1};
15 int dc[] = {0, 0, 1, -1, 1, -1};
16 ~ bitmask operations
17 int Set(int n, int pos) { return n = n | (1 << pos); }
18 int reset(int n, int pos) { return n = n & ~(1 << pos); }
19 bool check(int n, int pos) { return (bool)(n & (1 << pos)); }
20 int toggle(int n, int pos) { return n = (n ^ (1 << pos)); }
21 bool isPower2(int x) { return (x && !(x & (x - 1))); }
22 ll LargestPower2LessEqualX(ll x) { for (int i = 1; i <= x / 2; i *= 2) x = x |
    ⇨ (x >> i); return (x + 1) / 2; }
23 // for unlimited stack, run the command in terminal and run the code in terminal
24 ulimit -s unlimited

```

## 8 Notes

### 8.1 Stars and Bars Theorem

1. The number of ways to put  $n$  identical objects into  $k$  labeled boxes is  $\binom{n+k-1}{n}$
2. Suppose, there are  $n$  objects to be placed into  $k$  bins, ways =  $\binom{n-1}{k-1}$
3. Statement of 1no. and empty bins are valid, ways =  $\binom{n+k-1}{k-1}$

### 8.2 GCD

1.  $\gcd(a, b) = \gcd(a, a - b)$  [ $a > b$ ]
2.  $\gcd(F(a), F(b)) = F(\gcd(a, b))$  [ $F = \text{fibonacci}$ ]
3.  $\gcd(a, b) = \sum \phi(k)$  where  $k$  are all common divisors of  $a$  and  $b$

### 8.3 Geometric Formula

1. Point Slope Form:  $y - y_1 = m \cdot (x - x_1)$
2. Slope,  $m = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$
3. Slope from line,  $m = -\frac{A}{B}$
4. Angle,  $\tan \theta = \frac{m_1 - m_2}{1 + m_1 \cdot m_2}$
5. Distance from a Point  $(x_0, y_0)$  to a Line  $(Ax + By + C = 0) = \frac{|Ax_0 + By_0 + C|}{\sqrt{A^2 + B^2}}$
6. Area of segment in radian angle:  $A = \frac{1}{2} \cdot r^2 (\theta - \sin \theta)$
7. The sum of interior angles of a polygon with  $n$  sides  $= 180 \cdot (n - 2)$
8. Number of diagonals of a  $n$ -sided polygon  $= \frac{n(n-3)}{2}$
9. The measure of interior angles of a regular  $n$ -sided polygon  $= \frac{(n-2) \cdot 180}{n}$
10. The measure of exterior angles of a regular  $n$ -sided polygon  $= \frac{360}{n}$
11. Picks theorem:  $A = I + \frac{B}{2} - 1$  where A = Area of Polygon, B = Number of integral points on edges of polygon, I = Number of integral points strictly inside the polygon.

### 8.4 Series/Progression

1. Sum of first  $n$  positive number  $= \frac{n(n+1)}{2}$
2. Sum of first  $n$  odd number  $= n^2$
3. Sum of first  $n$  even number  $= n \cdot (n + 1)$
4. Arithmetic Progression:  $n$ -th term  $= a + (n - 1) \cdot d$ , sum  $= \frac{n}{2} \{2a + (n - 1) \cdot d\}$  ; a = first element, d = difference between two elements
5. Geometric Progression:  $n$ -th term  $= a \cdot r^{n-1}$ , sum  $= a \cdot \frac{r^n - 1}{r - 1}$  ; a = first element, r = ratio of two elements
6. Catalan Numbers:  $1, 1, 2, 5, 14, 42, 132 \dots C_n = \frac{(2n)!}{n! \cdot (n+1)!}; n \geq 0$

### 8.5 Combinatorial formulas

1.  $\sum_{k=0}^n k^2 = n(n+1)(2n+1)/6$
2.  $\sum_{k=0}^n k^3 = n^2(n+1)^2/4$
3.  $\sum_{k=0}^n k^4 = (6n^5 + 15n^4 + 10n^3 - n)/30$
4.  $\sum_{k=0}^n k^5 = (2n^6 + 6n^5 + 5n^4 - n^2)/12$
5.  $\sum_{k=0}^n x^k = (x^{n+1} - 1)/(x - 1)$

$$6. \sum_{k=0}^n kx^k = (x - (n+1)x^{n+1} + nx^{n+2})/(x-1)^2$$

$$7. \binom{n}{k} = \frac{n!}{(n-k)!k!}$$

$$8. \binom{n}{k} = \binom{n-1}{k} + \binom{n-1}{k-1}$$

$$9. \binom{n}{k} = \frac{n}{n-k} \binom{n-1}{k}$$

$$10. \binom{n}{k} = \frac{n-k+1}{k} \binom{n}{k-1}$$

$$11. \binom{n+1}{k} = \frac{n+1}{n-k+1} \binom{n}{k}$$

$$12. \binom{n}{k+1} = \frac{n-k}{k+1} \binom{n}{k}$$

$$13. \sum_{k=1}^n k \binom{n}{k} = n2^{n-1}$$

$$14. \sum_{k=1}^n k^2 \binom{n}{k} = (n + n^2)2^{n-2}$$

$$15. \binom{m+n}{r} = \sum_{k=0}^r \binom{m}{k} \binom{n}{r-k}$$

$$16. \binom{n}{k} = \prod_{i=1}^k \frac{n-k+i}{i}$$

$$17. a^{\phi(n)} \equiv 1 \pmod{n} \text{ where } \phi(n) \text{ is Euler Totient Function.}$$

$$18. a^{b \pmod{\phi(m)}} \equiv a^{b \pmod{\phi(m)}} \pmod{m} \text{ where } a \text{ and } m \text{ are coprime.}$$

