

Riley Smith, Richard Hua, and Caitlin Feldewerth

Comparing Sorting Algorithms

CPE 202-05

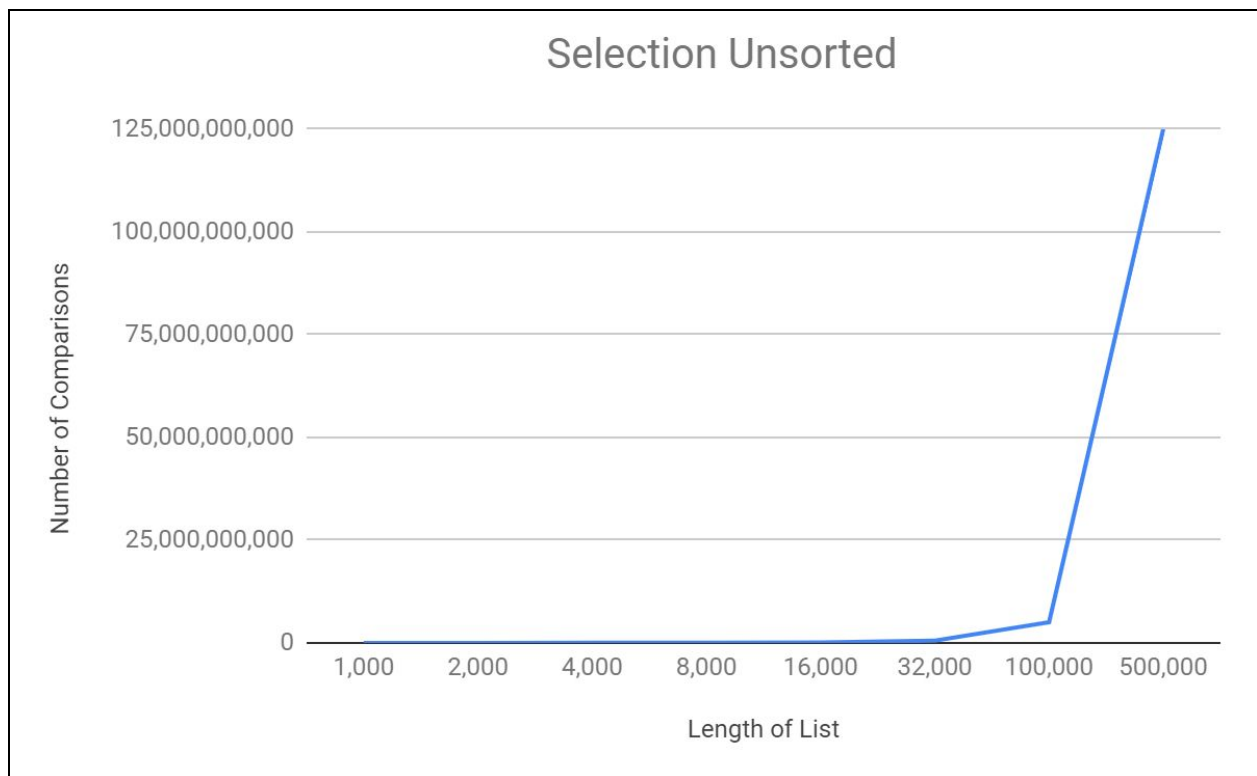
Toshihiro Kuboi

02/24/2020

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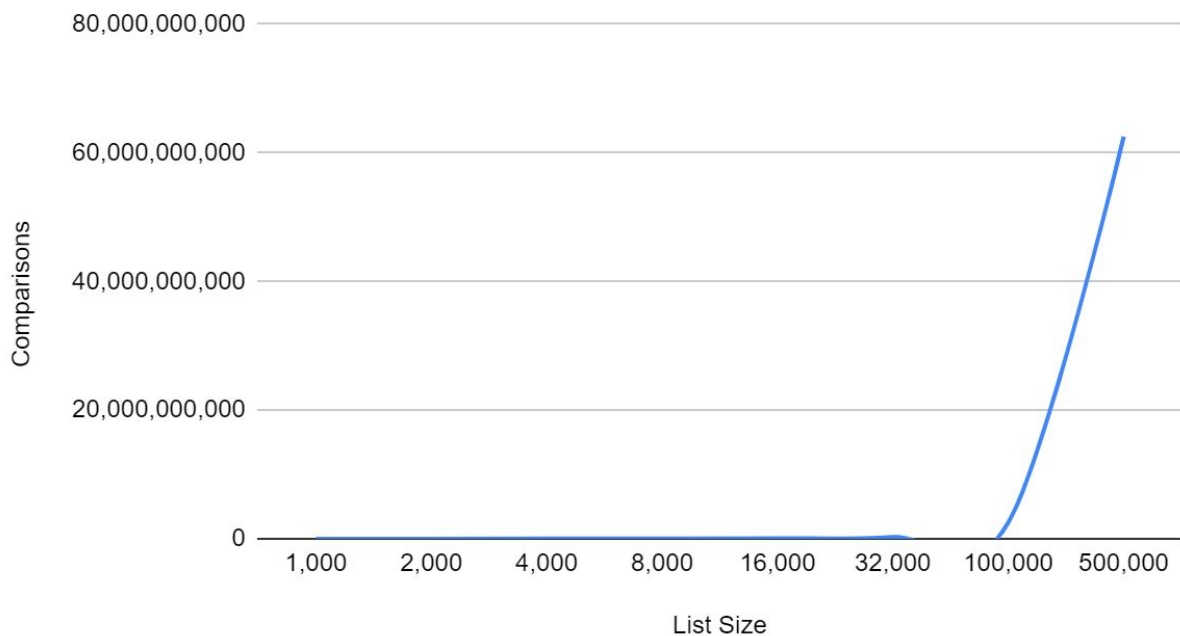
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Selection Sort (Unsorted List)		
List Size	Comparisons	Time (seconds)
1,000	499,500	0.12432527542114258
2,000	1,999,000	0.5058417320251465
4,000	7,998,000	2.215327739715576
8,000	31,996,000	9.760668277740479
16,000	127,992,000	37.508360862731934
32,000	511,984,000	151.21382403373718
100,000	4,999,950,000	1688.3581149578094
500,000	124,999,750,000	142367.876892647

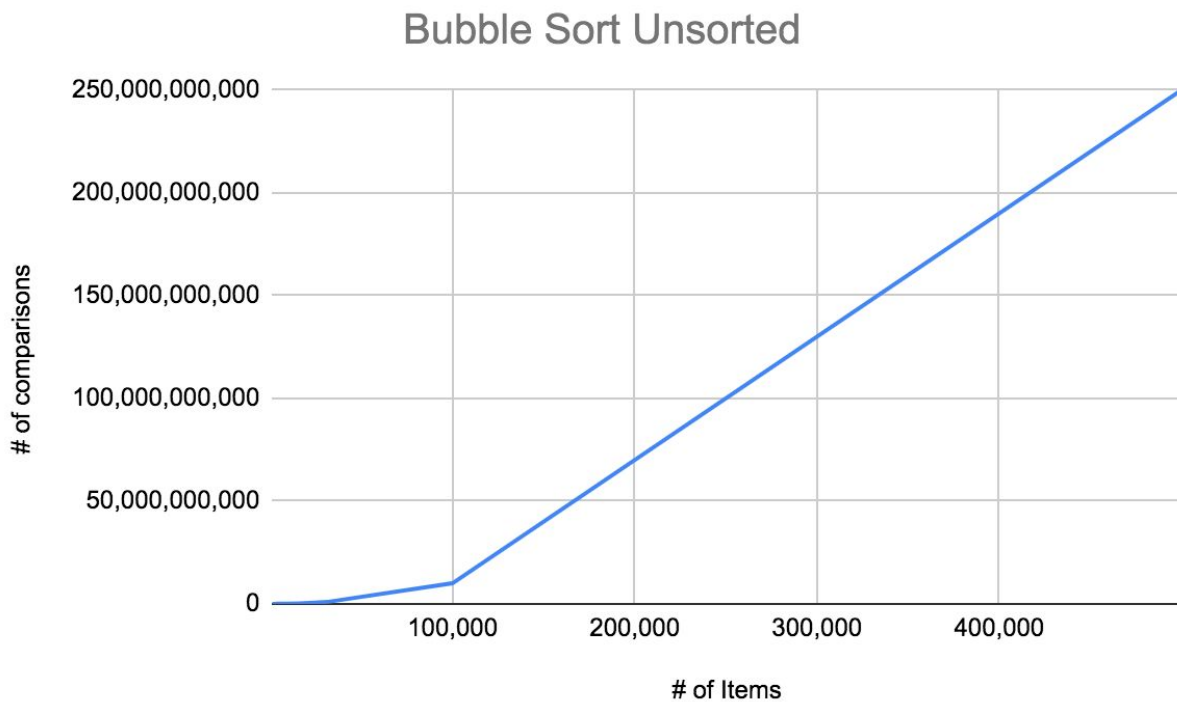


Insertion Sort (Unsorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	249,655	0.258291
2,000	997,982	0.956803
4,000	4,050,919	4.302346
8,000	16,137,520	18.385138
16,000	64,488,700	109.607708
32,000	255,925,135	405.932389
100,000	2,499,656,027	3308.376714
500,000	62,508,426,921	16508.268954

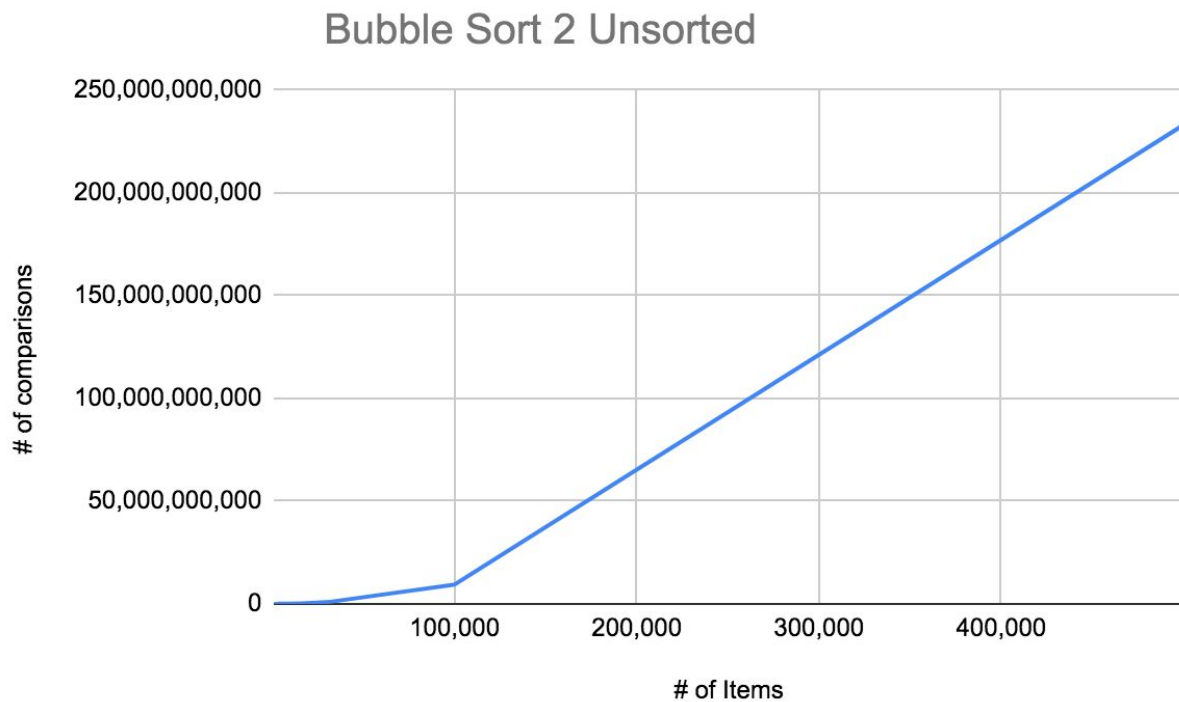
Insertion Sort (Unsorted): Comparisons vs. List Size



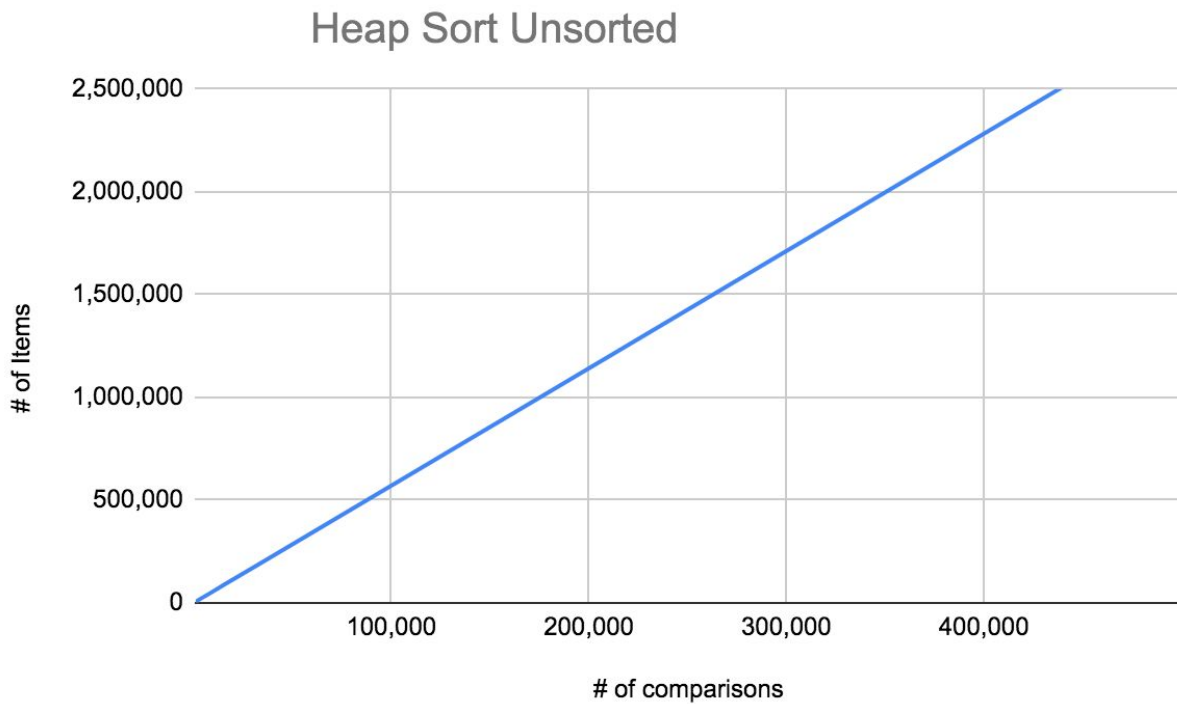
Bubble Sort (Unsorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	999,000	0.4341693761935452
2,000	3,998,000	1.7618364513743854
4,000	15,996,000	7.28194356103456195
8,000	63,992,000	29.62397235690657
16,000	255,984,000	119.13540987364124
32,000	1,023,968,000	483.2349716351868
100,000	9,999,900,000	5424.1249764824312
500,000	249,999,500,000	135603.1241567658



Bubble Sort 2 (Unsorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	986,013	0.3227822780609131
2,000	3,886,056	1.2701349258422852
4,000	15,568,107	5.180327415466309
8,000	63,760,029	20.74586009979248
16,000	255,312,042	87.31421685218811
32,000	1,021,247,832	345.6104579543056
100,000	4,094,992,935	1392.5671208943568
500,000	16,732,556,256	5642.139756032345

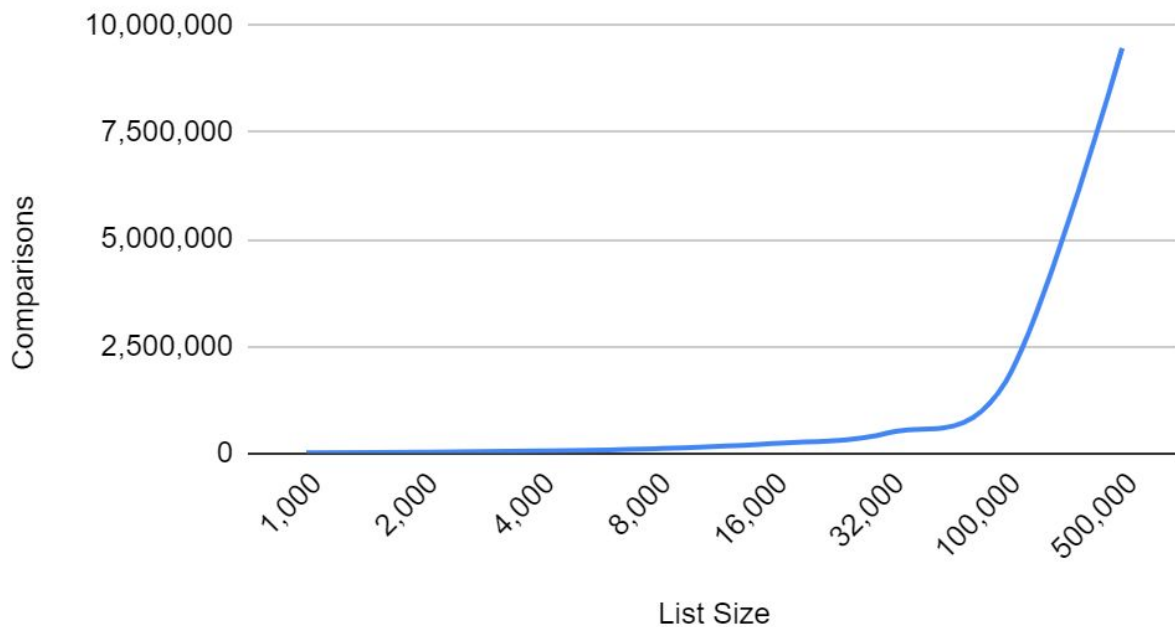


Heap Sort (Unsorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	5,606	0.00319818450141411
2,000	11,350	0.0065862148754608
4,000	22,752	0.01308333083451245
8,000	45,476	0.02637082376846453
16,000	91,399	0.05358694974779544
32,000	182,732	0.1168546086964944
100,000	570,396	0.3683962813614809
500,000	2,853,444	1.9228098076857565

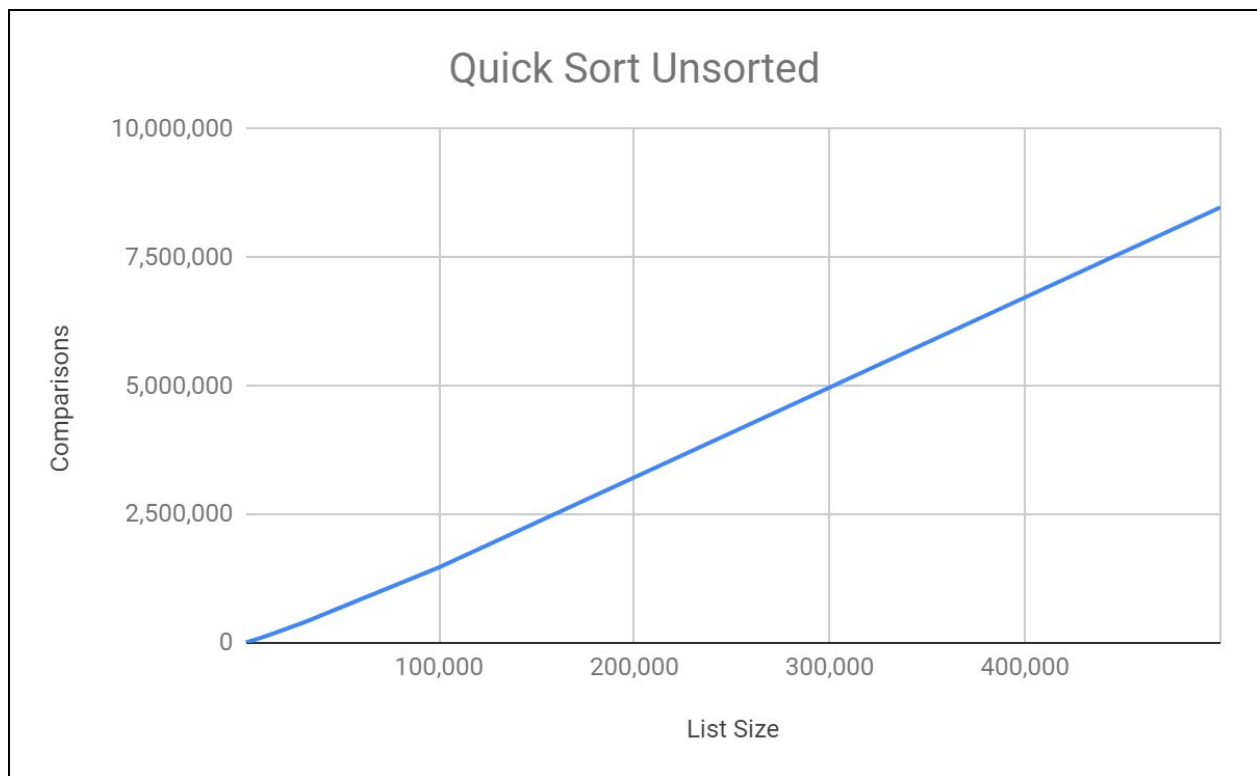


Merge Sort (Unsorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	9,976	0.008014
2,000	21,952	0.013962
4,000	47,904	0.028996
8,000	103,808	0.063829
16,000	223,616	0.134565
32,000	479,232	0.321771
100,000	1,668,928	1.102915
500,000	9,475,712	6.330691

Merge Sort (Unsorted): Comparisons vs. List Size



Quick Sort (Unsorted List)		
List Size	Comparisons	Time (seconds)
1,000	7,987	0.010088920593261719
2,000	17,964	0.028272628784179688
4,000	39,917	0.039319515228271484
8,000	87,822	0.09403586387634277
16,000	191,631	0.19470667839050293
32,000	415,248	0.45737528800964355
100,000	1,468,946	1.4908151626586914
500,000	8,475,732	7.952672243118286

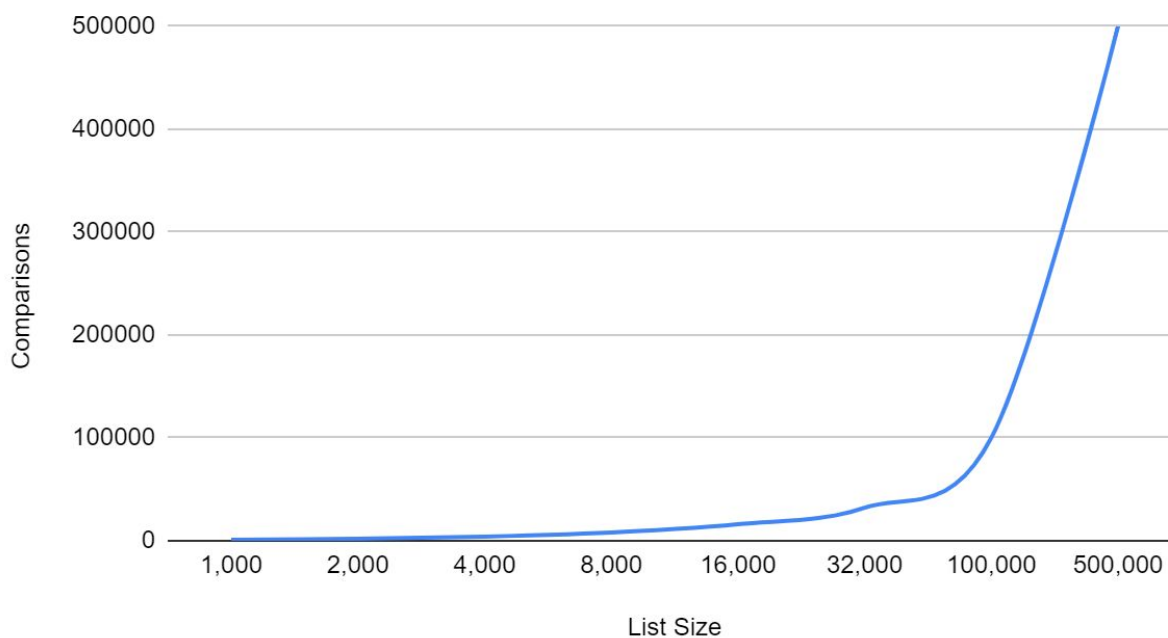


Selection Sort (Sorted List)		
List Size	Comparisons	Time (seconds)
1,000	499,500	0.1512000560760498
2,000	1,999,000	0.482633113861084
4,000	7,998,000	2.4250333309173584
8,000	31,996,000	8.644640684127808
16,000	127,992,000	36.27250647544861
32,000	511,984,000	139.73194479942322
100,000	4,999,950,000	1413.14169383049
500,000	124,999,750,000	16375.4563721901

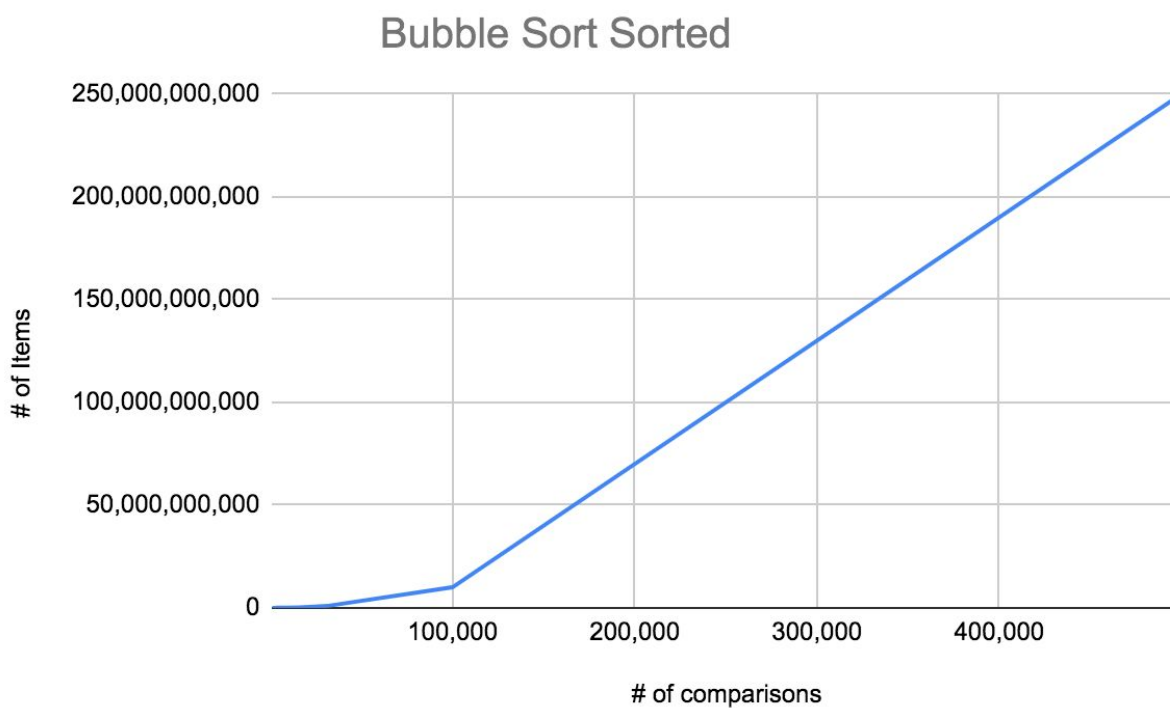


Insertion Sort (Sorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	999	0.001137
2,000	1,999	0.000997
4,000	3,999	0.001597
8,000	7,999	0.002609
16,000	15,999	0.006981
32,000	31,999	0.015958
100,000	99,999	0.026966
500,000	499,999	0.173655

Insertion Sort (Sorted): Comparisons vs. List Size

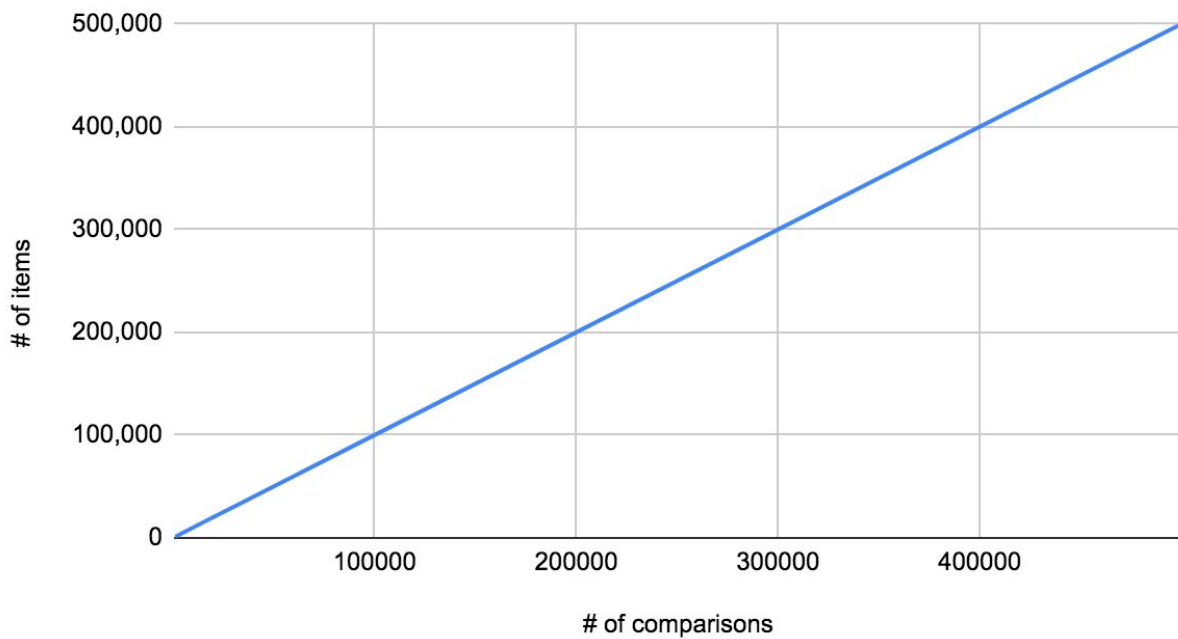


Bubble Sort (Sorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	999,000	0.29463624954223633
2,000	3,998,000	1.2923145294189453
4,000	15,996,000	5.601490020751953
8,000	63,992,000	20.136396884918213
16,000	255,984,000	81.1761257648468
32,000	1,023,968,000	327.3061249256134
100,000	9,999,900,000	3196.347854857544
500,000	249,999,500,000	79908.696544569032



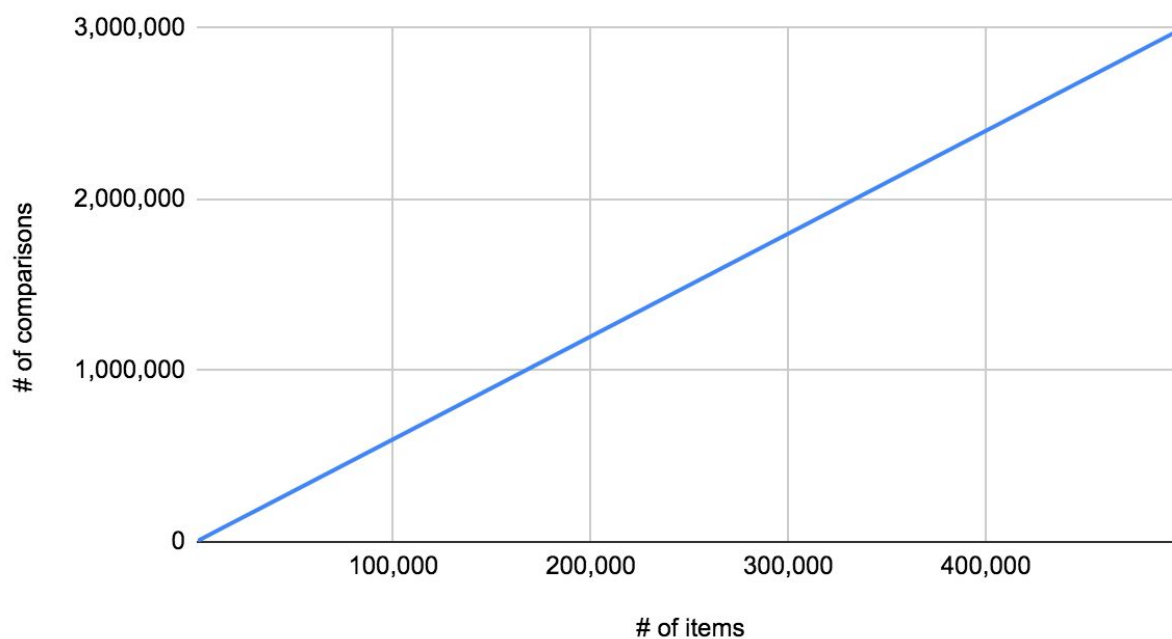
Bubble Sort 2 (Sorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	999	0.0002503395080566406
2,000	1,999	0.00044918060302734375
4,000	3,999	0.0009319782257080078
8,000	7,999	0.0017287731170654297
16,000	15,999	0.0036623477935791016
32,000	31,999	0.011517524719238281
100,000	99,999	0.03772878646850586
500,000	499,999	0.30599188804626465

Bubble Sort 2 Sorted



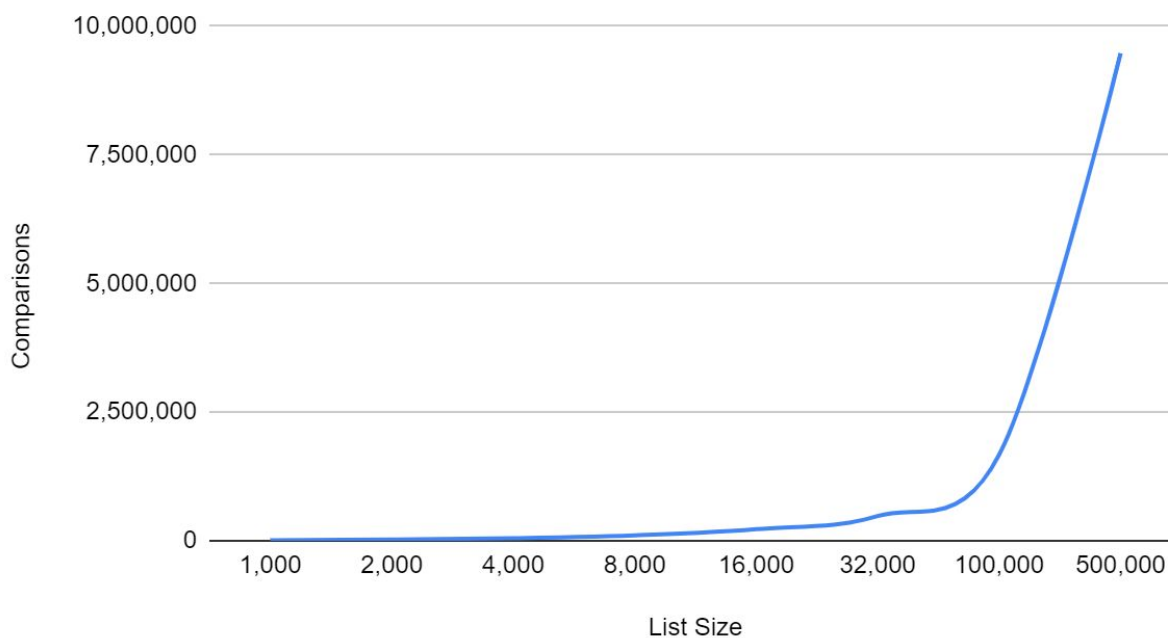
Heap Sort (Sorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	5,947	0.0035741329193115234
2,000	11,941	0.005722999572753906
4,000	23,935	0.011286497116088867
8,000	47,929	0.022029876708984375
16,000	95,923	0.0473935604095459
32,000	191,917	0.09520626068115234
100,000	599,905	0.27698397636413574
500,000	2,999,893	1.8897888660430908

Heap Sort Sorted

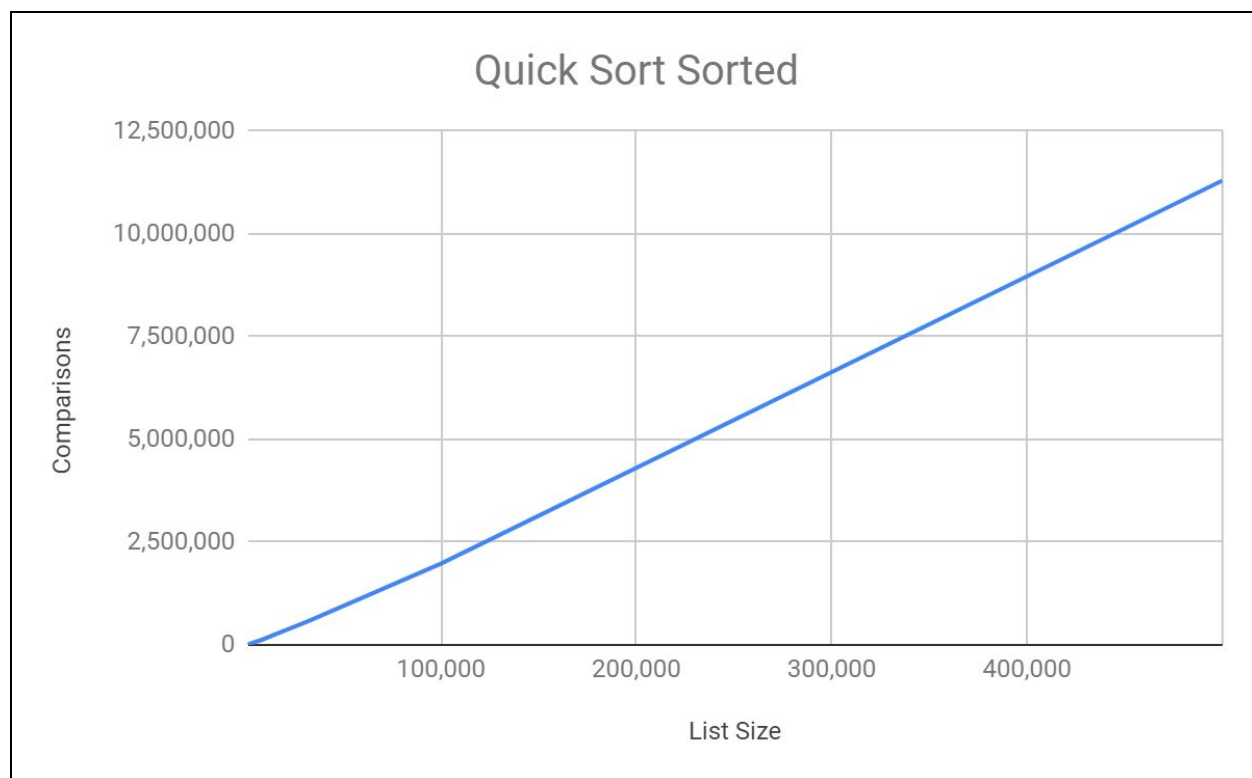


Merge Sort (Sorted List)		
List Size:	Comparisons:	Time (seconds):
1,000	9,976	0.004986
2,000	21,952	0.011969
4,000	47,904	0.024452
8,000	103,808	0.048869
16,000	223,616	0.107174
32,000	479,232	0.230814
100,000	1,668,928	0.938532
500,000	9,475,712	5.310837

Merge Sort (Sorted): Comparisons vs. List Size



Quick Sort (Sorted List)		
List Size	Comparisons	Time (seconds)
1,000	11,515	0.009360074996948242
2,000	23,235	0.019350290298461914
4,000	56,534	0.036003828048706055
8,000	117,266	0.0812985897064209
16,000	271,525	0.2079460620880127
32,000	573,524	0.3598630428314209
100,000	1,976,867	1.3532264232635498
500,000	11,296,579	7.721241235733032



1. Which sort do you think is better? Why?

I think that Heap sort is the best because it is $O(n \log n)$ in both worst and best cases and it also has a space complexity of $O(1)$. In our trials it was a few seconds faster than both Merge sort and Quick sort in the 500,000 item trial. The only drawback that I see with Heap sort is that it is not stable, although in this lab stability was not something that was important since we were only sorting simple integers.

2. Which sort is better when sorting a list that is already sorted (or mostly sorted)? Why?

When a list is nearly sorted completely sorted, insertion sort and bubble sort 2 are the best algorithms to use. Insertion sort is better for a nearly sorted list because it does not need to run through n numbers to sort each item, so when the list is nearly sorted it can be closer to $O(n)$ time than its worst case of $O(n^2)$. When we have a sorted list, the best algorithm to use would be bubble sort 2. This is because bubble sort 2 can recognize when it goes through an iteration and no swaps were made. This means that it can sort the list in $O(n)$ time.

3. You probably found that insertion sort had about as many comparisons as selection sort. Why? Why are the times for insertion sort not half what they are for selection sort?

The reason why insertion sort can finish sorting with so many less comparisons than selection sort is because insertion sort does not always go through the n numbers in the array when it picks a number to insert into the sorted portion of the list. It will on average only go through $n/2$ items before inserting an item to a sorted portion of the list.