

MATHS-7B

SEMESTER-5

LONGS

▶ short tricks 40

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*UNIT-1:-

① find the Laplace transforms of the function

$$f(t) = \begin{cases} 2t & ; 0 \leq t \leq 5 \\ 1 & ; t > 5 \end{cases}$$

★
② State and prove first shifting theorem? Also find the Laplace transforms of $e^{-3t}(2\cos 5t - 3\sin 5t)$. (Pg. 15)

★
③ state and prove Second shifting theorem? Also find Laplace transforms of $G(t) = \begin{cases} \sin(t - \frac{\pi}{3}) & ; t \geq \frac{\pi}{3} \\ 0 & ; t < \frac{\pi}{3} \end{cases}$. (Pg. 19)

★
④ State and prove change of scale property? Applying the change of scale property if $L[f(t)] = \frac{p^{\gamma} - p + 1}{(2p+1)^{\gamma}(p-1)}$
then S.T. $L[f(2t)] = \frac{p^{\gamma} - 2p + 4}{4(p+1)^{\gamma}(p-2)}$. (Pg. 22)

*UNIT-2 :-

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① State and prove Initial Value theorem? (Pg. NO. 16)

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② State and prove final Value theorem? (Pg. NO. 17)

③ state and prove Laplace transforms of integrals? (Pg. 18)

④ Evaluate i, $\int_0^{\infty} t e^{-2t} \sin t \, dt$

ii, $\int_0^{\infty} t e^{-2t} \cos t \, dt$. (Pg. NO. 7)

* UNIT-3 :-

① Find the Inverse Laplace of i, $\frac{s^2}{(s-2)^3}$ [Pg. 6]

ii, $\frac{6}{2s-3} - \frac{3+4s}{9s^2-16} + \frac{8-6s}{16s^2+9}$

★
② Define Inverse Laplace Transforms? State and Prove first shifting on inverse Laplace transforms [Pg. 13]

③ state and prove range of Scale property on Inverse Laplace Transforms. (Pg. 15)

★
④ state and prove Second shifting theorem on inverse Laplace Transforms? (Pg. 15)

* UNIT-4 :-

① Solve $(D^2 + D)x = 2$ if $x(0) = 3$, $x'(0) = 1$.

★
② solve by Laplace transform $\frac{d^2 y}{dt^2} + 2 \frac{dy}{dt} + 5y = e^t \sin t$,
where $y(0) = 0$, $y'(0) = 1$.

★
③ Solve the integral equation $f(t) = 1 + \int_0^t f(u) \sin(t-u) du$
& Verify your solution.

★
④ Solve the integral equation $\int_0^t \frac{f(u) du}{(t-u)^{1/3}} = t(1+t)$.

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* UNIT-5 :-

★ ① Find the Fourier transform of $f(x) = \begin{cases} 1-x^2 & ; |x| \leq 1 \\ 0 & ; |x| > 1 \end{cases}$
and Hence evaluate $\int_0^{\infty} \left(\frac{x \cos x - \sin x}{x^3} \right) \cos \frac{x}{2} dx$.

② Find Fourier Sine transform of $\frac{e^{-ax}}{x}$ and deduce
that $\int_0^{\infty} \frac{e^{-ax} - e^{-bx}}{x} \sin px \, dx = \tan^{-1} \frac{p}{a} - \tan^{-1} \frac{p}{b}$.

★ ③ Find the finite sine transform of $f(x)$ if

$$f(x) = \begin{cases} x & ; 0 \leq x \leq \pi/2 \\ \pi - x & ; \pi/2 \leq x \leq \pi. \end{cases}$$

★ ④ Find the finite Fourier Sine transform of
 $f(x) = x^2$, $0 \leq x \leq 4$.

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SHORTS

* UNIT-1 :-

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- ★ ① Find Laplace Transforms of
- $e^{2t} - ut^3 - 2\sin 3t + 3\cos 3t$
 - $t^3 + 2t^2 - ut + 6$ (Pg. NO. 6)
- ② Find $L(\cos(at+b))$ and $L(\sin t - \cos t)^2$ (Pg. NO. 10)
- ★ ③ Evaluate $L(e^{3t} \sin^2 t)$ and $L(e^{-2t} \sin 4t)$. (Pg. 17)
- ★ ④ Find $L(f(t))$, where
- $$f(t) = \begin{cases} 4 & ; 0 < t < 1 \\ 3 & ; t > 1 \end{cases} \quad [\text{Pg. NO. 12}]$$

* UNIT-2 :-

- ① Find the Laplace Transforms of i, $t \cos at$ ii, $t^2 \sin at$ iii, $t^3 e^{-3t}$. (Pg. 3)
- ★ ② P.T. $L\left(\frac{\sin t}{t}\right) = \tan^{-1} \frac{1}{p}$. Hence find $L\left(\frac{\sin at}{t}\right)$. (Pg. 5)
- ★ ③ Evaluate i, $L\left(e^{-ut} \frac{\sin 3t}{t}\right)$ ii, $\int_p^\infty t \sin^{-3t} \sin t$ (Pg. 9)

* UNIT-3 :-

- ★ ① Evaluate $L^{-1}\left[\frac{s+1}{s^2+6s+25}\right]$. (Pg. NO. 5)
- ② Evaluate $L^{-1}\left[\frac{s+3}{s^2-4s+13}\right]$ (Pg. 6)
- ③ Evaluate $L^{-1}\left[\frac{3(s^2-2)^2}{2s^5}\right]$ (Pg. 9)
- ★ ④ Evaluate $L^{-1}\left[\frac{2s-5}{4s^2+25} + \frac{4s-18}{9-s^2}\right]$ (Pg. 9)

UNIT-4 :-

- ★ ① Solve $(D^2 - 2D + 2)y = 0$, $y = Dy = 1$, when $t = 0$.
- ② Show that $f(t) = \cos t + \int_0^t e^{-u} f(t-u) du$.
- ★ ③ Solve the integral equation $F(t) = a \sin t - 2 \int_0^t F(u) \cos(t-u) du$.
- ④ Solve $(D^2 + 1)x = t \cos 2t$ given $x = 0, \frac{dx}{dt} = 0$, at $t = 0$.

* Unit 5:

- ★ ① Define Fourier Sine and Cosine integrals.
- ② Define shifting property.
- ★ ③ Find Fourier Sine & cosine transform of $f(x) = x$.
- ④ Show that $\int_0^\infty \frac{\cos \lambda x}{\lambda^2 + 1} d\lambda = \frac{\pi}{2} e^{-x}$, $x > 0$
- ★ ⑤ state and prove parseval's Identity.

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