## **Tutorial 2 Question**

- Text: Ch. 42: Pr. 54.
- An ancient club is found that contains  $190~\mathrm{g}$  of carbon and has an activity of  $5.0~\mathrm{decays}$  per second. Determine its age assuming that in living trees the ratio of  $^{14}\mathrm{C}/^{12}\mathrm{C}$  atoms is about  $1.3\times10^{-12}$ .

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## Solution, contd

- ▶ Now  $N_0$ . Initially, a fraction  $1.3 \times 10^{-12}$  of the carbon was  $^{14}C$
- ▶ Using that and  $\boxed{1~u=1.66\times10^{-27}~kg}$  we can calculate the initial number of  $^{14}C$  atoms,

$$N_0 = (1.3 \times 10^{-12})(0.190 \text{ kg}) \times \frac{1 \text{ u}}{1.66 \times 10^{-27} \text{ kg}} \times \frac{1 \text{ atom}}{12 \text{ u}}$$
  
=  $1.2 \times 10^{13} \text{ atoms}.$ 

- ▶ We used an atomic mass of  $12~\mathrm{u}$  because  $\overline{\text{almost all}}$  of the carbon is  $^{12}\mathrm{C}$ .
- ▶ Lastly N. We are given the activity  $\left| \frac{dN}{dt} \right| = 5.0 \ \mathrm{atoms/s.}$

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## Solution

■ We know  $N(t) = N_0 e^{-\lambda t}$  . Want to solve for t, so

$$t = \frac{1}{\lambda} \ln \frac{N_0}{N}.$$

- ▶ Need to find  $\lambda$ ,  $N_0$ , and N.
- ullet First  $\lambda$ . Given  $\left|T_{1/2}=rac{\ln 2}{\lambda}
  ight|$  we find

$$\lambda = \frac{\ln 2}{T_{1/2}} = \frac{0.693}{5730 \text{ yr}}$$
$$= 1.21 \times 10^{-4} \text{ yr}^{-1}$$
$$= 3.83 \times 10^{-12} \text{ s}^{-1}.$$

(Note:  $1 \text{ yr} \approx 3.166 \times 10^7 \text{ s.}$ )

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## Solution, contd

■ Differentiating  $N(t) = N_0 e^{-\lambda t}$  gives

$$\frac{dN}{dt} = -\lambda N_0 e^{-\lambda t}$$
$$= -\lambda N.$$

So we find

$$N = \frac{1}{\lambda} \left| \frac{dN}{dt} \right|$$

$$= \frac{1}{3.83 \times 10^{-12} \, \text{s}^{-1}} \times 5.0 \text{ atoms/s}$$

$$= 1.3 \times 10^{12} \text{ atoms.}$$

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Solution, contd $t = \frac{1}{\lambda} \ln \frac{N_0}{N}$ $t = \frac{1}{\lambda} \ln \frac{N_0}{N}$ $= \frac{1}{3.83 \times 10^{-12}  \mathrm{s}^{-1}} \ln \left( \frac{1.2 \times 10^{13}  \mathrm{atoms}}{1.3 \times 10^{12}  \mathrm{atoms}} \right)$ $= 5.8 \times 10^{11}  \mathrm{s}$ $= 18,000  \mathrm{yr}.$	The club is around 18,000 years old.	