

# Magnetic Resonant Coupling As a Potential Means for Wireless Power Transfer to Multiple Small Receivers

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**Abstract**—Wireless power transfer via magnetic resonant coupling is experimentally demonstrated in a system with a large source coil and either one or two small receivers. Resonance between source and load coils is achieved with lumped capacitors terminating the coils. A circuit model is developed to describe the system with a single receiver, and extended to describe the system with two receivers. With parameter values chosen to obtain good fits, the circuit models yield transfer frequency responses that are in good agreement with experimental measurements over a range of frequencies that span the resonance. Resonant frequency splitting is observed experimentally and described theoretically for the multiple receiver system. In the single receiver system at resonance, more than 50% of the power that is supplied by the actual source is delivered to the load. In a multiple receiver system, a means for tracking frequency shifts and continuously retuning the lumped capacitances that terminate each receiver coil so as to maximize efficiency is a key issue for future work.

**Index Terms**—Microrobotics, resonant coupling, swarm robotics, wireless power.

## I. INTRODUCTION

A N EFFICIENT method for wireless power transfer would enable advances in such diverse areas as embedded computing, mobile computing, sensor networks, and microrobotics. The need to minimize energy consumption is often the main design driver in applications where devices need to operate untethered. Energy consumption often restricts or severely limits functionality in such applications.

The work described in this paper is motivated by potential application of magnetic resonant coupling as a means for wireless power transfer from a source coil to multiple receivers. Through simple experimental setups and corresponding circuit models, we address issues that are involved in applying the basic mechanism to both a single receiver and multiple receivers with sizes much smaller than the source coil.

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Inductive coupling is an old and well-understood method of wireless power transfer. The source drives a primary coil, creating a sinusoidally varying magnetic field, which induces a voltage across the terminals of a secondary coil, and thus transfers power to a load. This mechanism, responsible for power transfer in a transformer, where the magnetic field is typically confined to a high permeability core, also functions when the region between the primary and secondary coils is simply air. Inductive coupling without high permeability cores is used, for example, to power RF ID tags and medical implants [1]–[3]. A common technique for increasing the voltage received by the device to be powered is to add a parallel capacitor to the secondary to form a resonant circuit at the operating frequency [1], [2]. Application of this principle has also been demonstrated for powering robot swarms [4]. In this case, resonance was used on the primary but not on the secondary windings on the robots. This was done to minimize performance variations resulting from interactions among the robots. Recent work [5] has shown that when resonance is used on both the primary and secondary, power can be transferred with very little radiated loss and with 40%–50% of the source power delivered to the load, even when the secondary coil links only a relatively small part of the magnetic field that is created by the primary. A coupled-mode analysis of the interaction between a pair of resonant coils has also been presented [5], [6]. Finally, an inductively coupled radio frequency wireless transmission system has been described, with reference to multiple resonant peaks for multiple receivers [7].

In the work described here, there are two new contributions:

- 1) We demonstrate power transfer from a single resonant source coil to multiple resonant receivers, focusing upon the resonant frequency splitting issues that arise in multiple receiver applications.
- 2) We show that resonant coupling systems with either single or multiple receivers can be modeled using a relatively simple circuit description. The model rigorously takes into account mutual coupling between all coils, and does not make approximations usually associated with the coupled-mode approach [8]. This description makes it clear that high Q resonant coupling is key to the efficiency of the system, through an implementation where the primary coil is inductively coupled to the power source and the receiving coils are inductively coupled to the loads.

We expect this work to form a basis for understanding and extending the resonant coupling mechanism to multiple mobile receivers. The main challenge for such a system is to adjust the

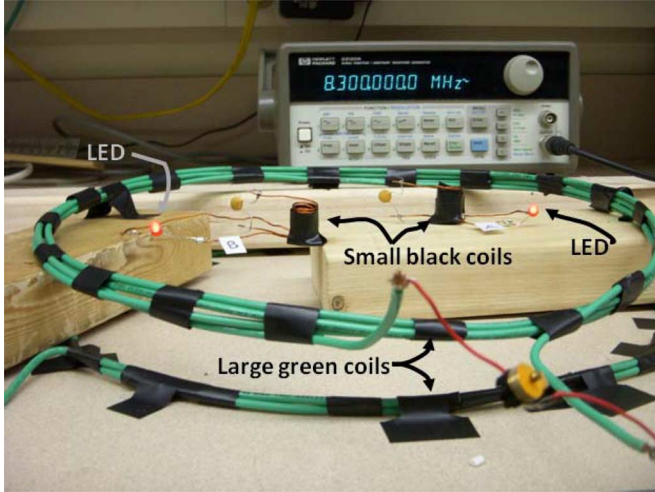


Fig. 1. Photograph of a signal generator wirelessly supplying power to two LEDs (tagged A and B) through magnetic resonant coupling between large (green) and small (black) coils. The signal generator drives the lower green coil, while lumped capacitors terminate the upper green coil and each of two small receiving coils, which in turn are inductively coupled to coils that drive the LEDs.

lumped capacitances at the terminals of the receivers as they move with respect to the source coil and with respect to one another.

## II. EXPERIMENTAL SETUP OF A RESONANT COUPLED SYSTEM WITH TWO LOADS

Fig. 1 shows a photograph of a resonant coupling system wherein a signal generator delivers power to two illuminated LEDs (tagged A and B). The source, operating at a resonant frequency of 8.3 MHz, is connected directly across the terminals of the lower of two large green coils with diameters of 30 cm, spaced 3.8 cm apart. The upper green coil is inductively coupled to the lower coil, and is terminated by an adjustable lumped capacitor (with red leads). In the center of the upper green coil are two small receivers, each of which consists of a coil with diameter 1.3 cm that is terminated by a lumped capacitor, inductively coupled to a separate coil with the same diameter that is terminated by an LED. The two coils in each of the two receivers are together wrapped in black electrical tape. The system thus involves a total of six coils, a “source coil pair” and a “receiving coil pair” for each of two receivers associated with the two loads. The fact that the source and loads are connected to coils that are inductively coupled to, but distinct from the coils that are terminated by lumped capacitances is key to establishing a high Q resonant coupling, with the resonant frequency determined by adjusting the lumped capacitances.

## III. CIRCUIT REPRESENTATION OF A RESONANT COUPLED SYSTEM WITH A SINGLE LOAD

Fig. 2 shows a schematic circuit representation of a system like the experimental system shown in Fig. 1, but with only a single load coil pair. We use this system to develop an understanding of the resonant coupling mechanism and to serve as

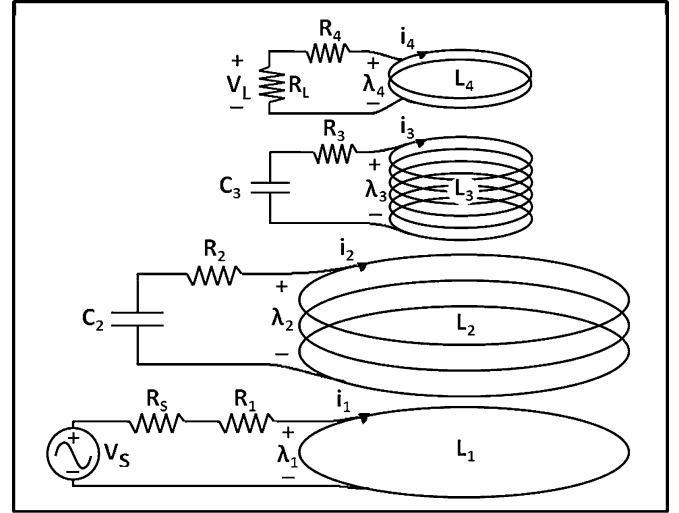


Fig. 2. A schematic circuit drawing of a source coil pair and a single-receiving coil pair. Each load in a multiple receiver system involves a receiving coil pair.

a basis for extending it to multiple receivers. Our experimental results include measurements for both the two-receiver system that is shown in Fig. 1 and for a single-receiver system corresponding to the circuit representation shown in Fig. 2.

In the single-receiver system of Fig. 2, the source drives a large single-turn coil, labeled  $L_1$  that is inductively coupled to a large multiturn resonant coil  $L_2$  of the same diameter. The small resonant coil  $L_3$  is inductively coupled to a small coil of the same diameter, labeled  $L_4$ , that is terminated by a load element. Lumped capacitors  $C_2$  and  $C_3$  respectively terminate the resonant coils  $L_2$  and  $L_3$ . The resistances  $R_1$ ,  $R_2$ ,  $R_3$ , and  $R_4$  are the small resistances of the coils themselves, while  $R_S$  is the internal resistance of the source, and  $R_L$  is the load resistance. (The LEDs in Fig. 1 are nonlinear elements, used to demonstrate wireless power transfer. Measurements and the corresponding circuit representation described here and in subsequent sections use a resistive load.)

The work described in [5] used two identical open-circuited “self-resonant” coils, with a resonant frequency based upon the distributed inductance and distributed capacitance of each coil. Here, with completely different source and receiver coils, the lumped capacitances are chosen so as to yield identical resonant frequencies,

$$\omega_0 = \frac{1}{\sqrt{L_2 C_2}} = \frac{1}{\sqrt{L_3 C_3}}. \quad (1)$$

This alteration provides a simple means to achieve resonant coupling between a large source coil and one or several small receiving coils.

## IV. CIRCUIT ANALYSIS

A circuit model for the experimental setup with only one receiving coil pair driving a single load, as represented in Fig. 2, is based upon the application of Kirchhoff’s voltage law around each of the four loops. The voltage at the terminals of each coil is described as the time rate of change of flux linkage.  $\Lambda_1$  through

$\Lambda_4$  and  $i_1$  through  $i_4$  represent complex amplitudes of flux linkages and currents in each of the four coils;  $V_S$  represents the complex amplitude of the ideal voltage source. With resistances  $R_1$  through  $R_4$ ,  $R_S$ , and  $R_L$ , and capacitances  $C_2$  and  $C_3$ , the circuit constraints at frequency  $\omega$  are

$$V_S = (R_S + R_1) i_1 + j\omega\Lambda_1 \quad (2)$$

$$0 = R_2 i_2 + \frac{i_2}{j\omega C_2} + j\omega\Lambda_2 \quad (3)$$

$$0 = R_3 i_3 + \frac{i_3}{j\omega C_3} + j\omega\Lambda_3 \quad (4)$$

$$0 = (R_4 + R_L) i_4 + j\omega\Lambda_4. \quad (5)$$

Since each of the four coils is inductively coupled to the other three, the flux linkages are related to the currents by a symmetric  $4 \times 4$  inductance matrix:

$$\begin{bmatrix} \Lambda_1 \\ \Lambda_2 \\ \Lambda_3 \\ \Lambda_4 \end{bmatrix} = \begin{bmatrix} L_{11} & M_{12} & M_{13} & M_{14} \\ M_{12} & L_{22} & M_{23} & M_{24} \\ M_{13} & M_{23} & L_{33} & M_{34} \\ M_{14} & M_{24} & M_{34} & L_{44} \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ i_3 \\ i_4 \end{bmatrix}. \quad (6)$$

For a known ideal source voltage  $V_S$  and known resistances, capacitances, and self inductances and mutual inductances, (2) to (5), with (6) substituted for the flux linkages, comprise four simultaneous equations that determine the currents  $i_1$  through  $i_4$ , and thus the complex amplitude of the load voltage  $V_L = -R_L i_4$ . Since the system is linear, this analysis determines the transfer function based upon the source frequency,  $|(V_L/V_S)(\omega)|$ .

Extension of the circuit model to multiple loads, as for the experimental two-load system shown in Fig. 1, is straightforward, with six equations replacing four. More generally, extension to an arbitrary number of loads is described in Section VIII.

The use of a circuit model here is appropriate because, as described in [5], the interaction involves magnetoquasistatic field structures. Equivalently, we can compare radiated electromagnetic power with power dissipated in the resistances of the circuit model. The radiation resistance  $R_r$  of a coil with  $N$  turns and radius  $a$ , at source frequency  $f$  and corresponding free space wavelength  $\lambda = c/f$  where  $c = 3.00 \times 10^8$  m/s is [9]

$$R_r = 20 \left( \frac{2\pi}{\lambda} \right)^4 (\pi a^2 N)^2. \quad (7)$$

Coil 2, then has the largest radiation resistance, with value  $R_{r2} = 8.7 \times 10^{-4} \Omega$ , which is far too small in comparison with the ohmic resistance  $R_2$  to be significant.

Unintended magnetic coupling with nearby objects is of far less significance than it would be at higher frequencies, with wavelengths on the scale of the transmitting coil.

## V. COMPARISON OF CIRCUIT MODEL WITH EXPERIMENTAL MEASUREMENTS WITH A SINGLE RECEIVER

Methods of determination and values for the various parameters in the circuit model described in Sections III and IV are given in the Appendix. Resistances, capacitances, and self-inductances are calculated values, while the coupling coefficients

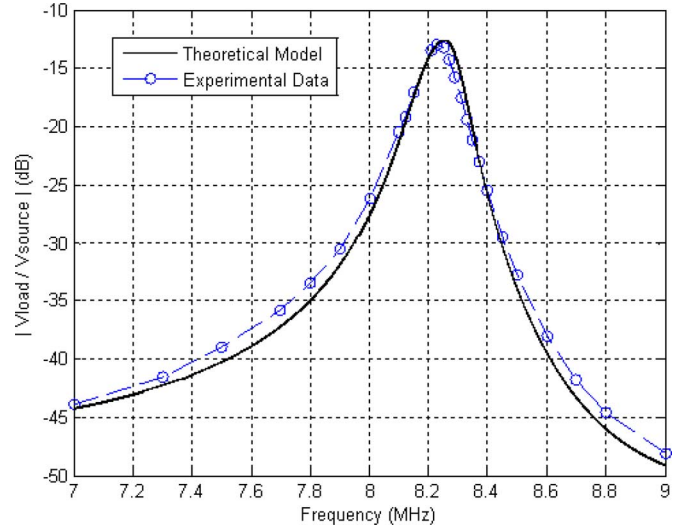


Fig. 3. Transfer function  $|(V_L/V_S)(\omega)|$  near the resonant peak as measured experimentally and as calculated from the circuit model for the resonant coupled system with a single receiver.

coefficients that determine mutual inductances are chosen so as to fit the theoretical model to the experimental frequency response of the system. Fig. 3 shows a theoretical curve based upon the circuit model for a set of coupling coefficients that yields a good fit, along with experimental data points on a power decibel scale.

It is apparent from Fig. 3 that the circuit model, with appropriately chosen parameter values, accurately describes the measured behavior of the resonant coupled system with a single receiver. It is likely that a robust minimization algorithm could be used to obtain even better agreement, but derivation of the coupling coefficients from first principles and refinement of the calculations of resistances, capacitances, and self-inductances are goals of ongoing work.

## VI. EFFICIENCY AND EVALUATION OF POWER LOSSES WITH A SINGLE RECEIVER

For the experimental setup with a single receiver, the rms voltage across a 100- $\Omega$  resistive load placed in the center of the transmitting coil is 1.68 V, corresponding to a wireless delivered power of 28.2 mW. When the receiver is displaced 17 cm away from and along the axis of the transmitting coil (about 1 coil radius), the voltage drops by about a factor of 3 to 0.57 V, corresponding to 3.3 mW power delivered.

The difference between supplied and received power for the system with a single receiver is accounted for in the circuit model through power dissipation in the resistances. For the parameter values listed in the Appendix, 51.4% of the power that leaves the terminals of the actual source (ideal source in series with internal resistance  $R_S$ ) is delivered to the load resistance  $R_L$ .

The percentages of the total power that is supplied by the ideal source  $V_S$  for the single-receiver system are:

- 1) 9.1% to load resistance  $R_L$ ;
- 2) 82.3% to internal source resistance  $R_S$ ;
- 3) 0.1% to source coil resistance  $R_1$ ;
- 4) 6.8% to primary coil resistance  $R_2$ ;

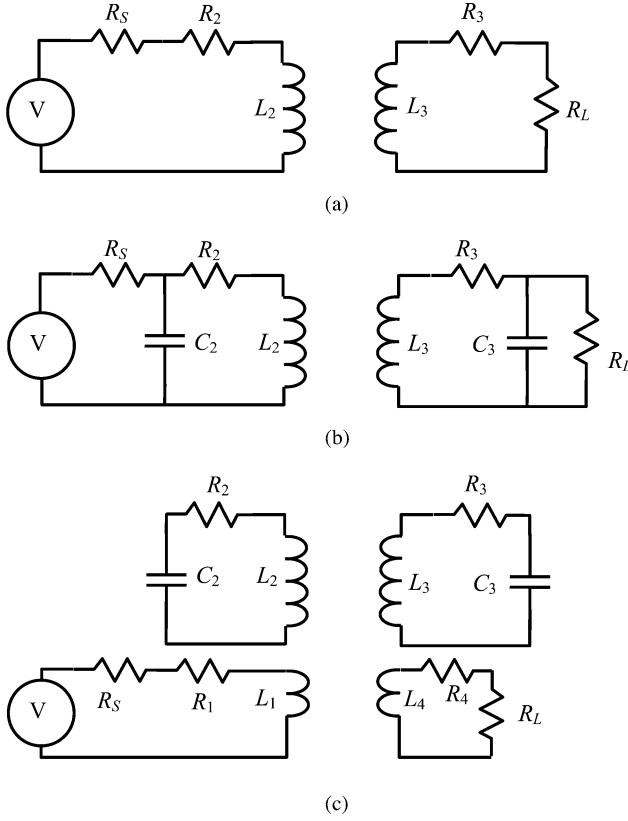


Fig. 4. Circuits illustrating nonresonant and resonant coupling. (a) Nonresonant inductive coupling. (b) Resonant coupling with significant loading by the source and load, resulting in low  $Q$ . (c) Resonant coupling with source and load inductively coupled to the resonant circuits in such a way as to reflect high parallel impedances, resulting in a high  $Q$ .

- 5) 1.7% to secondary coil resistance  $R_3$ ;
- 6) 0.0% to load coil resistance  $R_4$ .

Thus, the dominant loss occurs in the internal source resistance  $R_S$ . This loss occurs whenever a source delivers power to a load, whether through wires or through a wireless power transfer method. (The high internal resistance of the function generator, used here only for concept demonstration, can be significantly reduced by using a more practical power source.) More than half of the remaining power is delivered to the load resistance  $R_L$ , with dissipation in the primary coil resistance  $R_2$ , the largest loss beyond the actual source terminals. The degree to which resistive losses can be reduced from the simple demonstration setup described here is a subject of our ongoing work.

## VII. COMPARISON WITH FREQUENCY RESPONSE FOR SIMPLE INDUCTIVE COUPLING

The circuit model provides a simple way to understand what is accomplished by the resonant coupling mechanism and how it differs from simple inductive coupling. Fig. 4 shows three circuits providing inductive coupling to the load. Fig. 4(a) shows simple nonresonant coupling, while (b) and (c) shows variations of resonant coupling. In Fig. 4(b), the source and load resistances are approximately in parallel with parallel  $LC$  reso-

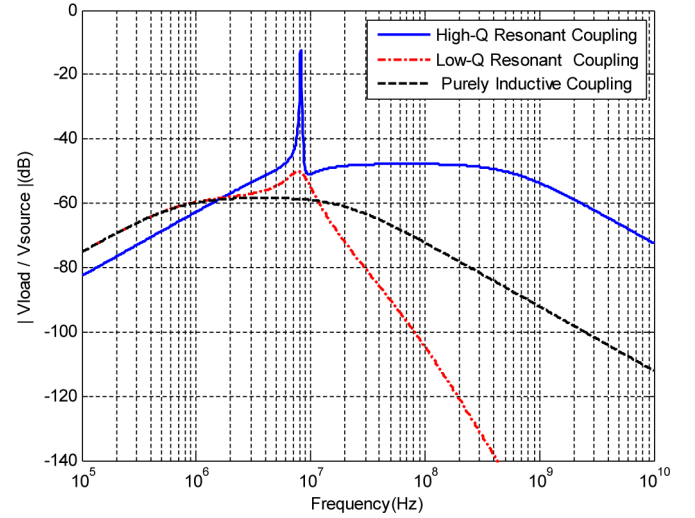


Fig. 5. Transfer function  $|(V_L/V_S)(\omega)|$  over a wide frequency range from the circuit model for the resonant coupled system, and for two simple systems that connect the source and load directly to the coupled coils.

nant circuits if the ohmic resistances  $R_2, R_3$  are small. Here the circuit  $Q$  is determined by the loading provided by  $R_S, R_L$ . In contrast, in Fig. 4(c), which corresponds to the system described in this paper, the source and load impedances are inductively coupled to the resonant circuits. In this case, the turns ratios can be chosen so that  $R_S, R_L$  are transformed into much larger effective resistances in parallel with the  $LC$  resonant circuits, resulting in a larger  $Q$ . Fig. 5 shows  $|(V_L/V_S)(\omega)|$  as computed using these circuit models and component values appropriate for our experiment, as given in the Appendix. For the case of simple inductive coupling [Fig. 4(a)], the transfer function is almost constant at  $-58$  dB for frequencies between 1 and 10 MHz, with low and high frequency 20 dB/decade roll-offs. For the values chosen, the  $Q$  of the circuit shown in Fig. 4(b) is relatively small, with only a weak resonant peak at a frequency that corresponds to  $\omega_0$ . In contrast, the impedance transformation provided by the coupling coils  $L_1, L_4$  for the circuit shown in Fig. 4(c) results in a much higher  $Q$  and coupling that is stronger by about 40 dB than the circuit shown in Fig. 4(b). Thus, the low  $Q$  and purely inductive systems have efficiencies many orders of magnitude lower than the high  $Q$  system.

## VIII. DELIVERY OF POWER TO MULTIPLE LOADS

Wireless power delivery to multiple small receivers is simply a replication for each receiver of the principle that has been demonstrated and modeled in the prior sections of this paper, provided that two conditions are met.

- 1) Each receiver must carry small coils that remain within the region of relatively uniform magnetic field generated by the source coil.
- 2) Each receiver must be far enough separated from each other receiver that their interactions with the source coil are decoupled. Said another way, mutual inductances between the receiving coils must have a negligible effect upon the resonant coupling interaction.



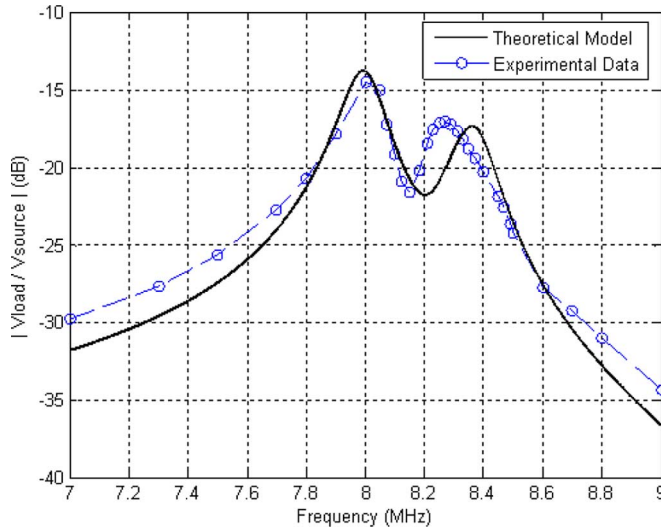


Fig. 6. Transfer function  $|(V_L/V_S)(\omega)|$  near the resonant peak as measured experimentally and as calculated from the circuit model for two identical receiving coils stacked directly on top of one another in the center of the transmitting coil pair, so as to maximize the coupling interaction between receivers. Coupled mode splitting of the resonant peak is apparent.

The second of these conditions is likely to be repeatedly violated if the receivers move (for example, if they are micro-robots). For this reason, we explore in this section the effect of bringing two receivers into close proximity. Coupled mode theory [7] predicts a splitting of the single-transfer function resonant peak into two separate peaks. Fig. 6 shows the measured transfer function across one of the two load resistors for two receiver coil pairs, each identical to the single coil pair that is described in prior sections, when the coils are stacked directly on top of one another in the center of the transmitting coil pair, so as to maximize the coupling interaction between receivers. The coupling between the two receivers in this case is stronger than in Fig. 1, where the receivers are side by side. Here, the single peak has split into two peaks, separated in frequency by about 3% of the original resonant frequency.

Also shown in Fig. 6 is a theoretical curve deriving from an extension of the circuit model to include two pairs of load coils, with coupling coefficients again chosen by using rough estimates of the fractions of magnetic flux from each coil that link each other coil, with adjustments in values so as to obtain a good overall fit of the circuit model to the experimental measurement. The circuit model clearly shows the same qualitative behavior with regard to frequency splitting.

As with the single receiver coil pair, our ongoing work involves determination of all parameter values for multiple receivers from first principles. The complexity of the circuit model grows quadratically with the number of receivers.

Of considerable interest for application of magnetic resonant coupling to wireless power transfer to multiple receivers is the degree to which frequency splitting degrades the efficiency of the interaction, and practical means for dealing with this potential difficulty. For example, it may be possible, through onboard control systems, to continuously retune the lumped capacitances

that terminate each receiver coil so as to maximize efficiency. This area is a separate subject of our ongoing work.

## IX. SUMMARY

The following points have been demonstrated in this paper.

- 1) Magnetic resonant coupling can be used to deliver power from a large source coil to one or many small load coils, with lumped capacitors at the coil terminals providing a simple means to match resonant frequencies for the coils. This mechanism is a potentially robust means for delivering wireless power to multiple receivers from a single large-source coil.
- 2) A relatively simple circuit model describes the essential features of the resonant coupling interaction, with parameters that can be either derived from first principle descriptions, from direct measurement or from curve fitting techniques.
- 3) A key issue for powering of multiple receivers is the coupled mode frequency splitting that occurs when two receivers are in close enough proximity that their magnetic fields are relatively strongly coupled. Control circuitry to track the resonant frequency shifts and to retune the receiving coil capacitances is a potentially viable strategy for addressing this issue.

## APPENDIX

### DETERMINATION OF PARAMETER VALUES

In principle, all the parameter values in the circuit model can be determined from first principles, based upon geometries and material parameters, and can be verified through individual measurements. While these calculations, as well as comparisons with direct measurements, are the subject of our ongoing work, our purpose here is simply to show that, using reasonable parameter values, the circuit model yields a frequency response description that is in good agreement with experimental measurements.

The parameter values in the circuit model are determined as follows:

- 1) *Coil Resistances  $R_1, R_2, R_3$ , and  $R_4$ :*

Skin effect causes the currents in the resonant coils to concentrate toward the surfaces of the copper wires, so that their effective areas are reduced from their cross-sectional areas. Thus, the resistances are described by

$$R = \frac{2\pi a N}{\sigma 2\pi r \delta} = \frac{aN}{\sigma r \delta} \quad (8)$$

with the following definitions of physical parameters:

$a$  = major radius of coil ( $a_1 = a_2 = 15$  cm,  $a_3 = a_4 = 0.635$  cm)

$r$  = cross-sectional radius of wire ( $r_1 = r_2 = 1.5$  mm,  $r_3 = r_4 = 0.45$  mm)

$N$  = number of turns ( $N_1 = 1, N_2 = 3, N_3 = 10.5, N_4 = 3$ )

$\sigma$  = copper conductivity ( $\sigma = 5.8 \times 10^7$  S/m)

$f$  = source frequency ( $f = 8.3$  MHz)

$$\delta = \frac{1}{\sqrt{\pi f \mu_0 \sigma}} \text{ (skin depth) } (\delta = 22.9 \mu\text{m})$$

$$\mu_0 = 4\pi \times 10^{-7} \text{ H/m}$$

Equation (8) yields the following values for coil resistances at 8.3 MHz:

$$R_1 = 0.075 \Omega, \quad R_2 = 0.23 \Omega$$

$$R_3 = 0.11 \Omega, \quad R_4 = 0.032 \Omega$$

- 2) *Source Internal Resistance*: The HP 33120A Function/Arbitrary Waveform Generator has a manufacturer specified internal resistance:

$$R_S = 50 \Omega.$$

- 3) *Load Resistance*: The load resistance is taken as the resistor color code value:

$$R_L = 100 \Omega.$$

- 4) Self-inductance  $L_2$  and capacitance  $C_2$ :

The coil  $L_2$  was connected directly across the terminals of the function generator, and the frequency was adjusted so as to yield an amplitude of terminal voltage reduced by  $1/\sqrt{2}$  from the open circuit voltage. At this frequency, the pure imaginary coil impedance has the same magnitude as the pure real source impedance of  $50 \Omega$ , so that  $2\pi f L_2 = 50 \Omega$ . The measured frequency yields a self-inductance for coil 2 of

$$L_2 = 11.2 \mu\text{H}.$$

A variable capacitor was used for  $C_2$  so as to tune the resonance. Since its value was not directly available, the capacitance  $C_2$  is determined from (1), with a resonant frequency  $\omega_0 = 2\pi$  (8.3 MHz). (The value obtained in this way is actually the sum of  $C_2$  and the distributed capacitance of the coil.) This yields the value:

$$C_2 = 34 \text{ pF}$$

- 5) Self-inductance  $L_3$  and capacitance  $C_3$ : The capacitance  $C_3$  is taken as the value printed on the lumped element:

$$C_3 = 470 \text{ pF}.$$

The inductance  $L_3$  is then determined from (1), again with a resonant frequency  $\omega_0 = 2\pi$  (8.3 MHz). (This value is an effective inductance that also includes the effects of the distributed capacitance of the coil.) This yields the value:

$$L_3 = 0.80 \mu\text{H}.$$

- 6) Self-inductances  $L_1$  and  $L_4$ : Since coils 1 and 4 are essentially identical respectively to coils 2 and 3, except that they have fewer turns, their self-inductances are inferred from  $L_2$  and  $L_3$  and the number of turns in the two resonant coils. Thus, using  $L_1/L_2 = N_1^2/N_2^2$  and  $L_4/L_3 = N_4^2/N_3^2$  yields the values:

$$L_1 = 1.2 \mu\text{H}, \quad L_4 = 0.065 \mu\text{H}.$$

- 7) Mutual inductances  $M_{12}, M_{13}, M_{14}, M_{23}, M_{24}$ , and  $M_{34}$ : The mutual inductance between any pair of coils is proportional, through a coupling coefficient  $\kappa \leq 1$  to the geometric mean of the two self-inductances [10]. Thus, the mutual inductances in (6) are represented in terms of coupling coefficients by

$$M_{ij} = \kappa_{ij} \sqrt{L_i L_j}. \quad (9)$$

Values for the six coupling coefficients  $\kappa_{12}, \kappa_{13}, \kappa_{14}, \kappa_{23}, \kappa_{24}$ , and  $\kappa_{34}$  are chosen by using rough estimates of the fractions of magnetic flux from each coil that link each other coil, and then by making small adjustments in values so as to fit the theoretical transfer function  $|(V_L/V_S)(\omega)|$  to experimental data points over a range of frequencies that span the resonance. The specific values used are

$$\kappa_{12} = 0.17; \quad \kappa_{13} = 0.0010; \quad \kappa_{14} = 0.021;$$

$$\kappa_{23} = 0.0047; \quad \kappa_{24} = 0.021; \quad \kappa_{34} = 0.76.$$

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