

## Design Considerations of Recent Advanced Low-Voltage Low-Temperature-Coefficient CMOS Bandgap Voltage Reference

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### Abstract

The design considerations of CMOS bandgap voltage references focusing on low-voltage and low-temperature-coefficient methodologies are discussed in this paper. Some recently reported circuits of bandgap voltage references are included and analyzed. Moreover, a CMOS voltage reference is also addressed.

### Introduction

Voltage reference is a pivotal building block in mixed-signal and radio-frequency systems. For example, a generic mixed-signal system, as shown in Fig. 1, has more than one voltage reference due to different voltage reference requirements and also to avoid crosstalk through a single reference circuit. In such a system, a voltage reference is needed for the power-management block, which includes many on-chip DC-DC power converters to provide regulated power. Some other voltage references are utilized in ADCs and DACs, which need high-accuracy reference voltages to provide high-resolution high-speed data conversions even in low supply-voltage conditions.

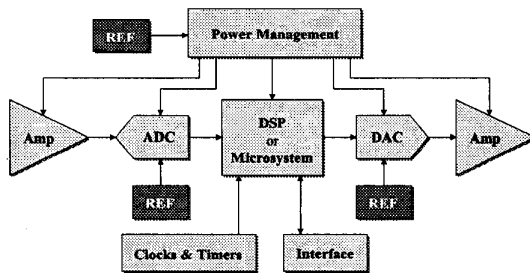


Fig. 1: A generic mixed-signal system.

Undoubtedly, reference-voltage accuracy determines the maximum achievable performance of all IC systems. There are many types state-of-the-art design [1]. Bandgap voltage reference, which was firstly proposed by Widlar [2] and was further developed by Kuijk [3] and Brokaw [4], is the one commonly used in many advanced designs and commercial products since it can provide a predictable reference voltage. Moreover, it is also possible for low voltage and low temperature dependence.

The working principle of a bandgap voltage reference can be illustrated by Fig. 2. Since  $V_{BE}$  decreases approximately linearly with temperature while  $V_T$  increases linearly with

temperature, a low-temperature-dependence  $V_{REF}$  can be obtained by scaling up  $V_T$  and summing it with  $V_{BE}$ .

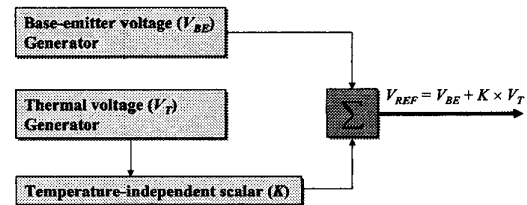


Fig. 2: Concept of bandgap voltage reference.

The above-mentioned concept can be implemented as shown in Fig. 3 [5] by using parasitic vertical BJTs. Current mirrors formed by M1, M2 and M3 enforce branch currents equal to a proportional-to-absolute-temperature (PTAT)  $I$ , which is generated by Q1, Q2 and  $R_1$  when  $V_A = V_B$  is enforced by a voltage-clamping circuit composed of M4 and M5. Thus,  $V_{REF}$  is given by

$$V_{REF} = V_{EB3} + (R_2/R_1) \ln(N) \cdot V_T \quad (1)$$

The achieved  $V_{REF}$  is around 1.205V, which is the value of energy bandgap of silicon. A  $V_{REF}$  with low temperature coefficient (tempco) can be easily obtained by optimizing temperature-independent circuit parameters  $R_2/R_1$  and  $N$ .

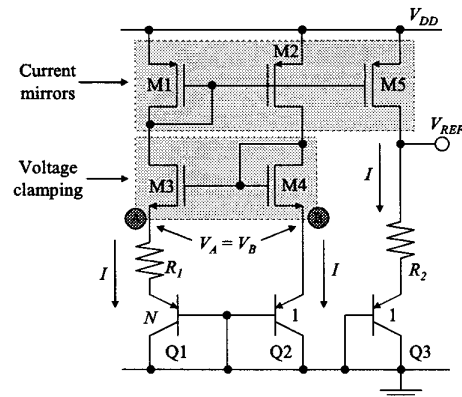


Fig. 3: Simple implementation of bandgap reference.

The previous review reveals the design problems of bandgap voltage reference in a low supply voltage. The intrinsically-defined 1.205-V  $V_{REF}$  is one of the limitations. Moreover, a perfect voltage reference should contain no

error. However, there are many sources of error in the voltage reference such as error current from the current mirrors, error voltage from the clamping circuit, as well as device mismatches of Q1-Q2 and  $R_1$ - $R_2$ . Undoubtedly, there are many well-developed circuits and layout techniques to minimize the errors. However, low supply voltages limit the available methodologies and cause severe design problems.

Moreover, typical bandgap references have non-zero tempco of typically around 25-50ppm/°C [1]. This is, no doubt, an error of  $V_{REF}$ . This error is not significant in the past 5-V and 10-V systems, but is a fatal error in current 1.8-V or even future sub-1-V systems. Solutions have been proposed but are less useful in low-voltage conditions.

In regards to the above-mentioned low-voltage design trends and problems, many novel structures of bandgap reference have been proposed and well-proven by experimental results. Thereby, in this paper, the designs of low-voltage and low-tempco bandgap voltage reference are reviewed and studied. Discussions will not only be on the circuit structures, but some design considerations and design problems due to technology limitations will also be discussed as well. Lastly, a CMOS voltage reference is introduced.

## I. Design Challenges and Considerations

The design of voltage reference mainly improves accuracy and rejects errors. Thus, the errors in every part should be minimized by circuit and layout techniques. With reference to Fig. 3, considerations should be focused on BJT-ratio and resistor-ratio matching, current mirror, as well as voltage clamping. These considerations are discussed below.

### A. Design Issues on BJT and Resistor

Laser trimming can be used to optimize the performance of bandgap voltage references, but it is a costly procedure. As a result, layouts on both BJTs and resistors should be well planned and designed so that consistent performance can be maintained with minimum need of trimming in mass productions. Better matching can be achieved by a common-centroid layout [6], [7]. In Fig. 4(a), there shows two matched BJTs in a ratio of 1:8 as shown.

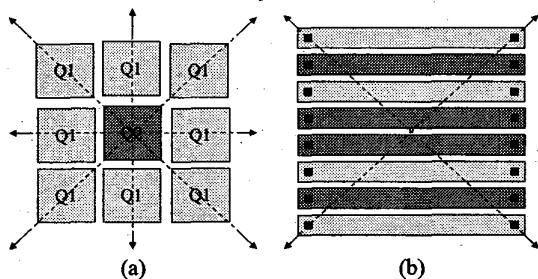


Fig. 4: Layouts of (a) two BJTs (b) two resistors.

In the figure,  $N = 8$  is chosen and all BJTs are placed closely.  $N$ , in fact, can be 24, 48 or even 80 as these integers can be used to obtain common-centroid structures. However, a large value of  $N$  is not preferred as the separation of devices increases, and this will introduce more errors. Moreover, as shown in (1), there is no significant increase on the  $\ln(N)$  function when  $N$  increases.

For the resistor layout, common-centroid layout should be also used to obtain better matching. Fig. 4(b) shows two resistors with equal values in two layout arrangements. The resistor layout should be arranged in a square-like structure instead of a thin and long structure. Although the structure in Fig. 4(b) provides a very stable resistor ratio including the effect of contact resistances, each resistor must be sufficiently long such that the contact resistances are negligible and cause less influence. Moreover, polysilicon is a better material than diffusion to implement resistors since the minimum separation is shorter and that provides a better matching.

The tempco of  $V_{REF}$  is also affected by the materials used to implement the resistors. It is known that the finite tempco of  $V_{REF}$  is due to the non-linear behavior of  $V_{BE}$  at different temperatures. Tsividis has found that the  $V_{BE}$  can be expressed by [8]

$$V_{BE} = V_{GO} + \frac{T}{T_r} \cdot [V_{BE}(T_r) - V_G(T_r)] + (\eta - \beta) \frac{kT}{q} \ln\left(\frac{T_r}{T}\right) \quad (2)$$

where  $V_{GO}$  is the extrapolated bandgap voltage of silicon at 0K,  $T_r$  is the reference temperature,  $\eta$  is a constant of less than 4 depending on doping level, and  $\beta$  is the order of temperature dependence of the collector current (i.e.  $I_C = I_{CO}T^\beta$ ). The non-linear voltage is due to  $T\ln T$  term in (2).

In fact, the current  $I$  in Fig. 3 is not a pure PTAT current. When a material with a low tempco is used,  $(\eta - \beta)$  in (2) becomes smaller and this results in a smaller non-linear voltage. Therefore, polysilicon is a better material than diffusion since its tempco is low [6]. An even better material is high-resistive polysilicon (lightly-doped polysilicon), since it has a negative tempco [6]. Fig. 5 shows different  $V_{REF}$ - $T$  plots of different tempcos of resistors. The tradeoff on low-tempco resistors is higher current level at high temperatures, and that implies more power consumption.

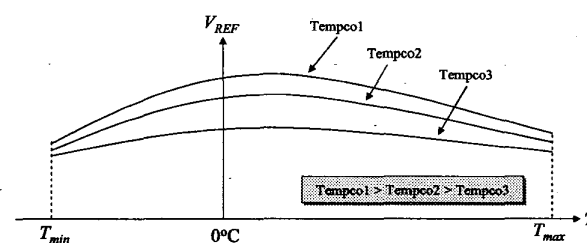


Fig. 5: Reference voltage using different resistor materials.



Fig. 8 shows an example bandgap voltage reference, which is designed based on some of the previous suggestions.

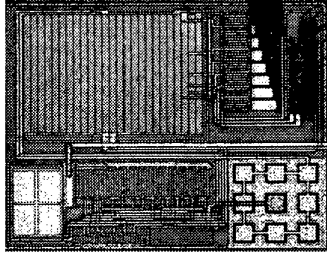


Fig. 8: Micrograph of a bandgap voltage reference.

## II. Advanced Bandgap Voltage References with Sub-1-V Supply Operation

The 1.205-V bandgap reference voltage is a hindrance to developing a reference voltage with a sub-1-V supply. Therefore, Banba *et al.* [9] and Leung *et al.* [10] have developed bandgap references with sub-1-V operations. The concept is basically a current-mode method to scale down the bandgap reference voltage by a factor defined by a resistor ratio.

### A. A CMOS Bandgap Reference with Sub-1-V Operation Proposed by Banba *et al.* [9]

Fig. 9 shows the circuit proposed by Banba [9]. The reference voltage is formed by two currents  $I_1$  and  $I_2$ . For  $I_1$ , it is a PTAT current formed by Q1, Q2 and  $R_1$  as given by  $I_1 = V_T \ln(N)/R_1$ , while  $I_2$  is a current due to  $V_{EB2}$  and  $R_2$  as given by  $I_2 = V_{EB2}/R_2$ . Thus,  $V_{REF}$  is given by

$$V_{REF} = (I_1 + I_2) \cdot R_3$$

$$= \left( \frac{R_3}{R_2} \right) \cdot \left[ V_{EB2} + \left( \frac{R_2}{R_1} \right) \ln(N) \cdot V_T \right] \quad (3)$$

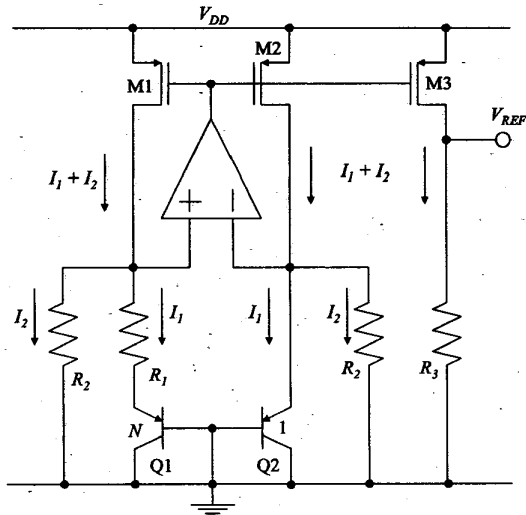


Fig. 9: A CMOS bandgap reference with sub-1-V operation proposed by Banba *et al.* [9].

It is noted that the temperature dependence of the reference voltage can be cancelled by an appropriate  $R_2/R_1$  ratio and  $N$ . A resistor ratio of  $R_3/R_2$ , which is less than one, is used to scale down the bandgap voltage reference to be less than 1.205V. Therefore, the magnitude of  $V_{REF}$  can be adjusted for different applications. In [9],  $V_{REF}$  is set to 515mV, which is a good value to achieve  $V_{DS1} = V_{DS2} \approx V_{DS3}$  for good current matching at different temperatures. Moreover, the error amplifier shown in Fig. 6 with biasing current from the bandgap core is used to minimize  $V_{OFFS}$ .  $V_{OFFS}$  can be reduced by a small  $g_m$  ratio of MA3 to MA1 and a large transistor size of MA1 and MA2 [5].

### B. A Sub-1-V CMOS Bandgap Voltage Reference without Low Threshold-Voltage Devices by Leung *et al.* [10]

The bandgap reference by Banba *et al.* has been implemented in a technology having native NMOSTs (non-standard devices in CMOS technology) to implement an NMOS input stage of the error amplifier. The threshold voltage of NMOSTs should be always much lower than one  $V_{EB}$  in the full operational temperature. Thus, one  $V_{EB}$ , even at the highest operational temperature (lowest  $V_{EB}$ ), is therefore sufficiently high to turn on the input stage of the error amplifier for proper operation as shown in Fig. 10(a) (i.e.  $V_{EB} > V_{THN} + 2V_{DS(sat)}$ ). When a PMOS input stage is used, a low supply voltage cannot be achieved easily since the minimum supply voltage, as shown in Fig. 10(b), is given by  $V_{DD(min)} = V_{EB} + |V_{THP}| + 2V_{SD(sat)}$ . The above implies a low  $|V_{THP}|$  is needed.

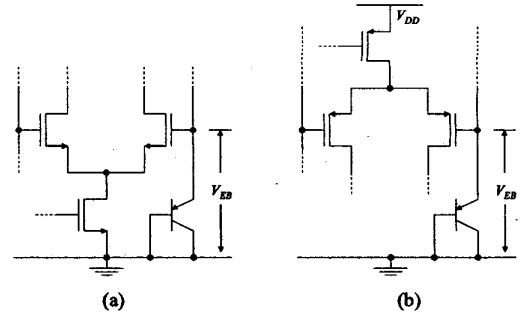


Fig. 10: Bandgap voltage references using (a) an NMOS input stage (b) a PMOS input stage.

Therefore, a circuit technique based on potential divider can be used, as shown in Fig. 11. Instead of enforcing the voltages at E and F directly, the voltages at X and Y are enforced to be equal. As the resistances at the two current branches are set to be equal, the voltages at E and F are equal. It is noted that the voltages at X and Y are given by

$$V_X = V_Y = \left( \frac{R_{2B}}{R_{2A} + R_{2B}} \right) \cdot V_{EB2} \quad (4)$$

An error amplifier with a PMOS input stage can therefore be used. The minimum supply voltage of the bandgap voltage reference is reduced, and  $V_{REF}$  of this circuit is

given by

$$V_{REF} = \left( \frac{R_3}{R_2} \right) \cdot \left[ V_{EB2} + \left( \frac{R_2}{R_1} \right) \ln(N) \cdot V_T \right] \quad (5)$$

However, the tradeoff of this design is the amplified effect of the offset voltage ( $V_{OFF}$ ) due to the error amplifier. This relationship can be stated clearly by

$$V_{REF} = \left( \frac{R_3}{R_2} \right) \cdot \left\{ V_{EB2} + \left( \frac{R_2}{R_1} \right) \cdot [\ln(N) \cdot V_T + V_{ERR1}] \right\} \quad (6)$$

where  $V_{ERR1} = [(R_{2A} + R_{2B})/R_{2A}] \cdot V_{OFF} > V_{OFF}$  is the increased error voltage due to the offset voltage. This, in practice, can be reduced by using a large value of  $N$  in this design. In the design of [10],  $N = 64$  is used.

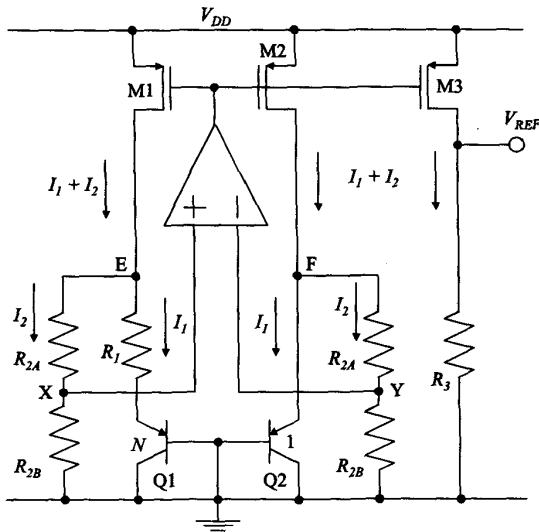


Fig. 11: A sub-1-V CMOS bandgap reference without low threshold-voltage devices proposed by Leung *et al.* [10].

In addition, the bulk-source junctions of M1-M3 are forward-biased such that  $|V_{THP}|$  is reduced. The forward bias voltage is set to about 0.3V at the highest operational temperature so that the p-n junction of the p-substrate and N-well will not be turned on. With this scheme, the error amplifier can operate in its high-gain output region to enforce voltages at nodes X and F more closely.

### C. A Bandgap Voltage Reference Using Transimpedance Amplifier Proposed by Jiang *et al.* [11]

The minimum supply voltage of the previous bandgap reference structures is limited by the input stage of the voltage-mode error amplifier. A novel structure using transimpedance amplifier in Fig. 12 has been reported [11].

The transimpedance amplifier has a very low input resistance and has a large impedance gain. The internal nodes of the two inputs are set to  $V_B$ , which is lower than one  $V_{EB}$ .

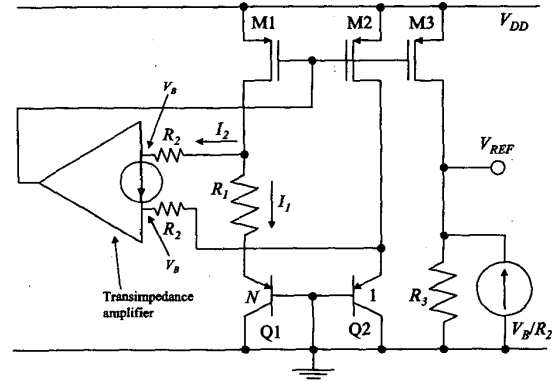


Fig. 12: Bandgap voltage reference using transimpedance amplifier proposed by Jiang *et al.* [11].

As a result, the current  $I_2$  is given by  $I_2 = (V_{EB2} - V_B)/R_2$ . In addition, the PTAT loop generates a current given by  $I_1 = V_T \ln(N)/R_1$ . Therefore, the drain currents of M1, M2 and M3 are the sum of  $I_1$  and  $I_2$ . With a current source depending on  $V_B$ ,  $V_{REF}$  is given by

$$\begin{aligned} V_{REF} &= (I_1 + I_2 + V_B/R_2) \cdot R_3 \\ &= \left[ \frac{V_T \ln(N)}{R_1} + \frac{V_{EB2} - V_B}{R_2} + \frac{V_B}{R_2} \right] \cdot R_3 \\ &= \frac{R_3}{R_2} \cdot \left[ V_{EB2} + \left( \frac{R_2}{R_1} \right) \ln(N) \cdot V_T \right] \end{aligned} \quad (7)$$

which is a scalable bandgap reference voltage.

In this design, the matching of devices is very important so that the required node voltages can be set to  $V_B$  accurately to reduce the error appearing at  $V_{REF}$ . As there is no critical constraint on  $V_B$ , it can be any value. Although the reported minimum supply voltage is 1.2V, this approach has a great potential to further reduce the minimum supply voltage.

### III. Advanced Structures of Low-Tempco Bandgap Voltage References

In addition to low-voltage bandgap-reference structures, low-tempco structures are also important, especially for high-resolution ADCs and DACs. This is due to the fact that the errors suffering from temperature variations will significantly increase the bit-error rate.

Many novel and creative methods for low-tempco voltage reference have been proposed, including the second-order curvature compensation by Song *et al.* [12] and exponential-curvature compensation by Lee *et al.* [13]. Moreover, low-tempco bandgap reference based on linearized  $V_{BE}$  was proposed by Meijer *et al.* [14] and was used by Malcovati *et al.* [15] in their low-voltage BiCMOS bandgap design.

**A. A Curvature-Compensated Bandgap Voltage Reference**  
Proposed by Malcovati *et al.* [15]

The circuit proposed by Malcovati *et al.* is shown in Fig. 12. It can be shown from (2) that different  $V_{BE}$  can be obtained by different temperature-dependent collector currents. In this circuit, Q2 is biased by a PTAT current:

$$V_{EB2} = V_G(T_r) + \frac{T}{T_r} \cdot [V_{BE}(T_r) - V_G(T_r)] + (\eta - 1) \frac{kT}{q} \ln\left(\frac{T_r}{T}\right) \quad (8)$$

while Q3 is biased by a temperature-independent current:

$$V_{EB3} = V_G(T_r) + \frac{T}{T_r} \cdot [V_{BE}(T_r) - V_G(T_r)] + \eta \frac{kT}{q} \ln\left(\frac{T_r}{T}\right) \quad (9)$$

A non-linear current  $I_{NL}$ , which is the current flowing through  $R_4$  is generated and is given by  $I_{NL} = (V_{EB2} - V_{EB3})/R_4 = -V_T \ln(T_r/T)/R_4$ .

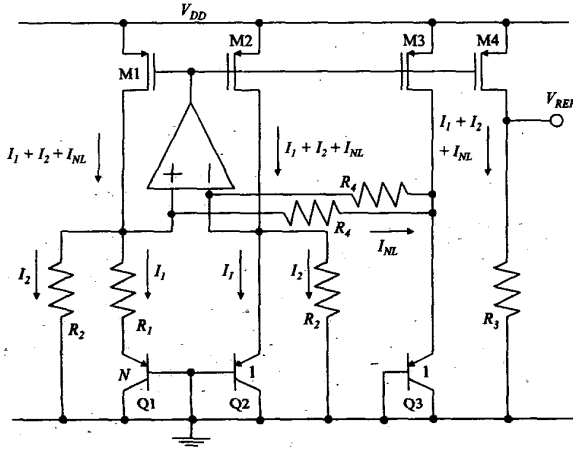


Fig. 12: A curvature-compensated bandgap voltage reference proposed by Malcovati *et al.* [15].

Therefore,  $V_{REF}$  is given by

$$\begin{aligned} V_{REF} &= (I_1 + I_2 + I_{NL}) \cdot R_3 \\ &= \left[ \frac{V_T \ln(N)}{R_1} + \frac{V_{EB2}}{R_2} - \frac{V_T \ln\left(\frac{T_r}{T}\right)}{R_4} \right] \cdot R_3 \\ &= \left( \frac{R_3}{R_2} \right) \cdot \left[ V_{EB2} + \left( \frac{R_2}{R_1} \right) \ln(N) \cdot V_T - \frac{R_2}{R_4} \ln\left(\frac{T_r}{T}\right) \cdot V_T \right] \quad (10) \end{aligned}$$

When the easy-control resistor ratio  $R_2/R_4 = \eta - 1$ , the non-linear voltage in  $V_{EB2}$  is cancelled. A theoretical zero-tempo  $V_{REF}$  can be obtained. However, it cannot always be achieved due to the non-ideal PTAT and temperature-independent currents from the temperature dependence of resistors. In addition, errors due to mismatch of current mirrors is another problem. However, it is not due to M3 as  $V_{DS1} = V_{DS2} = V_{DS3} = V_{DD} - V_{EB}$ . Attention should be

given, instead, to M4 and  $V_{REF}$ .  $V_{REF}$  can be set to about one  $V_{EB}$  in order to match the  $V_{DS}$  of M4 with M1-M3.

**B. A Curvature-Corrected Bandgap Reference Based on Temperature-Dependent Resistor Ratio**  
Proposed by Lewis *et al.* [16], Audy [17] and Leung *et al.* [18]

Another method is to implement a bandgap circuit that has a temperature-dependent resistor ratio. This idea can be implemented by the circuit shown in Fig. 13. Both  $R_1$  and  $R_2$  are made of the same material, while  $R_3$  is made of high-resistive polysilicon, which has a negative tempco. Therefore,  $V_{REF}$  is given by

$$V_{REF} = V_{EB2} + \left( \frac{R_2}{R_1} \right) \ln(N) \cdot V_T + \left( \frac{R_3}{R_1} \right) \ln(N) \cdot V_T \quad (11)$$

T-dependent resistor ratio

Since the non-linear temperature-dependent voltage in  $V_{EB}$  ( $T \ln T$ ) can be expressed into a sum of high-order  $T$  terms, high-order temperature-dependence cancellation can be achieved depending on the relative temperature-coefficients of  $R_1$  and  $R_3$ . In [18], a fourth-order curvature correction has been reported. It is noted here that  $R_4$  is made of the same material of  $R_1$  and  $R_2$ , and is set to  $R_2 + R_3$  at room temperature to achieve good matching of  $V_{DS1}$  and  $V_{DS2}$ .

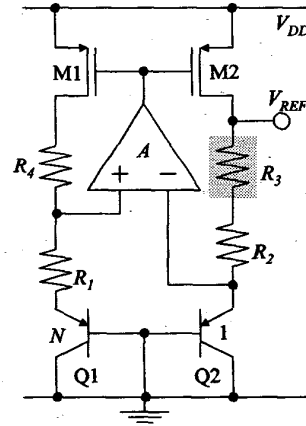


Fig. 13: A curvature-corrected bandgap reference based on T-dependent resistor ratio proposed by Leung *et al.* [18].

Trimming of this circuit can be done by adjusting  $R_3/R_1$  such that the nonlinear error voltage is minimum. Then, the second step involves the minimization of the linear temperature dependence by finding an optimum  $R_2/R_1$ . In the trimming procedure, two temperature measurements (minimum and maximum) are sufficient for linear trimming, while four temperature measurements evenly distributed in the considered temperature range are sufficient for nonlinear trimming. In [18], the tempco is proven to be improved by 5 times when comparing the first-order compensated bandgap voltage reference.

#### IV. A CMOS Bandgap Design without Resistor

In the previous sections, low-voltage and low-tempco methodologies in the state-of-the-art CMOS voltage reference have been reviewed. It is well understood that technology limitations on passive components may occur. Large values of resistors are problematic in IC technologies as the resistors require large chip area that increases production cost. Moreover, coupling noise causes the reference voltage to become noisy, and this affects some noise-sensitive analog circuits. Therefore, a CMOS bandgap voltage reference without the resistor was developed by Buck *et al.* [19] and shown below.

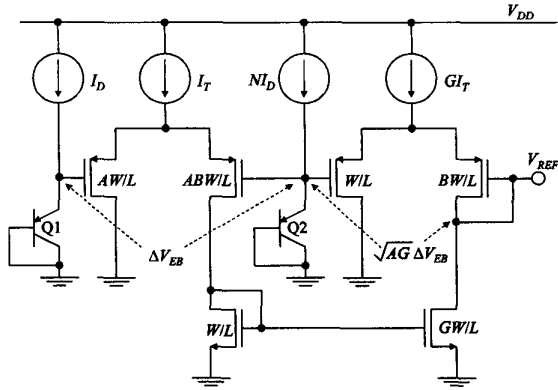


Fig. 14: A CMOS bandgap voltage reference without resistors proposed by Buck *et al.* [19].

The circuit makes use of voltage-to-current transducer to eliminate the need of the resistors. From Fig. 14, when  $I_D$  is a PTAT current, there is a  $\Delta V_{EB}$  formed by the differently biased Q1 and Q2. Therefore,

$$\Delta V_{EB} = \Delta V_{GS} = \sqrt{\frac{2I_1}{\mu_N C_{OX} (AW/L)}} - \sqrt{\frac{2I_2}{\mu_N C_{OX} (ABW/L)}} \quad (12)$$

where  $I_T = I_1 + I_2$ . It is noted that this  $\Delta V_{EB}$  is a PTAT voltage. With the use of the voltage-to-current transducer, the re-generated voltage is given by  $\sqrt{AG} \Delta V_{EB}$ . This can be explained by

$$\sqrt{\frac{2GI_1}{\mu_N C_{OX} (BW/L)}} - \sqrt{\frac{2GI_2}{\mu_N C_{OX} (W/L)}} = \sqrt{AG} \Delta V_{EB} \quad (13)$$

Therefore,  $V_{REF}$  is equal to the sum of  $V_{EB2}$  and this scaled-up PTAT voltage is given by

$$V_{REF} = V_{EB2} + \sqrt{AG} \Delta V_{EB} \quad (14)$$

By appropriate values of  $A$  and  $G$ , a bandgap reference voltage can be obtained with no need of a resistor. The zero-tempco performance can be obtained by trimming of transistor arrays.

In this design, the PTAT current to bias Q1 and Q2 is generated from the bandgap core itself. Therefore, a startup circuit is necessary. Moreover, the current and

device matching are both critical to achieve a good result. Any variations on the threshold voltage and mobility will lead to additional temperature errors on the reference voltage.

#### V. Alternative Solution - A CMOS Voltage Reference

Although bandgap voltage reference shows very good performance, it is not the only voltage reference available in CMOS technologies. Thus, a voltage reference based on MOS characteristics is introduced in this section.

A voltage reference can be implemented by using MOS transistors only. This type of voltage reference relies on the temperature dependence of  $V_{TH}$ . The threshold voltage is approximated as a linear function of temperature, and the temperature dependences of NMOS and PMOS transistors are different in different technologies, as illustrated in Fig. 16.

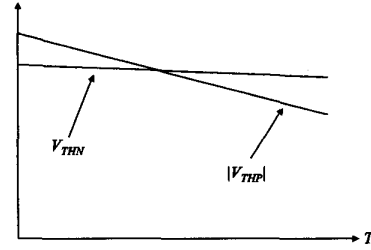


Fig. 16: Temperature dependence of  $V_{TH}$  [20]-[22].

It is very difficult to extract  $V_{TH}$  by simple circuits. Instead,  $V_{GS}$  is used in the design of [21] and [22]. Fig. 17 shows the simple circuit to form a temperature-insensitive  $V_{REF}$  based on weighted differences of  $V_{GS}$  of an NMOST and a PMOST.

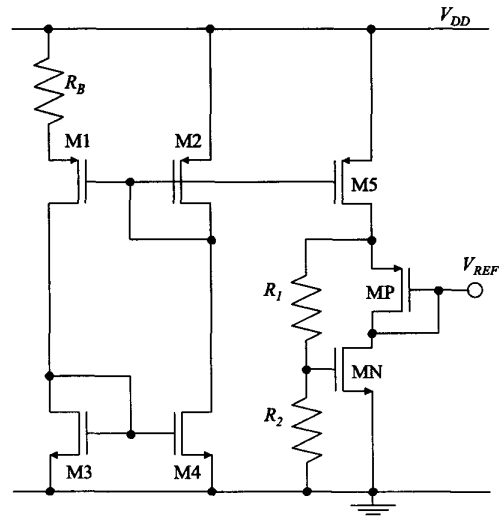


Fig. 15: A voltage reference in standard CMOS technologies proposed by Leung *et al.* [21], [22].

The reference voltage is given by

$$V_{REF} = \left(1 + \frac{R_1}{R_2}\right) \cdot V_{GSN} - |V_{GSP}| \quad (15)$$

When  $R_1$  and  $R_2$  are large, the current in these two resistors is negligible. The temperature dependence of the reference voltage can be obtained by taking differentiation to the function of  $V_{REF}$  with respect to  $T$ . It is found that the circuit can be optimized by a resistor ratio of  $R_1/R_2$  and a transistor-size ratio of the NMOST to PMOST. The reported tempco can be as low as 24ppm/°C, which is close to the performance of a bandgap voltage reference.

Moreover, the supply dependence is low. Since, as shown in equation (15), both  $V_{GSN}$  and  $|V_{GSP}|$  increase/decrease simultaneously when  $I_B$  increases/decreases due to the change of the supply voltage, the effect is partially cancelled to achieve supply-less-sensitive performance.

One issue of concern on this design is that  $V_{REF}$  depends on process parameters. As a result, the magnitude of  $V_{REF}$  may vary. However, it is not a problem in some applications such as power-management ICs since the magnitude trimming can be easily done in the resistive feedback network of the on-chip power converters.

### Conclusion

The design trend and current design methodologies of bandgap voltage reference have been discussed. The focus of this paper is mainly on the low-voltage and low-tempco designs, which are the vital requirements of future IC systems. Several reported circuit structures, therefore, have been analyzed. In addition, a design technique of no-resistor feature has also been studied.

Finally, a voltage reference other than bandgap type has been included. The working principle of this voltage reference is based on MOSFET characteristics. It has advantages, especially in its simple circuit implementation. This voltage reference is found to be a good voltage reference particularly for power-management applications.

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