HW₂

A random sample of 18 2-year-old girls is drawn from a child care center, and their heights are measured: 44.1 38.6 38.2 27.2 21.1 53.8 28.0 41.8 23.6 39.2 42.6 36.5 29.5 28.3 25.9 52.9 19.1 29.2

- 1) Assume the heights in the population of 2 year old girls are normally distributed with unknown mean μ and known standard deviation 10 inches. Suppose your prior distribution for μ is normal with mean 30 and standard deviation 6.
 - a) Get the posterior distribution for μ .
 - b) Get the posterior mean, variance, sd, 5^{th} and 95^{th} percentile for μ .
- 2) Assume the heights in the population of 2 year old girls are normally distributed with known mean μ =32 inches and unknown variance σ^2 . Suppose your prior distribution for σ^2 is inverse gamma(2,20).
 - a) Get the posterior distribution for σ^2 .
 - b) Get the posterior mean, variance, sd, 5^{th} and 95^{th} percentile for σ^2 .

Use exact values, not Monte Carlo approximation.