

The results below are generated from an R script.

```
# Question 1

# Decimal to binary
# a. 0.625
# Answer
# using double dabble method
# Step 1 multiply by 2
#  $0.625 \times 2 = 1.25$ 
# Step 2 if number is larger than 1, put 1 if not put 0.
# 0.1--
# use the fractional part of 1.25 and repeat step 1.
#  $0.25 \times 2 = 0.5$ 
# 0.10-
# repeat step 1 again to fractional value of 0.5.
#  $0.5 \times 2 = 1$ 
# 0.101
# therefore, the decimal value of 0.625 to binary is 0.101 of base 2.

# b.  $1/9$  (0.1111...)
# we only take some decimal place since it is not efficient to show all of the numbers
#  $0.1111 \times 2 = 0.2222 = 0.0-----$ 
#  $0.2222 \times 2 = 0.4444 = 0.00-----$ 
#  $0.4444 \times 2 = 0.8888 = 0.000-----$ 
#  $0.8888 \times 2 = 1.7776 = 0.0001----$ 
#  $0.7776 \times 2 = 1.5552 = 0.00011---$ 
#  $0.5552 \times 2 = 1.1104 = 0.000111--$ 
#  $0.1104 \times 2 = 0.2208 = 0.0001110-$ 
#  $0.2208 \times 2 = 0.4416 = 0.00011100$ 

# we can also keep going since it is repeating, there will be a pattern
# therefore, the decimal value of  $1/9$  is 0.00011100 (repeated) of base 2.

# binary to decimal
# using positional notation binary
# the 1 and 0 corresponds if the number has a value or not.
# if it is 0, the number will be multiplied by 0.

# a. 1111
 $1 \times 2^3 + 1 \times 2^2 + 1 \times 2^1 + 1 \times 2^0$ 

## [1] 15

# b. 1010
 $1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$ 

## [1] 10

# c. 1010.0101
# write out the integer part first.
intPart =  $1 \times 2^3 + 0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0$ 
intPart

## [1] 10
```

```

# now write the fractional part (0.0101)
fracPart = 0*2(-1) + 1*2(-2) + 0*2(-3) + 1*2(-4)
fracPart

## [1] 0.3125

# the answer will be the int + frac which is
intPart + fracPart

## [1] 10.312

# d. 1.010101...(repeated)
# do the same as c.
intPart = 1*21
intPart

## [1] 2

# fractional part (0.010101)
fracPart = 0*2(-1) + 1*2(-2) + 0*2(-3) + 1*2(-4) + 0*2(-5) + 1*2(-6)
fracPart

## [1] 0.32812

# add them all to get answer
intPart + fracPart

## [1] 2.3281

# Question 2
# a. 6/7 (0.8571429)
# 0.8571*2 = 1.7142
# 0.7142*2 = 1.4284
# 0.4284*2 = 0.8568
# 0.8568*2 = 1.7136
# answer: 0.1101

# b. 1/7 (0.1428571)
# 0.1428*2 = 0.2856
# 0.2856*2 = 0.5712
# 0.5712*2 = 1.1424
# 0.1424*2 = 0.2848
# answer: 0.0010

# c.
# 0.1101 + 0.0010 = 0.1111
1*2(-1) + 1*2(-2) + 1*2(-3) + 1*2(-4)

## [1] 0.9375

# d.
# 110 (6) + 1 (1) = 111 (7)
# 111/111 = 1

# Question 3

```

```

x = 1000000
y = 999999
A = function(x,y){
  x^4 - y^4
}
B = function(x,y){
  (x^2+y^2)*(x+y)*(x-y)
}
options(digits=15)
A(x,y)

## [1] 3999993999971581952

B(x,y)

## [1] 3.999994000004e+18

# B is more accurate since R cannot handle big number, and the number x^4 and y^4
# is very very big.

# Question 4
# a.
# pretend these numbers are prime numbers (1 to 10000 are primes)
primes = 1:10000
# this code will print last 100 elements of this vector
primes[(10000-100):10000]

## [1] 9900 9901 9902 9903 9904 9905 9906 9907 9908 9909 9910 9911 9912 9913
## [15] 9914 9915 9916 9917 9918 9919 9920 9921 9922 9923 9924 9925 9926 9927
## [29] 9928 9929 9930 9931 9932 9933 9934 9935 9936 9937 9938 9939 9940 9941
## [43] 9942 9943 9944 9945 9946 9947 9948 9949 9950 9951 9952 9953 9954 9955
## [57] 9956 9957 9958 9959 9960 9961 9962 9963 9964 9965 9966 9967 9968 9969
## [71] 9970 9971 9972 9973 9974 9975 9976 9977 9978 9979 9980 9981 9982 9983
## [85] 9984 9985 9986 9987 9988 9989 9990 9991 9992 9993 9994 9995 9996 9997
## [99] 9998 9999 10000

#b.
#this code will add up first 9000 numbers in vector primes.
sum(primes[1:9000])

## [1] 40504500

# Question 5.
x = 100
y = 99
myfunc = function(x,y){
  (x^16)*((x^8 - y^8) / ((196059601)*(19801)*(199))) - 1)
}
myfunc(x,y)

## [1] 133226762955018784

# Question 6
# to approach this we can use the as.Date library.
tom = as.Date("1999-07-05")
david = as.Date("2003-12-12")

difftime(david, tom, units = "days")

```

```
## Time difference of 1621 days

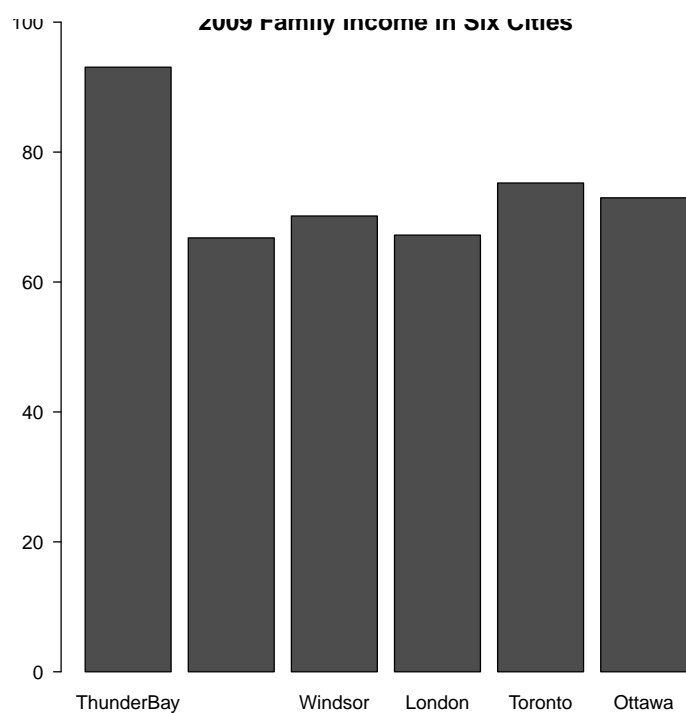
# 7.
cities = c("ThunderBay", "Sudbury", "Windsor", "London", "Toronto", "Ottawa")
inc = c(93.07, 66.79, 70.16, 67.22, 75.24, 72.96)

income = matrix(inc, nrow = 1, ncol = length(cities))
colnames(income) <- cities

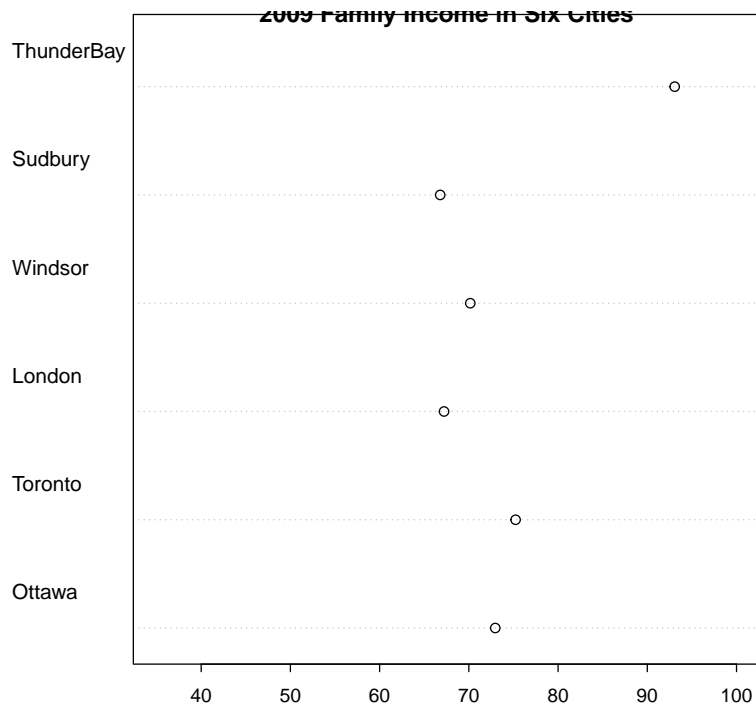
income

##      ThunderBay Sudbury Windsor London Toronto Ottawa
## [1,]      93.07   66.79   70.16  67.22   75.24   72.96

barplot(income, ylim = c(0,100), main = "2009 Family Income in Six Cities")
```



```
dotchart(income, labels = "", xlim = c(35,100), main = "2009 Family Income in Six Cities")
```



The R session information (including the OS info, R version and all packages used):

```
sessionInfo()

## R version 4.2.2 (2022-10-31 ucrt)
## Platform: x86_64-w64-mingw32/x64 (64-bit)
## Running under: Windows 10 x64 (build 19044)
##
## Matrix products: default
##
## locale:
## [1] LC_COLLATE=English_United States.utf8  LC_CTYPE=English_United States.utf8
## [3] LC_MONETARY=English_United States.utf8 LC_NUMERIC=C
## [5] LC_TIME=English_United States.utf8
##
## attached base packages:
## [1] stats      graphics  grDevices  utils      datasets  methods   base
##
## loaded via a namespace (and not attached):
## [1] compiler_4.2.2 tools_4.2.2  tinytex_0.44  highr_0.10    knitr_1.42
## [6] xfun_0.37     evaluate_0.20
##
Sys.time()

## [1] "2023-02-25 19:56:43 PST"
```