



## MATHEMATICAL MODELING

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### Assignment

# Mathematical model for UTXO selection

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# 1 Introduction

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A decentralized cryptocurrency is a digital asset using cryptography systems collectively to secure the transactions and integrity without the third party's intervention. All the transactions in the system are registered on a ledger called blockchain that is constituted of a sequence of blocks. Each block contains an unfixed number of transactions and also a hash of the previous block so that all transactions in the blockchain are immutable and valid. A significant example of this kind cryptocurrency is Bitcoin introduced in 2008 which has currently over \$141 billion in the coin market, with an average of 229K transactions daily and around 183.89 GB of storage<sup>1</sup>.

In transaction-based blockchains, the selection strategy of UTXOs for the transaction plays an essential role in cryptocurrency balance management of any wallet. An optimized coin selection strategy should satisfy hard constraints and essential goals of three principal groups such as users, community and miners. Owing to consumers, they would like to create a transaction that minimizes the transaction fee and also reserves the privacy of their behaviors. By contrast, miners focus on mining transactions which have a higher fee as much as possible. To the community, the large UTXO pool size becomes a dramatic problem because it drops down the transaction processing performance and also produces a high cost of memory consumption. Like Bitcoin system, a snapshot of the current state required additional space in the memory to store objects for processing transactions [?].

In this work, we consider problem of strategy research in order to select a set of UTXOs for a given transaction which should cost a minimum fee for miners or gather as much as possible small UTXO in order to reduce the UTXO pool size. The remainder of this report is organized in the following. Section ?? presents short context and requirement of the considering problem. Then, we present our work in Section ?. Section ? summarizes the performance evaluation and discussion on experimental results. Finally, we conclude our work in the last section.

# 2 Problem formulation

Describe clearly problem statement or requirement of the problem that needs to be modeled.

# 3 Proposed model

Variables:

Constraints:

Objective function:

# 4 Experimental evaluation

Input format:

Output format:

Implementation in GLPK/AMPL:

Experimental results

# 5 Conclusion

# References

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<sup>1</sup><https://coinmarketcap.com>

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