

Unparsed Patterns: Easy User-Extensibility of Program Manipulation Tools^{*}

Extended Version

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Abstract

Pattern matching in concrete syntax is very useful in program manipulation tools. In particular, user-defined extensions to such tools are written much easier using concrete syntax patterns. A few advanced frameworks for language development implement support for concrete syntax patterns, but mainstream frameworks used today still do not support them. This prevents most existing program manipulation tools from using concrete syntax matching, which in particular severely limits the writing of tool extensions to a few language experts.

This paper argues that the major implementation obstacle to the pervasive use of concrete syntax patterns is the pattern parser. We propose an alternative approach based on “unparsed patterns”, which are concrete syntax patterns that can be efficiently matched without being parsed. This lighter approach gives up static checks that parsed patterns usually do. In turn, it can be integrated within any existing parser-based software tool, almost for free. One possible consequence is enabling a widespread adoption of extensible program manipulation tools by the majority of programmers.

Unparsed patterns can be used in any programming language, including multi-lingual environments. To demonstrate our approach, we implemented it both as a minimal patch for the gcc compiler, allowing to scan source code for user-defined patterns, and as a standalone prototype called matchbox.

Categories and Subject Descriptors D.3.3 [Language Constructs and Features]: Patterns

General Terms Algorithms, Languages

Keywords pattern matching, source code, unparsed patterns

^{*}This extended version contains an extra Appendix with the proof of the claimed properties. This Appendix has been omitted in the published PEPM’08 version because of space limitations.

1. Introduction

Pattern matching of source code is a very useful mechanism in tools for program analysis and transformation, such as compilers, interpreters, tools for legacy program understanding, code inspectors, refactoring tools, model checkers, code translators, etc. Source code matching is not only useful when implementing these tools, but especially for building extensible versions of these tools with user-defined behavior [12, 1, 8, 15, 21, 26].

As the problem of tree matching has been extensively studied and efficient algorithms are known, the problem of source code matching has usually been reduced to tree matching, according to two different approaches.

Tree patterns. In the first approach, code patterns are written as trees, using a domain-specific notation to describe an abstract syntax tree (AST). This approach based on tree patterns has been used for a long time, either supported by pattern matching mechanisms available in the implementation language, e.g., for tools written in ML, or otherwise by explicitly implementing a tree pattern matching mechanism, e.g. in inspection tools such as tawk [13] or SCRUPLE [23] or in model checking tools such as MOPS [8]. More recently, some extensible code inspectors such as PMD [26] represent ASTs in XML notation (which constitutes a standardized notation for trees). This allows using other standardized notations such as XPath/XQuery for expressing tree patterns, and thus reusing existing pattern matchers. The main advantage of expressing patterns as trees is that the implementation of pattern matching is simple, because any appropriate tree-matching algorithm can be directly used on this representation. However, an important shortcoming of this approach is that programmers writing patterns should be aware of the internal AST representation of programs, and also of a specific notation for it.

As a motivating example, consider a very simple user-defined inspection rule over C programs that searches for code fragments resetting all the elements in an array, such as the following fragment:

```
for(i=0; i<100; ++i)
  a[i]=0;
```

When such initialization code is found, the inspection rule may suggest that the same operation would be implemented more efficiently using the “bzero()” standard library function. Alternatively, the same rule might be predefined in a compiler in order to recognize such initializations and automatically implement them more efficiently using the “bzero()” function.

Depending on the AST representation of the C program in a particular tool, the tree pattern corresponding to the example above

would typically be expressed as follows (where the name of the array, its bound, and its index variable have been abstracted as variables in the pattern):

```
for_stmt(assign_expr(X, N),
         less_expr(X, M),
         preincr_expr(X),
         expr_stmt(assign_expr(array_expr(Y, X),
                               int_literal(0))))
```

As can be seen in the above tree pattern, the programmer writing the inspection rule must be aware of both the AST structure (for instance, that an assignment in C is an expression encapsulated in an “expression statement”) and of a specific notation for it (for instance, that the assignment operator is called “assign_expr”, that the “for_stmt” operator takes four arguments in a given order, etc.). Writing the same pattern in a language such as XPath doesn’t simplify things, and the pattern becomes even more verbose.

Concrete syntax patterns. In the second approach to source code matching, code patterns are expressed using the native syntax (i.e., the concrete syntax) of the subject programming language, augmented with pattern variables. Then, patterns are parsed to trees before being matched with the program AST. In this approach, the pattern to be searched can be written much more naturally and concisely as follows (where variables in the pattern are prefixed by a special character such as “%”):

```
for(%x=0; %x<%n; ++%x) %y[%x]=0;
```

This second approach based on concrete syntax patterns has been used, for instance, in several extensible model checkers [22, 12, 1, 15], and extensible tools for legacy program understanding and transformation [30, 27]. The main advantage of concrete syntax patterns is that they are trivial to write and read back by any programmer, without knowledge of the AST representation. However, as far as the implementation is concerned, parsing the pattern requires a modified parser of the subject programming language, extended to:

- allow pattern variables, which do not occur in ordinary code, and
- parse patterns that represent program *fragments* (statements, expressions, declarations), whereas the base grammar only parsed whole programs.

Extending the parser of a programming language in these ways is not a simple task, even in frameworks that automate the addition of the extra grammar productions [7], because it typically introduces many conflicts in the parser. These conflicts may correspond to real ambiguities in the extended language (for example, in C, the pattern “f(%x);” may represent either a function call or a function declaration with an implicit return type of “int”), or may be just be caused by a parsing algorithm with limited lookahead. Indeed, existing parsers most commonly use limited lookahead algorithms such as LALR(1) or LL(1). Solving many such conflicts in a complex grammar of a real programming language may be very hard to do. Moreover, the resolution of some conflicts may require introducing special pattern syntax (such as “#stmt f(%x);” in the previous example), which make the patterns look less similar to native code. This is the reason why most of the existing tools following this approach allow only restricted forms of concrete syntax patterns, described by a limited pattern grammar (e.g., matching only assignments and function calls [3]).

In theory, generalized parsers, handling the general class of context-free grammars, can deal with both kinds of conflicts, by computing all possible parses: conflicts due to limited lookahead are rejected later during the parsing; conflicts due to the ambiguity

of the grammar itself result in several possible ASTs. However, mainstream generalized parsers such as Bison [4] use an extremely inefficient, exponential-time algorithm, creating a new process at each local ambiguity. This scheme may quickly prove infeasible when parsing even small fragments in a pattern grammar where conflicts are scattered everywhere.

Alternatively, the polynomial-time GLR parsing algorithm [31] was used to implement tools such as SDF [14], used by ASF+SDF [5] and Stratego/XT [32] to implement concrete syntax rewriting rules, or very recently BRNGLR [29]. Even so, there is still a performance issue, because GLR parsers are typically much less efficient than LALR(1) parsers (a factor of 10 is not uncommon [19]). Also recently, a hybrid GLR/LALR parser called Elkhound [19] has been delivered whose running time is close to that of a standard LALR(1) parser on all the portions of a grammar that are LALR(1). But as discussed above, an extended pattern grammar is highly ambiguous (unless we severely restrict the patterns), so then GLR parsing time would fall back to usual GLR-class performance. Therefore, GLR parsing may not be in general an efficient, production-quality, solution to the problem of parsing source code patterns. Other generalized parsing algorithms such as Earley [11] may eventually perform better on such highly ambiguous grammars.

Besides this performance issue, there is also an even more important porting issue, when talking about legacy parsers. Indeed, for either performance or historical reasons, generalized parsers are very rarely used in existing tools. Porting an existing parser to a different technology may be difficult — typically, the grammar has to be rewritten from scratch. Furthermore, rewriting the parser may profoundly impact the rest of the tool. This effort is simply unaffordable for most legacy tools.

Our solution. Summarizing, there is no simple solution today for adding concrete syntax pattern matching in existing parser-based tools without either profoundly restructuring the parser, rewriting it in another framework, severely restricting the patterns, or compromising performance. As a consequence, concrete patterns are rarely used in existing parser-based tools such as mainstream compilers. In particular, the lack of concrete patterns is particularly limiting the implementation of convenient user extensions in tools such as extensible compilers, code inspectors, model checkers, etc.

To solve this problem in a pragmatic way, we designed a pattern matching technique based on “unparsed patterns”, that allows using efficient, unrestricted, concrete syntax patterns while requiring no extension of the parser for the subject programming language. In particular, this technique is applicable to existing parsers, based on any parsing technology, without porting them to a different framework.

In a previous paper [34], we showed some concrete application of unparsed patterns within a checking compiler called mygcc. That application paper first introduced the idea of unparsed patterns, and briefly mentioned that they work by unparsing the AST, rather than parsing the pattern. However, no details were previously published about their implementation, nor about the theoretical aspects raised by these patterns. Both are the subject of the current paper. As we will show in the following, the simple idea of unparsing the AST must be combined non-trivially with other ingredients in order to obtain a usable pattern matching algorithm.

The main contributions of this paper can be summarized as follows:

- we describe in detail the novel paradigm of pattern matching of source code in concrete syntax, based on unparsing;
- we describe a family of linear-time pattern matching algorithms combining in different ways: unparsing, laziness, token analysis, lookahead and parenthesizing;

- we show how our pattern matching technology can be implemented in a completely language-independent way;
- from a theoretical point of view, our approach goes beyond the presented algorithms, by opening a series of interesting questions about: optimal parenthesizing, classes of grammars needing no parentheses in the patterns, pattern extensions, etc.;
- from a practical point of view, we expect that our approach will have a significant impact on existing parser-based tools written in imperative languages, by providing them pattern matching at a minimal cost, as demonstrated by our very concise implementation within the gcc compiler.

The rest of this paper is organized as follows. Section 2 defines unparsed patterns. Section 3 informally describes and Section 4 precisely defines a family of pattern matching algorithms for unparsed patterns. Section 5 describes two implementations of unparsed patterns. Section 6 puts into perspective unparsed patterns. Section 7 discusses related work and Section 8 concludes.

2. Unparsed patterns

Unparsed patterns are a particular form of concrete syntax patterns: they are written using the native syntax of the underlying programming language, except that they may contain pattern variables. Pattern variables may replace any sub-construct of a program fragment that is represented by a subtree in the AST. For example, pattern variables may replace any subexpression of an expression or of a statement; the “then” or “else” branch of a conditional, etc. Pattern variables are sometimes called meta-variables, to distinguish them from the variables of the subject programming language.

We illustrate the notion of unparsed patterns mainly in the context of C programs, but the idea is completely language-independent, and we occasionally give examples in other languages.

Unparsed patterns are always represented as quoted strings, in which pattern variables are preceded by an escape character. The escape character used in this paper is “%”, adhering to the familiar convention used for C “format strings”, but any other escape sequence can be used. For example, “buf = malloc(sizeof(int));”, “%x = malloc(%y);”, “%l = %l->next;” are unparsed patterns representing C statements, and “%x = malloc(%y)” (without the ending semicolon), “%x >= threshold”, and “p == NULL” are unparsed patterns representing C (or C++, or Java) expressions.

A *program fragment* is a substring of contiguous program source text that can be parsed entirely as a single AST. For example, “x + (y/2)”, “y=0; x=1;”, and “while(i--) /* update p */ *p++;” are program fragments, while “if(p!=0)”, “x=”, and “(sizeof(int)” are not program fragments. The AST of a program fragment “f” is noted $AST(f)$. Note that several program fragments, differing only in whitespace, comments, and redundant parentheses, may correspond to the same AST.

The *unparsed string* of an AST t , noted $TXT(t)$, is the string obtained by “unparsing” t , i.e. by recursively printing the concrete syntax of t in a standard way, with no comments and with sufficient whitespace and parentheses to make the text parsable back to t . Ideally, the unparsed string should not contain redundant whitespace and parentheses. The unparsed string of an AST t obviously is a program fragment, its AST being t itself.

An AST t is said to *match* an unparsed pattern p containing meta-variables x_i if there is a substitution $\{x_i \leftarrow t_i\}$ where t_i are subtrees of t such that $TXT(t) = p[\{x_i \leftarrow TXT(t_i)\}]$. If we use the corresponding textual substitution $\sigma^{TXT} = \{x_i \leftarrow TXT(t_i)\}$, we can write the above condition in a simpler way: $TXT(t) = \sigma^{TXT}(p)$

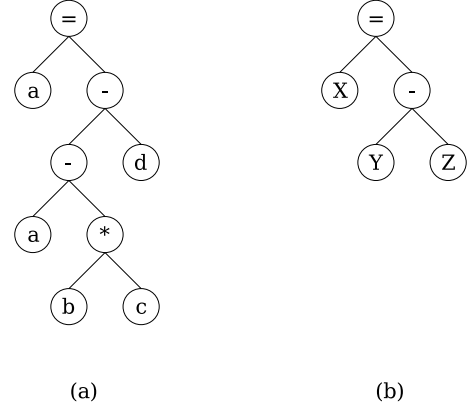


Figure 1. Matching AST(“a = a - b * c - d”) with the pattern “X = %y - %z”.

In the previous equality, the first term represents the unparsed string of the AST, and the second term represents the instantiated unparsed pattern, obtained by substituting in the pattern all variables by the unparsed string of their bound subtree.

By extension, a program fragment is said to match an unparsed pattern if its AST matches the pattern. We also say sometimes that the pattern matches the program fragment.

The above definition of pattern matching implies that a same variable occurring several times in a pattern must stand for the same subtree (in other words, non-linear patterns are correctly handled). However, for cases where the value of the variable is not important, there is an anonymous variable, noted “%.” in the patterns, that is always free. The anonymous variable is a special case in that different occurrences of it in the same pattern may be bound to different subtrees.

For instance, the pattern “%l = %l->next;” matches the statement “list = list->next;” under the substitution $\{l \leftarrow AST(“list”) \}$. We sometimes write the resulting substitution simply $\{l \leftarrow list\}$, where the subtrees are denoted by their unparsed strings. The same pattern does not match the statement “p = buf[0]->next;”.

3. Matching unparsed patterns

Before presenting precise algorithms for unparsed pattern matching in Section 4, we discuss them informally on a running example. Consider the problem of matching the C expression “a = a - b * c - d” with the code pattern “%x = %y - %z”.

Traditional, parser-based, pattern matching would first parse the expression using the usual program parser down to the AST in Figure 1(a), parse the pattern using an extended pattern parser to the tree in Figure 1(b), and then match the two trees, finally binding pattern variables in the only correct way: $\{x \leftarrow a, y \leftarrow a - b * c, z \leftarrow d\}$.

3.1 Using unparsing

The key idea of unparsed patterns is to avoid parsing the pattern by going the other way around, i.e., by unparsing the program AST to compare it with a textual pattern.

However, if the AST is simply unparsed to a string, matching would fall back to the case of matching between two strings. Plain string matching is very imprecise, because it would allow to bind both $\{x \leftarrow a, y \leftarrow a - b * c, z \leftarrow d\}$, which is correct, and $\{x \leftarrow a, y \leftarrow a, z \leftarrow b * c - d\}$, which is incorrect, since the subtraction operator is left-associative.

3.2 Using meta-parentheses

The trivial solution is to make explicit in the string pattern all of the tree structure information, using some form of parentheses. Thus, to match the AST in Figure 1(a) with the code pattern “ $%x = \%y - \%z$ ”, we can re-write the pattern to make explicit the language structure, by using “meta-parentheses” written as escape sequences, for instance “ $\%()$ ” and “ $\%\%$ ”: “ $\%(\%x = \%(\%y - \%z\%) \%)$ ”. Note that in general we cannot use plain parentheses to unveil the structure because the language may already contain parentheses, which may have a completely different meaning than grouping constructs.

Using this representation, it is straightforward to perform pattern matching equivalent to tree matching, in linear time. However, there are two manifest problems with this trivial solution. First, meta-variables are bound to strings in concrete syntax, rather than being bound to subtrees of the AST. This is not suitable when using pattern matching to manipulate the matched subtrees, which is a quite common case within parser-based tools. The second problem is that the explicit structure comes at the price of seriously obfuscating the pattern. Fully meta-parenthesized patterns are very difficult to read and to write.

3.3 Using lazy unparsing

The first problem of the trivial solution, of not being able to retrieve the matched subtrees, is due to the fact that the whole AST is unparsed at once, dropping the references to all the subtrees. To avoid that, ASTs can be unparsed lazily instead. This is formalized by the following definition.

An AST t is said to be non-empty if its program fragment $\text{TXT}(t)$ contains at least one token (i.e. it does not consist of only whitespace). The *unparsed list* of a non-empty AST t , noted $\text{LST}(t)$, is a non-empty ordered list of concrete syntax tokens (such as identifiers, keywords, etc.) and non-empty sub-trees of t , that represents the top-level of t . For example, $\text{LST}(\text{AST}(\text{“if}(a>0)$ return $a+1;$ ”))) is the list [“if”, “(”, $\text{AST}(\text{“}a>0\text{”})$, “), “], $\text{AST}(\text{“return } a+1;$ ”)). Note that empty subtrees of t are not present in $\text{LST}(t)$. For instance, $\text{LST}(\text{AST}(\text{“int } x;$ ”))) = [“int”, $\text{AST}(\text{“}x\text{”})$, “;”]; there is no empty sub-tree corresponding to the list of optional qualifiers such as “const” or “static” that are missing.

The unparsed list of the AST is a means to incrementally unparsing an AST: the top-level structure information in the AST is decomposed, but all the subtrees are kept unchanged.

A second benefit of lazy unparsing is that meta-parentheses will not be confused anymore with the parentheses in the language (this will be proven in Section 4.1). Thus, our pattern can be written simply as “ $(\%x = (\%y - \%z))$ ”.

Lazy unparsed pattern matching first parses the expression using the usual program parser to construct the same AST in Figure 1(a). It then pushes the AST on an empty stack, and considers the textual code pattern “ $(\%x = (\%y - \%z))$ ” as a stream of characters and meta-variables. The algorithm proceeds by two kinds of steps:

- match step: Match the element on top of the stack with some prefix of the stream. This can be done in three different situations:
 - If the element on top of the stack is a token (which is a string of characters) that matches the prefix of the stream, consume the element and the prefix. Note that the stream does *not* need to be separated into tokens by some kind of lexical analysis; token information existing only in the stack (coming from the unparsed tree) is sufficient.

- If the element on top of the stack is a tree t and the stream starts with a meta-variable bound to a subtree equal to t , consume t and the meta-variable.
- If the element on top of the stack is a tree t and the stream starts with a free meta-variable, bind the variable to the tree and consume the two.
- unparse step: If the element on top of the stack is a tree t and the stream starts with a token, replace t with its partially unparsed form $\text{LST}(t)$ and leave the stream unchanged.

If the algorithm consumes the whole stream ending up with an empty stack, it successfully matched all the elements in the initial AST with elements in the pattern stream, and reports a successful match. Otherwise, it reports that the matching has failed.

In our example, the top of the stack is the whole AST t in Figure 1(a) and the beginning of the pattern “ $(\%x = (\%y - \%z))$ ” is not a variable. Therefore, it cannot directly match the two, so it performs an unparse step, replacing the tree t with the elements in $\text{LST}(t)$. Of course, as the pattern contains parentheses at each level, the lazy unparse algorithm will surround the elements in $\text{LST}(t)$ by a left and a right plain parentheses. This step changes the stack to [“(”, $\text{AST}(\text{“}a\text{”})$, “=”, $\text{AST}(\text{“}a-b*c-d\text{”})$, “)”], and leaves the stream unchanged. Then, it is able to consume the initial left parenthesis, bind $\text{AST}(\text{“}a\text{”})$ to meta-variable x , match the “=” symbol, which gives the stack [$\text{AST}(\text{“}a-b*c-d\text{”})$, “)”] and the stream “ $(\%y - \%z))$ ”. As above, as it cannot match the top tree with the starting “(”, it first unparses the tree yielding the stack [“(”, $\text{AST}(\text{“}a-b*c\text{”})$, “-”, $\text{AST}(\text{“}d\text{”})$, “)”], then is able to consume the starting left parenthesis, successfully binds y to $\text{AST}(\text{“}a-b*c\text{”})$ and z to $\text{AST}(\text{“}d\text{”})$. Finally, the two right parentheses in the tree are matched with the corresponding parentheses in the pattern. Thus, the algorithm finds the only correct match, given by the substitution $\{x \leftarrow a, y \leftarrow a - b * c, z \leftarrow d\}$.

Note that this algorithm binds the variables directly to the AST subtrees, and not just to their unparsed strings, as the trivial algorithm. This considerably increases its possible practical applications in parser-based tools.

Using lexical information. In the definition of the unparsing function LST , one can wonder about the usefulness of generating distinct tokens between the subtrees, instead of compacting adjacent tokens. For example, $\text{LST}(\text{“if}(a>0)$ return $a+1$ ”)) could have been defined as [“(if”, $\text{AST}(\text{“}a>0\text{”})$, “. . .], grouping all adjacent tokens of the top level together. Using this compact LST function, the match would still succeed as described above. However, separating the tokens in the unparsing function allows more flexibility in writing the patterns. Specifically, if the programming language ignores whitespace between the tokens (as most programming languages do), the matching algorithm may skip whitespace in the patterns before any step. This way, patterns can be written with arbitrary whitespace to maximize readability and still match ASTs.

In terms of usability, lazy unparsed patterns might be considered by some programmers as convenient enough for many practical applications. Compared to writing tree patterns, programmers do not have to know the API for building ASTs, but in order to fully parenthesize a pattern, they must still be aware of the AST structure, which tends to reduce their advantage.

3.4 Using lookahead

An alternative to the parentheses introduced by the unparse function is to use a lookahead mechanism.

Coming back to our running example, the lookahead-based pattern matching algorithm matches the AST in Figure 1(a) with the pattern written simply as “ $\%x = \%y - \%z$ ”. As the pattern stream starts with a meta-variable x and the stack contains just the initial

This example clearly shows that the lookahead(1)-based unparsed matching algorithm is incomplete: there are some patterns and ASTs that it cannot match, while a tree-based matching algorithm would. A theoretical characterization of all such cases will be given in the next section.

The idea is that introducing escaped meta-parentheses in the pattern around some (pattern segment corresponding to an) unparsed subtree has the effect of forcing the matching algorithm to perform an unparse step. This is because the algorithm will face a situation when it has such a subtree on top of the stack, and the left meta-parenthesis in the pattern; as it cannot directly match the two, it is forced to choose an unparse step. If this situation corresponds to a conflict unsolvable by the one-token lookahead, the introduction of parentheses is a direct way to circumvent the default solution to the bind/unparse conflict, which is a bind.

Rule 1 deals with the case when the stack begins with a token and the pattern also begins with a token (i.e., with anything else than an escape sequence). If this is the case, the token on the stack is compared to the prefix of the string, and if they are equal, the matching advances by consuming both. Rule 2 performs an unparse step by replacing t with the elements in $LST(t)$, surrounded by two meta-parentheses tokens. Rules 3 and 4 deal with the case when the stack begins with a tree and the pattern begins with a meta-variable, and depending on the state of the variable, either bind the free variable to the tree or compare the already instantiated variable

$$\begin{aligned}
\langle [k|s], k + p, \sigma \rangle &\longrightarrow \langle s, p, \sigma \rangle & (1) \\
\langle [t|s], k + p, \sigma \rangle &\longrightarrow \langle [“” + LST(t) + [“”] + s, k + p, \sigma \rangle & (2) \\
\langle [t|s], “%x” + p, \sigma \rangle &\longrightarrow \langle s, p, \sigma \cup \{x \leftarrow t\} \rangle & \text{if } x \notin \text{domain}(\sigma) & (3) \\
\langle [t|s], “%x” + p, \sigma \rangle &\longrightarrow \langle s, p, \sigma \rangle & \text{if } x \in \text{domain}(\sigma) \wedge \sigma(x) = t & (4)
\end{aligned}$$

Figure 2. The lazy unparse pattern matching algorithm: F(0).

to the tree. Note that the algorithm does not allow to bind a meta-variable to a token, since in our definition, variables are allowed to match only trees.

Complexity. The F(0) algorithm runs in linear time $O(|t| + |p|)$ (where t is the tree and p is the pattern). This is no worse than algorithms that require a pattern parser. A proof is provided in the Appendix.

Correctness. The F(0) algorithm is correct, which means that if the algorithm rewrites $\langle [t|s], p, \{\} \rangle$ to $\langle [], [], \sigma \rangle$, then the tree t matches p under substitution σ . A proof is provided in the Appendix.

Completeness. The F(0) algorithm is complete, in the sense that it finds all matches that are found by a conventional tree matching algorithm. That is, for any tree $t \in T_\Sigma$, and tree pattern $P \in T_\Sigma(V)$ (where Σ consists of the AST constructors in the language and V is the set of meta-variables), such that t matches P (in the classic sense, as trees), the algorithm F(0) succeeds in matching t with the corresponding unparsed pattern $p = TXT_{F(0)}(P)$. Note that here we extend the function $TXT_{F(0)}$ to tree pattern variables in the obvious way: $TXT_{F(0)}(x) = “%x”$. The variables in V occurring in P are handled by the algorithm as trees of height one, so that it is possible to bind a meta-variable “%x” to a variable $x \in V$.

A sketch of the proof is provided in the Appendix.

For the example in the introduction, the F(0) pattern would be written as:

```
"(for((%x=0); (%x<%n); (++%x)) ((%y[%x]=0);))"
```

4.2 Using lookahead

The lookahead-based pattern matching algorithm uses no meta-parentheses in the pattern and a lookahead of one token. We will refer to it as “N(1)”. The PAR function for N(1) is the identity function. Therefore, $TXT_{N(1)}$ is simply TXT .

The rewrite rules of the lookahead-based pattern matching algorithm are given in Figure 3. The modified rules with respect to the lazy unparse algorithm are:

- Rule 2 is modified as Rule 6 not to add meta-parentheses anymore around an unparsed tree;
- Rules 3 and 4 have been guarded by successful lookahead, giving Rules 8 and 9;
- the new Rule 7 has been added to trigger an unparse step when a variable cannot be bound to a tree or compared with a tree because of negative lookahead.

The lookahead function is defined by the following equations (where e stands for any stack element, either a token or a tree):

$$\begin{aligned}
\text{lookahead}([], []) &= \text{true} \\
\text{lookahead}([e|s], k + p) &= (\text{first_token}(e) = k) \\
\text{lookahead}([t|s], “%x” + p) &= \text{true}
\end{aligned}$$

If no equation applies, the default value of *lookahead* is false. Function *first_token* returns the first token of a stack element, i.e. the token appearing first in its unparsed string. If the element e is a

tree, then it returns its recursively defined leftmost token; if e is a token then it returns e itself.

Complexity. The N(1) algorithm runs in linear time. A proof is provided in the Appendix.

Correctness. The N(1) algorithm is correct. The proof is similar to that for F(0).

Incompleteness. Concerning the incompleteness of the lookahead-based matching (shown in Section 3 by means of a counterexample), it is useful to characterize more precisely the matches that cannot be found by this algorithm. The bad choices of the algorithm always occur in “dilemma” states, in which the one-token lookahead is unable to distinguish the correct next step. All dilemma states are of the form $\langle [t_1|s_1], “%x” + p', \sigma \rangle$ where the top of the stack is a tree and a pattern starts with a variable. In such a state, the lookahead(1) is compatible with two different paths. The greedy algorithm always chooses a bind or compare (which ultimately may lead the algorithm to fail) even if an unparse could have led to a success. We can deduce two further properties of such a state:

- because the algorithm chose a bind, *lookahead*(s_1, p') must be true
- if the unparse would have led to a match, the state that would have been reached $\langle LST(t_1) + s_1, “%x” + p', \sigma \rangle$ must not be an obvious failure (independently of the matching algorithm!). Therefore, $LST(t_1)$ cannot start with a token (because by definition of matching we do not allow variables to match tokens), and it cannot be empty either (by definition of unparsing), so $LST(t_1) = [t_2|s_2]$. Moreover, a *Bind*(x) step must be reached, possibly after other unparse steps $LST(t_i) = [t_{i+1}|s_{i+1}]$, in a state $\langle LST(t_n) + s_n + \dots + s_1, “%x” + p', \sigma \rangle$. In this state, *lookahead*($s_n + \dots + s_1, p'$) must also be true, because violating the lookahead leads to a sure failure (again independently of the algorithm used).

Thus, we can characterize dilemma states by the following predicate:

$$\text{dilemma}(\langle [t_1|s_1], “%x” + p', _ \rangle) \Rightarrow$$

$$(\exists n > 1) \bigwedge_{i=2}^n LST(t_{i-1}) = [t_i|s_i] \wedge$$

$$\text{lookahead}(s_1, p') \wedge \text{lookahead}(s_n + \dots + s_1, p')$$

Conversely, it can be easily seen that any state verifying the predicate above is a dilemma state, because from such a state it is possible, without violating the lookahead, both to perform a bind step or a sequence of unparse steps followed by a bind step. Therefore the above predicate defines in fact an equivalent condition for dilemma states.

By inspecting the definition of *lookahead*, we can find that dilemma states fall in one of the following classes, depending on the first element in pattern p' :

1. p' is empty, and $s_1 = \dots = s_n = []$, so t_1 is at the end of its list and for $i > 1$, t_i are alone in their lists;

$$\begin{aligned}
\langle [k|s], k + p, \sigma \rangle &\longrightarrow \langle s, p, \sigma \rangle & (5) \\
\langle [t|s], k + p, \sigma \rangle &\longrightarrow \langle LST(t) + s, k + p, \sigma \rangle & (6) \\
\langle [t|s], \text{"\%x"} + p, \sigma \rangle &\longrightarrow \langle LST(t) + s, \text{"\%x"} + p, \sigma \rangle & \text{if } \neg \text{lookahead}(s, p) & (7) \\
\langle [t|s], \text{"\%x"} + p, \sigma \rangle &\longrightarrow \langle s, p, \sigma \cup \{x \leftarrow t\} \rangle & \text{if } x \notin \text{domain}(\sigma) \wedge \text{lookahead}(s, p) & (8) \\
\langle [t|s], \text{"\%x"} + p, \sigma \rangle &\longrightarrow \langle s, p, \sigma \rangle & \text{if } x \in \text{domain}(\sigma) \wedge \sigma(x) = t \wedge \text{lookahead}(s, p) & (9)
\end{aligned}$$

Figure 3. The lookahead-based pattern matching algorithm: N(1).

2. p' starts with a token k , s_1 is non-empty, and $k = \text{first_token}(s_1)$ is split into two rules:
 $\text{first_token}(s_n + \dots + s_1)$, where we extend first_token to treat non-empty lists in the obvious way;
3. p' starts with a variable, and both s_1 and $s_n + \dots + s_1$ start with a tree.

We have now a necessary condition for *dilemma*, indicating where unsolvable conflicts could occur. Based on it, we can define conflicting ASTs in a given stack context as trees that may lead to a dilemma state for *some* pattern:

$$\begin{aligned}
\text{conflicting}(t_1, s_1) &\iff (\exists p') \text{dilemma}(\langle [t_1|s_1], \text{"\%x"} + p', - \rangle) \\
&\iff (\exists n > 1) \bigwedge_{i=2}^n LST(t_{i-1}) = [t_i|s_i] \wedge \\
&\quad (s_1 = \dots = s_n = [] \vee \\
&\quad \text{first_token}(s_1) = \text{first_token}(s_n + \dots + s_1) \vee \\
&\quad (s_1 = [t'_1|-] \wedge s_n + \dots + s_1 = [t'_n|-]))
\end{aligned}$$

Left-recursive operators such as the “-” in our running example are an instance of the second class. An instance of the first class is matching the C text “-a” with “-%x”, where “a” might be matched to the C identifier, but also to the C expression that consists of just this identifier (note that this case is also conflicting for conventional pattern matching). This algorithm will always take the last option. An instance of the third class might be matching the C function definition “int f(a){}” with “int %x%y{ }”, if we assume that the C grammar is defined so that the whole definition unparses as [“int”, AST(“f(a)”), AST(“{ }”)], and “f(a)” unparses to [AST(“f”), AST(“(a)”)]. The algorithm will never find the match, because it will map x to AST(“f(a)”), then fail.

Therefore, we can conclude that when variables in patterns are never glued together, the most common case of incompleteness of the lookahead algorithm are left recursive operators.

4.3 Lookahead with escaped meta-parentheses

The incompleteness of the N(1) algorithm may be eliminated by using escaped meta-parentheses. The ES(1) algorithm uses escaped meta-parentheses only in the pattern around some subtrees to force unparsing steps, and uses a one-token lookahead. In other words, the *PAR* function for ES(1) is still the identity function (and therefore, $TXT_{ES(1)}$ is simply TXT).

The rules of ES(1) are given in Figure 4. The only changes with respect to N(1) are that new rules were added to deal with meta-parentheses. In particular, Rule 13 comparing a tree to a left meta-parenthesis forces an unparse step, which consumes the left meta-parenthesis and adds a right meta-parenthesis in the stack to match the corresponding left meta-parenthesis in the pattern. Rule 11 consumes both meta-parentheses after matching the subtree.

The lookahead function is redefined to skip meta-parentheses, and the rule:

$$\text{lookahead}([e|s], k + p) = (\text{first_token}(e) = k)$$

$$\begin{aligned}
\text{lookahead}([k|s], k' + p) &= (k = k') \\
\text{lookahead}([t|s], k + p) &= \text{true}
\end{aligned}$$

This leads to a more conservative definition of lookahead, succeeding whenever the top element on the stack is a tree t and the top element on the pattern is a token k , even if the first token in the tree is not k . The reason we adopt this approximation is to gain a very useful property of the matching algorithm, that we call composability. Composability means that whenever the algorithm successfully matches a tree $t \in T_\Sigma(V)$ to the pattern $TXT_x(t)$, it will also match any instance $t' = \theta(t)$ to the same pattern, by the same derivation (modulo substituting in all steps t with $\theta(t)$). A sufficient condition for composability is that all the guards of the rules be invariant to ground substitutions, that is, when substituting the variables in t with any AST. As variables in t are handled as trees by the algorithm, and trees occur in guards just as arguments to the lookahead function, only the lookahead function needs to be invariant to ground substitutions. This obviously is the case for the new definition, but is not the case for the old definition.

According to the new definition of lookahead, the predicate *conflicting* has to be recomputed from the predicate *dilemma* in Section 4.2 (which is algorithm-independent). By considering the different possible first elements in a pattern that does not contain meta-parentheses and by examining for each one the corresponding lookahead clauses making the predicate true, we distinguish the following cases of bind/unparse conflicts:

- the pattern p' is empty and $s_1 = \dots = s_n = []$
- the pattern p' starts with a token k , and either both s_1 and $s_n + \dots + s_1$ begin with the same token k or at least one of them begins with a tree
- the pattern p' starts with a variable “%x”, and both s_1 and $s_n + \dots + s_1$ begin with a tree

By abstracting away the pattern, we can define the *conflicting* predicate as:

$$\begin{aligned}
\text{conflicting}(t_1, s_1) &\iff (\exists p') \text{dilemma}(\langle [t_1|s_1], \text{"\%x"} + p', - \rangle) \\
&\iff (\exists n > 1) \bigwedge_{i=2}^n LST(t_{i-1}) = [t_i|s_i] \wedge \\
&\quad (s_1 = \dots = s_n = [] \vee \\
&\quad (\exists k)(s_1 = [k|-] \wedge s_n + \dots + s_1 = [k|-]) \vee \\
&\quad (\exists t'_1)(s_1 = [t'_1|-] \wedge \\
&\quad (\exists t'_n)(s_n + \dots + s_1 = [t'_n|-]))
\end{aligned}$$

Thus, a new case of bind/unparse conflict (compared to N(1)) is when two subtrees in an unparsed list are not separated by any token.

Complexity. The ES(1) algorithm runs in linear time. Details are provided in the Appendix.

$$\langle [k|s], k + p, \sigma \rangle \longrightarrow \langle s, p, \sigma \rangle \quad (10)$$

$$\langle [“%”|s], “%” + p, \sigma \rangle \longrightarrow \langle s, p, \sigma \rangle \quad (11)$$

$$\langle [t|s], k + p, \sigma \rangle \longrightarrow \langle LST(t) + s, k + p, \sigma \rangle \quad (12)$$

$$\langle [t|s], “%(” + p, \sigma \rangle \longrightarrow \langle LST(t) + [“%”], s, p, \sigma \rangle \quad (13)$$

$$\langle [t|s], “%x” + p, \sigma \rangle \longrightarrow \langle LST(t) + s, “%x” + p, \sigma \rangle \quad \text{if } \neg \text{lookahead}(s, p) \quad (14)$$

$$\langle [t|s], “%x” + p, \sigma \rangle \longrightarrow \langle s, p, \sigma \cup \{x \leftarrow t\} \rangle \quad \text{if } x \notin \text{domain}(\sigma) \wedge \text{lookahead}(s, p) \quad (15)$$

$$\langle [t|s], “%x” + p, \sigma \rangle \longrightarrow \langle s, p, \sigma \rangle \quad \text{if } x \in \text{domain}(\sigma) \wedge \sigma(x) = t \wedge \text{lookahead}(s, p) \quad (16)$$

Figure 4. The ES(1) matching algorithm.

Correctness. The ES(1) algorithm is correct. The proof is similar to the F(0) case.

Before stating the completeness of ES(1), we must first define how a pattern must be minimally parenthesized so as to avoid match failures.

Meta-parentheses are optional in the pattern, but they are needed at least around conflicting subtrees. In addition to these conflicting subtrees, meta-parentheses are also needed around “leftmost-conflicting” trees, i.e. any tree t having a leftmost descendant nested at depth n which is a conflicting subtree t_n . This is because t_n being conflicting, its pattern must start with a left meta-parenthesis; when Rule 13 applies on t , it consumes one parenthesis. In fact, this rule must execute $n - 1$ times on t , consuming $n - 1$ meta-parentheses in the pattern before arriving at t_n ; in order to force the unparsing of t_n , the pattern should contain at least n parentheses ($n - 1$ to unparse until t_n is reached, then one more to unparse t_n itself). Thus, trees that need to have meta-parentheses in the pattern are characterized by the following predicate:

$$\text{leftmost_conflicting}(t_1, s_1) \iff \text{conflicting}(t_1, s_1) \vee \\ (\exists n > 1) \bigwedge_{i=2}^n LST(t_{i-1}) = [t_i|s_i] \wedge \text{conflicting}(t_n, s_n)$$

The predicate *leftmost_conflicting* defines all the subtrees that might need to be meta-parenthesized to force an unparse instead of a bind. Based on this predicate, it is therefore possible to define a transcription function *Trans* taking a tree $t \in T_\Sigma(V)$, and returning an unparsed pattern in which all leftmost conflicting subtrees have been parenthesized. The function *Trans*(t) can be defined as follows:

$$\begin{aligned} \text{Trans}(t) &= \text{Trans}(t, []) \\ \text{Trans}(t, s) &= \text{if } \text{leftmost_conflicting}(t, s) \\ &\quad \text{then “%(”} + L\text{Trans}(LST(t), s) + “%”)” \\ &\quad \text{else } L\text{Trans}(LST(t), s) \\ L\text{Trans}([], s) &= “” \\ L\text{Trans}([k|l], s) &= “k” + L\text{Trans}(l, s) \\ L\text{Trans}([x|l], s) &= “%x” + L\text{Trans}(l, s) \\ L\text{Trans}([t|l], s) &= \text{Trans}(t, l + s) + L\text{Trans}(l, s) \end{aligned}$$

Completeness. The ES(1) algorithm is complete, in the sense that it finds all matches that are found by a conventional tree matching algorithm. More precisely, for any tree $t \in T_\Sigma$ and tree pattern $P \in T_\Sigma(V)$, if t matches P under conventional tree matching, ES(1) matches t with *Trans*(P) (with the same derivation as when matching P with *Trans*(P)). A proof is provided in the Appendix.

Thus, the *Trans* function gives a simple way to automatically parenthesize unparsed patterns, starting from the desired conventional tree pattern.

Using algorithm ES(1), the pattern from our running example has to be written “%x = %y - %z”, using no meta-parentheses. Also

the example in the introduction would be written simply as (to be compared with that for F(0)):

```
"for(%x=0; %x<%n; ++%x) %y[%x]=0;"
```

5. Implementation

Avoiding the parsing of patterns dramatically simplifies the implementation of pattern matching, as can be seen from the following two implementations.

Implementation in mygcc. Unparsed patterns were first implemented in the context of a lightweight checking compiler called mygcc [21]. Mygcc is an extensible version of the gcc compiler, able to perform user-defined checks on C, C++, and Ada code. Checks are expressed by defining incorrect sequences of program operations, where each program operation is described as an unparsed pattern or a disjunction of unparsed patterns.

The implementation of pattern matching within mygcc counts for only about 600 lines of new C code, plus about 250 lines of code adapting the existing tree pretty-printer of gcc to perform unparsing on demand. The existing pretty-printer dumped the unparsed representation of a whole AST in a debug file. We added a flag called “lazy_mode” to switch between the standard dumping behavior and the new on-demand behavior. When in on-demand mode, the pretty-printer returns for a given AST its unparsed list, instead of dumping it entirely to a file. This modification was pretty straightforward.

It is important to note that even though three different input languages can be checked, every single line of the patch is language-independent. As a proof for that, the patched gcc compiler restricted to the C front-end was initially tested only on C code, as reported in [34]; subsequently, by just re-compiling gcc with all the front-ends enabled it became possible to check C++ and Ada programs. Part of this extreme language independence comes from the fact that all the three front-ends generate intermediate code in a language called Gimple, and the dumper for different languages shared a common Gimple-based infrastructure that we be modified just once. However, this is not required for our pattern matching framework. If the common infrastructure of the language-specific dumpers did not exist, we would just have to modify each of the dumpers to make them lazy.

Standalone implementation. The ES(1) pattern matching algorithm was also implemented as a freely available, standalone prototype called matchbox [20]. This very simple prototype, consisting of 500 lines of C code, takes a parse tree represented in a Lisp-like notation and an unparsed pattern, prints a complete trace of all the rules applied, and finally reports a successful match or a failure. The prototype may already be used to reproduce all the examples in this paper (using the ES(1) algorithm). The aim of matchbox is to evolve into a standalone library for unparsed pattern matching, that can be linked in any parser-based tool.

6. Assessment

The technique of pattern matching based on unparsed patterns is completely language independent. Patterns are simply strings, which exist as a base type in any programming language. No pattern parser is required, which means that also the implementation of the pattern matcher is language independent. The only part tied to a specific language is the unparsed, but AST unparsers can be automatically generated from any grammar.

Unparsed patterns are an unrestricted solution to code pattern matching, because they allow pattern variables to stand for any program sub-construct or sub-expression — in fact, for any subtree in the AST. As opposed to this unrestricted use, many pattern-based tools implement parsed patterns only for a few common program constructs.

By being an easy-to-implement and a general solution, unparsed patterns have the potential to enable widespread use of concrete syntax code pattern matching within any parser-based tool. There are two quite different ways to use this enabling technology.

Internal uses. First, patterns can be used in the implementation of the tool itself, to simplify various code analyses and transformations. For instance, an analysis or optimization pass could use pattern matching to look for statements matching a given pattern, e.g., increment assignments. This can simplify the implementation especially if the tool is written in a language that doesn't provide any support for pattern matching, like C or Java. However, as shown in the introduction, unparsed patterns may be useful even when the tool is written in a language that does provide a form of tree pattern matching (e.g. ML): some ASTs patterns — especially verbose patterns — are more easily expressed in native syntax than in tree syntax. Thus, for the least, unparsed patterns offer an alternative for the programmer to freely choose the more convenient form for each pattern.

External uses. Second, patterns can be used to make the tool extensible by associating user-defined behavior to some patterns. For example, in mygcc users can define sequences of operations that constitute bugs. As a particular case, mygcc allows searching all the code for a given pattern, by using a new option “-tree-check”. For instance, the following command will issue a warning for all the read statements whose result is unused, but otherwise compile the file as usual:

```
gcc --tree-check="read(%x, %y, %z);" foo.c
```

Indeed, because of the final semi-colon, this pattern only matches complete statements, and not simple expressions consisting of a “read” function call. Therefore, statements using the value of the call will not be reported (which is the intended behavior).

Comparison with parsed patterns. When comparing unparsed patterns with traditional, parsed patterns, also expressed in native syntax, the advantages of unparsed patterns include:

- The implementation is much simpler, almost no investment is needed. In particular, existing tools do not need to be ported to different parsing technologies.
- The implementation is completely language-independent (modulo linking it with a specific unparsed LST).
- Meta-variables may stand for anything that is represented as a subtree in the AST, including types, qualifiers, etc. This is as good as classic tree matching, but difficult to implement efficiently with parsed patterns.
- As they are not parsed, patterns may be constructed dynamically with no performance penalty.

The limitations of unparsed patterns include:

- Extra parentheses are needed in some patterns to resolve conflicts that are not solvable by one-token lookahead.

The ES(1) algorithm reduces this need to a limited number of well-defined situations, and signaled by the implementation as a warning (when tracing is on). Knowing both theoretically and practically which constructs in the language need parentheses, programmers will be able to correctly parenthesize the patterns. To further assist the programmer, a function (described in the Appendix) may be provided to dump a minimally parenthesized pattern matching a program fragment.

- Ill-formed patterns are not signaled at compile time: they simply do not match any code at runtime.

This problem can be avoided to some extent by the dumping feature described above.

- Unparsed patterns cannot be used to *build* code in native syntax. When used in code transformation tools, they can serve only for matching code (on the left side of rewriting rules). However, trees can be built using conventional AST constructors out of the subtrees selected by the left-hand sides.

Therefore, unparsed patterns are not meant to replace traditional, parsed code patterns if they are available, but rather provide a pragmatic, lightweight alternative when parsed patterns are unavailable, and would be too expensive to implement.

7. Related work

The idea of matching a tree with a pattern expressed as a string without parsing the pattern was apparently first mentioned in our previous paper [34]. Combining this idea with the use of token information in the AST, meta-parentheses, and lookahead is new, and so is the analysis of precise cases of bind/unparse conflicts and the study of the algorithmic complexity.

Efficient algorithms for matching a tree with a pattern also represented as a tree have been known for a long time. This pattern matching problem can be solved in linear time as a particular case of unification [25] where variables may occur only in the pattern. We saw that reducing code pattern matching to tree matching is either difficult to use (patterns expressed as trees) or difficult to implement in most existing tools (pattern parser). Our approach avoids both difficulties while keeping the same linear execution time.

Many variants of the tree pattern matching problem have been studied. The subtree matching problem consists of deciding if a pattern matches any subtree of a subject tree. The “dictionary” version of this problem involves N patterns to be searched against the subject's subtrees. Some known algorithms [17] begin with a pre-processing phase that reduces both the subject tree and the pattern to their pre-order strings. However, re-writing a text pattern as a pre-order string requires first representing the pattern as a tree, so it cannot be used to avoid parsing the pattern. In terms of execution time, the preprocessing phase reduces the asymptotic complexity of the search, and thus ensures a very efficient search of the patterns against all subtrees. Our approach is less efficient on the problem of dictionary subtree searches.

In the last decade, XML has increasingly been adopted as a standard for representing tree-shaped data, including program ASTs as a particular case. Therefore, XML-specific tree pattern languages such as XPath are being used for matching code. Compared to XPath, unparsed patterns provide the convenience of concrete syntax, but less matching power — for instance, matching a subtree nested at an arbitrary level is not possible. XPath has been integrated in more powerful query languages such as XQuery or in transformation languages such as XSLT or CDuce [2]. Unparsed patterns can be embedded in any programming languages providing

a string type, eventually as a complement to tree matching mechanisms already in the language.

Native patterns [30] are completely legal code fragments, but in which some reserved names can be used as pattern variables. Actually, the reserved names are the names of non-terminals in the grammar of the language as described in its reference manual (which is supposed to be known by programmers). These nonterminal names may be suffixed by a number to denote different occurrences of the nonterminal and by “*” or “+” to denote lists of such nonterminals. The extended grammar of the patterns can be generated automatically from the base grammar. However, this requires expressing or porting the base grammar in a syntax definition formalism called SDF. As opposed to this constraint, unparsed patterns can be incorporated in any existing parser-based tool with minimal effort.

Scruple [23] is a generic pattern language specialized for matching source code. Scruple patterns are more general than ours, as they allow for instance matching lists of subtrees in a single pattern variable, or matching in the same pattern a tree and one of its subtrees nested at an arbitrary level. Execution time is not linear, as the algorithm involves backtracking. The patterns are compiled into a recursive network of automata that consume “tokens” in the subject AST that correspond to its subtrees. This is rather similar to our algorithm. However, Scruple patterns are parsed by a pattern parser which extends the native parser of the subject language. Unlike our approach, the tokens in the AST do not include tokens in the concrete syntax (keywords, separators, etc.).

An elegant language embedding technique for meta-programming is described in [32], which allows embedding an arbitrary context-free subject language S in a host context-free programming language H , and using the concrete syntax of S to match and build subject code fragments within H programs. This technique requires defining the grammar of both languages in the SDF framework, which combines the two in a single grammar. This grammar fusion uses SDF’s support for modules and user-defined grammar injection rules (that can be automated). The advantage of their approach is that syntax errors in both the host language and its subject patterns are checked by a single parser. After this combined parsing, a generic AST transformation reduces the bi-lingual AST to a plain H AST. Hence, a meta-program in $H + S$ is preprocessed to a program in H , that can be compiled with any compiler for H , and linked with appropriate tree manipulation libraries for using the parsed patterns. In particular, pattern matching is supported if the language M or the linked libraries provide tree matching. The main inconvenience of this approach from a practical point of view is the porting effort of both languages to SDF. Besides, an acknowledged limitation of that work is that it cannot express context-sensitive syntax such as type identifiers in C or offside rules in Haskell. Unparsed patterns can serve as a lightweight alternative to this approach, when re-writing the two parsers in SDF is not feasible. It requires a really minimal effort to implement, and is not limited to a given class of languages, once they are parsed to ASTs by an existing parser. Thus, unparsed patterns are meant to be easily incorporated in most existing tools. In turn, our approach does not provide support for building ASTs in concrete syntax, nor syntax checking of the patterns.

Also related to our work is the problem of pattern disambiguation, consisting in choosing among the several possible trees corresponding to a textual pattern. As we mentioned in the introduction, disambiguation is traditionally done by introducing special pattern syntax, which tends to reduce the advantages of concrete syntax patterns. A clearly better solution, used in several meta-programming systems, consists in exploiting type information associated to the pattern variables or to the whole pattern. This technique has been applied for instance in Meta-AspectJ [36] to allow

producing AspectJ code within Java meta-programs using particularly convenient concrete patterns. Patterns are parsed, using a backtracking ANTLR-based parser, mixing LL(k) parsing and type checking. By greatly exploiting the specifics of the Java and AspectJ languages, the tool is able to infer the type of variables containing object code, and automatically introduce some type conversions from basic host types to object code types when needed. However, patterns are used only for generating code, while our patterns are used only in pattern matching. Their parsing algorithm may exhibit exponential time behavior.

A general, language-independent solution for the type-based disambiguation of patterns is described by Bravenboer *et al.* [6]. Their solution consists in three phases. First, the host language code with embedded object language patterns is parsed using a scannerless GLR algorithm according to the method mentioned above [32], which returns a parse forest for each ambiguous pattern. A second phase translates each such object AST into host language code for building that AST. The disambiguation phase is done by a slightly extended version of the host language type checker, and keeps only the valid AST builders. As the disambiguation phase sees no object code, its implementation is independent from the object language, but not from the host language. This is much like our language-independent approach. Their technique itself is portable to any statically typed language, if different AST nodes are mapped to different types in the host language.

In our framework, disambiguation is done using meta-parentheses. These chiefly serve to eliminate ambiguities due to some tree structure that is absent in the unparsed patterns, but can also serve to eliminate other ambiguities that would also exist in the corresponding parsed patterns. For instance, the C or Java pattern “f(%x)” may represent either a function call with a single argument (bound to variable x) or a function call with any number of arguments (then x is bound to the list of all the arguments). This ambiguity also exist with parsed patterns, where it is eliminated by specifying the type of x as a list of object ASTs or as a single object AST. When matched with the greedy ES(1) algorithm, x will always match the AST representing the whole list of arguments. Single-argument calls can be matched by introducing extra meta-parentheses, yielding the pattern “f(%(%x%))”.

8. Conclusion

We have shown how concrete syntax pattern matching can be integrated with minimal effort in any parser-based tool, written in any host language and manipulating any subject language, including multi-language tools such as legacy systems analyzers or intentional programming systems. Matching concrete syntax can make the code of such tools more concise and more readable. The purely syntactic matching can be easily complemented with any other checks in the host language, due to a natural embedding of patterns as strings in the host language. Furthermore, unparsed patterns give a very simple means to make such tools extensible with user-defined behavior. In particular, most existing tools can be made extensible with minimal effort. Extensible compilers are a particular application in which users may add their own program checks. Other possible applications may involve model checkers, program inspectors, etc.

Unparsed patterns can be improved in several respects. It would be interesting, both from a practical and theoretical point of view, to reduce even further the amount of meta-parentheses required to obtain a complete matching algorithm. In terms of expressiveness, pattern variables could be typed and could also match tokens, and a single pattern variable could match a list of elements such as in other matchers, even when that list of elements is not grouped as a distinct subtree. Also, it would be useful to allow for empty trees in the definition of unparsing (yielding an empty list). In

terms of execution time, it is an open question whether the subtree matching problem, when using unparsed patterns, can be solved more efficiently than in quadratic time. Finally, concrete uses of dynamic patterns remain to be investigated.

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A. The proofs of the claimed properties

A.1 Algorithm F(0)

A.1.1 Complexity

Note that in any state at most one rule may be applicable. The algorithm performs at most $|AST| + |p|$ rewrite steps, where $|AST|$ and $|p|$ are the sizes of the AST and of the pattern. Indeed, the algorithm performs at most $|p|$ match steps, because each such step consumes a stream prefix, and at most $|AST|$ unparsed steps, because each node of the AST can be unparsed at most once. The sum of all the unparsed steps correspond to at most one complete traversal of the whole AST. The tests selecting between different rules are constant time except comparing a bound meta-variable with a subtree, which may involve traversing both subtrees to check for equality.

If common subtrees are shared in the original AST, comparing subtrees is constant time. This is frequently the case in compilers if a global value numbering (GVN) scheme [28] has been used to label expressions in the AST.

On the other hand, if all these subtree comparison steps are not constant time but are applied to disjoint subtrees, and every subtree may be compared at most once, then the sum of all these comparisons would correspond to at most one traversal of the whole AST. It is easy to see that subtrees compared successfully (by Rule 4) are then skipped, so they satisfy the disjoint criterion, and trees compared unsuccessfully cause the matching to fail immediately because no rule may apply in this case.

Therefore, in both cases (subtree comparison in constant or linear time), the pattern matching algorithm runs in linear time $O(|AST| + |p|)$. This is no worse than algorithms that require a pattern parser.

A.1.2 Correctness

Let us prove now that the lazy unparsed pattern matching algorithm is correct, which means that if the algorithm rewrites $\langle [t], p, \{ \} \rangle$ to $\langle [], [], \sigma \rangle$, then the tree t matches p under substitution σ .

The fact that the algorithm completed means that it followed the rules completely consuming the stack and the stream. We will note the application of these rules as:

- $Tok(k)$: Rule 1 matching a token k ;
- $Unp(t)$: Rule 2 performing an unparsed step of tree t ;
- $Bind(x, t)$: Rule 3 binding variable x to subtree t ;
- $EqVar(x, t)$: Rule 4 successfully comparing instantiated variable x with subtree t .

If the pattern consists of a single variable $p = \%x$, the algorithm surely performed a $Bind(x, t)$ step (or an $EqVar(x, t)$ step if we allow the initial substitution to be non-empty). Then $p[x \leftarrow TXT(t)] = TXT(t)$, so t matches p , according to the definition of matching in Section 2.

Otherwise, the pattern must be of form $p = \langle \dots \rangle$, because all unparsed trees using $PAR_{F(0)}$ begin and end with meta-parentheses. For this kind of pattern, the proof is by induction on the depth of the tree t .

If the depth of the tree is one, $LST(t)$ contains only tokens, and no subtree: $LST(t) = [k_1, \dots, k_n]$. It follows that the algorithm performed the following sequence of steps:

$$Trace(t) = Unp(t), Tok("("), Tok(k_1), \dots Tok(k_n), Tok(")")$$

By examining the conditions of each rule, it follows that $p = (k_1 \dots k_n)$. Therefore, p trivially matches t because $p = TXT_{F(0)}(t)$.

Let us assume that the algorithm is correct for any tree of depth $d < D$, and consider a tree of depth D . Then the unparsed list of t is a list arbitrarily mixing tokens and subtrees: $LST(t) = [k_{i_0}, t_{j_1}, k_{i_1} \dots t_{j_n}, k_{i_n}]$. The trace of the successful algorithm application must begin with:

$$Trace(t) = Unp(t), Tok("("), Tok(k_{i_0})$$

After unparsing the tree, matching the left meta-parenthesis and consuming all the tokens k_{i_0} (possibly none), the algorithm reaches some state $\langle [t_1] + s, p'_{1_1}, \sigma' \rangle$. Because the algorithm manipulates the first member of the tuple as a stack, and consumes the second member as a stream, it will have to match the subtree on top of the stack before arriving to some state $\langle s, p''_{1_1}, \sigma'' \rangle$, where p''_{1_1} must be a suffix of p'_{1_1} , hence $p'_{1_1} = p_{1_1} + p''_{1_1}$ for some pattern prefix p_{1_1} . If we note the sequence of steps between these two states as $Trace(t_{j_1})$, then it is easy to see that this trace would constitute a successful matching of the tree t_{j_1} against pattern p_{1_1} , computing some substitution σ_{1_1} . Thus, we can decompose the trace as:

$$Trace(t) = Unp(t), Tok("("), Tok(k_{i_0}), Trace(t_{j_1}), Tok(k_{i_1}) \dots Trace(t_{j_n}), Tok(k_{i_n}), Tok(")")$$

and we can decompose the pattern p as $\langle (k_{i_0} p_{j_1} \dots p_{j_n} k_{i_n}) \rangle$.

By the induction hypothesis, t_{j_1} matches p_{1_1} under substitution σ_{1_1} ; in other words, $\sigma_{1_1}^{TXT}(p_{1_1}) = TXT(t_{j_1})$ ¹. Furthermore, all the substitutions σ_{j_k} matching the subtrees t_{j_k} are compatible, since $Trace(t)$ contains only successful comparisons of instantiated variables (otherwise, the match would have failed). Hence, all these substitutions are subsets of the substitution computed by the algorithm: $\sigma_{j_k} \subset \sigma$. Therefore,

$$\begin{aligned} \sigma^{TXT}(p) &= \sigma^{TXT}(\langle (k_{i_0} p_{j_1} \dots p_{j_n} k_{i_n}) \rangle) = \\ &= \langle (k_{i_0} \sigma^{TXT}(p_{j_1}) \dots \sigma^{TXT}(p_{j_n}) k_{i_n}) \rangle = \\ &= \langle (k_{i_0} TXT(t_{j_1}) \dots TXT(t_{j_n}) k_{i_n}) \rangle = TXT(t) \end{aligned}$$

In other words, t matches p , which closes the proof.

A.1.3 Completeness

It is easy to see that it is sufficient to prove that the algorithm finds a match between P itself and p (with a resulting identity substitution $\sigma = x_i \leftarrow x_i$). Indeed, any other tree t matching P can be expressed as $t = \theta(P)$ (by the definition of conventional tree matching). In the successful trace of the algorithm matching P with p , if we replace each step $Bind(x_i, x_y)$ by a step $Bind(x_i, \theta(x_i))$ and each step $EqVar(x_i, x_y)$ by a step $EqVar(x_i, \theta(x_i))$, we obtain a successful trace for matching t with p .

The proof that the algorithm finds a match between P and $p = TXT_{F(0)}(P)$, by induction on the depth of P , is straightforward and omitted here.

¹ To simplify the notation, we omit the index $TXT_{F(0)}$.

A.2 Algorithm N(1)

A.2.1 Complexity

The *first_token* function can be implemented in constant time by a linear-time pre-processing phase that computes it during a bottom-up traversal of the AST. Thus, the *lookahead* function will also run in constant time. The modified rules do not change the fact that the compared subtrees are disjoint. Thus, all the arguments for the complexity remain valid for the lookahead-based algorithm, so this algorithm has also a linear running time.

We omit the correctness proof for the lookahead-based matching algorithm, but it can be done by induction. Intuitively, similar to the previous algorithm, each step that consumes elements compares an element from the stack and a compatible element from the pattern, putting them in a one-to-one mapping. Therefore, if the algorithm succeeds, the tree matches the pattern.

A.3 Algorithm ES(1)

A.3.1 Complexity

Function *lookahead* can be implemented in constant time, after a linear pre-processing over the pattern ensuring that sequences of meta-parentheses can be skipped in constant time. For similar reasons as in the previous subsections the matching algorithm runs in linear time.

Note that the complexity of functions *conflicting* and *leftmost_conflicting* does not influence the complexity of the ES(1) matching algorithm, because these functions are not used by the algorithm, but just by the user when writing a pattern.

We omit the correctness proof, but the same intuition tells us that each matching step establishes a correspondence between a part of the tree and a part of the pattern, so if the algorithm finishes successfully, then the tree matches the pattern.

A.3.2 Completeness

In order to show the completeness of ES(1), we will now show that algorithm ES(1) matches any tree $t \in T_{\Sigma}(V)$ with the unparsed pattern $Trans(t)$. We will prove this by induction using the following induction hypothesis:

$$\begin{aligned} (\forall t)(\forall s)(\forall p)(\forall \sigma \subset \{x_i \leftarrow x_i\}) lookahead(s, p) \Rightarrow \\ \langle [t|s], Trans(t) + p, \sigma \rangle \xrightarrow{*}_{ES(1)} \langle s, p, \sigma' \rangle \\ \wedge (\sigma \subset \sigma' \subset \{x_i \leftarrow x_i\}) \end{aligned}$$

Let us consider a tree t , a stack s , a pattern p , and a substitution $\sigma \subset \{x_i \leftarrow x_i\}$, such that $lookahead(s, p)$.

If the tree consists of only a variable $t = x$, we have $Trans(t) = \text{"\%x"}$. If $x \in domain(\sigma)$, $\sigma(x) = x$, so the algorithm will successfully match the variable in an EqVar(x) step, and $\sigma' = \sigma$. Otherwise, $x \notin domain(\sigma)$, and the algorithm will successfully bind the variable in a Bind(x) step, and $\sigma' = \sigma \cup \{x \leftarrow x\} \subset \{x_i \leftarrow x_i\}$.

If the tree t has a depth $D > 1$, its unparsed list may contain an arbitrary mix of tokens and subtrees (including variables): $LST(t) = [k_{i_0}, t_{j_1}, k_{i_1} \dots t_{j_n}, k_{i_n}]$.

If *leftmost_conflicting*(t, s), we have:

$$\begin{aligned} Trans(t) = \\ \text{"\%(k_{i_0} Trans(t_{j_1}) k_{i_1} \dots Trans(t_{j_n}) k_{i_n} \%)" } \end{aligned}$$

In order to use our induction hypothesis, we must check that for any subtree t_{j_l} the lookahead is successful. This can be easily shown by a case-by-case reasoning:

- if the subtree is followed by a token, this token is k_{i_l} and occurs both in the unparsed list after t_{j_l} and in the pattern after $Trans(t_{j_l})$

- if the subtree is followed by another subtree, this subtree is $t_{j_{l+1}}$, and by inspecting the definition of the lookahead function, $lookahead([t_{j_{l+1}}], Trans(t_{j_{l+1}}) + _) = true$ because $Trans(t_{j_{l+1}})$ cannot contain only meta-parentheses
- if the subtree is the last element in the unparsed list ($n_n = 0$), the following element both in the pattern and in the stack is "\%" , because the right meta-parenthesis was pushed by the *Unppar* rule; as lookahead ignores meta-parentheses, the lookahead is the same as $lookahead(s, p)$, which is true.

Therefore, the lookahead pre-condition in the induction hypothesis is verified for each subtree, so the algorithm will execute the steps

$$\begin{aligned} Unppar(t), Tok(\text{"\%("}) Tok(k_{i_0}), Trace(t_{j_1}), Tok(k_{i_1}) \dots \\ Trace(t_{j_n}), Tok(k_{i_n}), Tok(\text{"\%)"}) \end{aligned}$$

and successfully find a match.

If $\neg leftmost_conflicting(t, s)$, we have:

$$Trans(t) = \text{"k_{i_0} Trans(t_{j_1}) k_{i_1} \dots Trans(t_{j_n}) k_{i_n}"}$$

By the same reasoning as above, the lookahead precondition is satisfied for any of the subtrees. However, the rule that is first executed by ES(1) depends now on the first element in the pattern, which is not always a left meta-parenthesis in this case. We distinguish the following two sub-cases.

If the pattern starts with a variable: $Trans(t) = \text{"\%x"} + p'$, then $n_0 = 0$ and the left-most descendant of t must be the variable x . Either x is directly the first child of t , and then we apply the induction hypothesis, or x is a deeper leftmost descendant of t . In the latter case, $(\exists n > 1) \bigwedge_{i=2}^n LST(t_{i-1}) = [t_i | s_i]$ (where $t_1 = t$), and it can be shown that $lookahead(s, p') = false$. Indeed, it can be easily shown, knowing how the pattern was constructed, that $lookahead(s_n + \dots + s_1, p') = true$ (where $s_1 = s$)². If we suppose that $lookahead(s, p') = true$, this would imply that t is conflicting, and hence leftmost-conflicting, which is in contradiction with the current case assumption. Therefore we have $lookahead(s, p') = false$ so the algorithm would unparse the tree t by Rule 14, and using the induction hypothesis, find a successful match with the trace:

$$Unpvar(t), Trace(t_{j_1}), Tok(k_{i_1}) \dots Trace(t_{j_n}), Tok(k_{i_n})$$

If the pattern starts with a token, then $n_0 > 0$ and the algorithm will execute first Rule 12, and using the induction hypothesis, successfully find a match with the trace:

$$Unptok(t), Tok(k_{i_0}), Trace(t_{j_1}), Tok(k_{i_1}) \dots Trace(t_{j_n}), Tok(k_{i_n})$$

In all cases, the condition on the substitution, $\sigma \subset \sigma' \subset \{x_i \leftarrow x_i\}$, is easily verified, and this closes the proof.

Thus, ES(1) matches any tree $P \in T_{\Sigma}(V)$ with the unparsed pattern $Trans(P)$. It is easy to see why the unparsed pattern has been defined by parenthesizing *all* the leftmost-conflicting subtrees in P : because the solution assigns any variable to an elementary tree (the corresponding variable); therefore, any bind to a non-elementary subtree must be avoided by forcing an unparse step.

Due to the composability property, the completeness of ES(1) directly follows.

²In fact, by exploiting the particular lookahead definition, it can be even shown that $[s_n + \dots + s_1] = [k_n]$ (otherwise t would be leftmost-conflicting), and $p' = [k_n]$ (because the pattern is the unparsed form of t). Furthermore, it can be shown that $s = [k]$ where $k \neq k_n$ (otherwise t would be conflicting)