

# COSC 320: Steps in Algorithm Design and Analysis\*

In this worksheet, you'll practice five useful steps for designing and analyzing algorithms, starting from a possibly vague problem statement. These steps will be useful throughout the class. They could also be useful when you find yourself thinking on your feet in an interview situation. And hopefully they will serve you well in your work post-graduation too!

We'll use the **Stable Matching Problem (SMP)** as our working example. Following the historical literature, the text formulates the problem in terms of marriages between men and women. We'll avoid the gender binaries inherent in that literature and use employers and job applicants instead. Imagine for example the task faced by UBC's co-op office each semester, which seeks to match hundreds of student applicants to employer internships. To keep the problem as simple as possible for now, assume that every applicant has a full ranking of employers and vice versa (no ties).

## Step 1: Build intuition through examples.

### 1. Write down small and trivial instances of the problem.

We'll use the words "instance" and "inputs" interchangeably.

### 2. Write down potential solutions for your instances.

Are some solutions better than others? How so?

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## Step 2: Develop a formal problem specification

1. **Develop notation for describing a problem instance.** What quantities or data (such as numbers, sets, lists, etc.) matter? Give them short, usable names. Think of these as input parameters to the algorithm code. Use your earlier examples to illustrate your notation.

2. **Develop notation for describing a potential solution.**  
Use your earlier examples to illustrate your notation.

3. **Describe what you think makes a solution *good*.**

Step 3: Identify similar problems. What are the similarities?

Step 4: Evaluate simple algorithmic approaches, such as brute force.

1. **Design a brute force algorithm for the SMP problem.**

Given as input a problem instance, a "brute force" algorithm enumerates all potential solutions, and checks each to see if it is good. If a good solution is found, the algorithm outputs this solution, and otherwise reports that there is no good solution. **Flesh out the details: what is a problem instance, and potential solution in this case? How would you test if a potential solution is a good solution?**

2. Analyze the worst case running time of brute force.
  - Bound the running time, say  $t(n)$ , of your procedure to test if a potential solution is a good solution. Assume that the input  $M$  is represented as a list of pairs  $(e, a)$  such that  $e$  is matched with  $a$ , where  $1 \leq e, a \leq n$ .

- [illegible]

## Step 5: Design a better algorithm.

1. **Brainstorm some ideas, then sketch out an algorithm.**

Carefully try out your algorithm on your examples, and design instances that challenge the correctness of your approach.

Hopefully, we've already bounced back and forth between these steps in today's worksheet! You usually *will* have to. Especially repeat the steps where you generate instances and challenge your approach(es).