

# Homework 2

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√1. unsigned:

$$0_{10} \rightarrow 000000_2$$

$$13_{10} \rightarrow 001101_2$$

$$24_{10} \rightarrow 011000_2$$

$$63_{10} \rightarrow 111111_2$$

signed:

$$16_{10} \rightarrow 010000_2$$

$$-2_{10} \rightarrow 111110_2$$

$$31_{10} \rightarrow 011111_2$$

$$-32_{10} \rightarrow 100000_2$$

$$\begin{array}{r} +2 \rightarrow 000010 \\ \text{reverse} \quad 111101 \\ + \quad 1 \\ \hline 111110 \end{array}$$

$$\begin{array}{r} +32 \rightarrow 100000 \\ \text{reverse} \quad 011111 \\ + \quad 1 \\ \hline 100000 \end{array}$$

√2.

given	unsigned	signed
$000101_2 \rightarrow$	$5_{10}$	$5_{10}$
$101011_2 \rightarrow$	$43_{10}$	$-21_{10}$
$111111_2 \rightarrow$	$63_{10}$	$-1_{10}$
$100000_2 \rightarrow$	$32_{10}$	$-32_{10}$

draft:

$$-1: 101010 \rightarrow 21$$

$$-1: 111110 \rightarrow 1$$

$$-1: 011111 \rightarrow 32$$

√3.  $7_{10} \rightarrow 00000111_2 \rightarrow 0x07$  (or  $07_{16}$ )

$240_{10} \rightarrow 11110000_2 \rightarrow 0xF0$

$171_{10} \rightarrow 10101011_2 \rightarrow 0xAB$

$126_{10} \rightarrow 01111110_2 \rightarrow 0x7E$

A	10	1010
B	11	1011
C	12	1100
D	13	1101
E	14	1110
F	15	1111

√4.  $0x3C \rightarrow 00111100_2$

$0x7E \rightarrow 01111110_2$

$0xFF \rightarrow 11111111_2$

$0xA5 \rightarrow 10100101_2$

√5.  $00111100_2 \rightarrow 11000011 + 1 = 11000100_2$

$01111110_2 \rightarrow 10000001 + 1 = 10000010_2$

$11111111_2 \rightarrow 00000000 + 1 = 00000001_2$

$10100101_2 \rightarrow 01011010 + 1 = 01011011_2$

√6. 0x DEADBEEF

Big-Endian

address: 0x100 0x101 0x102 0x103

value: DE AD BE EF

↑  
most  
significant  
byte

Little-Endian

0x100 0x101 0x102 0x103

EF BE AD DE

↑ less significant  
byte

√7.  $7_{10} \rightarrow 00111_2$   
 $15_{10} \rightarrow 01111_2$   
 $-16_{10} \rightarrow 10000_2$   
 $-5_{10} \rightarrow 11011_2$

zero-extended

$00000111_2$   
 $00001111_2$   
 $00010000_2$   
 $00011011_2$

sign-extended

$00000111_2$   
 $00001111_2$   
 $11110000_2$   
 $11111011_2$

√8. unsigned:

$7 \rightarrow 0111$   
 $9 \rightarrow +1001$   
 $\hline 10000_2$

4 bits  
 $\swarrow$   
 $\left[ \begin{array}{l} 0000_2 \text{ is } 0 \\ 10000_2 \text{ is } 16 \end{array} \right]$   
 $\nwarrow$  5 bits

signed:

$4 \rightarrow 0100$   
 $-5 \rightarrow +1011$   
 $\hline 1111_2 \text{ (which is } -1)$

√8. \* (16) 1)  $x \& (x-1)$  - turning off the rightmost 1-bit

•  $x-1 \rightarrow$  all the bits after the rightmost 1-bit are inverted  
 ex:  $01011000 - 1 = 01010111$

•  $x \& (x-1) \rightarrow$  all the bits stay the same up to the rightmost 1-bit, which "turns off"

ex:  
 $\begin{array}{r} 01011000 \\ \text{AND } 01010111 \\ \hline 01010000 \end{array}$

2)  $x | (x+1)$  - turning on the rightmost 0-bit

•  $x+1 \rightarrow$  all the bits after the rightmost 0-bit are inverted  
 ex:  $10100111 + 1 = 10101000$

- $X \mid (X+1) \rightarrow$  all bits remain unchanged, the rightmost 0-bit "turns on"

$$\text{ex: } \begin{array}{r} 10100111 \\ \text{OR } 10101000 \\ \hline 10101111 \end{array}$$

- 3)  $X \mid (X-1)$  - turning on the trailing 0's

- $X-1 \rightarrow$  all the bits after the rightmost 1-bit are inverted

$$\text{ex: } 10101000 - 1 = 10100111$$

- $X \mid (X-1) \rightarrow$  trailing 0's of the original number "turn on", all other bits stay the same

$$\text{ex: } \begin{array}{r} 10101000 \\ \text{OR } 10100111 \\ \hline 10101111 \end{array}$$

(12)

$$X = X \wedge y; \rightarrow X = X \text{ XOR } y$$

$$y = X \wedge y; \rightarrow y = X \text{ XOR } (y \text{ XOR } y) = 0 = X \text{ XOR } 0 = X$$

$$X = X \wedge y; \rightarrow X = X \text{ XOR } y \text{ XOR } X = \underbrace{(X \text{ XOR } X)}_0 \text{ XOR } y = y$$

that is,  $x$  and  $y$  are swapped

$$\text{example: Let } \begin{array}{l} x = 10101111 \\ y = 00010011 \end{array}$$

$$\text{then after } \begin{array}{ll} x = x \wedge y; & x = 10111100 \\ & y = 00010011 \end{array}$$

$$\text{after } \begin{array}{ll} y = x \wedge y; & x = 10111100 \\ & y = 10101111 \end{array}$$

$$\text{after } \begin{array}{ll} x = x \wedge y; & x = 00010011 \\ & y = 10101111 \\ & x \text{ and } y \text{ are swapped now} \end{array}$$