



MATHEMATICS SPECIALIST ATAR COURSE

FORMULA SHEET

2019

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Differentiation and integration

$\frac{d}{dx}\left(x^{n}\right) = nx^{n-1}$		$\int x^n dx = \frac{x^{n+1}}{n+1} + c, \qquad n \neq -1$	
$\frac{d}{dx}\left(e^{ax}\right) = ae^{ax}$		$\int e^{ax}dx = \frac{1}{a}e^{ax} + c$	
$\frac{d}{dx}(\ln x) = \frac{1}{x}$		$\int \frac{1}{x} dx = \ln x $	+ c
$\frac{d}{dx}(\ln f(x)) = \frac{f'(x)}{f(x)}$		$\int \frac{f'(x)}{f(x)} dx = \ln f(x) + c$	
$\frac{d}{dx}(\sin f(x)) = f'(x)\cos(f(x))$		$\int \sin(ax) dx =$	$=-\frac{1}{a}\cos{(ax)}+c$
$\frac{d}{dx}(\cos f(x)) = -f'(x)\sin(f(x))$		$\int \cos(ax) dx =$	$=\frac{1}{a}\sin\left(ax\right)+c$
$\frac{d}{dx}(\tan f(x)) = f'(x) \sec^2 x$	$c^{2}(f(x)) = \frac{f'(x)}{\cos^{2} f(x)}$	$\int \sec^2(ax) dx =$	$=\frac{1}{a}\tan\left(ax\right)+c$
	If $y = uv$		If y = f(x) g(x)
Product rule	then	or	then
Product rule	$\frac{d}{dx}(uv) = u\frac{dv}{dx} + \frac{du}{dx}v$		y' = f'(x) g(x) + f(x) g'(x)
	If $y = \frac{u}{v}$		If $y = \frac{f(x)}{g(x)}$
Quotient rule	then	or	then
	$\left \frac{d}{dx} \left(\frac{u}{v} \right) \right = \frac{v \frac{du}{dx} - u \frac{dv}{dx}}{v^2}$		$y' = \frac{f'(x) g(x) - f(x) g'(x)}{(g(x))^2}$
	f y = f(u) and u = g(x)		If $y = f(g(x))$
Chain rule	then	or	then
	$\frac{dy}{dx} = \frac{dy}{du} \times \frac{du}{dx}$		y' = f'(g(x)) g'(x)
Fundamental theorem	$\frac{d}{dx} \left(\int_{a}^{x} f(t) dt \right) = f(x)$	and	$\int_{a}^{b} f'(x) dx = f(b) - f(a)$

Applications of calculus

Growth and decay			
Exponential equation	$\frac{dP}{dt} = kP \iff P = P_0 e^{kt}$		
Logistic equation	$\frac{dP}{dt} = rP(k-P) \Leftrightarrow P = \frac{kP_0}{P_0 + (k-P_0)e^{-rkt}}$		
Volumes of solids of revol	ution		
About the <i>x</i> -axis	$V = \pi \int_{a}^{b} \left[f(x) \right]^{2} dx$		
About the <i>y</i> -axis	$V = \pi \int_{c}^{d} [f(y)]^{2} dy$		
Simple harmonic motion			
$If \frac{d^2x}{dt^2} = -k^2x$	then $x = A \sin(kt + \alpha)$ or $x = A \cos(kt + \beta)$		
where A is the amplitude, α and β are phase angles, v is the velocity and x is the displacement			
$v^2 = k^2(A^2 - $	(x^2) Period: $T = \frac{2\pi}{k}$ Frequency: $f = \frac{1}{T}$		
Increments formula	$\delta y \approx \frac{dy}{dx} \times \delta x$		
Acceleration	$\frac{dv}{dt}$ or $v\frac{dv}{dx}$ or $\frac{d}{dx}\left(\frac{1}{2}v^2\right)$		

Functions

Quadratic function	If $f(x) = ax^2 + bx + c$ and $f(x) = 0$, then $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$
Absolute value function	$ x = \begin{cases} x, & \text{for } x \ge 0 \\ -x, & \text{for } x < 0 \end{cases}$

Statistical inference

Confidence interval for the mean of the population	$\overline{X} - z \frac{s}{\sqrt{n}} \le \mu \le \overline{X} + z \frac{s}{\sqrt{n}}$
Sample size	$n = \left(\frac{z \times s}{d}\right)^2$

Mensuration

Parallelogram	A = bh	
Triangle	$A = \frac{1}{2} bh$ or $A = \frac{1}{2} ab \sin C$	
Trapezium	$A = \frac{1}{2} (a+b)h$	
Circle	$A=\pi r^2$ and $C=2\pi r=\pi d$	
Prism	V = Ah, where A is the area of the cross section	
Pyramid	$V = \frac{1}{3} Ah$, where A is the area of the cross section	
Cylinder	$V = \pi r^2 h$	$S = 2\pi r h + 2\pi r^2$
Cone	$V = \frac{1}{3} \pi r^2 h$	$S = \pi r s + \pi r^2$, where s is the slant height
Sphere	$V = \frac{4}{3} \pi r^3$	$S = 4\pi r^2$

Vectors in 3D

Magnitude	$ (a_1, a_2, a_3) = \sqrt{a_1^2 + a_2^2 + a_3^2}$	
Dot product	$\mathbf{a} \cdot \mathbf{b} = \mathbf{a} \mathbf{b} \cos\theta = a_1b_1 + a_2b_2 + a_3b_3$	
Cross product	$\mathbf{a} \times \mathbf{b} = \begin{pmatrix} a_1 \\ a_2 \\ a_3 \end{pmatrix} \times \begin{pmatrix} b_1 \\ b_2 \\ b_3 \end{pmatrix} = \begin{pmatrix} a_2 b_3 - a_3 b_2 \\ a_3 b_1 - a_1 b_3 \\ a_1 b_2 - a_2 b_1 \end{pmatrix}$	
Equation of a line	One point and direction $\mathbf{r} = \mathbf{a} + \lambda \mathbf{u}$	
Equation of a line	Two points A and B $\mathbf{r} = \mathbf{a} + \lambda(\mathbf{b} - \mathbf{a})$	
Equation of a plane	$\mathbf{r} = \mathbf{a} + \lambda \mathbf{u}_1 + \mu \mathbf{u}_2$ or $\mathbf{r} \cdot \mathbf{n} = \mathbf{a} \cdot \mathbf{n}$	
Equation of a sphere	$ \mathbf{r} - \mathbf{d} = r$ or $(x-a)^2 + (y-b)^2 + (z-c)^2 = r^2$	
Cartesian equation of a line	$\frac{x - a_1}{u_1} = \frac{y - a_2}{u_2} = \frac{z - a_3}{u_3}$	
Cartesian equation of a plane	ax + by + cz = d	
Parametric equation of a line	$x = a_1 + \lambda u_1 \dots (1)$ $y = a_2 + \lambda u_2 \dots (2)$ $z = a_3 + \lambda u_3 \dots (3)$	

Complex numbers

Cartesian form	
z = a + bi	$\overline{z} = a - bi$
Mod $(z) = z = \sqrt{a^2 + b^2} = r$	$\operatorname{Arg}(z) = \theta$, $\tan \theta = \frac{b}{a}$, $-\pi < \theta \le \pi$
$ z_1 z_2 = z_1 z_2 $	$\left \frac{z_1}{z_2}\right = \frac{ z_1 }{ z_2 }$
$arg(z_1 z_2) = arg(z_1) + arg(z_2)$	$\arg\left(\frac{z_1}{z_2}\right) = \arg(z_1) - \arg(z_2)$
$z\overline{z} = z ^2$	$z^{-1} = \frac{1}{z} = \frac{\overline{z}}{ z ^2}$
$\overline{z_1 + z_2} = \overline{z_1} + \overline{z_2}$	$\overline{z_1}\overline{z_2} = \overline{z_1}\overline{z_2}$
Polar form	
$z = a + bi = r(\cos \theta + i \sin \theta) = r \cos \theta$	$\overline{z} = r \operatorname{cis}(-\theta)$
$z_1 z_2 = r_1 r_2 \operatorname{cis} (\theta_1 + \theta_2)$	$\frac{z_1}{z_2} = \frac{r_1}{r_2} \operatorname{cis} (\theta_1 - \theta_2)$
$\operatorname{cis}(\theta_1 + \theta_2) = \operatorname{cis} \theta_1 \operatorname{cis} \theta_2$	$\operatorname{cis}(-\theta) = \frac{1}{\operatorname{cis}\theta}$
De Moivres theorem	
$z^n = z ^n \operatorname{cis}(n\theta)$	$(\operatorname{cis} \theta)^n = \operatorname{cos} n\theta + i \sin n\theta$
$z^{\frac{1}{q}} = r^{\frac{1}{q}} \left(\cos \frac{\theta + 2\pi k}{q} + i \sin \frac{\theta + 2}{q} \right)$	$\left(\frac{\pi k}{k}\right)$, for k an integer

Trigonometry

$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$	Length of $\operatorname{arc} = r\theta$
$a^2 = b^2 + c^2 - 2bc \cos A$	Area of segment = $\frac{1}{2}r^2(\theta - \sin\theta)$
$\cos A = \frac{b^2 + c^2 - a^2}{2bc}$	Area of sector = $\frac{1}{2} r^2 \theta$
Identities	
$\cos^2 x + \sin^2 x = 1$	$1 + \tan^2 x = \sec^2 x$
	$\cos 2x = \cos^2 x - \sin^2 x$
$\cos(x \pm y) = \cos x \cos y \mp \sin x \sin y$	$=2\cos^2 x - 1$
	$=1-2\sin^2 x$
$\sin(x \pm y) = \sin x \cos y \pm \cos x \sin y$	$\sin 2x = 2\sin x \cos x$
$\tan (x + y) = \frac{\tan x + \tan y}{1 + \tan x \tan y}$	$\tan 2x = \frac{2 \tan x}{1 - \tan^2 x}$
$\cos A \cos B = \frac{1}{2} (\cos(A-B) + \cos(A+B))$	$\sin A \cos B = \frac{1}{2} \left(\sin(A+B) + \sin(A-B) \right)$
$\sin A \sin B = \frac{1}{2} \left(\cos(A - B) - \cos(A + B) \right)$	$\cos A \sin B = \frac{1}{2} \left(\sin(A+B) - \sin(A-B) \right)$

Note: Any additional formulas identified by the examination panel as necessary will be included in the body of the particular question.

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