

**Stage 2 - BFS traversal starting at  $u_{low}$**

**while  $Q$  not empty do**

    dequeue  $v \leftarrow Q$ ;

**for all neighbor  $w$  of  $v$  do**

**if  $d[w] = (d[v] + 1)$  then**

**if  $t[w] = \text{Not-Touched}$  then**

                enqueue  $w \rightarrow Q_{BFS}$ ;

                enqueue  $w \rightarrow Q[d[w]]$ ;

$t[w] \leftarrow \text{Down}$ ;

$d[w] \leftarrow d[v] + 1$ ;

$dP[w] \leftarrow dP[v]$ ;

**else**

$dP[w] \leftarrow dP[w] + dP[v]$ ;

$\hat{\sigma}[w] \leftarrow \hat{\sigma}[w] + dP[v]$ ;

**Stage 3 - modified dependency accumulation**

$\hat{\delta}[v] \leftarrow 0, v \in \forall V$ ;  $level \leftarrow V$ ;

**while  $level > 0$  do**

**while  $Q[level]$  not empty do**

        dequeue  $w \leftarrow Q[level]$ ;

**for all  $v \in P[w]$  do**

**if  $t[v] = \text{Not-Touched}$  then**

                enqueue  $v \rightarrow Q[level - 1]$ ;

$t[v] \leftarrow \text{Up}$ ;

$\hat{\delta}[v] \leftarrow \delta[v]$ ;

$\hat{\delta}[v] \leftarrow \hat{\delta}[v] + \frac{\hat{\sigma}[v]}{\hat{\sigma}[w]}(1 + \hat{\delta}[w])$ ;

**if  $t[v] = \text{Up} \wedge (v \neq u_{high} \vee w \neq u_{low})$  then**

$\hat{\delta}[v] \leftarrow \hat{\delta}[v] - \frac{\sigma[v]}{\sigma[w]}(1 + \delta[w])$ ;

**if  $w \neq r$  then**

$C_B[w] \leftarrow C_B[w] + \hat{\delta}[w] - \delta[w]$ ;

$level \leftarrow level - 1$ ;

$\sigma[v] \leftarrow \hat{\sigma}[v], v \in \forall V$ ;

**for  $v \in V$  do**

**if  $t[v] \neq \text{Not-Touched}$  then**

$\delta[v] \leftarrow \hat{\delta}[v], v \in \forall V$