Algorithm 4. Edge-Update($G = (V, E), \mathbf{w}'(u, v)$)
Input: updated edge with $\mathbf{w}'(u, v)$, $d(s, t)$ and σ_{st} , $\forall s, t \in V$; DAG (s) , $\forall s \in V$.
Dutput: BC'(v), $\forall v \in V$; $d'(s,t)$ and $\sigma'_{st} \forall s,t \in V$; DAG'(s), $\forall s \in V$.
1: for every $v \in V$ do $BC'(v) \leftarrow 0$.
for every $s, t \in V$ do compute $d'(s, t), \sigma'_{st}, flag(s, t)$. // use Lemma 2
2: for every $s \in V$ do
3: Update-DAG $(s,(u,v))$. // use Alg. 3
4: Stack $S \leftarrow$ vertices in V in a reverse topological order in DAG'(s).
5: Accumulate-dependency (s, S) . // use Alg. 2