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**Algorithm 2:** VERTEX: vertex-based parallel BC

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...  
 $\ell \leftarrow 0$   
▷Forward phase  
while cont = true do  
    cont  $\leftarrow$  false  
    ▷Forward-step kernel  
    for each  $u \in V$  in parallel do  
1      if  $d[u] = \ell$  then  
2          for each  $v \in \Gamma(u)$  do  
3              if  $d[v] = -1$  then  
                   $d[v] \leftarrow \ell + 1$ , cont  $\leftarrow$  true  
              else if  $d[v] = \ell - 1$  then  $P_v[u] \leftarrow 1$   
4              if  $d[v] = \ell + 1$  then  $\sigma[v] \overset{atomic}{\leftarrow} \sigma[v] + \sigma[u]$   
           $\ell \leftarrow \ell + 1$   
...  
▷Backward phase  
while  $\ell > 1$  do  
     $\ell \leftarrow \ell - 1$   
    ▷Backward-step kernel  
    for each  $u \in V$  in parallel do  
        if  $d[u] = \ell$  then  
5            for each  $v \in \Gamma(u)$  do  
6                if  $P_v[u] = 1$  then  $\delta[u] \leftarrow \delta[u] + \delta[v]$   
    ▷Update bc values by using Equation (5)  
...
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